

## QUARTILE DEVIATION:

Half of the difference b/w third and first quartile is called semi-interquartile range / quartile deviation

$$Q.D = \frac{Q_3 - Q_1}{2}$$

$$\text{Coefficient of Quartile} = \frac{Q_3 - Q_1}{Q_3 + Q_1}$$

Interquartile Deviation is  $\frac{Q_3 - Q_1}{2}$

For ungrouped Data:

$$Q_1 = \left( \frac{N}{4} \right)^{\text{th}} \text{ item}$$

$$Q_2 = \left( \frac{N}{2} \right)^{\text{th}} \text{ item}$$

$$Q_3 = \left( \frac{3N}{4} \right)^{\text{th}} \text{ item.}$$

For Grouped Data:

$$Q_r = l_1 + \frac{\left[ r \left( \frac{N}{4} \right) - c \right]}{f} (l_2 - l_1)$$

where,  $Q_r \rightarrow$  the  $r^{\text{th}}$  quartile

$l_1$  = lower limit of quartile class

$l_2$  = upper limit of quartile class

$L$  = tot frequency

$f$  = Frequency

$c$  = Value preceding to quartile class  
in cumulative frequency

From the following table giving marks of students, calculate the interquartile range, quartile deviation and coefficient of quartile deviation.

Marks of Students	60	62	68	70	75	80	88	90
No. of Students	25	21	28	18	24	20	24	17
Cumulative Frequency	25	46	74	92	116	136	160	171

$$Q_1 = \frac{199}{4}$$

$$Q_1 = 49.75$$

$$\therefore Q_1 = 68$$

$$Q_3 = \frac{3 \times 199}{4}$$

$$Q_3 = \frac{59.70}{4}$$

$$Q_3 = 14.93$$

$$Q_3 = 88$$

$$Q.D = \frac{Q_3 - Q_1}{2} = \frac{88 - 68}{2}$$

$$= 10$$

$$\text{coeff. of } Q.D = \frac{20}{156} \\ = 0.13$$

Calculate interquartile range, quartile deviation  
and coeff. of quartile deviation from the  
following

Size $x$	0-10	10-20	20-30	30-40	40-50	50-60
Frequency	9	15	29	24	3	20
Cumulative Frequency	9	24	53	77	80	100

$$Q_1 = \frac{100}{4}$$

$$Q_3 = \frac{3 \times 100}{4}$$

$$Q_1 = 25$$

$$Q_3 = \frac{300}{4} = 75$$

$$\therefore Q_1 = 53$$

$$\therefore Q_3 = 77$$

$$Q_1 = l_1 + \left[ \frac{\left( \frac{N}{4} \right) - c \right]}{f} (l_2 - l_1)$$

$$= 20 + \left[ \frac{\left( \frac{100}{4} \right) - 24}{29} \right] (30 - 20)$$

$$= 20 + \frac{[25 - 24]}{29} 10$$

$$= 20 + \frac{10}{29}$$

$$Q_1 = 20 + 0.34$$

$$Q_1 = 20.34$$

$$Q_3 = 30 + \left[ \frac{3(25) - 53}{24} \right] (40 - 30)$$

$$= 30 + \left( \frac{22}{24} \right) 10$$

$$= 30 + 39.17$$

$$= 59.17$$

$$\text{Interquartile Range} = Q_3 - Q_1$$

$$= 39.17 - 20.34$$

$$= 18.83$$

Quantile Deviation =  $\frac{Q_3 - Q_1}{Q_3 + Q_1}$

$$= \frac{18.83}{2}$$

$$\boxed{Q.D = 9.42 //}$$

Coeff. of Q.D =  $\frac{Q_3 - Q_1}{Q_3 + Q_1}$

$$= \frac{18.83}{59.51}$$

$$= 0.32 //$$

Find interquartile range, Quantile deviation  
and coefficient for the following:

Class Interval	10-15	15-20	20-25	25-30	30-40	40-50
Frequency	4	12	16	22	10	8
Cumulative Frequency	4	16	32	54	64	72

50-60	60-70
6	4
78	82

$$Q_1 = \frac{82}{4}$$

$$= 20.50$$

$$Q_3 = 3 \times 20.50$$

$$Q_3 = 61.50$$

$$\therefore Q_1 = 32$$

$$\therefore Q_3 = 64$$

$$Q_1 = 20 + \left[ \frac{20.50 - 20}{16} \right] 5$$

$$= 20 + 0.28 \times 5$$

$$= 20 + 1.40$$

$$Q_1 = 21.40$$

$$Q_3 = 30 + \left[ \frac{61.50 - 30}{10} \right] 10$$

$$= 30 + 7.50$$

$$Q_3 = 37.50$$

$$\text{Quartile Deviation} = \frac{Q_3 - Q_1}{2}$$

$$= \frac{37.50 - 21.40}{2}$$

$$= 8.05$$

Interquartile Range =  $Q_3 - Q_1$

$$= 37.50 - 21.40$$

$$= 16.10 //$$

Coeff of Q.D =  $\frac{Q_3 - Q_1}{Q_3 + Q_1}$

$$= \frac{16.10}{58.90}$$

$$= 0.27 //$$

Calculate the quartile deviation of the following 39 students in Statistics given:

Marks	0 - 5	5 - 10	10 - 15	15 - 20	20 - 25	25 - 30	30 - 35
No. of students	4	6	8	12	7	2	1
Cumulative frequency	4	10	18	30	37	39	

$$Q_1 = \frac{39}{4} \\ = 9.75$$

$$Q_3 = 3 \times 9.75 \\ = 29.25$$

$$Q_1 = 10$$

$$Q_3 = 30$$

$$Q_1 = 5 + \left[ \frac{9.75 - 4}{6} \right] \times 5$$

$$= 5 + \frac{5.75}{6} \times 5$$

$Q_1 = 9.79$

//

$$Q_3 = 15 + \left[ \frac{3 \times \frac{39}{4} - 18}{12} \right] \times 5$$

$$= 15 + \frac{29.25 - 18}{12} \times 5$$

$$= 15 + \frac{11.25}{12} \times 5$$

$$= 15 + 4.69$$

$$Q_3 = 19.69 \quad //$$

$$\text{Quartile Deviation} = \frac{Q_3 - Q_1}{2}$$

$$= \frac{19.69 - 9.79}{2}$$

$$Q.D = 4.95 \quad //$$

$$\text{Interquartile Range} = Q_3 - Q_1$$

$$= 9.90 \quad //$$

Coefficient of Quartile Deviation :

$$\Rightarrow \frac{Q_3 - Q_1}{Q_3 + Q_1}$$

$$= \frac{9.90}{29.48}$$

$$= 0.34 \quad //$$

### STANDARD DEVIATION:

It is the root mean square deviation of the values from arithmetic mean.  $SD \rightarrow \sigma$

The square of SD is called variance

### For RAW DATA:

$$\sigma = \sqrt{\frac{\sum(x - \bar{x})^2}{n}}, \quad \bar{x} = \frac{\sum x}{n}$$

### For DISCRETE DATA

$$\sigma = \sqrt{\frac{\sum f(x - \bar{x})^2}{\sum f}}, \quad \bar{x} = \frac{\sum fx}{\sum f}$$

### CONTINUOUS DATA:

$$\sigma = \sqrt{\frac{\sum f(x - \bar{x})^2}{\sum f}}, \quad \bar{x} = \frac{\sum fx}{\sum f}$$

### COMBINED STD DEVIATION:

Calculating std deviation of 2 or more series.

$$\sigma_{12} = \sqrt{\frac{N_1 \sigma_1^2 + N_2 \sigma_2^2 + N_1 d_1^2 + N_2 d_2^2}{N_1 + N_2}}$$

$\sigma_{1,2}$  - Combined std deviation of 2 groups

$\sigma_1$  - std deviation of 1st group

$\sigma_2$  - std deviation of 2nd group.

$\bar{x}_{1,2}$  = Combined Arithmetic Mean of two groups

$$\bar{x}_{1,2} = \frac{N_1 \bar{x}_1 + N_2 \bar{x}_2}{N_1 + N_2}$$

$\bar{x}_1$  = Arithmetic Mean of 1st group

$\bar{x}_2$  = Arithmetic Mean of 2nd group

$N_1$  = No. of observation in the 1st grp

$N_2$  = No. of observation in 2nd group.

Find the mean and std deviation for the following data 75, 73, 70, 77, 72, 75, 76, 72, 74, 76.

$$\bar{x} = \frac{\sum x}{n}$$

$$= \frac{74}{10}$$

$$= 74$$

$x$	$d = x - \bar{x}$	$d^2 = (x - \bar{x})^2$
75	1	1
73	-1	1
70	-4	16
77	3	9
72	-2	4
75	1	1
76	2	4
72	-2	4
74	0	0
76	2	4

$$S.D = \sqrt{\frac{\sum (x - \bar{x})^2}{n}}$$

no. of no. points = 10

$$S.D = \sqrt{\frac{44}{10}} = \sqrt{4.4} = 2.010$$

$S.D = 2.010$

Find mean and std deviation of

Class	0-10	10-20	20-30	30-40	40-50
Frequency	15	18	14	40	13

Class	x	f	fx	$(x - \bar{x})^2$	$f(x - \bar{x})^2$
0-10	5	15	75	475.24	7128.60
10-20	15	18	270	139.24	2506.32
20-30	25	14	350	3.24	45.36
30-40	35	40	1400	67.24	2689.60
40-50	45	13	585	831.24	4306.12

$$\bar{x} = \frac{\sum f(x)}{\sum f} = \frac{2680}{100}$$

$$\bar{x} = 26.80$$

$$\sigma = \sqrt{\frac{\sum f(x - \bar{x})^2}{\sum f}}$$

$$= \sqrt{\frac{166.76}{100}}$$

$$= \sqrt{166.76}$$

$$\boxed{\sigma = 12.91}$$

Series A	53	54	32	30	60	46	28	35
Series B	55	41	48	49	27	25	23	25
48	72							
28	60							

$$\bar{x}_1 = \frac{\sum x_1}{N_1} = \frac{448}{10}$$

$$\boxed{\bar{x}_1 = 44.80}$$

$$\bar{x}_2 = \frac{376}{10}$$

$$\boxed{\bar{x}_2 = 37.60}$$

$$\bar{x}_{1,2} = \frac{N_1 \bar{x}_1 + N_2 \bar{x}_2}{N_1 + N_2}$$

$$= \frac{448 + 376}{20}$$

$$\boxed{\bar{x}_{1,2} = 41.20}$$

	$d = (x - \bar{x})^2$		$d = (x - \bar{x})^2$
53	67.24	55	302.76
54	84.64	41	11.56
32	163.84	48	108.16
30	219.04	49	129.96
60	231.04	27	112.36
46	1.44	25	158.76
28	282.24	23	213.16
25	392.04	20	309.76
48	10.24	28	92.16
72	739.84	60	501.76

Mean ad  $\sigma_1^2 = \frac{1}{10} \sum d_i^2$  for  $\sigma_1$  to find  $\sigma_1 = \sqrt{\frac{1}{10} \sum d_i^2}$

$\sigma_1 = \sqrt{\frac{2191.6}{10}}$   $\sigma_2 = \sqrt{\frac{1940.4}{10}}$

$\sigma_1 = 219.16$   $\sigma_2 = 194.04$

$b_{d_2}^2 = (\bar{x}_2 - \bar{x}_1)^2 = (446.80 - 41.29)^2 = 12.96$   $b_{d_2} = \sqrt{12.96} = 12.96$

$b_{d_2}^2 = (\bar{x}_2 - \bar{x}_1)^2 = (37.60 - 41.2)^2 = 12.96$

$\sigma_{1,2}^2 = \frac{10 \times 219.16 + 10 \times 194.04 + 10 \times 12.96 + 10 \times 12.96}{20}$

$= \frac{4391.20}{20}$

$\sigma_{1,2} = \sqrt{219.560}$

## Coefficient Of Variation :

$$\text{Coff of variation} = \frac{\sigma}{\text{mean}} \times 100$$

The measures of dispersion are expressed in the same units as original observation and are called absolute variability. These values cannot be used to compare two or more distribution given in different units. In such cases the relative measures of variability can be used which are independent of units of measurement.

Find the coefficient of variation for the following data.

Weight	Frequency	$x$	$fx$	$d$	$f(x-\bar{x})^2$
110 - 119	5	114.5	572.25	1122.25	5611.25
120 - 129	7	124.5	871.5	552.25	3865.75
130 - 139	12	134.5	1614.00	182.25	2187
140 - 149	20	144.5	2890	12.25	245
150 - 159	16	154.5	2472	42.25	676
160 - 169	10	164.5	1645	272.25	2722.5
170 - 179	7	174.5	1221.5	702.25	4915.75
180 - 189	3	184.5	553.5	1382.25	3996.75

$$\text{Mean} = \bar{x} = \frac{\sum f(x)}{\sum f}$$

$$= \frac{11840}{80}$$

$$\boxed{\bar{x} = 148}$$

$$\begin{aligned} \sigma &= \sqrt{\frac{\sum f(x^2) - (\sum f(x))^2}{\sum f}} \\ &= \sqrt{\frac{24220}{80}} \\ &= \sqrt{302.75} \end{aligned}$$

$$= 17.4$$

$$\text{Coeff of variation} = \frac{17.4}{148} \times 100$$

$$= 11.75 //$$

From the data given below which series is more variable (use S.D.).

Variable	f of Series A	f of Series B	x	$f_x A$	$f_x B$
10 - 20	10	18	5	150	270
20 - 30	18	22	25	450	550
30 - 40	32	40	35	1120	1400
40 - 50	40	32	45	1800	1440
50 - 60	22	18	55	1210	990
60 - 70	18	10	65	1170	650

$\rightarrow$  10 - 80

$$\bar{x}_A = \frac{\sum f x_A}{\sum f_A}$$

$$= \frac{5900}{140}$$

$$\bar{x}_A = 42.14$$

$$\bar{x}_B = \frac{\sum f_B}{\sum f_B}$$

$$= \frac{5300}{140}$$

$$\bar{x}_B = 37.85$$

$d_A = (x - \bar{x})^2$	$d_B = (x - \bar{x})^2$	$f(x - \bar{x})^2$	$f(x - \bar{x})^2$
736.57	522.12	7365.7	9398.16
293.78	165.12	5288.04	3632.64
50.98	8.12	1681.04	824.8
8.18	51.12	327.2	1635.84
165.88	594.12	3638.36	5294.16
522.58	787.12	9406.44	7371.2

$$\sigma_A = \sqrt{\frac{27656.78}{140}}$$

$$= \sqrt{197.54}$$

$$\boxed{\sigma_A = 140.5}$$

$$\sigma_B = \sqrt{\frac{27656.8}{140}}$$

$$= \sqrt{197.54}$$

$$\boxed{\sigma_B = 14.0}$$

$$\text{Coff of variation} = \frac{14.0}{37.85} \times 100$$

$$37.0 \quad 78.0 \quad 100 = 37 \text{ or } 36.9 \text{ (approx.)}$$

Calculate appropriate measure of dispersion

Wages in Rs per week	No. of earners	Wage
less than 35	14	
35 - 37	62	
38 - 40	99	
41 - 43	18	
Over 43	7.	

Sol:

Wages per week	x	f	$f_x$	$x - \bar{x}$	$(x - \bar{x})^2$	$f(x - \bar{x})^2$
32.5	34.5 33.0	14	462	-5.13	26.32	368.48
34.5-37.5	36 37.5	62	2232	-2.13	4.54	281.48
37.5-40.5	39 40.5	99	3861	0.87	0.76	75.24
40.5-43.5	42 43.5	18	756	3.87	14.98	269.64
43.5-46.5	45	7	313	6.87	47.22	330.94
						1325.88

$$\bar{x} = \frac{\sum f_x}{\sum x} = \frac{7626}{200} = 36.13.$$

$$G = \sqrt{\frac{1325.88}{200}} = 2.58 \text{ rupees}$$

Prob 2:

Find std deviation.

Height in inches

No. of students

Over 60 but not more than 62 25

" 62 84 27

" 64 " 66 20

" 66 " 68 13

" 68 " 70 5

100

Sol:

Class Interval	frequency	Mid (x)	$f(x - \bar{x})^2$	$\sum f(x - \bar{x})^2$
60 - 62	25	61	2135	6.3504 $\frac{222}{262}$
62 - 64	27	63	1701	0.2764 $\frac{7.302}{262}$
64 - 66	20	65	1300	2.1904 $\frac{4380}{262}$
66 - 68	13	67	871	12.1164 $\frac{157.43}{262}$
68 - 70	5	69	345	30.030 $\frac{150.15}{262}$

$$\bar{x} = \frac{\sum fx}{\sum f} = \frac{6352}{100} = 63.5$$

$$s = \sqrt{\frac{\sum f(x - \bar{x})^2}{\sum f}} = \sqrt{\frac{580.96}{100}} = 2.4103$$

## BIVARIATE DATA:

### Summarization Of Data:

#### 1. TYPES OF DATA

Quantitative

- Discrete
- Continuous

QUALITATIVE

- Nominal
- Ordinal

#### 2. DATA COLLECTION METHOD

- Survey & Questionnaires
- Experiments
- Observational Studies
- Interviews
- Secondary data source.

#### 3. DATA SUMMARIZATION TECHNIQUES:

Tabular

Graphical

Numerical

Mean, median, Mode

Range, Variance, Std deviation

#### 4. DATA DISTRIBUTION

#### 5. BIVARIATE AND MULTIVARIATE

Correlation

Covariance

Scatterplots

Principal Component (PCA)

Multiple

Regression Models

## 6. DATA CLEANING & PROCESSING

### Handle Missing Values

## 7. DESCRIPTIVE VS INFERENTIAL STATISTICS

### Data Conclusion

Summarize

Present Data

Bivariate data analyze defined as

the relation b/w two variables  
often represented graphically as a  
scatter plot. It helps to determine

the correlation b/w two variables.

### SCATTER PLOT

It is commonly used to visualize  
relation  
bivariate data represents  
b/w the data variables on x axis  
in y axis.

### FREQUENCY DISTRIBUTION

The No. of times the value

of x repeated in a distribution.

1. The No. of calls from motorists per day for road side service was recorded from the month of Dec 2024, follows
- The result were as follows
- 28, 122, 217, 130, 120, 86, 80, 90, 120, 140, 70, 40, 145, 187, 133, 90, 68, 174, 194, 170, 100, 75, 104, 97, 75, 123, 100, 82, 109, 120, 80.
- Find the frequency distribution.

Smallest value  $\rightarrow$  28

Largest value  $\rightarrow$  217

Diff  $\rightarrow$  189

$$\text{Class} = \frac{189}{5} = 37.8$$

Let us fix class width as 40.

Frequency

0 - 40	8
41 - 80	5
81 - 120	14
121 - 160	5
161 - 200	4
201 - 240	1

2. Consider the dataset of blood groups of 20 blood donate in blood donation camp.
- D, A, A, A, AB, B, O, AB, B, O, AB, A, B, B, O, B, A, A, AB, A

Construct a frequency distribution for the above data set.

Blood	Frequency
O	4
A	7
B	5
AB	4

3. Find relative frequency and percentage frequency of a class interval table.

Mark Obtained	No. of students	Relative Freq	% Freq
20 - 40	6	$6/25 = 0.24$	$0.24 \times 100$ 24
40 - 60	12	0.48	48
60 - 80	4	0.160	16
80 - 100	3	0.12	12
	25		

### LINEAR REGRESSION MODEL:

Regression Analysis is a measure to analyse the correlation (relation b/w 2 or more variables) in terms of the original units of the data.

Regression lines are the lines of best fit as a straight line.

A linear regression model is a statistical model that examines the relationship between 2 or more variables by fitting a linear equation to the observed data.

$$y = ax + b$$

$y \rightarrow$  dependent variable

$x \rightarrow$  independent variable

$a, b \rightarrow$  correlation variable.

1. Construct a scatter plot for the data shown

Company	Cars	Review
A	63.0	7
B	29.0	3.9
C	20.8	0.1
D	19.1	2.8
E	13.4	1.4
F	8.5	1.5

