#### UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS

GCE Advanced Subsidiary Level and GCE Advanced Level

# MARK SCHEME for the May/June 2012 question paper for the guidance of teachers

## 9709 MATHEMATICS

9709/22

Paper 2, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

• Cambridge will not enter into discussions or correspondence in connection with these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2012 question papers for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.

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### **Mark Scheme Notes**

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
  B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

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The following abbreviations may be used in a mark scheme or used on the scripts:

AEF	Any Equivalent Form (of answer is equally acceptable)
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
CWO	Correct Working Only - often written by a 'fortuitous' answer
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
sos	See Other Solution (the candidate makes a better attempt at the same question)
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

## **Penalties**

- MR -1 A penalty of MR -1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR-2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA -1 This is deducted from A or B marks in the case of premature approximation. The PA -1 penalty is usually discussed at the meeting.

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- State or imply non-modular inequality  $(x + 3)^2 < (2x + 1)^2$  or corresponding equation 1 Either: or pair of linear equations **B**1 Attempt solution of 3-term quadratic or of 2 linear equations M1Obtain critical values  $-\frac{4}{3}$  and 2 A1 State answer  $x < -\frac{4}{3}$ , x > 2A<sub>1</sub> Or: Obtain critical value x = 2 from graphical method, inspection, equation **B**1 Obtain critical value  $x = -\frac{4}{3}$  similarly B2 State answer  $x < -\frac{4}{3}, x > 2$ B1 [4] State or imply equation in the form  $(5^x)^2 + 5^x - 12 = 0$ 2 **B**1 Attempt solution of quadratic equation for  $5^x$ M1Obtain  $5^x = 3$  only **A**1 [3] (ii) Use logarithms to solve equation of the form  $5^x = k$  where k > 0M1 [2] **Obtain 0.683** A<sub>1</sub> 3 (i) Attempt division, or equivalent, at least as far as quotient 2x + kM1 Obtain quotient 2x - 3**A**1 Complete process to confirm remainder is 4 A<sub>1</sub> [3] (ii) State or imply  $(4x^2 + 4x - 3)$  is a factor **B**1 Obtain (2x-3)(2x-1)(2x+3)**B**1 [2] 4 State or imply R = 15**B**1 Use appropriate formula to find  $\alpha$ M1 Obtain 53.13° **A**1 [3] (ii) Attempt to find at least one value of  $\theta - \alpha$ M1Obtain one correct value 68.6° of  $\theta$ **A**1 Carry out correct method to find second answer M1 Obtain 217.7° and no others in range **A**1 [4] B1√ (iii) State 15, following their value of R from part (i) [1] (i) State  $\frac{dx}{dt} = \frac{1}{t+1}$ B1 State  $\frac{dy}{dt} = 2e^{2t} + 2$ B1
  - Attempt expression for  $\frac{dy}{dx}$ M1

Obtain  $\frac{dy}{dx} = (2e^{2t} + 2)(t+1)$  or equivalent A<sub>1</sub> [4]

(ii) Substitute t = 0 and attempt gradient of normal M1Obtain  $-\frac{1}{4}$  following their expression for  $\frac{dy}{dx}$ A1√ Attempt to find equation of normal through point (0, 1)M1Obtain x + 4y - 4 = 0[4] A1

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(i)	_			M1 A1	
	Equate nu	imerator to zero and attempt rearrangement		M1 A1	[4]
(ii)				M1 A1	[2]
(iii)	Obtain fir	nal answer 0.694	now a sign change ir	M1 A1	
	the interv $[0.6 \rightarrow 0.65 \rightarrow 0.65 \rightarrow 0.65]$	al $(0.6935, 0.6945)$ $0.69040 \rightarrow 0.69352 \rightarrow 0.69363$ $0.69215 \rightarrow 0.69358 \rightarrow 0.69363$	5 5	A1	[3]
(i)	_	· · · · · · · · · · · · · · · · · · ·		B1 M1	
	Attempt i Obtain ta Use limit	ntegration of expression $\ln x + \frac{1}{4}\sin 2x - \frac{1}{2}x$ s correctly for integral involving at least $\tan x$ and $\sin 2x$		A1 M1 A1 M1 A1	[7]
(ii)	State or in Attempt e Integrate	mply volume is $\int \pi (\tan x + \cos x)^2 dx$ expansion and simplification to obtain one term of form $k \cos x$		B1 M1 M1	[4]
	(i) (ii) (i)	<ul> <li>(i) Attempt to Obtain 2/2. Equate not Confirm §</li> <li>(ii) Consider Obtain -2</li> <li>(iii) Use iterate Obtain find Show suff the interveron [0.6 → 0.065 → 0.7 → 0]</li> <li>(i) Replace to Express confidence of Obtain gind Attempt in Obtain the Use limite Obtain 5/4</li> <li>(ii) State or in Attempt of Integrate</li> </ul>	<ul> <li>(i) Attempt use of quotient rule or equivalent Obtain  \$\frac{2(x+2)\cos 2x - \sin 2x}{(x+2)^2}\$ or equivalent Equate numerator to zero and attempt rearrangement Confirm given result tan 2x = 2x + 4</li> <li>(ii) Consider sign of tan 2x - 2x - 4 for 0.6 and 0.7 or equivalent Obtain -2.63 and 0.40 or equivalents and justify conclusion</li> <li>(iii) Use iteration process correctly at least once Obtain final answer 0.694 Show sufficient iterations to 5 decimal places to justify answer or sh the interval (0.6935, 0.6945) [0.6 → 0.69040 → 0.69352 → 0.69363 0.65 → 0.69215 → 0.69358 → 0.69363 0.7 → 0.69384 → 0.69364 → 0.69363]</li> </ul>	<ul> <li>(i) Attempt use of quotient rule or equivalent Obtain  <sup>2(x+2)\cos 2x - \sin 2x</sup>/(x+2)<sup>2</sup> or equivalent (x+2)<sup>2</sup> Equate numerator to zero and attempt rearrangement Confirm given result tan 2x = 2x + 4</li> <li>(ii) Consider sign of tan 2x - 2x - 4 for 0.6 and 0.7 or equivalent Obtain -2.63 and 0.40 or equivalents and justify conclusion</li> <li>(iii) Use iteration process correctly at least once Obtain final answer 0.694 Show sufficient iterations to 5 decimal places to justify answer or show a sign change in the interval (0.6935, 0.6945) [0.6 → 0.69040 → 0.69352 → 0.69363 0.65 → 0.69215 → 0.69358 → 0.69363 0.7 → 0.69384 → 0.69364 → 0.69363]</li> <li>(i) Replace tan² x by sec² x - 1 Express cos² x in the form ±½±½cos2x Obtain given answer sec² x +½cos2x -½ correctly Attempt integration of expression Obtain tan x +¼sin 2x -½x Use limits correctly for integral involving at least tan x and sin 2x Obtain  5/4 - 1/8 π or exact equivalent</li> <li>(ii) State or imply volume is ∫π(tan x + cos x)² dx Attempt expansion and simplification Integrate to obtain one term of form k cos x</li> </ul>	(i)Attempt use of quotient rule or equivalentM1Obtain $\frac{2(x+2)\cos 2x - \sin 2x}{(x+2)^2}$ or equivalentA1Equate numerator to zero and attempt rearrangementM1Confirm given result $\tan 2x = 2x + 4$ M1(ii)Consider sign of $\tan 2x - 2x - 4$ for 0.6 and 0.7 or equivalent Obtain $-2.63$ and 0.40 or equivalents and justify conclusionM1(iii)Use iteration process correctly at least once Obtain final answer 0.694 Show sufficient iterations to 5 decimal places to justify answer or show a sign change in the interval $(0.6935, 0.6945)$ $[0.6 \rightarrow 0.69040 \rightarrow 0.69352 \rightarrow 0.69363$ $0.7 \rightarrow 0.69344 \rightarrow 0.69358 \rightarrow 0.69363$ A1(i)Replace $\tan^2 x$ by $\sec^2 x - 1$ Express $\cos^2 x$ in the form $\pm \frac{1}{2} \pm \frac{1}{2} \cos 2x$ Obtain given answer $\sec^2 x + \frac{1}{2} \cos 2x - \frac{1}{2}$ correctly Attempt integration of expression Obtain $\tan x + \frac{1}{4} \sin 2x - \frac{1}{2} x$ Use limits correctly for integral involving at least $\tan x$ and $\sin 2x$ Obtain $\frac{5}{4} - \frac{1}{8} \pi$ or exact equivalentM1(ii)State or imply volume is $\int \pi(\tan x + \cos x)^2 dx$ Attempt expansion and simplification Integrate to obtain one term of form $k \cos x$ M1