



Cambridge International Examinations

Cambridge International Advanced Subsidiary and Advanced Level

CANDIDATE NAME										
CENTRE NUMBER						CANDIDATE NUMBER				
MATHEMATICS									97	09/12
Paper 1 Pure M	athematics	1 (P1)					Febi	ruary/l	March	າ 2017
							1	hour	45 mi	nutes
Candidates ansv	wer on the	Question	Paper.							
Additional Materials: List of Formulae (MF9)										

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

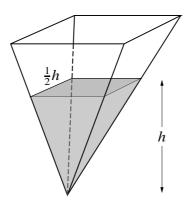
The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 75.



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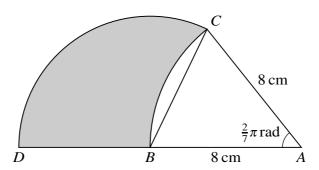
The diagram shows a water container in the form of an inverted pyramid, which is such that when the height of the water level is h cm the surface of the water is a square of side $\frac{1}{2}h$ cm.

(i)	Express the volume of water in the container in terms of h .	[1]
	[The volume of a pyramid having a base area A and vertical height h is $\frac{1}{3}Ah$.]	
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Water is steadily dripping into the container at a constant rate of $20\,\mathrm{cm}^3$ per minute.

	nd the rate, in cm per minute, at which the water level is rising when the height of the wavel is 10 cm.
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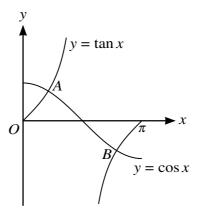
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In the diagram, AB = AC = 8 cm and angle $CAB = \frac{2}{7}\pi$ radians. The circular arc BC has centre A, the circular arc CD has centre B and ABD is a straight line.

(i)	Show that angle $CBD =$	$\frac{9}{14}\pi$ radians.			[1]
			•••••	 	

Find the perimeter of the shaded region.	[5



The diagram shows the graphs of $y = \tan x$ and $y = \cos x$ for $0 \le x \le \pi$. The graphs intersect at points A and B.

(i)	Find by calculation the x -coordinate of A .	[4]
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(ii)	Find by calculation the coordinates of B . [3]

6	Relative to an or	rigin O , the	position	vectors of the	points A	and B	are given	by
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$\overrightarrow{OA} = 2\mathbf{i} + 3\mathbf{j}$	i + 5k	and	$\overrightarrow{OB} = 7\mathbf{i} + 4\mathbf{j} + 3\mathbf{j}$	k
$O_1 - 21 + 3$	$\top J \mathbf{K}$	and	OD = II + II + J	\mathbf{r}

Use a scalar product to find angle <i>OAB</i> .	[5]

Find the area of triangle <i>OAB</i> .	[2]

function f is defined for $x \ge 0$ by $f(x) = (4x + 1)^{\frac{3}{2}}$.	
Find $f'(x)$ and $f''(x)$.	[3]
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first, second and third terms of a geometric progression are respectively $f(2)$, $f'(2)$ and $kf''(2)$	(2).
Find the value of the constant k .	[5]
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	Find f'(x) and f"(x). first, second and third terms of a geometric progression are respectively f(2), f'(2) and kf"(

8	The functions	f and	g are define	d for $x \ge 0$ by
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$$f: x \mapsto 2x^2 + 3$$
,
 $g: x \mapsto 3x + 2$.

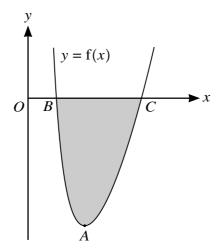
Show that $gf(x) = 6x^2 + 11$ and obtain an unsimplified expression for $fg(x)$.	[2]
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Find an expression for $(fg)^{-1}(x)$ and determine the domain of $(fg)^{-1}$.	[5]
	•••••
	••••••
	Find an expression for $(fg)^{-1}(x)$ and determine the domain of $(fg)^{-1}$.

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(iii)	Solve the equation $gf(2x) = fg(x)$.	3]
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(i)	Find the equation of the tangent to the curve at <i>A</i> .	
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he	normal to the curve at A intersects the curve again at B .	
ii)	Find the coordinates of <i>B</i> .	
		•••••

The	tangents at A and B intersect each other at C .
(iii)	Find the coordinates of C . [4]

10



The diagram shows the curve y = f(x) defined for x > 0. The curve has a minimum point at A and crosses the x-axis at B and C. It is given that $\frac{dy}{dx} = 2x - \frac{2}{x^3}$ and that the curve passes through the point $\left(4, \frac{189}{16}\right)$.

(i)	Find the x -coordinate of A .	[2]
(ii)	Find $f(x)$.	[3]

(iii)	Find the x -coordinates of B and C . [4]

[Question $10 \, (iv)$ is printed on the next page.]

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