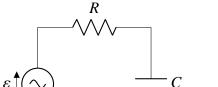
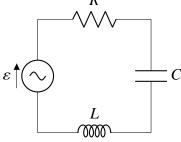
## 1

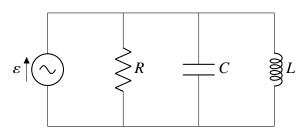
## NCERT ANALOG 12.7.17

## MANOJ KUMAR (EE23BTECH11211)

Question 17: Keeping the source frequency equal to the resonating frequency of the series LCR circuit, if the three elements, L, C, and R are arranged in parallel, show that the total current in the parallel LCR circuit is minimum at this frequency. Obtain the current rms value in each branch of the circuit for the elements and source specified in Exercise 7.11 for this frequency  $\varepsilon = 230V, L = 5.0H, C = 80\mu F, R = 40\Omega$ 



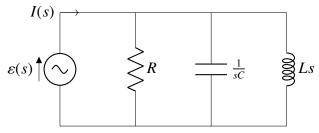




**Solution:** 

Symbol	Value	Description
L	50H	Inductance
С	$80\mu F$	Capacitance
R	40Ω	Resistance
ε	230 V	Voltage source
$\omega_0$	$\frac{1}{\sqrt{LC}}$	Resonant Angular Frequency
$I_R$	5.75A	Rms current value in Resistance
$I_L$	0.92A	Rms current value in Inductor
$I_C$	0.92A	Rms current value in Capacitor

TABLE 1: Input Parameter



The impedance of the circuit is.

$$\frac{1}{z} = \frac{1}{R} + sC + \frac{1}{Ls} \tag{1}$$

$$I(s) = V(s) \left(\frac{1}{R} + sC + \frac{1}{Ls}\right) \tag{2}$$

At resonance, the circuit becomes purely resistive The admittance of capacitor and inductor cancel out as follows:

$$sC + \frac{1}{Ls} = 0 \tag{3}$$

$$\implies s = j \frac{1}{\sqrt{LC}} \tag{4}$$

s can be expressed in terms of angular resonance frequency as

$$s = j\omega_0 \tag{5}$$

Comparing (4) and (5), we get

$$\omega_0 = \frac{1}{\sqrt{LC}} \tag{6}$$

Plot of Impedance vs Angular Frequency Impedance is defined as

$$H(s) = \frac{V(s)}{I(s)} \tag{7}$$

Using (5),

$$H(s) = \frac{1}{\frac{1}{R} + sC + \frac{1}{Ls}}$$
 (8)

$$\implies H(j\omega) = \frac{1}{\frac{1}{R} + j\omega C + \frac{1}{i\omega L}}$$
 (9)

$$\implies |H(j\omega)| = \frac{1}{\sqrt{\frac{1}{R^2} + \left(\omega C - \frac{1}{\omega L}\right)^2}} \tag{10}$$

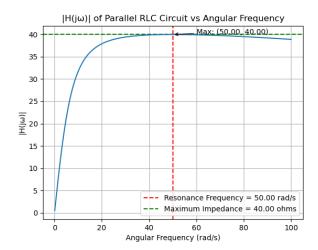


Fig. 0: Maximum impedance at resonating frequency in parallel RLC circuit

Hence it is proved that in parallel RLC circuit the total current is minimum at resonance frequency (b)

At resonance frequency, Rms currents are

$$\omega_0 = \frac{1}{\sqrt{LC}} = 50 rad/s \tag{11}$$

$$I_L = \frac{V}{\omega_0 L} = \frac{230}{250} = 0.92A \tag{12}$$

$$I_C = \omega_0 CV = 0.92A \tag{13}$$

$$I_R = \frac{V}{R} = \frac{230}{40} = 5.75A \tag{14}$$