

Package ‘VEMIRT’

July 3, 2024

Type Package

Title Variational Expectation Maximization for High-Dimensional IRT Models

Version 2.0

Date 2024-07-03

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Description

VEMIRT is created to assist researchers in conducting high-dimensional exploratory and confirmatory multidimensional item response theory (MIRT) analysis and corresponding differential item functioning (DIF) analysis. The core computation engine of VEMIRT is a family of Gaussian Variational EM algorithms that are considerably more efficient than currently available algorithms in other statistical packages, especially when the number of latent factors exceeds four.

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Imports abind,

GPArotation,

MASS,

Matrix,

mirt,

mvQuad,

mvnfast,

polycor,

psych,

Rcpp,

RcppArmadillo,

testit,

tibble,

torch

LinkingTo Rcpp, RcppArmadillo, RcppEigen

Encoding UTF-8

Depends R (>= 3.10)

LazyData true

RoxygenNote 7.3.1

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VEMIRT-package

VEMIRT: A package for high-dimensional IRT models

Description

VEMIRT is created to assist researchers to conduct exploratory and confirmatory multidimensional item response theory (MIRT) analysis and coresponding item differential functioning (DIF) analysis. The core computation engine of VEMIRT is a family of Gaussian Variational EM algorithms that are considerably more efficient than currently available algorithms in other software packages, especially when the number of latent factors exceeds four.

Identifying the number of factors

[pa_poly](#) identifies the number of factors via parallel analysis.

Exploratory factor analysis

- [E2PL_gvem_rot](#) conducts M2PL Analysis with post-hoc rotation (Promax & CF-Quartimax)
- [E2PL_gvem_lasso](#) conducts M2PL Analysis with Lasso penalty
- [E2PL_gvem_adaptlasso](#) conducts M2PL Analysis with adaptive Lasso penalty
- [E2PL_iw](#) conducts importance sampling to correct bias for M2PL analysis
- [E3PL_sgvem_rot](#) conducts stochastic GVEM to further improve the computational efficiency for exploratory M3PL analysis

- [E3PL_sgvm_lasso](#) conducts M3PL Analysis with Lasso penalty
- [E3PL_sgvm_adaptlasso](#) conducts M3PL Analysis with adaptive Lasso penalty

Confirmatory factor analysis

- [C2PL_gvem](#) conducts GVEM for confirmatory M2PL analysis
- [C2PL_bs](#) conducts bootstrap sampling to correct bias and produce standard errors for confirmatory M2PL analysis
- [C2PL_iw](#) conducts importance sampling to correct bias for M2PL analysis
- [C3PL_sgvm](#) conducts stochastic GVEM for confirmatory M3PL analysis

Differential item functioning analysis

- [D2PL_em](#) conducts DIF analysis for M2PL models using EM algorithms
- [D2PL_gvem](#) conducts DIF analysis for M2PL models using GVEM algorithms
- [D2PL_lrt](#) conducts DIF analysis for M2PL models using the likelihood ratio test

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C2PL_bs

Bootstrap Version of GVEM Confirmatory Analysis for M2PL

Description

A bootstrap version of GVEM (i.e., GVEM-BS) can be implemented to correct the bias on item parameters and compute standard errors under confirmatory M2PL models

Usage

```
C2PL_bs(gvem_result, boots = 5)
```

Arguments

| | |
|-------------|--|
| gvem_result | a list that includes exploratory or confirmatory GVEM results for M2PL models. |
| boots | the number of bootstrap samples; default is 5 |

Value

a list containing the following objects:

| | |
|---------|---|
| boots_a | item discrimination parameters corrected by bootstrap sampling, a $J \times K$ matrix |
| boots_b | item difficulty parameters corrected by bootstrap sampling, a vector of length J |
| sd_a | standard errors of item discrimination parameters, a $J \times K$ matrix |
| sd_b | standard errors of item difficulty parameters, a vector of length J |

Author(s)

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See Also

[C2PL_gvem](#), [C2PL_iw](#)

Examples

```
## Not run:
gvem_result <- with(C2PL_data, C2PL_gvem(data, model))
C2PL_bs(gvem_result, boots=10)
## End(Not run)
```

C2PL_data

Simulated Data Set for Confirmatory M2PL Analysis

Description

Responses are simulated based on a between-item M2PL model with 5 factors. The true factor correlations are set as 0.1.

Usage

```
C2PL_data
```

Format

A list of components of the data set:

| | |
|--------|--|
| data | Item responses |
| model | Loading indicators |
| params | True parameters used for generating the item responses |

C2PL_gvem

*Confirmatory M2PL Analysis***Description**

Confirmatory M2PL Analysis

Usage

```
C2PL_gvem(u, indic, max.iter = 5000, SE.est = FALSE)
```

Arguments

| | |
|-----------------------|---|
| <code>u</code> | an $N \times J$ matrix or a <code>data.frame</code> that consists of binary responses of N individuals to J items. The missing values are coded as NA |
| <code>indic</code> | a $J \times K$ matrix or a <code>data.frame</code> that describes the factor loading structure of J items to K factors. It consists of binary values where 0 refers to the item is irrelevant with this factor, 1 otherwise |
| <code>max.iter</code> | the maximum number of iterations for the EM cycle; default is 5000 |
| <code>SE.est</code> | whether to estimate SE for item parameters using the updated supplemented expectation maximization (USEM); default is FALSE |

Value

a list containing the following objects:

| | |
|---------------------|--|
| <code>ra</code> | item discrimination parameters, a $J \times K$ matrix |
| <code>rb</code> | item difficulty parameters, vector of length J |
| <code>reta</code> | variational parameters $\eta(\xi)$, a $N \times J$ matrix |
| <code>reps</code> | variational parameters ξ , a $N \times J$ matrix |
| <code>rsigma</code> | population variance-covariance matrix, a $K \times K$ matrix |
| <code>mu_i</code> | mean parameter for each person, a $K \times N$ matrix |
| <code>sig_i</code> | covariance matrix for each person, a $K \times K \times N$ array |
| <code>n</code> | the number of iterations for the EM cycle |
| <code>Q_mat</code> | factor loading structure, a $J \times K$ matrix |
| <code>GIC</code> | model fit index |
| <code>AIC</code> | model fit index |
| <code>BIC</code> | model fit index |
| <code>SE</code> | Standard errors of item parameters, a $J \times (K + 1)$ matrix where the last column includes SE estimates for item difficulty parameters |

Author(s)

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See Also[C3PL_sgvem](#), [C2PL_bs](#), [C2PL_iw](#)

Examples

```
## Not run:
with(C2PL_data, C2PL_gvem(data, model))
## End(Not run)
```

C2PL_iw

Importance Weighted Version of GVEM Analysis for M2PL Models

Description

An importance weighted version of GVEM (i.e., IW-GVEM) can be implemented to correct the bias on item parameters under M2PL models

Usage

```
C2PL_iw(u, gvem_result, S = 10, M = 10, max.iter = 10)
```

```
E2PL_iw(u, gvem_result, S = 10, M = 10, max.iter = 10)
```

Arguments

| | |
|--------------------------|---|
| <code>u</code> | a $N \times J$ matrix or a data.frame that consists of binary responses of N individuals to J items. The missing values are coded as NA |
| <code>gvem_result</code> | a list that includes exploratory or confirmatory GVEM results for M2PL models. |
| <code>S</code> | the number of times to draw samples; default is 10 |
| <code>M</code> | the number of samples drawn from the variational distributions; default is 10 |
| <code>max.iter</code> | the maximum number of iterations for the EM cycle; default is 10 |

Value

a list containing the following objects:

| | |
|---------------------|--|
| <code>ra</code> | item discrimination parameters estimated by GVEM, a $J \times K$ matrix |
| <code>rb</code> | item difficulty parameters estimated by GVEM, vector of length J |
| <code>reta</code> | variational parameters $\eta(\xi)$, a $N \times J$ matrix |
| <code>reps</code> | variational parameters ξ , a $N \times J$ matrix |
| <code>rsigma</code> | population variance-covariance matrix estimated by GVEM, a $K \times K$ matrix |
| <code>mu_i</code> | mean parameter for each person, a $K \times N$ matrix |
| <code>sig_i</code> | covariance matrix for each person, a $K \times K \times N$ array |
| <code>n</code> | the number of iterations for the EM cycle |
| <code>rk</code> | factor loadings, a $J \times K$ matrix, for exploratory analysis only |
| <code>Q_mat</code> | factor loading structure, a $J \times K$ matrix |
| <code>GIC</code> | model fit index |
| <code>AIC</code> | model fit index |
| <code>BIC</code> | model fit index |

| | |
|-----------------|--|
| SE | Standard errors of item parameters, a $J \times (K + 1)$ matrix where the last column includes SE estimates for item difficulty parameters, for confirmatory analysis only |
| ur_a | item discrimination parameters before conducting the rotation, a $J \times K$ matrix, for exploratory analysis only |
| new_a | item discrimination parameters estimated by IW-GVEM, a $J \times K$ matrix |
| new_b | item difficulty parameters estimated by IW-GVEM, vector of length J |
| new_Sigma_theta | population variance-covariance matrix estimated by IV-GVEM, a $K \times K$ matrix |
| best_lr | The learning rate used for importance sampling |
| best_lb | The lower bound value for importance sampling |

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See Also

[C2PL_gvem](#), [E2PL_gvem_rot](#), [C2PL_bs](#)

Examples

```
## Not run:
CFA_result <- with(C2PL_data, C2PL_gvem(data, model))
C2PL_iw(C2PL_data$data, CFA_result)
## End(Not run)
## Not run:
EFA_result <- with(E2PL_data_C1, E2PL_gvem_lasso(data, model, constrain = constrain, non_pen = non_pen))
E2PL_iw(E2PL_data_C1$data, EFA_result)
## End(Not run)
```

| | |
|-----------|--|
| C3PL_data | <i>Simulated Data Set for Confirmatory M3PL Analysis</i> |
|-----------|--|

Description

Responses are simulated based on a within-item M3PL model with 3 factors. The true factor correlations are set as 0.1.

Usage

C3PL_data

Format

A list of components of the data set:

| | |
|-------|--------------------|
| data | Item responses |
| model | Loading indicators |

params True parameters used for generating the item responses

C3PL_sgvm

Stochastic GVEM for Confirmatory M3PL Analysis

Description

Stochastic GVEM for Confirmatory M3PL Analysis

Usage

```
C3PL_sgvm(
  u,
  indic,
  samp = 50,
  forgetrate = 0.51,
  mu_b,
  sigma2_b,
  Alpha,
  Beta,
  max.iter = 5000
)
```

Arguments

| | |
|------------|--|
| u | an $N \times J$ matrix or a data.frame that consists of binary responses of N individuals to J items. The missing values are coded as NA |
| indic | a $J \times K$ matrix or a data.frame that describes the factor loading structure of J items to K factors. It consists of binary values where 0 refers to the item is irrelevant with this factor, 1 otherwise |
| samp | a subsample for each iteration; default is 50 |
| forgetrate | the forget rate for the stochastic algorithm. The value should be within the range from 0.5 to 1. Default is 0.51 |
| mu_b | the mean parameter for the prior distribution of item difficulty parameters |
| sigma2_b | the variance parameter for the prior distribution of item difficulty parameters |
| Alpha | the α parameter for the prior distribution of guessing parameters |
| Beta | the β parameter for the prior distribution of guessing parameters |
| max.iter | the maximum number of iterations for the EM cycle; default is 5000 |

Value

a list containing the following objects:

| | |
|----|---|
| ra | item discrimination parameters, a $J \times K$ matrix |
| rb | item difficulty parameters, vector of length J |
| rc | item guessing parameters, vector of length J |
| rs | variational parameters s , a $N \times J$ matrix |

| | |
|--------|--|
| reta | variational parameters $\eta(\xi)$, a $N \times J$ matrix |
| reps | variational parameters ξ , a $N \times J$ matrix |
| rsigma | population variance-covariance matrix, a $K \times K$ matrix |
| mu_i | mean parameter for each person, a $K \times N$ matrix |
| sig_i | covariance matrix for each person, a $K \times K \times N$ array |
| n | the number of iterations for the EM cycle |
| Q_mat | factor loading structure, a $J \times K$ matrix |
| GIC | model fit index |
| AIC | model fit index |
| BIC | model fit index |

Author(s)

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References

- Cho, A. E., Wang, C., Zhang, X., & Xu, G. (2021). Gaussian variational estimation for multidimensional item response theory. *British Journal of Mathematical and Statistical Psychology*, 74, 52-85.
- Cho, A. E., Xiao, J., Wang, C., & Xu, G. (2022). Regularized Variational Estimation for Exploratory Item Factor Analysis. *Psychometrika*. <https://doi.org/10.1007/s11336-022-09874-6>

See Also

[C2PL_gvem](#)

Examples

```
## Not run:
with(C3PL_data, C3PL_sgvem(data, model, samp=50, forgetrate=0.51, mu_b=0, sigma2_b=4, Alpha=10, Beta=40))
## End(Not run)
```

| | |
|-----------------|---|
| coef.vemirt_DIF | <i>Extract Parameter Estimates from D2PL Analysis</i> |
|-----------------|---|

Description

Extract Parameter Estimates from D2PL Analysis

Usage

```
coef(object, criterion = NULL)
```

Arguments

| | |
|-----------|---|
| object | An object of class vemirt_DIF |
| criterion | Information criterion for model selection, one of 'AIC', 'BIC', 'GIC', or the constant for computing GIC, otherwise use the criterion specified when fitting the model(s) |

Author(s)

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See Also

[em_D2PL](#), [gveem_D2PL](#), [lrt_D2PL](#), [print.vemirt_DIF](#), [summary.vemirt_DIF](#)

| | |
|-----------------------------|--|
| <code>coef.vemirt_FA</code> | <i>Extract Parameter Estimates from Explanatory or Confirmatory Analysis</i> |
|-----------------------------|--|

Description

Extract Parameter Estimates from Explanatory or Confirmatory Analysis

Usage

`coef(object)`

Arguments

`object` An object of class `vemirt_FA`

Author(s)

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See Also

[C2PL_gvem](#), [C2PL_bs](#), [C2PL_iw](#), [C3PL_sgvem](#), [E2PL_gvem_adaptlasso](#), [E2PL_gvem_lasso](#), [E2PL_gvem_rot](#), [E2PL_IS](#), [E3PL_sgvem_adaptlasso](#), [E3PL_sgvem_lasso](#), [E3PL_sgvem_rot](#), [print.vemirt_FA](#)

| | |
|------------------------|---|
| <code>D2PL_data</code> | <i>Simulated Data Set for DIF M2PL Analysis</i> |
|------------------------|---|

Description

Simulated Data Set for DIF M2PL Analysis

Usage

`D2PL_data`

Format

A list of components of the data set:

| | |
|------------|---|
| data | Item responses |
| model | Loading indicators |
| group | Group indicators |
| j | Number of DIF items (the first j items have DIF) |
| params | A list of true parameters used for generating the item responses: |
| ...\$a | Slopes |
| ...\$b | Negated intercepts |
| ...\$theta | Latent traits |

D2PL_em

EM Algorithms for DIF Detection in M2PL Models

Description

EM Algorithms for DIF Detection in M2PL Models

Usage

```
D2PL_em(
  data,
  model = matrix(1, ncol(data)),
  group = rep(1, nrow(data)),
  method = "EMM",
  Lambda0 = if (length(unique(group)) == 1) 0 else seq(0.2, 0.8, by = 0.1),
  level = 10,
  criterion = "BIC",
  iter = 200,
  eps = 0.001,
  c = 1
)
```

Arguments

| | |
|-------|--|
| data | An $N \times J$ binary matrix of item responses (missing responses should be coded as NA) |
| model | A $J \times K$ binary matrix of loading indicators (all items load on the only dimension by default) |
| group | An N dimensional vector of group indicators from 1 to G (all respondents are in the same group by default) |

| | |
|-----------|--|
| method | Estimation algorithm, one of 'EM' or 'EMM' |
| Lambda0 | A vector of lambda0 values for L_1 penalty (lambda equals $\sqrt{N} * \text{lambda0}$) |
| level | Accuracy level, either a number for mvQuad or a vector indicating the grid for each latent dimension |
| criterion | Information criterion for model selection, one of 'BIC' (recommended), 'AIC', or 'GIC' |
| iter | Maximum number of iterations |
| eps | Termination criterion on numerical accuracy |
| c | Constant for computing GIC |

Value

An object of class vemirt_DIF, which is a list containing the following elements:

| | |
|--------------|--|
| N | Number of respondents |
| niter0 | Number(s) of iterations for initialization |
| fit | The best (with lowest information criterion) model, which is an element of all |
| best | The index of fit in all |
| all | A list of models which has the same length as Lambda0: |
| ...\$lambda0 | Corresponding element in Lambda0 |
| ...\$lambda | $\sqrt{N} * \text{lambda0}$ |
| ...\$niter | Number(s) of iterations |
| ...\$Sigma | Group-level posterior covariance matrices |
| ...\$Mu | Group-level posterior mean vectors |
| ...\$a | Slopes for group 1 |
| ...\$b | Intercepts for group 1 |
| ...\$gamma | D2PL parameters for the slopes |
| ...\$beta | D2PL parameters for the intercepts |
| ...\$ll | Log-likelihood |
| ...\$l0 | Number of nonzero D2PL parameters in gamma and beta |
| ...\$AIC | Akaike Information Criterion: $-2*ll+10*2$ |
| ...\$BIC | Bayesian Information Criterion: $-2*ll+10*\log(N)$ |
| ...\$GIC | Generalized Information Criterion: $-2*ll+c*10*\log(N)*\log(\log(N))$ |

Author(s)

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See Also

[D2PL_gvem](#), [D2PL_lrt](#), [coef.vemirt_DIF](#), [print.vemirt_DIF](#), [summary.vemirt_DIF](#)

Examples

```
## Not run:
with(D2PL_data, D2PL_em(data, model, group))
## End(Not run)
```

Description

GVEM Algorithms for DIF Detection in M2PL Models

Usage

```
D2PL_gvem(
  data,
  model = matrix(1, ncol(data)),
  group = rep(1, nrow(data)),
  method = "IWGVEMM",
  Lambda0 = if (length(unique(group)) == 1) 0 else seq(0.2, 0.8, by = 0.1),
  criterion = "GIC",
  iter = 200,
  eps = 0.001,
  c = 1,
  S = 10,
  M = 10,
  lr = 0.1
)
```

Arguments

| | |
|-----------|--|
| data | An $N \times J$ binary matrix of item responses (missing responses should be coded as NA) |
| model | A $J \times K$ binary matrix of loading indicators (all items load on the only dimension by default) |
| group | An N dimensional vector of group indicators from 1 to G (all respondents are in the same group by default) |
| method | Estimation algorithm, one of 'GVEM' or 'IWGVEMM' |
| Lambda0 | A vector of lambda0 values for L_1 penalty (lambda equals $\sqrt{N} * \text{lambda0}$) |
| criterion | Information criterion for model selection, one of 'GIC' (recommended), 'BIC', or 'AIC' |
| iter | Maximum number of iterations |
| eps | Termination criterion on numerical accuracy |
| c | Constant for computing GIC |
| S | Sample size for approximating the expected lower bound ('IWGVEMM' only) |
| M | Sample size for approximating a tighter lower bound ('IWGVEMM' only) |
| lr | Learning rate for the Adam optimizer ('IWGVEMM' only) |

Value

An object of class `vemirt_DIF`, which is a list containing the following elements:

| | |
|---------------------------|---|
| <code>N</code> | Number of respondents |
| <code>niter0</code> | Number(s) of iterations for initialization |
| <code>fit</code> | The best (with lowest information criterion) model, which is an element of <code>all</code> |
| <code>best</code> | The index of <code>fit</code> in <code>all</code> |
| <code>all</code> | A list of models which has the same length as <code>Lambda0</code> : |
| <code>...\$lambda0</code> | Corresponding element in <code>Lambda0</code> |
| <code>...\$lambda</code> | $\sqrt{N} * \text{lambda0}$ |
| <code>...\$niter</code> | Number(s) of iterations |
| <code>...\$SIGMA</code> | Person-level posterior covariance matrices |
| <code>...\$MU</code> | Person-level posterior mean vectors |
| <code>...\$Sigma</code> | Group-level posterior covariance matrices |
| <code>...\$Mu</code> | Group-level posterior mean vectors |
| <code>...\$a</code> | Slopes for group 1 |
| <code>...\$b</code> | Intercepts for group 1 |
| <code>...\$gamma</code> | D2PL parameters for the slopes |
| <code>...\$beta</code> | D2PL parameters for the intercepts |
| <code>...\$RMSE</code> | Root mean square error of fitted probability of each item for each group |
| <code>...\$l1</code> | Estimated lower bound of log-likelihood |
| <code>...\$l0</code> | Number of nonzero D2PL parameters in <code>gamma</code> and <code>beta</code> |
| <code>...\$AIC</code> | Akaike Information Criterion: $-2 * l1 + l0 * 2$ |
| <code>...\$BIC</code> | Bayesian Information Criterion: $-2 * l1 + l0 * \log(N)$ |
| <code>...\$GIC</code> | Generalized Information Criterion: $-2 * l1 + c * l0 * \log(N) * \log(\log(N))$ |

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See Also

[D2PL_em](#), [D2PL_lrt](#), [coef.vemirt_DIF](#), [print.vemirt_DIF](#), [summary.vemirt_DIF](#)

Examples

```
## Not run:
with(D2PL_data, D2PL_gvem(data, model, group))
## End(Not run)
```

D2PL_lrt

*Likelihood Ratio Test for DIF Detection in M2PL Models***Description**

Likelihood Ratio Test for DIF Detection in M2PL Models

Usage

```
D2PL_lrt(data, model, group, unif = F)
```

Arguments

| | |
|-------|--|
| data | An $N \times J$ binary matrix of item responses |
| model | A $J \times K$ binary matrix of loading indicators |
| group | An N dimensional vector of group indicators (integers from 1 to G) |
| unif | Whether to detect uniform D2PL only |

Value

A list:

| | |
|-------|---|
| Sigma | Group-level posterior covariance matrices |
| Mu | Group-level posterior mean vectors |
| a | Slopes for group 1 |
| b | Intercepts for group 1 |
| gamma | D2PL parameters for the slopes |
| beta | D2PL parameters for the intercepts |

Author(s)

Ruoyi Zhu <zhux0445@uw.edu>

See Also[D2PL_em](#), [D2PL_gvem](#)**Examples**

```
## Not run:
with(D2PL_data, D2PL_lrt(data, model, group))
## End(Not run)
```

| | |
|--------------|--|
| E2PL_data_C1 | <i>Simulated Data Set for Exploratory M2PL Analysis Under C1 Constraints</i> |
|--------------|--|

Description

Responses are simulated based on a between-item M2PL model with 5 factors. The true factor correlations are set as 0.1.

Usage

E2PL_data_C1

Format

A list of components of the data set:

| | |
|-----------|--|
| data | Item responses |
| model | Loading indicators for (adaptive) lasso penalty |
| constrain | Constraint for model identification ('C1') |
| non_pen | Index of an item that is associated with all the factors (NULL under C1) |

| | |
|--------------|--|
| E2PL_data_C2 | <i>Simulated Data Set for Exploratory M2PL Analysis Under C2 Constraints</i> |
|--------------|--|

Description

Responses are simulated based on a between-item M2PL model with 5 factors. The true factor correlations are set as 0.1.

Usage

E2PL_data_C2

Format

A list of components of the data set:

| | |
|-----------|--|
| data | Item responses |
| model | Loading indicators for (adaptive) lasso penalty |
| constrain | Constraint for model identification ('C2') |
| non_pen | Index of an item that is associated with all the factors |

Description

Exploratory M2PL Analysis with Adaptive Lasso Penalty

Usage

```
E2PL_gvem_adaptlasso(
  u,
  indic,
  max.iter = 5000,
  constrain = "C1",
  non_pen = NULL,
  gamma = 2
)
```

Arguments

| | |
|------------------------|--|
| <code>u</code> | an $N \times J$ matrix or a data.frame that consists of binary responses of N individuals to J items. The missing values are coded as NA |
| <code>indic</code> | a $J \times K$ matrix or a data.frame that describes the factor loading structure of J items to K factors. It consists of binary values where 0 refers to the item is irrelevant to this factor, and 1 otherwise. For exploratory factor analysis with adaptive lasso penalty, <code>indic</code> should include constraints on the a $K \times K$ sub-matrix to ensure identifiability. The remaining parts do not assume any pre-specified zero structure but instead, the appropriate lasso penalty would recover the true zero structure. Also see <code>constrain</code> |
| <code>max.iter</code> | the maximum number of iterations for the EM cycle; default is 5000 |
| <code>constrain</code> | <p>the constraint setting: "C1" or "C2". To ensure identifiability, "C1" sets a $K \times K$ sub-matrix of <code>indic</code> to be an identity matrix. This constraint anchor K factors by designating K items that load solely on each factor respectively. Note that the $K \times K$ matrix does not have to appear at the top of the <code>indic</code> matrix. "C2" sets the $K \times K$ sub-matrix to be a lower triangular matrix with the diagonal being ones. That is, there are test items associated with each factor for sure and they may be associated with other factors as well. Nonzero entries (in the lower triangular part) except for the diagonal entries of the sub-matrix are penalized during the estimation procedure. For instance, assume $K = 3$, then the "C2" constraint will imply the following submatrix: $C2 = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$. As shown, item 1 is allowed to only load on the first factor, item 2 will for sure load on the second factor but it may also load on the first factor (hence a penalty is added on the $(2, 1)$ element of "C2", i.e., $C2_{2,1}$). Item 3 will for sure load on the third factor but it may also load on the first two factors. However, note that for all remaining items their loading vector will all be $(1, 1, 1)$ hence indistinguishable from the third anchor item. Therefore, we need to alert the algorithm that this third anchor item will for sure load on the third factor, and whether or not it loads on the first two factors depends on the regularization results. Therefore, we</p> |

| | |
|---------|---|
| | need to specify "non_pen=" to identify the K th anchor item. Although, "C2" is much weaker than "C1", it still ensures empirical identifiability. Default is "C1". During estimation, under both the "C1" and "C2" constraints, the population means and variances are constrained to be 0 and 1, respectively. |
| non_pen | the index of an item that is associated with every factor under constraint "C2". For C1, the input can be NULL |
| gamma | a numerical value of adaptive lasso parameter. Zou (2006) recommended three values, 0.5, 1, and 2. The default value is 2. |

Value

a list containing the following objects:

| | |
|--------|--|
| ra | item discrimination parameters, a $J \times K$ matrix |
| rb | item difficulty parameters, vector of length J |
| reta | variational parameters $\eta(\xi)$, a $N \times J$ matrix |
| reps | variational parameters ξ , a $N \times J$ matrix |
| rsigma | population variance-covariance matrix, a $K \times K$ matrix |
| mu_i | mean parameter for each person, a $K \times N$ matrix |
| sig_i | covariance matrix for each person, a $K \times K \times N$ array |
| n | the number of iterations for the EM cycle |
| Q_mat | factor loading structure, a $J \times K$ matrix |
| GIC | model fit index |
| AIC | model fit index |
| BIC | model fit index |
| lbd | numerical value of lasso penalty parameter λ |

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

References

- Cho, A. E., Xiao, J., Wang, C., & Xu, G. (2022). Regularized Variational Estimation for Exploratory Item Factor Analysis. *Psychometrika*. <https://doi.org/10.1007/s11336-022-09874-6>
- Zou, H. (2006). The adaptive LASSO and its oracle properties. *Journal of the American Statistical Association*, 7, 1011418–1429.

See Also

[E2PL_gvem_rot](#), [E2PL_gvem_lasso](#), [exampleIndic_efa2pl_c1](#), [exampleIndic_efa2pl_c2](#)

Examples

```
## Not run:
with(E2PL_data_C1, E2PL_gvem_adaptlasso(data, model, constrain = constrain, non_pen = non_pen, gamma=2))
with(E2PL_data_C2, E2PL_gvem_adaptlasso(data, model, constrain = constrain, non_pen = non_pen, gamma=2))
## End(Not run)
```

Description

Exploratory M2PL Analysis with Lasso Penalty

Usage

```
E2PL_gvem_lasso(u, indic, max.iter = 5000, constrain = "C1", non_pen = NULL)
```

Arguments

- | | |
|------------------------|--|
| <code>u</code> | an $N \times J$ matrix or a data.frame that consists of binary responses of N individuals to J items. The missing values are coded as NA |
| <code>indic</code> | a $J \times K$ matrix or a data.frame that describes the factor loading structure of J items to K factors. It consists of binary values where 0 refers to the item is irrelevant with this factor, 1 otherwise. For exploratory factor analysis with lasso penalty, <code>indic</code> should be imposed certain constraints on the a $K \times K$ sub-matrix to ensure identifiability. The remaining parts do not assume any pre-specified zero structure but instead, the appropriate lasso penalty would recover the true zero structure. Also see <code>constrain</code> |
| <code>max.iter</code> | the maximum number of iterations for the EM cycle; default is 5000 |
| <code>constrain</code> | <p>the constraint setting: "C1" or "C2". To ensure identifiability, "C1" sets a $K \times K$ sub-matrix of <code>indic</code> to be an identity matrix. This constraint anchor K factors by designating K items that load solely on each factor respectively. Note that the $K \times K$ matrix does not have to appear at the top of the <code>indic</code> matrix. "C2" sets the $K \times K$ sub-matrix to be a lower triangular matrix with the diagonal being ones. That is, there are test items associated with each factor for sure and they may be associated with other factors as well. Nonzero entries (in the lower triangular part) except for the diagonal entries of the sub-matrix are penalized during the estimation procedure. For instance, assume $K = 3$, then the "C2" constraint will imply the following submatrix: $C2 = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$. As shown, item 1 is allowed to only load on the first factor, item 2 will for sure load on the second factor but it may also load on the first factor (hence a penalty is added on the (2, 1) element of "C2", i.e., $C2_{2,1}$). Item 3 will for sure load on the third factor but it may also load on the first two factors. However, note that for all remaining items their loading vector will all be (1, 1, 1) hence indistinguishable from the third anchor item. Therefore, we need to alert the algorithm that this third anchor item will for sure load on the third factor, and whether or not it loads on the first two factors depends on the regularization results. Therefore, we need to specify "non_pen=" to identify the Kth anchor item. Although, "C2" is much weaker than "C1", it still ensures empirical identifiability. Default is "C1". During estimation, under both the "C1" and "C2" constraints, the population means and variances are constrained to be 0 and 1, respectively.</p> |
| <code>non_pen</code> | the index of an item that is associated with every factor under constraint "C2". For C1, the input can be NULL |

Value

a list containing the following objects:

| | |
|--------|--|
| ra | item discrimination parameters, a $J \times K$ matrix |
| rb | item difficulty parameters, vector of length J |
| reta | variational parameters $\eta(\xi)$, a $N \times J$ matrix |
| reps | variational parameters ξ , a $N \times J$ matrix |
| rsigma | population variance-covariance matrix, a $K \times K$ matrix |
| mu_i | mean parameter for each person, a $K \times N$ matrix |
| sig_i | covariance matrix for each person, a $K \times K \times N$ array |
| n | the number of iterations for the EM cycle |
| Q_mat | factor loading structure, a $J \times K$ matrix |
| GIC | model fit index |
| AIC | model fit index |
| BIC | model fit index |
| lbd | numerical value of lasso penalty parameter λ |

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

References

Cho, A. E., Xiao, J., Wang, C., & Xu, G. (2022). Regularized Variational Estimation for Exploratory Item Factor Analysis. *Psychometrika*. <https://doi.org/10.1007/s11336-022-09874-6>

See Also

[E2PL_gvem_rot](#), [E2PL_gvem_adaptlasso](#), [exampleIndic_efa2pl_c1](#), [exampleIndic_efa2pl_c2](#)

Examples

```
## Not run:
with(E2PL_data_C1, E2PL_gvem_lasso(data, model, constrain = constrain, non_pen = non_pen))
with(E2PL_data_C2, E2PL_gvem_lasso(data, model, constrain = constrain, non_pen = non_pen))
## End(Not run)
```

E2PL_gvem_rot

Exploratory M2PL Analysis with Post-hoc Rotation

Description

Exploratory M2PL Analysis with Post-hoc Rotation

Usage

```
E2PL_gvem_rot(u, domain, max.iter = 5000, rot = "Promax")
```

Arguments

| | |
|-----------------------|--|
| <code>u</code> | an $N \times J$ matrix or a data.frame that consists of binary responses of N individuals to J items. The missing values are coded as NA |
| <code>domain</code> | the number of factors |
| <code>max.iter</code> | the maximum number of iterations for the EM cycle; default is 5000 |
| <code>rot</code> | the post-hoc rotation method: Promax or CF-Quartimax; default is "Promax", but may also be "cfQ" for conducting the CF-Quartimax rotation |

Value

a list containing the following objects:

| | |
|---------------------|--|
| <code>ra</code> | item discrimination parameters, a $J \times K$ matrix |
| <code>rb</code> | item difficulty parameters, vector of length J |
| <code>reta</code> | variational parameters $\eta(\xi)$, a $N \times J$ matrix |
| <code>reps</code> | variational parameters ξ , a $N \times J$ matrix |
| <code>rsigma</code> | population variance-covariance matrix, a $K \times K$ matrix |
| <code>mu_i</code> | mean parameter for each person, a $K \times N$ matrix |
| <code>sig_i</code> | covariance matrix for each person, a $K \times K \times N$ array |
| <code>n</code> | the number of iterations for the EM cycle |
| <code>rk</code> | factor loadings, a $J \times K$ matrix |
| <code>Q_mat</code> | factor loading structure, a $J \times K$ matrix |
| <code>GIC</code> | model fit index |
| <code>AIC</code> | model fit index |
| <code>BIC</code> | model fit index |
| <code>ur_a</code> | item discrimination parameters before conducting the rotation, a $J \times K$ matrix |

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

See Also

[E2PL_gvem_lasso](#), [E2PL_gvem_adaptlasso](#)

Examples

```
## Not run:
E2PL_gvem_rot(E2PL_data_C1$data, domain=5,max.iter=3000)
E2PL_gvem_rot(E2PL_data_C1$data, domain=5,rot="cfQ")
## End(Not run)
```

| | |
|--------------|--|
| E3PL_data_C1 | <i>Simulated Data Set for Exploratory M3PL Analysis Under C1 Constraints</i> |
|--------------|--|

Description

Responses are simulated based on a within-item M3PL model with 3 factors. The true factor correlations are set as 0.1.

Usage

E3PL_data_C1

Format

A list of components of the data set:

| | |
|-----------|--|
| data | Item responses |
| model | Loading indicators for (adaptive) lasso penalty |
| constrain | Constraint for model identification ('C1') |
| non_pen | Index of an item that is associated with all the factors (NULL under C1) |

| | |
|--------------|--|
| E3PL_data_C2 | <i>Simulated Data Set for Exploratory M3PL Analysis Under C2 Constraints</i> |
|--------------|--|

Description

Responses are simulated based on a within-item M3PL model with 3 factors. The true factor correlations are set as 0.1.

Usage

E3PL_data_C2

Format

A list of components of the data set:

| | |
|-----------|--|
| data | Item responses |
| model | Loading indicators for (adaptive) lasso penalty |
| constrain | Constraint for model identification ('C2') |
| non_pen | Index of an item that is associated with all the factors |

E3PL_sgvem_adaptlasso *Stochastic GVEM with Adaptive Lasso Penalty for Exploratory M3PL Analysis*

Description

Stochastic GVEM with Adaptive Lasso Penalty for Exploratory M3PL Analysis

Usage

```
E3PL_sgvem_adaptlasso(
  u,
  indic,
  samp = 50,
  forgetrate = 0.51,
  mu_b,
  sigma2_b,
  Alpha,
  Beta,
  max.iter = 5000,
  constrain = "C1",
  non_pen = NULL,
  gamma = 2
)
```

Arguments

| | |
|-------------------------|---|
| <code>u</code> | an $N \times J$ matrix or a data.frame that consists of binary responses of N individuals to J items. The missing values are coded as NA |
| <code>indic</code> | a $J \times K$ matrix or a data.frame that describes the factor loading structure of J items to K factors. It consists of binary values where 0 refers to the item is irrelevant with this factor, 1 otherwise. For exploratory factor analysis with lasso penalty, <code>indic</code> should be imposed certain constraints on the a $K \times K$ sub-matrix to ensure identifiability. The remaining parts do not assume any pre-specified zero structure but instead, the appropriate lasso penalty would recover the true zero structure. Also see <code>constrain</code> |
| <code>samp</code> | a subsample for each iteration; default is 50 |
| <code>forgetrate</code> | the forget rate for the stochastic algorithm. The value should be within the range from 0.5 to 1. Default is 0.51 |
| <code>mu_b</code> | the mean parameter for the normal prior distribution of item difficulty parameters |
| <code>sigma2_b</code> | the variance parameter for the normal prior distribution of item difficulty parameters |
| <code>Alpha</code> | the α parameter for the beta prior distribution of guessing parameters |
| <code>Beta</code> | the β parameter for the beta prior distribution of guessing parameters |
| <code>max.iter</code> | the maximum number of iterations for the EM cycle; default is 5000 |

| | |
|-----------|--|
| constrain | <p>the constraint setting: "C1" or "C2". To ensure identifiability, "C1" sets a $K \times K$ sub-matrix of indic to be an identity matrix. This constraint anchor K factors by designating K items that load solely on each factor respectively. Note that the $K \times K$ matrix does not have to appear at the top of the indic matrix. "C2" sets the $K \times K$ sub-matrix to be a lower triangular matrix with the diagonal being ones. That is, there are test items associated with each factor for sure and they may be associated with other factors as well. Nonzero entries (in the lower triangular part) except for the diagonal entries of the sub-matrix are penalized during the estimation procedure. For instance, assume $K = 3$, then the "C2" constraint will imply the following submatrix: $C2 = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$. As shown, item 1 is allowed to only load on the first factor, item 2 will for sure load on the second factor but it may also load on the first factor (hence a penalty is added on the $(2, 1)$ element of "C2", i.e., $C2_{2,1}$). Item 3 will for sure load on the third factor but it may also load on the first two factors. However, note that for all remaining items their loading vector will all be $(1, 1, 1)$ hence indistinguishable from the third anchor item. Therefore, we need to alert the algorithm that this third anchor item will for sure load on the third factor, and whether or not it loads on the first two factors depends on the regularization results. Therefore, we need to specify "non_pen=" to identify the Kth anchor item. Although, "C2" is much weaker than "C1", it still ensures empirical identifiability. Default is "C1". During estimation, under both the "C1" and "C2" constraints, the population means and variances are constrained to be 0 and 1, respectively.</p> |
| non_pen | the index of an item which is associated with each factor to satisfy "C2". For C1, the input can be NULL |
| gamma | a numerical value of adaptive lasso parameter. Zou (2006) recommended three values, 0.5, 1, and 2. The default value is 2. |

Value

a list containing the following objects:

| | |
|--------|--|
| ra | item discrimination parameters, a $J \times K$ matrix |
| rb | item difficulty parameters, vector of length J |
| rc | item guessing parameters, vector of length J |
| rs | variational parameters s , a $N \times J$ matrix |
| reta | variational parameters $\eta(\xi)$, a $N \times J$ matrix |
| reps | variational parameters ξ , a $N \times J$ matrix |
| rsigma | population variance-covariance matrix, a $K \times K$ matrix |
| mu_i | mean parameter for each person, a $K \times N$ matrix |
| sig_i | covariance matrix for each person, a $K \times K \times N$ array |
| n | the number of iterations for the EM cycle |
| Q_mat | factor loading structure, a $J \times K$ matrix |
| GIC | model fit index |
| AIC | model fit index |
| BIC | model fit index |
| lbd | numerical value of lasso penalty parameter λ |

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

References

Cho, A. E., Xiao, J., Wang, C., & Xu, G. (2022). Regularized Variational Estimation for Exploratory Item Factor Analysis. *Psychometrika*. <https://doi.org/10.1007/s11336-022-09874-6>

Zou, H. (2006). The adaptive LASSO and its oracle properties. *Journal of the American Statistical Association*, 7, 1011418–1429.

See Also

[E3PL_sgvem_rot](#), [E3PL_sgvem_lasso](#), [exampleIndic_efa3pl_c1](#), [exampleIndic_efa3pl_c2](#)

Examples

```
## Not run:
with(E3PL_data_C1, E3PL_sgvem_adaptlasso(data, model, samp=50, forgetrate=0.51, mu_b=0, sigma2_b=4, Alpha=10, Beta=10))
with(E3PL_data_C2, E3PL_sgvem_adaptlasso(data, model, samp=50, forgetrate=0.51, mu_b=0, sigma2_b=4, Alpha=10, Beta=10))
## End(Not run)
```

E3PL_sgvem_lasso

Stochastic GVEM with Lasso Penalty for Exploratory M3PL Analysis

Description

Stochastic GVEM with Lasso Penalty for Exploratory M3PL Analysis

Usage

```
E3PL_sgvem_lasso(
  u,
  indic,
  samp = 50,
  forgetrate = 0.51,
  mu_b,
  sigma2_b,
  Alpha,
  Beta,
  max.iter = 5000,
  constrain = "C1",
  non_pen = NULL
)
```

Arguments

u an $N \times J$ matrix or a data.frame that consists of binary responses of N individuals to J items. The missing values are coded as NA

| | |
|-------------------------|--|
| <code>indic</code> | a $J \times K$ matrix or a data.frame that describes the factor loading structure of J items to K factors. It consists of binary values where 0 refers to the item is irrelevant with this factor, 1 otherwise. For exploratory factor analysis with lasso penalty, <code>indic</code> should be imposed certain constraints on the a $K \times K$ sub-matrix to ensure identifiability. The remaining parts do not assume any pre-specified zero structure but instead, the appropriate lasso penalty would recover the true zero structure. Also see <code>constrain</code> |
| <code>samp</code> | a subsample for each iteration; default is 50 |
| <code>forgetrate</code> | the forget rate for the stochastic algorithm. The value should be within the range from 0.5 to 1. Default is 0.51 |
| <code>mu_b</code> | the mean parameter for the normal prior distribution of item difficulty parameters |
| <code>sigma2_b</code> | the variance parameter for the normal prior distribution of item difficulty parameters |
| <code>Alpha</code> | the α parameter for the beta prior distribution of guessing parameters |
| <code>Beta</code> | the β parameter for the beta prior distribution of guessing parameters |
| <code>max.iter</code> | the maximum number of iterations for the EM cycle; default is 5000 |
| <code>constrain</code> | the constraint setting: "C1" or "C2". To ensure identifiability, "C1" sets a $K \times K$ sub-matrix of <code>indic</code> to be an identity matrix. This constraint anchor K factors by designating K items that load solely on each factor respectively. Note that the $K \times K$ matrix does not have to appear at the top of the <code>indic</code> matrix. "C2" sets the $K \times K$ sub-matrix to be a lower triangular matrix with the diagonal being ones. That is, there are test items associated with each factor for sure and they may be associated with other factors as well. Nonzero entries (in the lower triangular part) except for the diagonal entries of the sub-matrix are penalized during the estimation procedure. For instance, assume $K = 3$, then the "C2" constraint will imply the following submatrix: $C2 = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$. As shown, item 1 is allowed to only load on the first factor, item 2 will for sure load on the second factor but it may also load on the first factor (hence a penalty is added on the (2, 1) element of "C2", i.e., $C2_{2,1}$). Item 3 will for sure load on the third factor but it may also load on the first two factors. However, note that for all remaining items their loading vector will all be (1, 1, 1) hence indistinguishable from the third anchor item. Therefore, we need to alert the algorithm that this third anchor item will for sure load on the third factor, and whether or not it loads on the first two factors depends on the regularization results. Therefore, we need to specify "non_pen=" to identify the K th anchor item. Although, "C2" is much weaker than "C1", it still ensures empirical identifiability. Default is "C1". During estimation, under both the "C1" and "C2" constraints, the population means and variances are constrained to be 0 and 1, respectively. |
| <code>non_pen</code> | the index of an item which is associated with each factor to satisfy "C2". For C1, the input can be NULL |

Value

a list containing the following objects:

| | |
|-----------------|---|
| <code>ra</code> | item discrimination parameters, a $J \times K$ matrix |
| <code>rb</code> | item difficulty parameters, vector of length J |

| | |
|--------|--|
| rc | item guessing parameters, vector of length J |
| rs | variational parameters s , a $N \times J$ matrix |
| reta | variational parameters $\eta(\xi)$, a $N \times J$ matrix |
| reps | variational parameters ξ , a $N \times J$ matrix |
| rsigma | population variance-covariance matrix, a $K \times K$ matrix |
| mu_i | mean parameter for each person, a $K \times N$ matrix |
| sig_i | covariance matrix for each person, a $K \times K \times N$ array |
| n | the number of iterations for the EM cycle |
| Q_mat | factor loading structure, a $J \times K$ matrix |
| GIC | model fit index |
| AIC | model fit index |
| BIC | model fit index |
| lbd | numerical value of lasso penalty parameter λ |

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

References

Cho, A. E., Xiao, J., Wang, C., & Xu, G. (2022). Regularized Variational Estimation for Exploratory Item Factor Analysis. *Psychometrika*. <https://doi.org/10.1007/s11336-022-09874-6>

See Also

[E3PL_sgvem_rot](#), [E3PL_sgvem_adaptlasso](#), [exampleIndic_efa3pl_c1](#), [exampleIndic_efa3pl_c2](#)

Examples

```
## Not run:
with(E3PL_data_C1, E3PL_sgvem_lasso(data,model,samp=50,forgetrate=0.51,mu_b=0,sigma2_b=4,Alpha=10,Beta=40,m
with(E3PL_data_C2, E3PL_sgvem_lasso(data,model,samp=50,forgetrate=0.51,mu_b=0,sigma2_b=4,Alpha=10,Beta=40,m
## End(Not run)
```

E3PL_sgvem_rot

Stochastic GVEM for Exploratory M3PL Analysis

Description

Stochastic GVEM for Exploratory M3PL Analysis

Usage

```
E3PL_sgvem_rot(
  u,
  domain,
  samp = 50,
  forgetrate = 0.51,
  mu_b,
  sigma2_b,
  Alpha,
  Beta,
  max.iter = 5000,
  rot = "Promax"
)
```

Arguments

| | |
|-------------------------|--|
| <code>u</code> | an $N \times J$ matrix or a data.frame that consists of binary responses of N individuals to J items. The missing values are coded as NA |
| <code>domain</code> | the number of factors |
| <code>samp</code> | a subsample for each iteration; default is 50 |
| <code>forgetrate</code> | the forget rate for the stochastic algorithm. The value should be within the range from 0.5 to 1. Default is 0.51 |
| <code>mu_b</code> | the mean parameter for the prior distribution of item difficulty parameters |
| <code>sigma2_b</code> | the variance parameter for the prior distribution of item difficulty parameters |
| <code>Alpha</code> | the α parameter for the prior distribution of guessing parameters |
| <code>Beta</code> | the β parameter for the prior distribution of guessing parameters |
| <code>max.iter</code> | the maximum number of iterations for the EM cycle; default is 5000 |
| <code>rot</code> | the post-hoc rotation method: Promax or CF-Quartimax; default is "Promax", but may also be "cfQ" for conducting the CF-Quartimax rotation |

Value

a list containing the following objects:

| | |
|---------------------|--|
| <code>ra</code> | item discrimination parameters, a $J \times K$ matrix |
| <code>rb</code> | item difficulty parameters, vector of length J |
| <code>rc</code> | item guessing parameters, vector of length J |
| <code>rs</code> | variational parameters s , a $N \times J$ matrix |
| <code>reta</code> | variational parameters $\eta(\xi)$, a $N \times J$ matrix |
| <code>reps</code> | variational parameters ξ , a $N \times J$ matrix |
| <code>rsigma</code> | population variance-covariance matrix, a $K \times K$ matrix |
| <code>mu_i</code> | mean parameter for each person, a $K \times N$ matrix |
| <code>sig_i</code> | covariance matrix for each person, a $K \times K \times N$ array |
| <code>n</code> | the number of iterations for the EM cycle |
| <code>Q_mat</code> | factor loading structure, a $J \times K$ matrix |
| <code>rk</code> | factor loadings, a $J \times K$ matrix |

| | |
|------|--|
| GIC | model fit index |
| AIC | model fit index |
| BIC | model fit index |
| ur_a | item discrimination parameters before conducting the rotation, a $J \times K$ matrix |

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

See Also

[E3PL_sgvm_lasso](#), [E3PL_sgvm_adaptlasso](#)

Examples

```
## Not run:
E3PL_sgvm_rot(E3PL_data_C1$data, 3, samp=50, forgetrate=0.51,
mu_b=0, sigma2_b=4, Alpha=10, Beta=40, max.iter=5000, rot="Promax")
## End(Not run)
```

pa_poly

Parallel analysis using polychoric correlation

Description

Identify the number of factors

Usage

```
pa_poly(data, n.iter = 10, figure = TRUE)
```

Arguments

| | |
|--------|--|
| data | a $N \times J$ matrix or a data.frame that consists of the responses of N individuals to J items without any missing values. The responses are binary or polytomous. |
| n.iter | Number of simulated analyses to perform |
| figure | By default, pa_poly draws an eigenvalue plot. If FALSE, it suppresses the graphic output |

Value

pa_poly returns a data.frame with the eigenvalues for the real data and the simulated data.

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

Examples

```
## Not run:
pa_poly(C2PL_data$data, n.iter=20)
## End(Not run)
```

| | |
|------------------|----------------------------------|
| print.vemirt_DIF | <i>Print D2PL Items by Group</i> |
|------------------|----------------------------------|

Description

Print D2PL Items by Group

Usage

```
print(x, criterion = NULL, max = 99999L, digits = 3, ...)
```

Arguments

| | |
|-----------|---|
| x | An object of class vemirt_DIF |
| criterion | Information criterion for model selection, one of 'AIC', 'BIC', 'GIC', or the constant for computing GIC, otherwise use the criterion specified when fitting the model(s) |

Author(s)

Weicong Lyu <wlyu4@uw.edu>

See Also

[D2PL_em](#), [D2PL_gvem](#), [D2PL_lrt](#), [coef.vemirt_DIF](#), [summary.vemirt_DIF](#)

| | |
|-----------------|----------------------------------|
| print.vemirt_FA | <i>Print D2PL Items by Group</i> |
|-----------------|----------------------------------|

Description

Print D2PL Items by Group

Usage

```
print(x)
```

Arguments

| | |
|---|------------------------------|
| x | An object of class vemirt_FA |
|---|------------------------------|

Author(s)

Weicong Lyu <wlyu4@uw.edu>

See Also

[C2PL_gvem](#), [C2PL_bs](#), [C2PL_iw](#), [C3PL_sgvem](#), [E2PL_gvem_adaptlasso](#), [E2PL_gvem_lasso](#), [E2PL_gvem_rot](#), [E2PL_IS](#), [E3PL_sgvem_adaptlasso](#), [E3PL_sgvem_lasso](#), [E3PL_sgvem_rot](#), [coef.vemirt_FA](#)

| | |
|--------------------|-----------------------------|
| summary.vemirt_DIF | <i>Summarize D2PL Items</i> |
|--------------------|-----------------------------|

Description

Summarize D2PL Items

Usage

```
summary(x, criterion = NULL, max = 99999L, digits = 3, ...)
```

Arguments

| | |
|-----------|---|
| x | An object of class vemirt_DIF |
| criterion | Information criterion for model selection, one of 'AIC', 'BIC', 'GIC', or the constant for computing GIC, otherwise use the criterion specified when fitting the model(s) |

Author(s)

Weicong Lyu <wlyu4@uw.edu>

See Also

[D2PL_em](#), [D2PL_gvem](#), [D2PL_lrt](#), [coef.vemirt_DIF](#), [print.vemirt_DIF](#)

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