Package ‘VEMIRT’

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Type Package

Title Variational Expectation Maximization for High-Dimensional IRT Models

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Description
VEMIRT is created to assist researchers in conducting high-dimensional exploratory and confirmatory multidimensional item response theory (MIRT) analysis and corresponding differential item functioning (DIF) analysis. The core computation engine of VEMIRT is a family of Gaussian Variational EM algorithms that are considerably more efficient than currently available algorithms in other statistical packages, especially when the number of latent factors exceeds four.

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Imports abind,
bslib,
callr,
data.table,
DT,
GPArotation,
MASS,
Matrix,
mirt,
mvQuad,
mvnfast,
openxlsx,
plotly,
polycor,
psych,
Rcpp,
RcppArmadillo,
rstan,
shiny,
shinyjs,
shinyWidgets,
testit,
tibble,
torch,
viridis

LinkingTo Rcpp, RcppArmadillo, RcppEigen

Encoding UTF-8

Depends R (>= 3.10)

LazyData true

RoxygenNote 7.3.3

URL https://MAP-LAB-UW.github.io/VEMIRT, https://github.com/MAP-LAB-UW/VEMIRT

Suggests knitr,
rmarkdown

VignetteBuilder knitr

Contents

`VEMIRT-package` *VEMIRT: A Package for High-Dimensional IRT Models*

Description

VEMIRT is created to assist researchers to conduct exploratory and confirmatory multidimensional item response theory (MIRT) analysis and cooresponding item differential functioning (DIF) analysis. The core computation engine of VEMIRT is a family of Gaussian Variational EM algorithms that are considerably more efficient than currently available algorithms in other software packages, especially when the number of latent factors exceeds four.

Identifying the number of factors

`pa_poly` identifies the number of factors via parallel analysis.

Exploratory factor analysis

- `E2PL_gvem_rot` conducts M2PL Analysis with post-hoc rotation (Promax & CF-Quartimax)
- `E2PL_gvem_lasso` conducts M2PL Analysis with Lasso penalty
- `E2PL_gvem_adaptlasso` conducts M2PL Analysis with adaptive Lasso penalty
- `E2PL_iw` conducts importance sampling to correct bias for M2PL analysis
- `E3PL_sgvem_rot` conducts stochastic GVEM to further improve the computational effficiency for exploratory M3PL analysis
- `E3PL_sgvem_lasso` conducts M3PL Analysis with Lasso penalty
- `E3PL_sgvem_adaptlasso` conducts M3PL Analysis with adaptive Lasso penalty
- `MGRM_gvem` conducts GVEM for the multidimensional graded response model with post-hoc rotation
- `MGPCM_gvem` conducts GVEM for the multidimensional partial credit model with post-hoc rotation

Confirmatory factor analysis

- `C2PL_gvem` conducts GVEM for confirmatory M2PL analysis
- `C2PL_bs` conducts bootstrap sampling to correct bias and produce standard errors for confirmatory M2PL analysis
- `C2PL_iw` conducts importance sampling to correct bias for M2PL analysis
- `C2PL_iw2` conducts IW-GVEM for confirmatory M2PL analysis (alternative implementation to `C2PL_iw`)
- `C3PL_sgvem` conducts stochastic GVEM for confirmatory M3PL analysis
- `MGRM_gvem` conducts GVEM for the multidimensional graded response model
- `MGPCM_gvem` conducts GVEM for the multidimensional partial credit model

Differential item functioning analysis

- `D1PL_em` conducts DIF analysis for M1PL models using EM algorithms
- `D1PL_gvem` conducts DIF analysis for M1PL models using GVEM algorithms
- `D2PL_em` conducts DIF analysis for M2PL models using EM algorithms
- `D2PL_pair_em` conducts DIF analysis for 2PL models using EM algorithms with group pairwise truncated L_1 penalty
- `D2PL_gvem` conducts DIF analysis for M2PL models using GVEM algorithms
- `D2PL_lrt` conducts DIF analysis for M2PL models using the likelihood ratio test

Shiny apps for VEMIRT

- `shinyVEMIRT` Run the shiny app for VEMIRT
- `DIFdashboard` Run the shiny app for DIF Dashboard

Author(s)

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See Also

Useful links:

- https://MAP-LAB-UW.github.io/VEMIRT
- https://github.com/MAP-LAB-UW/VEMIRT

`C1PL_data` *Simulated Data Set for Confirmatory M1PL Analysis*

Description

Responses are simulated based on an M1PL model with 2 factors. The true factor correlations are set as 0.8.

Usage

```
C1PL_data
```

Format

A list of components of the data set:

`data`	Item responses
`model`	Loading indicators
`params`	True parameters used for generating the item responses

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

`C2PL_bs` *Bootstrap Version of GVEM Confirmatory Analysis for M2PL*

Description

A bootstrap version of GVEM (i.e., GVEM-BS) can be implemented to correct the bias on item parameters and compute standard errors under confirmatory M2PL models

Usage

```
C2PL_bs(gvem_result, boots = 5)
```

Arguments

`gvem_result`	a list that includes exploratory or confirmatory GVEM results for M2PL models.
`boots`	the number of bootstrap samples; default is 5

Value

a list containing the following objects:

`boots_a`	item discrimination parameters corrected by bootstrap sampling, a $J \times K$ `matrix`
`boots_b`	item difficulty parameters corrected by bootstrap sampling, a vector of length J
`sd_a`	stardard errors of item discrimination parameters, a $J \times K$ matrix
`sd_b`	stardard errors of item difficulty parameters, a vector of length J

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

See Also

`C2PL_gvem`, `C2PL_iw`

Examples

```
## Not run:
gvem_result <- with(C2PL_data, C2PL_gvem(data, model))
C2PL_bs(gvem_result, boots=10)
## End(Not run)
```

C2PL_data *Simulated Data Set for Confirmatory M2PL Analysis*

Description

Responses are simulated based on an M2PL model with 2 factors. The true factor correlations are set as 0.8.

Usage

```
C2PL_data
```

Format

A list of components of the data set:

`data`	Item responses
`model`	Loading indicators
`params`	True parameters used for generating the item responses

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

C2PL_gvem *Confirmatory M2PL Analysis*

Description

Confirmatory M2PL Analysis

Usage

```
C2PL_gvem(u, indic, max.iter = 5000, SE.est = FALSE)
```

Arguments

`u`	an $N \times J$ `matrix` or a `data.frame` that consists of binary responses of N individuals to J items. The missing values are coded as `NA`
`indic`	a $J \times K$ `matrix` or a `data.frame` that describes the factor loading structure of J items to K factors. It consists of binary values where 0 refers to the item is irrelevant with this factor, 1 otherwise
`max.iter`	the maximum number of iterations for the EM cycle; default is 5000
`SE.est`	whether to estimate SE for item parameters using the updated supplemented expectation maximization (USEM); default is FALSE

Value

a list containing the following objects:

ra	item discrimination parameters, a $J \times K$ matrix
rb	item difficulty parameters, vector of length J
reta	variational parameters $\eta(\xi)$, a $N \times J$ matrix
reps	variational parameters ξ, a $N \times J$ matrix
rsigma	population variance-covariance matrix, a $K \times K$ matrix
mu_i	mean parameter for each person, a $K \times N$ matrix
sig_i	covariance matrix for each person, a $K \times K \times N$ array
n	the number of iterations for the EM cycle
Q_mat	factor loading structure, a $J \times K$ matrix
GIC	model fit index
AIC	model fit index
BIC	model fit index
SE	Standard errors of item parameters, a $J \times (K+1)$ matrix where the last column includes SE estimates for item difficulty parameters

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

See Also

C3PL_sgvem, C2PL_bs, C2PL_iw

Examples

```
## Not run:
with(C2PL_data, C2PL_gvem(data, model))
## End(Not run)
```

C2PL_iw *Importance Weighted Version of GVEM Analysis for M2PL Models*

Description

An importance weighted version of GVEM (i.e., IW-GVEM) can be implemented to correct the bias on item parameters under M2PL models

Usage

```
C2PL_iw(u, gvem_result, S = 10, M = 10, max.iter = 10)

E2PL_iw(u, gvem_result, S = 10, M = 10, max.iter = 10)
```

Arguments

u	a $N \times J$ `matrix` or a `data.frame` that consists of binary responses of N individuals to J items. The missing values are coded as `NA`
gvem_result	a list that includes exploratory or confirmatory GVEM results for M2PL models.
S	the number of times to draw samples;default is 10
M	the number of samples drawn from the variational distributions;default is 10
max.iter	the maximum number of iterations for the EM cycle; default is 10

Value

a list containing the following objects:

ra	item discrimination parameters estimated by GVEM, a $J \times K$ `matrix`
rb	item difficulty parameters estimated by GVEM, vector of length J
reta	variational parameters $\eta(\xi)$, a $N \times J$ matrix
reps	variational parameters ξ, a $N \times J$ matrix
rsigma	population variance-covariance matrix estimated by GVEM, a $K \times K$ matrix
mu_i	mean parameter for each person, a $K \times N$ matrix
sig_i	covariance matrix for each person, a $K \times K \times N$ array
n	the number of iterations for the EM cycle
rk	factor loadings, a $J \times K$ `matrix`, for exploratory analysis only
Q_mat	factor loading structure, a $J \times K$ matrix
GIC	model fit index
AIC	model fit index
BIC	model fit index
SE	Standard errors of item parameters, a $J \times (K+1)$ matrix where the last column includes SE estimates for item difficulty parameters, for confirmatory analysis only
ur_a	item discrimination parameters before conducting the rotation, a $J \times K$ `matrix`, for exploratory analysis only
new_a	item discrimination parameters estimated by IW-GVEM, a $J \times K$ `matrix`
new_b	item difficulty parameters estimated by IW-GVEM, vector of length J
new_Sigma_theta	population variance-covariance matrix estimated by IW-GVEM, a $K \times K$ matrix
best_lr	The learning rate used for importance sampling
best_lb	The lower bound value for importance sampling

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

See Also

`C2PL_gvem`, `E2PL_gvem_rot`, `C2PL_bs`

Examples

```
## Not run:
CFA_result <- with(C2PL_data, C2PL_gvem(data, model))
C2PL_iw(C2PL_data$data, CFA_result)
## End(Not run)
## Not run:
EFA_result <- with(E2PL_data_C1, E2PL_gvem_lasso(data, model, constrain = constrain, non_pen = non_pen))
E2PL_iw(E2PL_data_C1$data, EFA_result)
## End(Not run)
```

C2PL_iw2 *IW-GVEM Algorithm for Confirmatory M2PL Analysis*

Description

IW-GVEM Algorithm for Confirmatory M2PL Analysis

Usage

```
C2PL_iw2(
  data,
  model = matrix(1, ncol(data)),
  criterion = "BIC",
  iter = 200,
  eps = 0.001,
  c = 1,
  S = 10,
  M = 10,
  lr = 0.1,
  SE.level = NULL
)
```

Arguments

data	An $N \times J$ binary matrix of item responses (missing responses should be coded as NA)
model	A $J \times K$ binary matrix of loading indicators (all items load on the only dimension by default)
criterion	Information criterion for model selection, one of 'GIC' (recommended), 'BIC', or 'AIC'
iter	Maximum number of iterations
eps	Termination criterion on numerical accuracy
c	Constant for computing GIC
S	Sample size for approximating the expected lower bound
M	Sample size for approximating a tighter lower bound
lr	Learning rate for the Adam optimizer
SE.level	Accuracy level of Gaussian quadrature for mvQuad to compute standard errors (SEs are not computed if SE.level is NULL)

Value

An object of class `vemirt_DIF`, which is a list containing the following elements:

`N`	Number of respondents
`niter0`	Number(s) of iterations for initialization
`fit`	The only element of `all`
`best`	Equal to `1`
`all`	A list of model which has one element:
`...$niter`	Number(s) of iterations
`...$SIGMA`	Person-level posterior covariance matrices
`...$MU`	Person-level posterior mean vectors
`...$Sigma`	Population covariance matrix
`...$Mu`	Population mean vector
`...$a`	Slopes
`...$b`	Intercepts
`...$SE.a`	Standard errors of `a`
`...$SE.b`	Standard errors of `b`
`...$ll`	Estimated lower bound of log-likelihood
`...$l0`	Number of nonzero elements in `model`
`...$AIC`	Akaike Information Criterion: `-2*ll+l0*2`
`...$BIC`	Bayesian Information Criterion: `-2*ll+l0*log(N)`
`...$GIC`	Generalized Information Criterion: `-2*ll+c*l0*log(N)*log(log(N))`

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

See Also

`C2PL_gvem`, `C2PL_iw`, `D2PL_gvem`, `coef.vemirt_DIF`, `print.vemirt_DIF`, `summary.vemirt_DIF`

Examples

```
## Not run:
with(C2PL_data, C2PL_iw2(data, model, SE = TRUE))
## End(Not run)
```

C3PL_data *Simulated Data Set for Confirmatory M3PL Analysis*

Description

Responses are simulated based on an M3PL model with 2 factors. The true factor correlations are set as 0.8.

Usage

```
C3PL_data
```

Format

A list of components of the data set:

`data`	Item responses
`model`	Loading indicators
`params`	True parameters used for generating the item responses

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

C3PL_sgvem *Stochastic GVEM for Confirmatory M3PL Analysis*

Description

Stochastic GVEM for Confirmatory M3PL Analysis

Usage

```
C3PL_sgvem(
  u,
  indic,
  samp = 50,
  forgetrate = 0.51,
  mu_b,
  sigma2_b,
  Alpha,
  Beta,
  max.iter = 5000
)
```

Arguments

`u`	an $N \times J$ `matrix` or a `data.frame` that consists of binary responses of N individuals to J items. The missing values are coded as `NA`
`indic`	a $J \times K$ `matrix` or a `data.frame` that describes the factor loading structure of J items to K factors. It consists of binary values where 0 refers to the item is irrelevant with this factor, 1 otherwise
`samp`	a subsample for each iteration; default is 50
`forgetrate`	the forget rate for the stochastic algorithm. The value should be within the range from 0.5 to 1. Default is 0.51
`mu_b`	the mean parameter for the prior distribution of item difficulty parameters
`sigma2_b`	the variance parameter for the prior distribution of item difficulty parameters
`Alpha`	the α parameter for the prior distribution of guessing parameters
`Beta`	the β parameter for the prior distribution of guessing parameters
`max.iter`	the maximum number of iterations for the EM cycle; default is 5000

Value

a list containing the following objects:

`ra`	item discrimination parameters, a $J \times K$ `matrix`
`rb`	item difficulty parameters, vector of length J
`rc`	item guessing parameters, vector of length J
`rs`	variational parameters s, a $N \times J$ matrix
`reta`	variational parameters $\eta(\xi)$, a $N \times J$ matrix
`reps`	variational parameters ξ, a $N \times J$ matrix
`rsigma`	population variance-covariance matrix, a $K \times K$ matrix
`mu_i`	mean parameter for each person, a $K \times N$ matrix
`sig_i`	covariance matrix for each person, a $K \times K \times N$ array
`n`	the number of iterations for the EM cycle
`Q_mat`	factor loading structure, a $J \times K$ matrix
`GIC`	model fit index
`AIC`	model fit index
`BIC`	model fit index

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

References

Cho, A. E., Wang, C., Zhang, X., & Xu, G. (2021). Gaussian variational estimation for multidimensional item response theory. *British Journal of Mathematical and Statistical Psychology, 74*, 52-85.

Cho, A. E., Xiao, J., Wang, C., & Xu, G. (2022). Regularized Variational Estimation for Exploratory Item Factor Analysis. *Psychometrika*. https://doi.org/10.1007/s11336-022-09874-6

See Also

C2PL_gvem

Examples

```
## Not run:
with(C3PL_data, C3PL_sgvem(data, model, samp=50, forgetrate=0.51, mu_b=0, sigma2_b=4, Alpha=10, Beta=40))
## End(Not run)
```

`coef.vemirt_DIF` *Extract Parameter Estimates from DIF 2PL Analysis*

Description

Extract Parameter Estimates from DIF 2PL Analysis

Usage

```
coef(object, criterion = NULL)
```

Arguments

`object`	An object of class `vemirt_DIF`
`criterion`	Information criterion for model selection, one of `'AIC'`, `'BIC'`, `'GIC'`, or the constant for computing GIC, otherwise use the criterion specified when fitting the model(s)

Author(s)

Weicong Lyu <wlyu4@uw.edu>

See Also

D2PL_em, D2PL_pair_em, D2PL_gvem, print.vemirt_DIF, summary.vemirt_DIF

`coef.vemirt_DIF_summary` *Extract DIF 2PL Items*

Description

Extract DIF 2PL Items

Usage

```
coef(object)
```

Arguments

`object`	An object of class `vemirt_DIF_summary`

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

See Also

summary.vemirt_DIF, print.vemirt_DIF_summary

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coef.vemirt_FA — *Extract Parameter Estimates from Explanatory or Confirmatory Analysis*

Description

Extract Parameter Estimates from Explanatory or Confirmatory Analysis

Usage

```
coef(object)
```

Arguments

object	An object of class vemirt_FA

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

See Also

C2PL_gvem, C2PL_bs, C2PL_iw, C3PL_sgvem, E2PL_gvem_adaptlasso, E2PL_gvem_lasso, E2PL_gvem_rot, E2PL_IS, E3PL_sgvem_adaptlasso, E3PL_sgvem_lasso, E3PL_sgvem_rot, print.vemirt_FA

D1PL_data — *Simulated Data Set for DIF M1PL Analysis*

Description

Simulated Data Set for DIF M1PL Analysis

Usage

```
D1PL_data
```

Format

A list of components of the data set:

`data`	Item responses
`model`	Loading indicators
`group`	Group indicators
`j`	Number of DIF items (the first `j` items have DIF)
`params`	A list of true parameters used for generating the item responses:
`...$a`	Slopes
`...$b`	Negated intercepts
`...$theta`	Latent traits

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

`D1PL_em` *EM Algorithms for DIF Detection in M1PL Models*

Description

EM Algorithms for DIF Detection in M1PL Models

Usage

```
D1PL_em(
  data,
  model = matrix(1, ncol(data)),
  group = rep(1, nrow(data)),
  a = 1,
  method = "EMM",
  Lambda0 = if (length(unique(group)) == 1) 0 else seq(0.1, 1, by = 0.1),
  level = 10,
  criterion = "BIC",
  iter = 200,
  eps = 0.001,
  c = 1,
  verbose = TRUE
)
```

Arguments

data	An $N \times J$ binary matrix of item responses (missing responses should be coded as NA)
model	A $J \times K$ binary matrix of loading indicators (all items load on the only dimension by default)
group	An N dimensional vector of group indicators from 1 to G (all respondents are in the same group by default)
a	A scalar indicating the common discrimination parameter for all the dimensions of all the items (takes 1 by default)
method	Estimation algorithm, one of 'EM' or 'EMM'
Lambda0	A vector of lambda0 values for L_1 penalty (lambda equals sqrt(N) * lambda0)
level	Accuracy level, either a number for mvQuad or a vector indicating the grid for each latent dimension
criterion	Information criterion for model selection, one of 'BIC' (recommended), 'AIC', or 'GIC'
iter	Maximum number of iterations
eps	Termination criterion on numerical accuracy
c	Constant for computing GIC
verbose	Whether to show the progress

Value

An object of class vemirt_DIF, which is a list containing the following elements:

N	Number of respondents
niter0	Number(s) of iterations for initialization
fit	The best (with lowest information criterion) model, which is an element of all
best	The index of fit in all
all	A list of models which has the same length as Lambda0:
...$lambda0	Corresponding element in Lambda0
...$lambda	sqrt(N) * lambda0
...$niter	Number(s) of iterations
...$Sigma	Group-level covariance matrices
...$Mu	Group-level mean vectors
...$a	Slopes for group 1
...$b	Intercepts for group 1
...$gamma	D1PL parameters for the slopes (all elements are zero)
...$beta	D1PL parameters for the intercepts
...$ll	Log-likelihood
...$l0	Number of nonzero D1PL parameters in gamma and beta
...$AIC	Akaike Information Criterion: -2*ll+l0*2
...$BIC	Bayesian Information Criterion: -2*ll+l0*log(N)
...$GIC	Generalized Information Criterion: -2*ll+c*l0*log(N)*log(log(N))

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

See Also

D1PL_gvem, coef.vemirt_DIF, print.vemirt_DIF, summary.vemirt_DIF

Examples

```
## Not run:
with(D1PL_data, D1PL_em(data, model, group))
## End(Not run)
```

D1PL_gvem *GVEM Algorithms for DIF Detection in M1PL Models*

Description

GVEM Algorithms for DIF Detection in M1PL Models

Usage

```
D1PL_gvem(
  data,
  model = matrix(1, ncol(data)),
  group = rep(1, nrow(data)),
  a = 1,
  method = "IWGVEMM",
  Lambda0 = if (length(unique(group)) == 1) 0 else seq(0.1, 1, by = 0.1),
  criterion = "GIC",
  iter = 200,
  eps = 0.001,
  c = 1,
  S = 10,
  M = 10,
  lr = 0.1,
  verbose = TRUE
)
```

Arguments

data	An $N \times J$ binary matrix of item responses (missing responses should be coded as NA)
model	A $J \times K$ binary matrix of loading indicators (all items load on the only dimension by default)
group	An N dimensional vector of group indicators from 1 to G (all respondents are in the same group by default)
a	A scalar indicating the common discrimination parameter for all the dimensions of all the items (takes 1 by default)
method	Estimation algorithm, one of 'GVEM' or 'IWGVEMM'

Lambda0	A vector of lambda0 values for L_1 penalty (lambda equals sqrt(N) * lambda0)
criterion	Information criterion for model selection, one of 'GIC' (recommended), 'BIC', or 'AIC'
iter	Maximum number of iterations
eps	Termination criterion on numerical accuracy
c	Constant for computing GIC
S	Sample size for approximating the expected lower bound ('IWGVEMM' only)
M	Sample size for approximating a tighter lower bound ('IWGVEMM' only)
lr	Learning rate for the Adam optimizer ('IWGVEMM' only)
verbose	Whether to show the progress

Value

An object of class vemirt_DIF, which is a list containing the following elements:

N	Number of respondents
niter0	Number(s) of iterations for initialization
fit	The best (with lowest information criterion) model, which is an element of all
best	The index of fit in all
all	A list of models which has the same length as Lambda0:
...$lambda0	Corresponding element in Lambda0
...$lambda	sqrt(N) * lambda0
...$niter	Number(s) of iterations
...$SIGMA	Person-level posterior covariance matrices
...$MU	Person-level posterior mean vectors
...$Sigma	Group-level covariance matrices
...$Mu	Group-level mean vectors
...$a	Slopes for group 1
...$b	Intercepts for group 1
...$gamma	D1PL parameters for the slopes (all elements are zero)
...$beta	D1PL parameters for the intercepts
...$RMSE	Root mean square error of fitted probability of each item for each group
...$ll	Estimated lower bound of log-likelihood
...$l0	Number of nonzero D1PL parameters in beta
...$AIC	Akaike Information Criterion: -2*ll+l0*2
...$BIC	Bayesian Information Criterion: -2*ll+l0*log(N)
...$GIC	Generalized Information Criterion: -2*ll+c*l0*log(N)*log(log(N))

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

See Also

D1PL_em, coef.vemirt_DIF, print.vemirt_DIF, summary.vemirt_DIF

Examples

```
## Not run:
with(D1PL_data, D1PL_gvem(data, model, group))
## End(Not run)
```

`D2PL_data` *Simulated Data Set for DIF M2PL Analysis*

Description

Simulated Data Set for DIF M2PL Analysis

Usage

```
D2PL_data
```

Format

A list of components of the data set:

`data`	Item responses
`model`	Loading indicators
`group`	Group indicators
`j`	Number of DIF items (the first `j` items have DIF)
`params`	A list of true parameters used for generating the item responses:
`...$a`	Slopes
`...$b`	Negated intercepts
`...$theta`	Latent traits

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

D2PL_em *EM Algorithms for DIF Detection in M2PL Models*

Description

EM Algorithms for DIF Detection in M2PL Models

Usage

```
D2PL_em(
  data,
  model = matrix(1, ncol(data)),
  group = rep(1, nrow(data)),
  method = "EMM",
  Lambda0 = if (length(unique(group)) == 1) 0 else seq(0.1, 1, by = 0.1),
  level = 10,
  criterion = "BIC",
  iter = 200,
  eps = 0.001,
  c = 1,
  verbose = TRUE
)
```

Arguments

`data`	An $N \times J$ binary matrix of item responses (missing responses should be coded as `NA`)
`model`	A $J \times K$ binary matrix of loading indicators (all items load on the only dimension by default)
`group`	An N dimensional vector of group indicators from `1` to `G` (all respondents are in the same group by default)
`method`	Estimation algorithm, one of `'EM'` or `'EMM'`
`Lambda0`	A vector of `lambda0` values for L_1 penalty (`lambda` equals `sqrt(N) * lambda0`)
`level`	Accuracy level, either a number for `mvQuad` or a vector indicating the grid for each latent dimension
`criterion`	Information criterion for model selection, one of `'BIC'` (recommended), `'AIC'`, or `'GIC'`
`iter`	Maximum number of iterations
`eps`	Termination criterion on numerical accuracy
`c`	Constant for computing GIC
`verbose`	Whether to show the progress

Value

An object of class `vemirt_DIF`, which is a list containing the following elements:

`N`	Number of respondents
`niter0`	Number(s) of iterations for initialization

fit	The best (with lowest information criterion) model, which is an element of all
best	The index of fit in all
all	A list of models which has the same length as Lambda0:
...$lambda0	Corresponding element in Lambda0
...$lambda	sqrt(N) * lambda0
...$niter	Number(s) of iterations
...$Sigma	Group-level covariance matrices
...$Mu	Group-level mean vectors
...$a	Slopes for group 1
...$b	Intercepts for group 1
...$gamma	D2PL parameters for the slopes
...$beta	D2PL parameters for the intercepts
...$ll	Log-likelihood
...$l0	Number of nonzero D2PL parameters in gamma and beta
...$AIC	Akaike Information Criterion: -2*ll+l0*2
...$BIC	Bayesian Information Criterion: -2*ll+l0*log(N)
...$GIC	Generalized Information Criterion: -2*ll+c*l0*log(N)*log(log(N))

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

See Also

D2PL_pair_em, D2PL_gvem, D2PL_lrt, coef.vemirt_DIF, print.vemirt_DIF, summary.vemirt_DIF

Examples

```
## Not run:
with(D2PL_data, D2PL_em(data, model, group))
## End(Not run)
```

D2PL_gvem *GVEM Algorithms for DIF Detection in M2PL Models*

Description

GVEM Algorithms for DIF Detection in M2PL Models

Usage

```
D2PL_gvem(
  data,
  model = matrix(1, ncol(data)),
  group = rep(1, nrow(data)),
  method = "IWGVEMM",
  Lambda0 = if (length(unique(group)) == 1) 0 else seq(0.1, 1, by = 0.1),
  criterion = "GIC",
  iter = 200,
  eps = 0.001,
  c = 1,
  S = 10,
  M = 10,
  lr = 0.1,
  verbose = TRUE
)
```

Arguments

data	An $N \times J$ binary matrix of item responses (missing responses should be coded as NA)
model	A $J \times K$ binary matrix of loading indicators (all items load on the only dimension by default)
group	An N dimensional vector of group indicators from 1 to G (all respondents are in the same group by default)
method	Estimation algorithm, one of 'GVEM' or 'IWGVEMM'
Lambda0	A vector of lambda0 values for L_1 penalty (lambda equals sqrt(N) * lambda0)
criterion	Information criterion for model selection, one of 'GIC' (recommended), 'BIC', or 'AIC'
iter	Maximum number of iterations
eps	Termination criterion on numerical accuracy
c	Constant for computing GIC
S	Sample size for approximating the expected lower bound ('IWGVEMM' only)
M	Sample size for approximating a tighter lower bound ('IWGVEMM' only)
lr	Learning rate for the Adam optimizer ('IWGVEMM' only)
verbose	Whether to show the progress

Value

An object of class vemirt_DIF, which is a list containing the following elements:

N	Number of respondents
niter0	Number(s) of iterations for initialization
fit	The best (with lowest information criterion) model, which is an element of all
best	The index of fit in all
all	A list of models which has the same length as Lambda0:
...$lambda0	Corresponding element in Lambda0

...$lambda	sqrt(N) * lambda0
...$niter	Number(s) of iterations
...$SIGMA	Person-level posterior covariance matrices
...$MU	Person-level posterior mean vectors
...$Sigma	Group-level covariance matrices
...$Mu	Group-level mean vectors
...$a	Slopes for group 1
...$b	Intercepts for group 1
...$gamma	D2PL parameters for the slopes
...$beta	D2PL parameters for the intercepts
...$RMSE	Root mean square error of fitted probability of each item for each group
...$ll	Estimated lower bound of log-likelihood
...$l0	Number of nonzero D2PL parameters in gamma and beta
...$AIC	Akaike Information Criterion: -2*ll+l0*2
...$BIC	Bayesian Information Criterion: -2*ll+l0*log(N)
...$GIC	Generalized Information Criterion: -2*ll+c*l0*log(N)*log(log(N))

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

See Also

D2PL_pair_em, D2PL_em, D2PL_lrt, coef.vemirt_DIF, print.vemirt_DIF, summary.vemirt_DIF

Examples

```
## Not run:
with(D2PL_data, D2PL_gvem(data, model, group))
## End(Not run)
```

D2PL_lrt *Likelihood Ratio Test for DIF Detection in M2PL Models*

Description

Likelihood Ratio Test for DIF Detection in M2PL Models

Usage

```
D2PL_lrt(data, model, group, unif = F)
```

Arguments

data	An $N \times J$ binary matrix of item responses
model	A $J \times K$ binary matrix of loading indicators
group	An N dimensional vector of group indicators (integers from 1 to G)
unif	Whether to detect uniform D2PL only

Value

A list:

Sigma	Group-level posterior covariance matrices
Mu	Group-level posterior mean vectors
a	Slopes for group 1
b	Intercepts for group 1
gamma	D2PL parameters for the slopes
beta	D2PL parameters for the intercepts

Author(s)

Ruoyi Zhu <zhux0445@uw.edu>

See Also

D2PL_em, D2PL_pair_em, D2PL_gvem

Examples

```
## Not run:
with(D2PL_data, D2PL_lrt(data, model, group))
## End(Not run)
```

D2PL_pair_em — *EM Algorithm with ADMM for DIF Detection Using Group Pairwise Truncated L_1 Penalty in 2PL Models*

Description

EM Algorithm with ADMM for DIF Detection Using Group Pairwise Truncated L_1 Penalty in 2PL Models

Usage

```
D2PL_pair_em(
  data,
  group = rep(1, nrow(data)),
  Lambda0 = if (length(unique(group)) == 1) 0 else seq(0.5, 1.5, by = 0.1),
  Tau = if (length(unique(group)) == 1) 0 else c(Inf, seq(0.05, 0.3, by = 0.05)),
  rho0 = 0.5,
  level = 10,
  criterion = "BIC",
  iter = 200,
  eps = 0.001,
  c = 1,
  verbose = TRUE
)
```

Arguments

data	An $N \times J$ binary matrix of item responses (missing responses should be coded as NA)
group	An N dimensional vector of group indicators from 1 to G (all respondents are in the same group by default)
Lambda0	A vector of lambda0 values for truncated L_1 penalty (lambda equals sqrt(N) / G * lambda0)
Tau	A vector of tau values for truncated L_1 penalty (becomes L_1 penalty when tau equals Inf)
rho0	A value of rho for augmented Lagrangian in ADMM (tau equals sqrt(N) / G * tau0)
level	Accuracy level of Gaussian quadrature for mvQuad
criterion	Information criterion for model selection, one of 'BIC' (recommended), 'AIC', or 'GIC'
iter	Maximum number of iterations
eps	Termination criterion on numerical accuracy
c	Constant for computing GIC
verbose	Whether to show the progress

Value

An object of class vemirt_DIF, which is a list containing the following elements:

N	Number of respondents
niter0	Number(s) of iterations for initialization
fit	The best (with lowest information criterion) model, which is an element of all
best	The index of fit in all
all	A list of models which has the same length as Lambda0:
...$lambda0	Corresponding element in Lambda0
...$lambda	sqrt(N) / G * lambda0
...$tau	Corresponding element in Tau
...$rho0	Same as rho0 in input
...$rho	sqrt(N) / G * rho0
...$niter	Number(s) of iterations
...$Sigma	Group-level covariance matrices
...$Mu	Group-level mean vectors
...$a	Slopes
...$b	Intercepts
...$d.a	Group pairwise differences of slopes
...$d.b	Group pairwise differences of intercepts
...$u.a	Lagrangian multipliers of corresponding elements in d.a
...$u.b	Lagrangian multipliers of corresponding elements in d.b
...$ll	Log-likelihood
...$l0	Number of nonzero D2PL parameters in gamma and beta
...$AIC	Akaike Information Criterion: -2*ll+l0*2
...$BIC	Bayesian Information Criterion: -2*ll+l0*log(N)
...$GIC	Generalized Information Criterion: -2*ll+c*l0*log(N)*log(log(N))

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

See Also

D2PL_em, D2PL_gvem, D2PL_lrt, coef.vemirt_DIF, print.vemirt_DIF, summary.vemirt_DIF

Examples

```
## Not run:
with(D2PL_data, D2PL_pair_em(data, group, Tau = c(Inf, seq(0.01, 0.05, by = 0.01))))
## End(Not run)
```

DIFdashboard — *Shiny App for DIF Dashboard*

Description

Shiny App for DIF Dashboard

Usage

```
DIFdashboard()
```

Author(s)

Yijun Cheng <chengxb@uw.edu>

E2PL_data_C1 — *Simulated Data Set for Exploratory M2PL Analysis Under C1 Constraint*

Description

Responses are simulated based on an M2PL model with 3 factors. The true factor correlations are set as 0.5.

Usage

```
E2PL_data_C1
```

Format

A list of components of the data set:

`data`	Item responses
`model`	Loading indicators for (adaptive) lasso penalty
`constrain`	Constraint for model identification ('C1')
`non_pen`	Index of an item that is associated with all the factors (`NULL` under `C1`)
`params`	True parameters used for generating the item responses

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

`E2PL_data_C2` *Simulated Data Set for Exploratory M2PL Analysis Under C2 Constraint*

Description

Responses are simulated based on an M2PL model with 3 factors. The true factor correlations are set as 0.5.

Usage

```
E2PL_data_C2
```

Format

A list of components of the data set:

`data`	Item responses
`model`	Loading indicators for (adaptive) lasso penalty
`constrain`	Constraint for model identification ('C2')
`non_pen`	Index of an item that is associated with all the factors
`params`	True parameters used for generating the item responses

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

E2PL_gvem_adaptlasso *Exploratory M2PL Analysis with Adaptive Lasso Penalty*

Description

Exploratory M2PL Analysis with Adaptive Lasso Penalty

Usage

```
E2PL_gvem_adaptlasso(
  u,
  indic,
  max.iter = 5000,
  constrain = "C1",
  non_pen = NULL,
  gamma = 2
)
```

Arguments

`u` an $N \times J$ `matrix` or a `data.frame` that consists of binary responses of N individuals to J items. The missing values are coded as `NA`

`indic` a $J \times K$ `matrix` or a `data.frame` that describes the factor loading structure of J items to K factors. It consists of binary values where 0 refers to the item is irrelevant to this factor, and 1 otherwise. For exploratory factor analysis with adaptive lasso penalty, `indic` should include constraints on the a $K \times K$ sub-matrix to ensure identifiability. The remaining parts do not assume any pre-specified zero structure but instead, the appropriate lasso penalty would recover the true zero structure. Also see `constrain`

`max.iter` the maximum number of iterations for the EM cycle; default is 5000

`constrain` the constraint setting: `"C1"` or `"C2"`. To ensure identifiability, `"C1"` sets a $K \times K$ sub-matrix of `indic` to be an identity matrix.This constraint anchor K factors by designating K items that load solely on each factor respectively. Note that the $K \times K$ matrix does not have to appear at the top of the `indic` matrix. `"C2"` sets the $K \times K$ sub-matrix to be a lower triangular matrix with the diagonal being ones. That is, there are test items associated with each factor for sure and they may be associated with other factors as well. Nonzero entries (in the lower triangular part) except for the diagonal entries of the sub-matrix are penalized during the estimation procedure. For instance, assume $K = 3$, then the `"C2"` constraint will imply the following submatrix: $C2 = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$. As shown, item 1 is allowed to only load on the first factor, item 2 will for sure load on the second factor but it may also load on the first factor (hence a penalty is added on the $(2, 1)$ element of `"C2"`, i.e., $C2_{2,1}$). Item 3 will for sure load on the third factor but it may also load on the first two factors. However, note that for all remaining items their loading vector will all be $(1, 1, 1)$ hence indistinguishable from the third anchor item. Therefore, we need to alert the algorithm that this third anchor item will for sure load on the third factor, and whether or not it loads on the first two factors depends on the regularization results. Therefore, we need to specify "non_pen=" to identify the Kth anchor item. Although, "C2" is much weaker than "C1", it still ensures empirical identifiability. Default is "C1". During estimation, under both the "C1" and "C2" constraints, the population means and variances are constrained to be 0 and 1, respectively.

non_pen
: the index of an item that is associated with every factor under constraint "C2". For C1, the input can be NULL

gamma
: a numerical value of adaptive lasso parameter. Zou (2006) recommended three values, 0.5, 1, and 2. The default value is 2.

Value

a list containing the following objects:

ra	item discrimination parameters, a $J \times K$ matrix
rb	item difficulty parameters, vector of length J
reta	variational parameters $\eta(\xi)$, a $N \times J$ matrix
reps	variational parameters ξ, a $N \times J$ matrix
rsigma	population variance-covariance matrix, a $K \times K$ matrix
mu_i	mean parameter for each person, a $K \times N$ matrix
sig_i	covariance matrix for each person, a $K \times K \times N$ array
n	the number of iterations for the EM cycle
Q_mat	factor loading structure, a $J \times K$ matrix
GIC	model fit index
AIC	model fit index
BIC	model fit index
lbd	numerical value of lasso penalty parameter λ

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

References

Cho, A. E., Xiao, J., Wang, C., & Xu, G. (2022). Regularized Variational Estimation for Exploratory Item Factor Analysis. *Psychometrika*. https://doi.org/10.1007/s11336-022-09874-6

Zou, H. (2006). The adaptive LASSO and its oracle properties. *Journal of the American Statistical Association, 7*, 1011418–1429.

See Also

E2PL_gvem_rot, E2PL_gvem_lasso, exampleIndic_efa2pl_c1, exampleIndic_efa2pl_c2

Examples

```
## Not run:
with(E2PL_data_C1, E2PL_gvem_adaptlasso(data, model, constrain = constrain, non_pen = non_pen, gamma=2))
with(E2PL_data_C2, E2PL_gvem_adaptlasso(data, model, constrain = constrain, non_pen = non_pen, gamma=2))
## End(Not run)
```

`E2PL_gvem_lasso` *Exploratory M2PL Analysis with Lasso Penalty*

Description

Exploratory M2PL Analysis with Lasso Penalty

Usage

```
E2PL_gvem_lasso(u, indic, max.iter = 5000, constrain = "C1", non_pen = NULL)
```

Arguments

`u`	an $N \times J$ `matrix` or a `data.frame` that consists of binary responses of N individuals to J items. The missing values are coded as `NA`
`indic`	a $J \times K$ `matrix` or a `data.frame` that describes the factor loading structure of J items to K factors. It consists of binary values where 0 refers to the item is irrelevant with this factor, 1 otherwise. For exploratory factor analysis with lasso penalty, `indic` should be imposed certain constraints on the a $K \times K$ sub-matrix to ensure identifiability. The remaining parts do not assume any pre-specified zero structure but instead, the appropriate lasso penalty would recover the true zero structure. Also see `constrain`
`max.iter`	the maximum number of iterations for the EM cycle; default is 5000
`constrain`	the constraint setting: `"C1"` or `"C2"`. To ensure identifiablity, `"C1"` sets a $K \times K$ sub-matrix of `indic` to be an identity matrix.This constraint anchor K factors by designating K items that load solely on each factor respectively. Note that the $K \times K$ matrix does not have to appear at the top of the `indic` matrix. `"C2"` sets the $K \times K$ sub-matrix to be a lower triangular matrix with the diagonal being ones. That is, there are test items associated with each factor for sure and they may be associated with other factors as well. Nonzero entries (in the lower triangular part) except for the diagonal entries of the sub-matrix are penalized during the estimation procedure. For instance, assume $K = 3$, then the `"C2"` constraint will imply the following submatrix: $C2 = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$. As shown, item 1 is allowed to only load on the first factor, item 2 will for sure load on the second factor but it may also load on the first factor (hence a penalty is added on the $(2, 1)$ element of `"C2"`, i.e., $C2_{2,1}$). Item 3 will for sure load on the third factor but it may also load on the first two factors. However, note that for all remaining items their loading vector will all be $(1, 1, 1)$ hence indistinguishable from the third anchor item. Therefore, we need to alert the algorithm that this third anchor item will for sure load on the third factor, and and whether or not it loads on the first two factors depends on the regularization results. Therefore, we need to specify `"non_pen="` to identify the Kth anchor item. Although, `"C2"` is much weaker than `"C1"`, it still ensures empirical identifiability. Default is `"C1"`. During estimation, under both the `"C1"` and `"C2"` constraints, the population means and variances are constrained to be 0 and 1, respectively.
`non_pen`	the index of an item that is associated with every factor under constraint `"C2"`. For `C1`, the input can be `NULL`

Value

a list containing the following objects:

ra	item discrimination parameters, a $J \times K$ matrix
rb	item difficulty parameters, vector of length J
reta	variational parameters $\eta(\xi)$, a $N \times J$ matrix
reps	variational parameters ξ, a $N \times J$ matrix
rsigma	population variance-covariance matrix, a $K \times K$ matrix
mu_i	mean parameter for each person, a $K \times N$ matrix
sig_i	covariance matrix for each person, a $K \times K \times N$ array
n	the number of iterations for the EM cycle
Q_mat	factor loading structure, a $J \times K$ matrix
GIC	model fit index
AIC	model fit index
BIC	model fit index
lbd	numerical value of lasso penalty parameter λ

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

References

Cho, A. E., Xiao, J., Wang, C., & Xu, G. (2022). Regularized Variational Estimation for Exploratory Item Factor Analysis. *Psychometrika*. https://doi.org/10.1007/s11336-022-09874-6

See Also

E2PL_gvem_rot, E2PL_gvem_adaptlasso, exampleIndic_efa2pl_c1, exampleIndic_efa2pl_c2

Examples

```
## Not run:
with(E2PL_data_C1, E2PL_gvem_lasso(data, model, constrain = constrain, non_pen = non_pen))
with(E2PL_data_C2, E2PL_gvem_lasso(data, model, constrain = constrain, non_pen = non_pen))
## End(Not run)
```

E2PL_gvem_rot *Exploratory M2PL Analysis with Post-hoc Rotation*

Description

Exploratory M2PL Analysis with Post-hoc Rotation

Usage

```
E2PL_gvem_rot(u, domain, max.iter = 5000, rot = "Promax")
```

Arguments

u — an $N \times J$ `matrix` or a `data.frame` that consists of binary responses of N individuals to J items. The missing values are coded as `NA`

domain — the number of factors

max.iter — the maximum number of iterations for the EM cycle; default is 5000

rot — the post-hoc rotation method: Promax or CF-Quartimax; default is `"Promax"`, but may also be `"cfQ"` for conducting the CF-Quartimax rotation

Value

a list containing the following objects:

ra — item discrimination parameters, a $J \times K$ `matrix`

rb — item difficulty parameters, vector of length J

reta — variational parameters $\eta(\xi)$, a $N \times J$ matrix

reps — variational parameters ξ, a $N \times J$ matrix

rsigma — population variance-covariance matrix, a $K \times K$ matrix

mu_i — mean parameter for each person, a $K \times N$ matrix

sig_i — covariance matrix for each person, a $K \times K \times N$ array

n — the number of iterations for the EM cycle

rk — factor loadings, a $J \times K$ `matrix`

Q_mat — factor loading structure, a $J \times K$ matrix

GIC — model fit index

AIC — model fit index

BIC — model fit index

ur_a — item discrimination parameters before conducting the rotation, a $J \times K$ `matrix`

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

See Also

E2PL_gvem_lasso, E2PL_gvem_adaptlasso

Examples

```
## Not run:
E2PL_gvem_rot(E2PL_data_C1$data, domain=5,max.iter=3000)
E2PL_gvem_rot(E2PL_data_C1$data, domain=5,rot="cfQ")
## End(Not run)
```

`E3PL_data_C1` *Simulated Data Set for Exploratory M3PL Analysis Under C1 Constraint*

Description

Responses are simulated based on an M3PL model with 3 factors. The true factor correlations are set as 0.5.

Usage

```
E3PL_data_C1
```

Format

A list of components of the data set:

`data`	Item responses
`model`	Loading indicators for (adaptive) lasso penalty
`constrain`	Constraint for model identification (`'C1'`)
`non_pen`	Index of an item that is associated with all the factors (`NULL` under `C1`)
`params`	True parameters used for generating the item responses

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

`E3PL_data_C2` *Simulated Data Set for Exploratory M3PL Analysis Under C2 Constraint*

Description

Responses are simulated based on an M3PL model with 3 factors. The true factor correlations are set as 0.5.

Usage

```
E3PL_data_C2
```

Format

A list of components of the data set:

`data`	Item responses
`model`	Loading indicators for (adaptive) lasso penalty
`constrain`	Constraint for model identification (`'C2'`)
`non_pen`	Index of an item that is associated with all the factors
`params`	True parameters used for generating the item responses

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

`E3PL_sgvem_adaptlasso` *Stochastic GVEM with Adaptive Lasso Penalty for Exploratory M3PL Analysis*

Description

Stochastic GVEM with Adaptive Lasso Penalty for Exploratory M3PL Analysis

Usage

```
E3PL_sgvem_adaptlasso(
  u,
  indic,
  samp = 50,
  forgetrate = 0.51,
  mu_b,
  sigma2_b,
  Alpha,
  Beta,
  max.iter = 5000,
  constrain = "C1",
  non_pen = NULL,
  gamma = 2
)
```

Arguments

`u`	an $N \times J$ `matrix` or a `data.frame` that consists of binary responses of N individuals to J items. The missing values are coded as `NA`
`indic`	a $J \times K$ `matrix` or a `data.frame` that describes the factor loading structure of J items to K factors. It consists of binary values where 0 refers to the item is irrelevant with this factor, 1 otherwise. For exploratory factor analysis with lasso penalty, `indic` should be imposed certain constraints on the a $K \times K$ sub-matrix

	to ensure identifiability. The remaining parts do not assume any pre-specified zero structure but instead, the appropriate lasso penalty would recover the true zero structure. Also see `constrain`
`samp`	a subsample for each iteration; default is 50
`forgetrate`	the forget rate for the stochastic algorithm. The value should be within the range from 0.5 to 1. Default is 0.51
`mu_b`	the mean parameter for the normal prior distribution of item difficulty parameters
`sigma2_b`	the variance parameter for the normal prior distribution of item difficulty parameters
`Alpha`	the α parameter for the beta prior distribution of guessing parameters
`Beta`	the β parameter for the beta prior distribution of guessing parameters
`max.iter`	the maximum number of iterations for the EM cycle; default is 5000
`constrain`	the constraint setting: `"C1"` or `"C2"`. To ensure identifiablity, `"C1"` sets a $K \times K$ sub-matrix of `indic` to be an identity matrix.This constraint anchor K factors by designating K items that load solely on each factor respectively. Note that the $K \times K$ matrix does not have to appear at the top of the `indic` matrix. `"C2"` sets the $K \times K$ sub-matrix to be a lower triangular matrix with the diagonal being ones. That is, there are test items associated with each factor for sure and they may be associated with other factors as well. Nonzero entries (in the lower triangular part) except for the diagonal entries of the sub-matrix are penalized during the estimation procedure. For instance, assume $K = 3$, then the `"C2"` constraint will imply the following submatrix: $C2 = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$. As shown, item 1 is allowed to only load on the first factor, item 2 will for sure load on the second factor but it may also load on the first factor (hence a penalty is added on the $(2, 1)$ element of `"C2"`, i.e., $C2_{2,1}$). Item 3 will for sure load on the third factor but it may also load on the first two factors. However, note that for all remaining items their loading vector will all be $(1, 1, 1)$ hence indistinguishable from the third anchor item. Therefore, we need to alert the algorithm that this third anchor item will for sure load on the third factor, and and whether or not it loads on the first two factors depends on the regularization results. Therefore, we need to specify `"non_pen="` to identify the Kth anchor item. Although, `"C2"` is much weaker than `"C1"`, it still ensures empirical identifiability. Default is `"C1"`. During estimation, under both the `"C1"` and `"C2"` constraints, the population means and variances are constrained to be 0 and 1, respectively.
`non_pen`	the index of an item which is associated with each factor to satisfy `"C2"`. For `C1`, the input can be `NULL`
`gamma`	a numerical value of adaptive lasso parameter. Zou (2006) recommended three values, 0.5, 1, and 2. The default value is 2.

Value

a list containing the following objects:

`ra`	item discrimination parameters, a $J \times K$ `matrix`
`rb`	item difficulty parameters, vector of length J
`rc`	item guessing parameters, vector of length J

rs	variational parameters s, a $N \times J$ matrix
reta	variational parameters $\eta(\xi)$, a $N \times J$ matrix
reps	variational parameters ξ, a $N \times J$ matrix
rsigma	population variance-covariance matrix, a $K \times K$ matrix
mu_i	mean parameter for each person, a $K \times N$ matrix
sig_i	covariance matrix for each person, a $K \times K \times N$ array
n	the number of iterations for the EM cycle
Q_mat	factor loading structure, a $J \times K$ matrix
GIC	model fit index
AIC	model fit index
BIC	model fit index
lbd	numerical value of lasso penalty parameter λ

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

References

Cho, A. E., Xiao, J., Wang, C., & Xu, G. (2022). Regularized Variational Estimation for Exploratory Item Factor Analysis. *Psychometrika*. https://doi.org/10.1007/s11336-022-09874-6

Zou, H. (2006). The adaptive LASSO and its oracle properties. *Journal of the American Statistical Association, 7*, 1011418–1429.

See Also

E3PL_sgvem_rot, E3PL_sgvem_lasso, exampleIndic_efa3pl_c1, exampleIndic_efa3pl_c2

Examples

```
## Not run:
with(E3PL_data_C1, E3PL_sgvem_adaptlasso(data, model,samp=50,forgetrate=0.51,mu_b=0,sigma2_b=4,Alpha=10,Bet
with(E3PL_data_C2, E3PL_sgvem_adaptlasso(data, model,samp=50,forgetrate=0.51,mu_b=0,sigma2_b=4,Alpha=10,Bet
## End(Not run)
```

E3PL_sgvem_lasso *Stochastic GVEM with Lasso Penalty for Exploratory M3PL Analysis*

Description

Stochastic GVEM with Lasso Penalty for Exploratory M3PL Analysis

Usage

```
E3PL_sgvem_lasso(
  u,
  indic,
  samp = 50,
  forgetrate = 0.51,
  mu_b,
  sigma2_b,
  Alpha,
  Beta,
  max.iter = 5000,
  constrain = "C1",
  non_pen = NULL
)
```

Arguments

`u`	an $N \times J$ `matrix` or a `data.frame` that consists of binary responses of N individuals to J items. The missing values are coded as `NA`
`indic`	a $J \times K$ `matrix` or a `data.frame` that describes the factor loading structure of J items to K factors. It consists of binary values where 0 refers to the item is irrelevant with this factor, 1 otherwise. For exploratory factor analysis with lasso penalty, `indic` should be imposed certain constraints on the a $K \times K$ sub-matrix to ensure identifiability. The remaining parts do not assume any pre-specified zero structure but instead, the appropriate lasso penalty would recover the true zero structure. Also see `constrain`
`samp`	a subsample for each iteration; default is 50
`forgetrate`	the forget rate for the stochastic algorithm. The value should be within the range from 0.5 to 1. Default is 0.51
`mu_b`	the mean parameter for the normal prior distribution of item difficulty parameters
`sigma2_b`	the variance parameter for the normal prior distribution of item difficulty parameters
`Alpha`	the α parameter for the beta prior distribution of guessing parameters
`Beta`	the β parameter for the beta prior distribution of guessing parameters
`max.iter`	the maximum number of iterations for the EM cycle; default is 5000
`constrain`	the constraint setting: `"C1"` or `"C2"`. To ensure identifiablity, `"C1"` sets a $K \times K$ sub-matrix of `indic` to be an identity matrix.This constraint anchor K factors by designating K items that load solely on each factor respectively. Note that the $K \times K$ matrix does not have to appear at the top of the `indic` matrix. `"C2"` sets the $K \times K$ sub-matrix to be a lower triangular matrix with the diagonal being ones. That is, there are test items associated with each factor for sure and they may be associated with other factors as well. Nonzero entries (in the lower triangular part) except for the diagonal entries of the sub-matrix are penalized during the estimation procedure. For instance, assume $K = 3$, then the `"C2"` constraint will imply the following submatrix: $C2 = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$. As shown, item 1 is allowed to only load on the first factor, item 2 will for sure load on the second factor but it may also load on the first factor (hence a penalty is added

on the $(2,1)$ element of "C2", i.e., $C2_{2,1}$). Item 3 will for sure load on the third factor but it may also load on the first two factors. However, note that for all remaining items their loading vector will all be $(1,1,1)$ hence indistinguishable from the third anchor item. Therefore, we need to alert the algorithm that this third anchor item will for sure load on the third factor, and and whether or not it loads on the first two factors depends on the regularization results. Therefore, we need to specify "non_pen=" to identify the Kth anchor item. Although, "C2" is much weaker than "C1", it still ensures empirical identifiability. Default is "C1". During estimation, under both the "C1" and "C2" constraints, the population means and variances are constrained to be 0 and 1, respectively.

`non_pen` the index of an item which is associated with each factor to satisfy "C2". For C1, the input can be NULL

Value

a list containing the following objects:

ra	item discrimination parameters, a $J \times K$ matrix
rb	item difficulty parameters, vector of length J
rc	item guessing parameters, vector of length J
rs	variational parameters s, a $N \times J$ matrix
reta	variational parameters $\eta(\xi)$, a $N \times J$ matrix
reps	variational parameters ξ, a $N \times J$ matrix
rsigma	population variance-covariance matrix, a $K \times K$ matrix
mu_i	mean parameter for each person, a $K \times N$ matrix
sig_i	covariance matrix for each person, a $K \times K \times N$ array
n	the number of iterations for the EM cycle
Q_mat	factor loading structure, a $J \times K$ matrix
GIC	model fit index
AIC	model fit index
BIC	model fit index
lbd	numerical value of lasso penalty parameter λ

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

References

Cho, A. E., Xiao, J., Wang, C., & Xu, G. (2022). Regularized Variational Estimation for Exploratory Item Factor Analysis. *Psychometrika*. https://doi.org/10.1007/s11336-022-09874-6

See Also

E3PL_sgvem_rot, E3PL_sgvem_adaptlasso, exampleIndic_efa3pl_c1, exampleIndic_efa3pl_c2

Examples

```
## Not run:
with(E3PL_data_C1, E3PL_sgvem_lasso(data,model,samp=50,forgetrate=0.51,mu_b=0,sigma2_b=4,Alpha=10,Beta=40,m
with(E3PL_data_C2, E3PL_sgvem_lasso(data,model,samp=50,forgetrate=0.51,mu_b=0,sigma2_b=4,Alpha=10,Beta=40,m
## End(Not run)
```

E3PL_sgvem_rot *Stochastic GVEM for Exploratory M3PL Analysis*

Description

Stochastic GVEM for Exploratory M3PL Analysis

Usage

```
E3PL_sgvem_rot(
  u,
  domain,
  samp = 50,
  forgetrate = 0.51,
  mu_b,
  sigma2_b,
  Alpha,
  Beta,
  max.iter = 5000,
  rot = "Promax"
)
```

Arguments

u	an $N \times J$ `matrix` or a `data.frame` that consists of binary responses of N individuals to J items. The missing values are coded as `NA`
domain	the number of factors
samp	a subsample for each iteration; default is 50
forgetrate	the forget rate for the stochastic algorithm. The value should be within the range from 0.5 to 1. Default is 0.51
mu_b	the mean parameter for the prior distribution of item difficulty parameters
sigma2_b	the variance parameter for the prior distribution of item difficulty parameters
Alpha	the α parameter for the prior distribution of guessing parameters
Beta	the β parameter for the prior distribution of guessing parameters
max.iter	the maximum number of iterations for the EM cycle; default is 5000
rot	the post-hoc rotation method: Promax or CF-Quartimax; default is `"Promax"`, but may also be `"cfQ"` for conducting the CF-Quartimax rotation

Value

a list containing the following objects:

ra	item discrimination parameters, a $J \times K$ `matrix`
rb	item difficulty parameters, vector of length J
rc	item guessing parameters, vector of length J
rs	variational parameters s, a $N \times J$ matrix
reta	variational parameters $\eta(\xi)$, a $N \times J$ matrix

reps	variational parameters ξ, a $N \times J$ matrix
rsigma	population variance-covariance matrix, a $K \times K$ matrix
mu_i	mean parameter for each person, a $K \times N$ matrix
sig_i	covariance matrix for each person, a $K \times K \times N$ array
n	the number of iterations for the EM cycle
Q_mat	factor loading structure, a $J \times K$ matrix
rk	factor loadings, a $J \times K$ `matrix`
GIC	model fit index
AIC	model fit index
BIC	model fit index
ur_a	item discrimination parameters before conducting the rotation, a $J \times K$ `matrix`

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

See Also

E3PL_sgvem_lasso, E3PL_sgvem_adaptlasso

Examples

```
## Not run:
E3PL_sgvem_rot(E3PL_data_C1$data, 3,samp=50,forgetrate=0.51,
mu_b=0,sigma2_b=4,Alpha=10,Beta=40,max.iter=5000,rot="Promax")
## End(Not run)
```

MGPCM_data *Simulated Data Set for Generalized Partial Credit Model*

Description

Simulated Data Set for Generalized Partial Credit Model

Usage

```
MGPCM_data
```

Format

A list of components of the data set:

data	Item responses
model	Loading indicators
params	A list of true parameters used for generating the item responses:
...$a	Slopes

`...$b`	Negated intercepts
`...$theta`	Latent traits

Author(s)

Yijun Cheng <chengxb@uw.edu>

`MGPCM_gvem` *GVEM Algorithm for the Generalized Partial Credit Model*

Description

GVEM Algorithm for the Generalized Partial Credit Model

Usage

```
MGPCM_gvem(
  data,
  model = matrix(1, nrow = J, ncol = 4),
  group = rep(1, nrow(data)),
  iter = 2000,
  eps = 1e-05,
  SE = FALSE,
  verbose = TRUE,
  EFA = FALSE
)
```

Arguments

`data`	An $N \times J$ matrix of item responses where 0 is the minimal partial credit score (missing responses should be coded as `NA`)
`model`	A $J \times K$ matrix of loading indicators (K is the Number of latent dimension)(all items load on the only dimension by default)
`iter`	Maximum number of iterations
`eps`	Termination criterion on numerical accuracy
`SE`	Whether to calculate the standard errors
`verbose`	Whether to show the progress
`EFA`	Whether to rotate the output

Value

An object of class `vemirt_DIF`, which is a list containing the following elements:

`...$Sigma`	Group-level covariance matrices

#'

`...$MU`	Person-level posterior mean vectors

`...$a`	Slopes for group 1
`...$b`	Intercepts for group 1
`...$ll`	Estimated lower bound of log-likelihood

Author(s)

Yijun Cheng <chengxb@uw.edu>

Examples

```
with(MGPCM_gvem, MGPCM_gvem(data, model))
```

`MGRM_data` *Simulated Data Set for the Graded Response Model*

Description

Simulated Data Set for the Graded Response Model

Usage

```
MGRM_data
```

Format

A list of components of the data set:

`data`	Item responses
`model`	Loading indicators
`params`	A list of true parameters used for generating the item responses:
`...$a`	Slopes
`...$b`	Negated intercepts
`...$theta`	Latent traits

Author(s)

Yijun Cheng <chengxb@uw.edu>

MGRM_gvem *GVEM Algorithm for the Graded Response Model*

Description

GVEM Algorithm for the Graded Response Model

Usage

```
MGRM_gvem(
  data,
  model = matrix(1, ncol(data)),
  method = "GVEM",
  iter = 200,
  tol = 1e-04,
  S = 10,
  M = 10,
  MinDim = 0,
  MaxDim = 0,
  verbose = FALSE,
  EFA = FALSE
)
```

Arguments

`data`	An $N \times J$ matrix of item responses where 0 is the minimal partial credit score (missing responses should be coded as `NA`)
`model`	A $J \times K$ matrix of loading indicators (K is the Number of latent dimension)(all items load on the only dimension by default)
`iter`	Maximum number of iterations
`tol`	Termination criterion on numerical accuracy
`S`	Sample size for approximating the expected lower bound (`'IWGVEM'` only)
`M`	Sample size for approximating a tighter lower bound (`'IWGVEM'` only)
`MinDim`	Minimum num of possible dimensions (`'EFA'` only)
`MaxDim`	Maximum num of possible dimensions (`'EFA'` only)
`verbose`	Whether to show the progress
`EFA`	Whether to run EFA or CFA
`criterion`	Information criterion for model selection, one of `'GIC'` (recommended), `'BIC'`, or `'AIC'`
`c`	Constant for computing GIC

Value

An object of class `vemirt_DIF`, which is a list containing the following elements:

`...$SIGMA`	Person-level posterior covariance matrices
`...$MU`	Person-level posterior mean vectors

`...$Sigma`	Group-level covariance matrices
`...$Mu`	Group-level mean vectors
`...$ksi1`	Variational parameter 1
`...$ksi2`	Variational parameter 2
`...$dim`	Num of dimension between latent variables
`...$a`	Slopes
`...$b`	Intercepts
`...$n2vlb`	Bayesian Information Criterion: `-2*ll+l0*log(N)`
`iter`	Number(s) of iterations for initialization

Author(s)

Yijun Cheng <chengxb@uw.edu>

Examples

```
## Not run:
with(MGRM_data, MGRM_gvem(data, method = "IWGVEM", model, EFA = FALSE))
## End(Not run)
```

---

pa_poly *Parallel analysis using polychoric correlation*

Description

Identify the number of factors

Usage

```
pa_poly(data, n.iter = 10, figure = TRUE)
```

Arguments

`data`	a $N \times J$ `matrix` or a `data.frame` that consists of the responses of N individuals to J items without any missing values. The responses are binary or polytomous.
`n.iter`	Number of simulated analyses to perform
`figure`	By default, `pa_poly` draws an eigenvalue plot. If FALSE, it suppresses the graphic output

Value

`pa_poly` returns a `data.frame` with the eigenvalues for the real data and the simulated data.

Author(s)

Jiaying Xiao <jxiao6@uw.edu>

Examples

```
## Not run:
pa_poly(C2PL_data$data, n.iter=20)
## End(Not run)
```

print.vemirt_DIF — *Print DIF 2PL Items by Group*

Description

Print DIF 2PL Items by Group

Usage

```
print(x, criterion = NULL, max = 99999L, digits = 3, ...)
```

Arguments

`x`	An object of class `vemirt_DIF`
`criterion`	Information criterion for model selection, one of `'AIC'`, `'BIC'`, `'GIC'`, or the constant for computing GIC, otherwise use the criterion specified when fitting the model(s)

Author(s)

Weicong Lyu <wlyu4@uw.edu>

See Also

`D2PL_em`, `D2PL_pair_em`, `D2PL_gvem`, `coef.vemirt_DIF`, `summary.vemirt_DIF`

print.vemirt_DIF_summary — *Print Summary of DIF 2PL Items*

Description

Print Summary of DIF 2PL Items

Usage

```
print(x, max = 99999L, ...)
```

Arguments

`x`	An object of class `vemirt_DIF_summary`

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

See Also

`summary.vemirt_DIF`, `coef.vemirt_DIF_summary` `print.vemirt_FA` *Print Parameter Estimates from Explanatory or Confirmatory Analysis*

Description

Print Parameter Estimates from Explanatory or Confirmatory Analysis

Usage

```
print(x)
```

Arguments

x	An object of class `vemirt_FA`

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

See Also

`C2PL_gvem`, `C2PL_bs`, `C2PL_iw`, `C3PL_sgvem`, `E2PL_gvem_adaptlasso`, `E2PL_gvem_lasso`, `E2PL_gvem_rot`, `E2PL_IS`, `E3PL_sgvem_adaptlasso`, `E3PL_sgvem_lasso`, `E3PL_sgvem_rot`, `coef.vemirt_FA`

`shinyVEMIRT` *Shiny App for VEMIRT*

Description

Shiny App for VEMIRT

Usage

```
shinyVEMIRT()
```

Author(s)

Weicong Lyu <weiconglyu@um.edu.mo>

`summary.vemirt_DIF` *Summarize DIF 2PL Items*

Description

Summarize DIF 2PL Items

Usage

```
summary(x, criterion = NULL)
```

Arguments

`criterion`	Information criterion for model selection, one of `'AIC'`, `'BIC'`, `'GIC'`, or the constant for computing GIC, otherwise use the criterion specified when fitting the model(s)
`x`	An object of class `vemirt_DIF`

Author(s)

Weicong Lyu <wlyu4@uw.edu>

See Also

`D2PL_em`, `D2PL_pair_em`, `D2PL_gvem`, `coef.vemirt_DIF`, `print.vemirt_DIF`, `coef.vemirt_DIF_summary`, `print.vemirt_DIF_summary`

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