Regression HW

Introduction

In this homework, you'll get a chance to practice the linear regression skills you learned in class on some real-world data! This data was taken from an online data science competition called SLICED! SLICED is like the cooking competition CHOPPED, but for data science. The dataset in question contains metadata about Super Store sales of different products as well as the profit made. Here is a data dictionary:

Variable	Description
id	unique id per row
ship_mode	what mode was used to ship the item: 'First Class', 'Same Day', 'Second Class', 'Standard Class'
segment	whether the recipient is corporate or consumer
country	always United States
city	where the item was shipped (a city in the United States)
state	where the item was shipped (a state in the United States)
$postal_code$	ZIP Code in the United States
region	region in the United States: 'Central', 'East', 'South', 'West'
category	type of item: 'Furniture', 'Office Supplies', 'Technology'
sub_category	sub-type of item: 'Accessories', 'Appliances', 'Art', 'Binders', 'Bookcases', 'Chairs', 'Copiers', 'Envelopes', 'Fasteners', 'Furnishings', 'Labels', 'Machines', 'Paper', 'Phones', 'Storage', 'Supplies', 'Tables'
sales	sales made for the order (USD)
quantity	quantity sold of the item
discount	discount applied to the order(from 0 to 1)

Variable	Description
profit	profit made on the order (USD)

Getting started

Here are the steps for getting started:

- Start with the assignment link that creates a repo on GitHub with starter documents. I have sent this to you through email.
- Clone this repo in RStudio
- Make any changes needed as outlined by the tasks you need to complete for the assignment
- Periodically commit changes (the more often the better, for example, once per each new task)
 - Remember, git will yell at you when you try to commit before running the following lines in the terminal

```
* git config --global user.name "Your Name Here"
* git config --global user.email "Your Email Here"
```

• Push all your changes back to your GitHub repo

and voila, you're done! Once you push your changes back you do not need to do anything else to "submit" your work. And you can of course push multiple times throughout the assignment. At the time of the deadline I will take whatever is in your repo and consider it your final submission, and grade the state of your work at that time (which means even if you made mistakes before then, you wouldn't be penalized for them as long as the final state of your work is correct).

Assignment

The first thing that we'll need to do is setup our R/RStudio session so that we can do our data analysis and perform linear regression. This involves loading the packages we'll need for the project. I've loaded the correct packages below. Remember to install the packages with install.packages() before you load them (you only have to install once, but load when starting a new session). I've added an option to the chunk below called message: FALSE to turn off all the messages given when loading the two packages.

```
library("tidyverse");theme_set(theme_bw())
library("tidymodels");theme_set(theme_bw())
```

Now we need to load the data into R! There are two datasets in the project space, super_stores_sales_train.csv and super_stores_sales_test.csv. We don't fully know about the concept of training and testing datasets yet, but I want you to load them into R with the read_csv() function and call them train and test respectively. Do that below now!

```
# load train
train <- read_csv("super_store_sales_train.csv")
# load test
test <- read_csv("super_store_sales_test.csv")</pre>
```

IMPORTANT: From now on, assume you are working with the train dataset unless explicitly told to use test.

The next step in your data analysis should always be to make sure that your data was parsed correctly by the loading function. This can mean making sure that numbers are parsed as numbers, words as characters, TRUE's and FALSE's as logicals. For this assignment, you can trust that everything works out right when loading the data.

Before we begin to perform linear regression, we need to understand the goal of the analysis and do some exploratory data analysis (EDA) to understand how the data is behaving. In the SLICED competition, the goal was to predict profit based on any of the metadata on the sales. For this assignment, we will focus on both prediction and inference with profit being the response variable and everything else as possible predictors.

When engaging in EDA your goal is to extract information that will inform your modeling choices down the road. For linear regression, and really any other "learning" method, we are looking for predictors that are correlated to the response. That should be what we focus on finding out during this EDA.

EDA

It is important to understand how the response behaves and so I want you to make a histogram of profit. By default, it will show you one very large bar at 0 because of some outliers. Zoom in on the picture by manually setting the x-axis limits to -100 to 500 using the xlim() function. Comment on the plot and if anything surprises you.

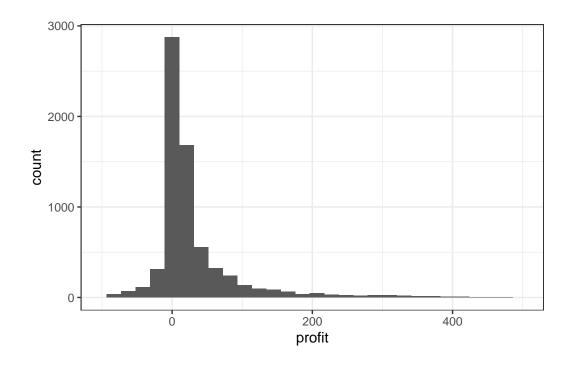
```
1 8522 Second Class Consum~ United~ Ever~ Mass~
                                                    2149 East
                                                                Office~ Art
2 7864 Standard Cl~ Corpor~ United~ Los ~ Cali~
                                                   90036 West
                                                                Furnit~ Chairs
3 3522 Standard Cl~ Consum~ United~ New ~ New ~
                                                   10035 East
                                                                Office~ Storage
4 8694 Standard Cl~ Consum~ United~ Los ~ Cali~
                                                   90045 West
                                                                Office~ Art
5 2306 Second Class Home O~ United~ San ~ Cali~
                                                   94110 West
                                                                Furnit~ Bookca~
6 8742 Standard Cl~ Corpor~ United~ Arli~ Texas
                                                   76017 Centr~ Furnit~ Furnis~
   2292 Standard Cl~ Consum~ United~ Yonk~ New ~
                                                   10701 East
                                                                Techno~ Phones
8
    713 Standard Cl~ Corpor~ United~ Spri~ Virg~
                                                   22153 South Office~ Binders
9 5904 First Class Consum~ United~ Des ~ Illi~
                                                   60016 Centr~ Furnit~ Furnis~
10 6023 Second Class Consum~ United~ Prov~ Rhod~
                                                                Office~ Binders
                                                    2908 East
# ... with 7,163 more rows, 4 more variables: sales <dbl>, quantity <dbl>,
   discount <dbl>, profit <dbl>, and abbreviated variable names
   1: postal_code, 2: category, 3: sub_category
```

```
ggplot(data = train, aes(x=profit)) + geom_histogram() + xlim(-100, 500)
```

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.

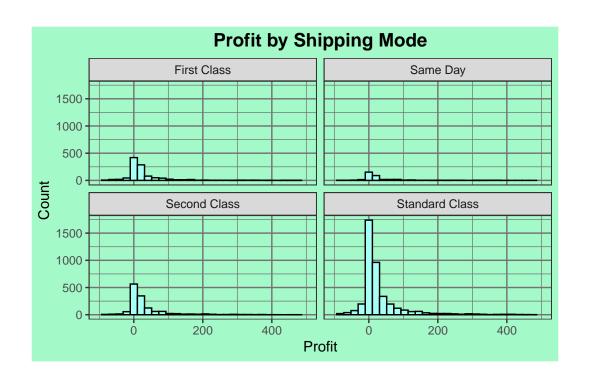
Warning: Removed 275 rows containing non-finite values (stat_bin).

Warning: Removed 2 rows containing missing values (geom_bar).



Comments: The majority of profits are well below \$200, which makes sense if we consider a "super store" to be something similar to a walmart which runs on volume and low costs. It is somewhat surprising how many transactions result in a loss, because the

Now we are interested in seeing if we can determine if any variables or combination of variables are correlated with the response. Let's start with some categorical variables ship_mode and segment. First, I want you to find the mean profit amount for each mode of shipping using group_by() and summarize(). Next, I want you to make histograms of profit that are faceted by ship_mode. In addition to regular gaplotting functions, you'll want to use facet_wrap() to do the faceting. Also, remember to use vars() instead of aes() inside facet_wrap(). You'll probably want to limit the x-axis scale with xlim() like you did previously. Comment on any possible correlation between the variables.





Comments: It's interesting to note that regardless of the profit distribution, the vast majority of classes are sent standard. Also interesting, the profit distribution of same day delivery appears to be less than that of first or second class.

What about ship_mode and segment together? Find the mean profit for each ship_mode and segment pair. You'll need to use group_by() and summarize() again. Any correlation?

```
# mean profit faceted on both variables
meanProfitDataTwo <- train %>%
    group_by(ship_mode, segment) %>%
    summarise(meanProfit = mean(profit))
```

`summarise()` has grouped output by 'ship_mode'. You can override using the `.groups` argument.

meanProfitDataTwo

A tibble: 12 x 3

Groups: ship_mode [4]

ship_mode segment meanProfit

	<chr></chr>	<chr></chr>	<dbl></dbl>
1	First Class	Consumer	29.5
2	First Class	Corporate	27.2
3	First Class	Home Office	69.2
4	Same Day	Consumer	34.0
5	Same Day	Corporate	20.1
6	Same Day	Home Office	33.7
7	Second Class	Consumer	29.5
8	Second Class	Corporate	36.6
9	Second Class	Home Office	48.8
10	Standard Class	Consumer	32.4
11	Standard Class	Corporate	42.8
12	Standard Class	Home Office	41.8

Comments: Home office appears to profit well regardless of how it is shipped. On the other hand, profit for corporate goods appears to correlate quite a bit with how they are shipped.

There are a number of different categorical variables that correspond to location in some sense (country, state, city, region, and zip code). Certainly they all convey similar information. The question becomes how fine a mesh do we need to capture the variation in over location without overfitting. An important fact to know is that the holdout samples (the data in the test dataset) are certain states. Discuss why it would be unwise to use state, or anything finer than state, as a predictor in the model. Also, discuss why id and country are bad predictors as well.

Comments: Different states have different costs of living, so this does play a role: however, as a main predictor it doesn't tell us much at all about what the consumer is buying and even with this difference in cost of living it's not much of a difference. Country would be bad because pretty much the entire dataset is the US and it's too broad to derive much information from. City/region/zip code are too narrow and the variation in cost between these doesn't make up for the fact that it partitions the data into very small subsets

Now we'll explore the category and sub_category variables! Again use group_by() and summarize() to show the mean profit and sample size (which you can find using the n() function) for each combination of category and sub-category. Then comment on your findings.

```
# summary for combinations of category and sub_category
categories <- train %>%
    group_by(category, sub_category) %>%
    summarise(meanProfit = mean(profit), sampleSize = n())
```

[`]summarise()` has grouped output by 'category'. You can override using the `.groups` argument.

categories

A tibble: 17 x 4

Groups: category [3]

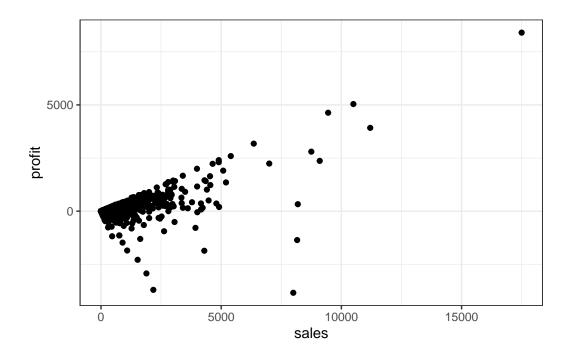
	categoi	-y	sub_category	${\tt meanProfit}$	sampleSize
	<chr></chr>		<chr></chr>	<dbl></dbl>	<int></int>
1	Furnit	ıre	Bookcases	13.2	172
2	Furnit	ıre	Chairs	52.3	442
3	Furnitu	ıre	Furnishings	13.3	664
4	Furniture		Tables	-56.9	230
5	${\tt Office}$	Supplies	Appliances	40.1	342
6	${\tt Office}$	Supplies	Art	8.94	574
7	${\tt Office}$	${\tt Supplies}$	Binders	22.4	1058
8	${\tt Office}$	${\tt Supplies}$	Envelopes	29.5	189
9	${\tt Office}$	${\tt Supplies}$	Fasteners	4.49	152
10	${\tt Office}$	${\tt Supplies}$	Labels	14.2	264
11	${\tt Office}$	${\tt Supplies}$	Paper	26.1	1023
12	${\tt Office}$	${\tt Supplies}$	Storage	32.5	611
13	${\tt Office}$	Supplies	Supplies	5.24	140
14	Technol	Logy	Accessories	56.6	550
15	Technol	Logy	Copiers	897.	47
16	Technol	Logy	Machines	268.	78
17	Technol	Logy	Phones	70.1	637

Comments: Tables lose a lot of money, maybe because their size makes distribution difficult, and to some extnt a smaller sample size than some categories. Copiers seem to make a ton of money, which despite their cost seems like a larger profit margin that I wouldve expected

Finally lets look at the quantitative predictors! I would like you to find and comment on the following:

- Scatterplot of sales vs. profit
- Correlation between sales and profit using cor()
- Correlation between quantity and profit
- Correlation between discount and profit
- Scatterplot of sales / quantity and profit

```
ggplot(train, aes(x=sales, y=profit)) + geom_point()
```



```
cor(train$sales, train$profit)
```

```
[1] 0.6218926
```

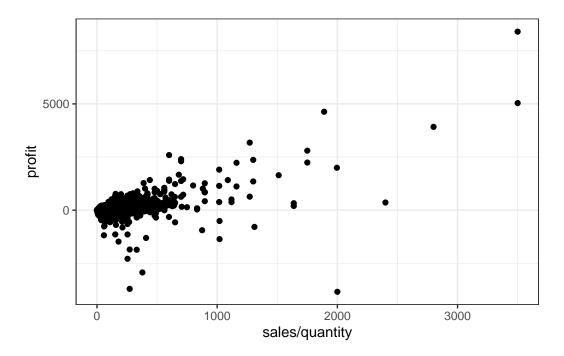
```
cor(train$quantity, train$profit)
```

[1] 0.0815635

```
cor(train$discount, train$profit)
```

[1] -0.2054159

```
ggplot(train, aes(x=sales/quantity, y=profit)) + geom_point()
```



Comments: 1) There is greater variance between data points at the far end of sales and profit. 2) There is a moderate correlation between sales and profit 3) There is no meaningful relationship between quantity and profit 4) There is a negligible negative correlation between discount and profit 5) There does appear to be correlation in this plot, even as sales/quantity approaches high/outlier values

Modeling

Let's start with just a simple model using sales as the predictor and profit as the response. Make the model, look at the summary, and comment on the usefulness of the model. Make sure to check the assumptions of simple linear regression!

```
fit <- lm(profit ~ sales, data = train)
fit</pre>
```

```
Call:
lm(formula = profit ~ sales, data = train)
Coefficients:
(Intercept) sales
-18.1576 0.2327
```

```
summary(fit)
```

```
Call:
lm(formula = profit ~ sales, data = train)
Residuals:
    Min
             1Q Median
                             3Q
                                    Max
-5683.6
                   19.6
            5.2
                           24.9 4345.5
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) -18.157582
                         2.209246
                                  -8.219 2.42e-16 ***
sales
              0.232721
                         0.003461 67.249 < 2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 174.1 on 7171 degrees of freedom
Multiple R-squared: 0.3868,
                                Adjusted R-squared: 0.3867
F-statistic: 4522 on 1 and 7171 DF, p-value: < 2.2e-16
```

Comments: The model estimates that about \$0.23 of profit is made for every \$1 of sales. The P value of 2.2e-16 indicates there is a strong relationship between these variables, but an r-squared of .39 indicates we should see significant variance along the way.

Now let's try sales / quantity instead of sales. To do this, you are going to have to use a special syntax in the formula. Instead of writing profit ~ sales / quantity you need to write profit ~ I(sales / quantity). The I() function tells the formula to treat whatever is inside it as literal. The division sign has a special meaning inside the formula syntax without the I(). Comment on the quality of fit and compare it to the previous one. Make sure to also look at the assumptions when comparing the two.

```
fit2 <- lm(profit ~ I(sales/quantity), data = train)
fit2</pre>
```

```
Call:
```

lm(formula = profit ~ I(sales/quantity), data = train)

Coefficients:

```
(Intercept) I(sales/quantity)
-20.4585 0.9165
```

```
summary(fit2)
```

Call:

lm(formula = profit ~ I(sales/quantity), data = train)

Residuals:

```
Min 1Q Median 3Q Max -5652.6 -2.7 19.2 25.4 5212.6
```

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept) -20.45853 2.33170 -8.774 <2e-16 ***
I(sales/quantity) 0.91654 0.01514 60.553 <2e-16 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 180.9 on 7171 degrees of freedom Multiple R-squared: 0.3383, Adjusted R-squared: 0.3382 F-statistic: 3667 on 1 and 7171 DF, p-value: < 2.2e-16

Comments: The model estimates that about 92 cents of profit are gained for every 1 point move of sales/quantity. With an r-squared of .34, there is significant variance along the trendline, but the p-value of 2.2e-16 shows us there is a correlation here.

Let's try to improve on our fit by adding in more variables that we saw were important from our EDA. I want you to include sales, quantity, discount, the interaction between category and subcategory, and the interaction between ship_mode and segment. To convey interactions between variables, you use the colon operator. For example, ship_mode:segment conveys the interaction between variables. Comment on the fit and compare to the other fits

```
fit3 <- lm(profit ~ sales + quantity + discount + category:sub_category + ship_mode:segmen
fit3</pre>
```

Call:

```
lm(formula = profit ~ sales + quantity + discount + category:sub_category +
```

ship_mode:segment, data = train) Coefficients: (Intercept) -127.8206 sales 0.2406 quantity -4.7890discount -219.4559 categoryFurniture:sub_categoryAccessories categoryOffice Supplies:sub_categoryAccessories categoryTechnology:sub_categoryAccessories 165.4858 categoryFurniture:sub_categoryAppliances NA categoryOffice Supplies:sub_categoryAppliances 168.0154 categoryTechnology:sub_categoryAppliances categoryFurniture:sub_categoryArt NA categoryOffice Supplies:sub_categoryArt 160.3569 categoryTechnology:sub_categoryArt categoryFurniture:sub_categoryBinders categoryOffice Supplies:sub_categoryBinders 209.6386 categoryTechnology:sub_categoryBinders categoryFurniture:sub_categoryBookcases 67.0892 categoryOffice Supplies:sub_categoryBookcases categoryTechnology:sub_categoryBookcases

107.4662

categoryFurniture:sub_categoryChairs

```
categoryOffice Supplies:sub_categoryChairs
                                             NA
          categoryTechnology:sub_categoryChairs
          categoryFurniture:sub_categoryCopiers
    categoryOffice Supplies:sub categoryCopiers
         categoryTechnology:sub categoryCopiers
                                       529.2610
        categoryFurniture:sub_categoryEnvelopes
  categoryOffice Supplies:sub_categoryEnvelopes
                                        172.0297
       categoryTechnology:sub_categoryEnvelopes
        categoryFurniture:sub_categoryFasteners
  categoryOffice Supplies:sub_categoryFasteners
                                       163.8926
       categoryTechnology:sub_categoryFasteners
      categoryFurniture:sub_categoryFurnishings
                                        168.2187
categoryOffice Supplies:sub_categoryFurnishings
     categoryTechnology:sub_categoryFurnishings
                                             NA
           categoryFurniture:sub_categoryLabels
                                             NA
     categoryOffice Supplies:sub_categoryLabels
                                        164.9791
          categoryTechnology:sub_categoryLabels
         categoryFurniture:sub_categoryMachines
                                             NA
   categoryOffice Supplies:sub categoryMachines
        categoryTechnology:sub_categoryMachines
                                        45.6333
            categoryFurniture:sub_categoryPaper
      categoryOffice Supplies:sub_categoryPaper
```

```
172.1167
categoryTechnology:sub_categoryPaper
categoryFurniture:sub_categoryPhones
                                  NA
```

categoryOffice Supplies:sub_categoryPhones

categoryTechnology:sub_categoryPhones 148.1339

categoryFurniture:sub_categoryStorage

NA

categoryOffice Supplies:sub_categoryStorage 128.3388

categoryTechnology:sub_categoryStorage

categoryFurniture:sub_categorySupplies

categoryOffice Supplies:sub_categorySupplies 104.2587

categoryTechnology:sub_categorySupplies

categoryFurniture:sub_categoryTables

categoryOffice Supplies:sub_categoryTables

NA

categoryTechnology:sub_categoryTables

ship_modeFirst Class:segmentConsumer -2.9132

ship_modeSame Day:segmentConsumer

5.5695

ship_modeSecond Class:segmentConsumer -8.5393

ship_modeStandard Class:segmentConsumer

-1.8032ship_modeFirst Class:segmentCorporate

0.2883

ship_modeSame Day:segmentCorporate

-72.5859

ship_modeSecond Class:segmentCorporate

-6.4441

ship_modeStandard Class:segmentCorporate

3.2000

```
ship_modeFirst Class:segmentHome Office
4.3741
ship_modeSame Day:segmentHome Office
1.0123
ship_modeSecond Class:segmentHome Office
2.9697
ship_modeStandard Class:segmentHome Office
NA
```

summary(fit3)

Call:

Residuals:

Min 1Q Median 3Q Max -5481.3 -23.3 0.3 30.4 3808.4

Coefficients: (36 not defined because of singularities)

	Estimate	Std. Error	t value
(Intercept)	-1.278e+02	1.287e+01	-9.931
sales	2.406e-01	3.767e-03	63.870
quantity	-4.789e+00	8.747e-01	-5.475
discount	-2.195e+02	1.077e+01	-20.374
categoryFurniture:sub_categoryAccessories	NA	NA	NA
<pre>categoryOffice Supplies:sub_categoryAccessories</pre>	NA	NA	NA
<pre>categoryTechnology:sub_categoryAccessories</pre>	1.655e+02	1.292e+01	12.808
categoryFurniture:sub_categoryAppliances	NA	NA	NA
<pre>categoryOffice Supplies:sub_categoryAppliances</pre>	1.680e+02	1.382e+01	12.155
<pre>categoryTechnology:sub_categoryAppliances</pre>	NA	NA	NA
categoryFurniture:sub_categoryArt	NA	NA	NA
<pre>categoryOffice Supplies:sub_categoryArt</pre>	1.604e+02	1.296e+01	12.370
categoryTechnology:sub_categoryArt	NA	NA	NA
categoryFurniture:sub_categoryBinders	NA	NA	NA
<pre>categoryOffice Supplies:sub_categoryBinders</pre>	2.096e+02	1.185e+01	17.691
categoryTechnology:sub_categoryBinders	NA	NA	NA
categoryFurniture:sub_categoryBookcases	6.709e+01	1.624e+01	4.132
<pre>categoryOffice Supplies:sub_categoryBookcases</pre>	NA	NA	NA
<pre>categoryTechnology:sub_categoryBookcases</pre>	NA	NA	NA

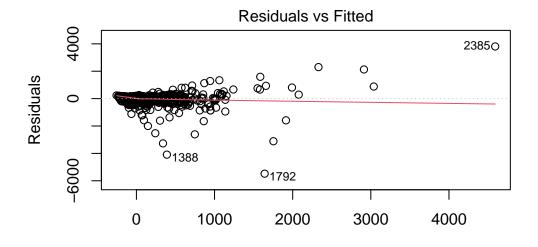
categoryFurniture:sub_categoryChairs	1.075e+02	1.311e+01	8.195
categoryOffice Supplies:sub_categoryChairs	NA	NA	NA
categoryTechnology:sub_categoryChairs	NA	NA	NA
categoryFurniture:sub_categoryCopiers	NA	NA	NA
categoryOffice Supplies:sub_categoryCopiers	NA	NA	NA
categoryTechnology:sub_categoryCopiers	5.293e+02	2.648e+01	19.990
categoryFurniture:sub_categoryEnvelopes	NA	NA	NA
categoryOffice Supplies:sub_categoryEnvelopes	1.720e+02	1.609e+01	10.694
categoryTechnology:sub_categoryEnvelopes	NA	NA	NA
categoryFurniture:sub_categoryFasteners	NA	NA	NA
categoryOffice Supplies:sub_categoryFasteners	1.639e+02	1.712e+01	9.573
categoryTechnology:sub_categoryFasteners	NA	NA	NA
categoryFurniture:sub_categoryFurnishings	1.682e+02	1.254e+01	13.413
<pre>categoryOffice Supplies:sub_categoryFurnishings</pre>	NA	NA	NA
categoryTechnology:sub_categoryFurnishings	NA	NA	NA
categoryFurniture:sub_categoryLabels	NA	NA	NA
<pre>categoryOffice Supplies:sub_categoryLabels</pre>	1.650e+02	1.488e+01	11.085
categoryTechnology:sub_categoryLabels	NA	NA	NA
categoryFurniture:sub_categoryMachines	NA	NA	NA
<pre>categoryOffice Supplies:sub_categoryMachines</pre>	NA	NA	NA
categoryTechnology:sub_categoryMachines	4.563e+01	2.147e+01	2.125
categoryFurniture:sub_categoryPaper	NA	NA	NA
<pre>categoryOffice Supplies:sub_categoryPaper</pre>	1.721e+02	1.215e+01	14.166
<pre>categoryTechnology:sub_categoryPaper</pre>	NA	NA	NA
categoryFurniture:sub_categoryPhones	NA	NA	NA
<pre>categoryOffice Supplies:sub_categoryPhones</pre>	NA	NA	NA
<pre>categoryTechnology:sub_categoryPhones</pre>	1.481e+02	1.250e+01	11.848
<pre>categoryFurniture:sub_categoryStorage</pre>	NA	NA	NA
<pre>categoryOffice Supplies:sub_categoryStorage</pre>	1.283e+02	1.271e+01	10.095
<pre>categoryTechnology:sub_categoryStorage</pre>	NA	NA	NA
categoryFurniture:sub_categorySupplies	NA	NA	NA
<pre>categoryOffice Supplies:sub_categorySupplies</pre>	1.043e+02	1.744e+01	5.979
<pre>categoryTechnology:sub_categorySupplies</pre>	NA	NA	NA
categoryFurniture:sub_categoryTables	NA	NA	NA
<pre>categoryOffice Supplies:sub_categoryTables</pre>	NA	NA	NA
<pre>categoryTechnology:sub_categoryTables</pre>	NA	NA	NA
<pre>ship_modeFirst Class:segmentConsumer</pre>	-2.913e+00	9.060e+00	-0.322
<pre>ship_modeSame Day:segmentConsumer</pre>	5.570e+00	1.257e+01	0.443
<pre>ship_modeSecond Class:segmentConsumer</pre>	-8.539e+00	8.421e+00	-1.014
ship_modeStandard Class:segmentConsumer	-1.803e+00	6.814e+00	-0.265
ship_modeFirst Class:segmentCorporate	2.883e-01	1.041e+01	0.028
ship_modeSame Day:segmentCorporate	-7.259e+01	1.963e+01	-3.698
<pre>ship_modeSecond Class:segmentCorporate</pre>	-6.444e+00	9.566e+00	-0.674

```
ship_modeStandard Class:segmentCorporate
                                                  3.200e+00 7.438e+00
                                                                          0.430
ship_modeFirst Class:segmentHome Office
                                                  4.374e+00 1.301e+01
                                                                          0.336
ship_modeSame Day:segmentHome Office
                                                  1.012e+00
                                                             1.822e+01
                                                                          0.056
ship_modeSecond Class:segmentHome Office
                                                  2.970e+00
                                                            1.186e+01
                                                                          0.250
ship modeStandard Class:segmentHome Office
                                                         NA
                                                                    NΑ
                                                                             NA
                                                 Pr(>|t|)
(Intercept)
                                                  < 2e-16 ***
sales
                                                  < 2e-16 ***
                                                 4.52e-08 ***
quantity
discount
                                                  < 2e-16 ***
                                                       NA
categoryFurniture:sub_categoryAccessories
                                                       NA
categoryOffice Supplies:sub_categoryAccessories
categoryTechnology:sub_categoryAccessories
                                                  < 2e-16 ***
categoryFurniture:sub_categoryAppliances
                                                       NA
categoryOffice Supplies:sub_categoryAppliances
                                                  < 2e-16 ***
                                                       NA
categoryTechnology:sub_categoryAppliances
categoryFurniture:sub_categoryArt
                                                       NA
categoryOffice Supplies:sub_categoryArt
                                                  < 2e-16 ***
categoryTechnology:sub_categoryArt
                                                       NA
categoryFurniture:sub categoryBinders
                                                       NA
categoryOffice Supplies:sub_categoryBinders
                                                  < 2e-16 ***
categoryTechnology:sub categoryBinders
                                                       NA
categoryFurniture:sub_categoryBookcases
                                                 3.64e-05 ***
categoryOffice Supplies:sub categoryBookcases
                                                       NA
categoryTechnology:sub_categoryBookcases
                                                       NΑ
                                                 2.95e-16 ***
categoryFurniture:sub_categoryChairs
categoryOffice Supplies:sub_categoryChairs
                                                       NA
categoryTechnology:sub_categoryChairs
                                                       NA
categoryFurniture:sub_categoryCopiers
                                                       NA
categoryOffice Supplies:sub_categoryCopiers
                                                       NA
                                                  < 2e-16 ***
categoryTechnology:sub_categoryCopiers
categoryFurniture:sub_categoryEnvelopes
                                                       NA
categoryOffice Supplies:sub_categoryEnvelopes
                                                  < 2e-16 ***
categoryTechnology:sub_categoryEnvelopes
                                                       NA
categoryFurniture:sub categoryFasteners
                                                       NA
categoryOffice Supplies:sub_categoryFasteners
                                                  < 2e-16 ***
categoryTechnology:sub categoryFasteners
                                                       NA
categoryFurniture:sub_categoryFurnishings
                                                  < 2e-16 ***
categoryOffice Supplies:sub_categoryFurnishings
                                                       NA
categoryTechnology:sub_categoryFurnishings
                                                       NΑ
categoryFurniture:sub_categoryLabels
                                                       NA
categoryOffice Supplies:sub_categoryLabels
                                                  < 2e-16 ***
categoryTechnology:sub_categoryLabels
                                                       NA
```

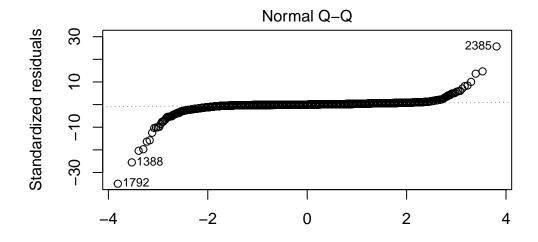
```
categoryFurniture:sub_categoryMachines
                                                      NA
categoryOffice Supplies:sub_categoryMachines
                                                      NA
categoryTechnology:sub_categoryMachines
                                                0.033623 *
categoryFurniture:sub_categoryPaper
                                                      NA
categoryOffice Supplies:sub categoryPaper
                                                 < 2e-16 ***
categoryTechnology:sub_categoryPaper
                                                      NA
categoryFurniture:sub categoryPhones
                                                      NA
categoryOffice Supplies:sub_categoryPhones
                                                      NA
categoryTechnology:sub_categoryPhones
                                                 < 2e-16 ***
categoryFurniture:sub_categoryStorage
                                                      NΑ
categoryOffice Supplies:sub_categoryStorage
                                                 < 2e-16 ***
categoryTechnology:sub_categoryStorage
                                                      NA
categoryFurniture:sub_categorySupplies
                                                      NA
                                                2.35e-09 ***
categoryOffice Supplies:sub_categorySupplies
categoryTechnology:sub_categorySupplies
                                                      NA
categoryFurniture:sub_categoryTables
                                                      NA
categoryOffice Supplies:sub_categoryTables
                                                      NA
categoryTechnology:sub_categoryTables
                                                      NA
ship_modeFirst Class:segmentConsumer
                                                0.747799
ship modeSame Day:segmentConsumer
                                                0.657798
ship_modeSecond Class:segmentConsumer
                                                0.310589
ship modeStandard Class:segmentConsumer
                                                0.791294
ship_modeFirst Class:segmentCorporate
                                                0.977913
ship_modeSame Day:segmentCorporate
                                                0.000219 ***
ship_modeSecond Class:segmentCorporate
                                                0.500566
ship_modeStandard Class:segmentCorporate
                                                0.667037
ship_modeFirst Class:segmentHome Office
                                                0.736739
                                                0.955705
ship_modeSame Day:segmentHome Office
ship_modeSecond Class:segmentHome Office
                                                0.802300
ship_modeStandard Class:segmentHome Office
                                                      NA
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 160.6 on 7142 degrees of freedom Multiple R-squared: 0.4807, Adjusted R-squared: 0.4785 F-statistic: 220.3 on 30 and 7142 DF, p-value: < 2.2e-16

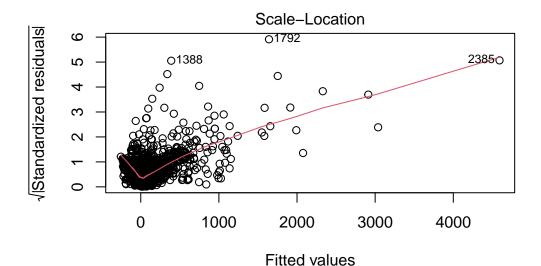
plot(fit3)



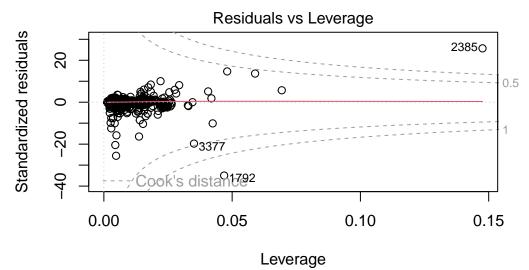
Fitted values
Im(profit ~ sales + quantity + discount + category:sub_category + ship_mo



Theoretical Quantiles
Im(profit ~ sales + quantity + discount + category:sub_category + ship_mo



Im(profit ~ sales + quantity + discount + category:sub_category + ship_mo



lm(profit ~ sales + quantity + discount + category:sub_category + ship_mo

Comments: In the interaction between ship_mode and segment, we see only one statistically significant grouping. These are the only outliers, as the rest appear to correlate strongly. The multiple r-squared of .48 isn't too great here, especially because we are working with multiple variables which should push the number up. It's also interesting that quantity negatively impacts profit so much.

Now we are going to use a simpler model to predict on the test set. Use a model that employs sales, quantity, and discount as the predictors. Fit the model and then use the predict()

function to predict new values on the test set. Unfortunately, we don't know the truth, so we can't compare our predictions.

```
fit4 <- lm(profit ~ sales + quantity + discount, data = train)
  fit4
Call:
lm(formula = profit ~ sales + quantity + discount, data = train)
Coefficients:
(Intercept)
                           quantity
                 sales
                                       discount
    25.1048
                 0.2339
                            -4.2897
                                       -205.2987
  summary(fit4)
Call:
lm(formula = profit ~ sales + quantity + discount, data = train)
Residuals:
            1Q Median
                           3Q
                                  Max
   Min
-5616.5 -14.6 1.5
                          29.1 4303.1
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) 2.510e+01 4.136e+00 6.070 1.34e-09 ***
            2.339e-01 3.431e-03 68.163 < 2e-16 ***
sales
quantity
           -4.290e+00 9.112e-01 -4.708 2.55e-06 ***
discount
           -2.053e+02 9.941e+00 -20.652 < 2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Residual standard error: 168.9 on 7169 degrees of freedom
Multiple R-squared: 0.4233, Adjusted R-squared: 0.423
F-statistic: 1754 on 3 and 7169 DF, p-value: < 2.2e-16
  predict(fit4, data.frame(sales = 1000, quantity = 10, discount = .2))
```

```
1
175.0454

predict(fit4, data.frame(sales = 500, quantity = 1, discount = .1))

1
117.234
```