MATPOWER Interior Point Solver MIPS 1.5.2 User's Manual

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Contents

1	Inti	roduct	ion	5				
	1.1	Backg	round	5				
	1.2		se and Terms of Use	6				
	1.3		g MIPS	7				
	1.4		Development	7				
2	Get	$ ag{ting S}$	tarted	8				
	2.1	Syster	m Requirements	8				
	2.2	Instal	$rac{1}{2} = 1$	8				
	2.3	Docur	nentation	9				
3	MIPS – MATPOWER Interior Point Solver							
	3.1	Exam	$\operatorname{ple} 1$	14				
	3.2	Exam	$\stackrel{ ext{-}}{ ext{ple}} 2$	15				
	3.3	Prima	ll-Dual Interior Point Algorithm	17				
		3.3.1	<u> </u>	17				
		3.3.2	Problem Formulation and Lagrangian	18				
		3.3.3	First Order Optimality Conditions	19				
		3.3.4	Newton Step					
4	Oth	ner Fur	actions	22				
	4.1	Linear	r System Solver - mplinsolve	22				
	4.2		ratic Programming Solver - qps_mips	23				
	4.3		te Feature Detection Functions	24				
		4.3.1	have_feature_lu_vec	24				
		4.3.2	have_feature_mips	24				
		4.3.3	have_feature_pardiso_legacy					
		4.3.4	have_feature_pardiso_object					
		4.3.5	have_feature_pardiso					
5	Ack	knowle	${f dgments}$	25				
\mathbf{A}	ppen	dix A	MIPS Files and Functions	26				
\mathbf{A}	ppen	dix B	PARDISO – Parallel Sparse Direct and Multi-Recursive	e				
			Linear Solvers	27				

Appendix C Release History	28
C.1 Version 1.0 – released Feb 7, 2011	28
C.2 Version 1.0.1 – released Apr 30, 2012	28
C.3 Version 1.0.2 – released Nov 5, 2013	28
C.4 Version 1.1 – released Dec 17, 2014	29
C.5 Version 1.2 – released Mar 20, 2015	29
C.6 Version 1.2.1 – released Jun 1, 2016	30
C.7 Version 1.2.2 – released Dec 16, 2016	30
C.8 Version 1.3 – released Oct 30, 2018	31
C.9 Version 1.3.1 – released Jun 20, 2019	32
C.10 Version 1.4 – released Oct 8, 2020	32
C.11 Version 1.5 – released Dec 12, 2022	33
C.12 Version 1.5.1 – released May 10, 2024	33
C.13 Version 1.5.2 – released Jul 5, 2025	34
References	35

List of Tables

3-1	Input Arguments for mips	
3-2	Output Arguments for mips	
3-3	Options for mips	
A-1	MIPS Files and Functions	

1 Introduction

1.1 Background

MATPOWER Interior Point Solver (MIPS) is a package of MATLAB language M-files¹ for solving non-linear programming problems (NLPs) using a primal dual interior point method. The MIPS project page can be found at:

https://github.com/MATPOWER/mips

MIPS is based on code written in C language [1] by Hongye Wang as a graduate student at Cornell University for optimal power flow applications [2, 3]. It was later ported to the MATLAB language by Ray D. Zimmerman of PSERC² at Cornell University for use in MATPOWER [4, 5].

Up until version 6 of MATPOWER, MIPS was distributed only as an integrated part of MATPOWER. After the release of MATPOWER 6, MIPS was split out into a separate project, though it is still included with MATPOWER as its default AC optimal power flow solver.

¹Also compatible with GNU Octave [7].

²http://pserc.org/

1.2 License and Terms of Use

The code in MIPS is distributed under the 3-clause BSD license³ [8]. The full text of the license can be found in the LICENSE file at the top level of the distribution or at https://github.com/MATPOWER/mips/blob/master/LICENSE and reads as follows.

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³Versions 1.0 through 1.1 of MIPS were distributed under version 3.0 of the GNU General Public License (GPL) [9] with an exception added to clarify our intention to allow MIPS to interface with MATLAB as well as any other MATLAB code or MEX-files a user may have installed, regardless of their licensing terms. The full text of the GPL can be found at https://www.gnu.org/licenses/gpl-3.0.txt.

1.3 Citing MIPS

We request that publications derived from the use of MIPS explicitly acknowledge that fact by citing the following 2007 paper [2].

```
H. Wang, C. E. Murillo-Sánchez, R. D. Zimmerman, and R. J. Thomas, "On Computational Issues of Market-Based Optimal Power Flow," Power Systems, IEEE Transactions on, vol. 22, no. 3, pp. 1185–1193, August 2007. doi: 10.1109/TPWRS.2007.901301
```

The MATPOWER Interior Point Solver (MIPS) User's Manual [6] should also be cited explicitly in work that refers to or is derived from its content. The citation and DOI can be version-specific or general, as appropriate. For version 1.5.2, use:

```
R. D. Zimmerman, H. Wang. MATPOWER Interior Point Solver (MIPS) User's Manual, Version 1.5.2. 2025. [Online]. Available: https://matpower.org/docs/MIPS-manual-1.5.2.pdf doi: 10.5281/zenodo.15815754
```

For a version non-specific citation, use the following citation and DOI, with $\langle YEAR \rangle$ replaced by the year of the most recent release:

```
R. D. Zimmerman, H. Wang. MATPOWER Interior Point Solver (MIPS) User's Manual. <\(YEAR\)>. [Online]. Available: https://matpower.org/docs/MIPS-manual.pdf
doi: 10.5281/zenodo.3236506
```

A list of versions of the User's Manual with release dates and version-specific DOI's can be found via the general DOI at https://doi.org/10.5281/zenodo.3236506.

1.4 MIPS Development

Following the release of MIPS 1.2.2 (with MATPOWER 6.0), the MIPS project moved to an open development paradigm, hosted on the MIPS GitHub project page:

```
https://github.com/MATPOWER/mips
```

The MIPS GitHub project hosts the public Git code repository as well as a public issue tracker for handling bug reports, patches, and other issues and contributions. There are separate GitHub hosted repositories and issue trackers for MATPOWER, MOST, MP-Opt-Model and the testing framework used by all of them, MP-Test, all available from https://github.com/MATPOWER/.

2 Getting Started

2.1 System Requirements

To use MIPS 1.5.2 you will need:

- Matlab[®] version 7 (R14) or later⁴, or
- GNU Octave version 3.4 or later⁵
- MP-Test version 7.1 or later.⁶

For the hardware requirements, please refer to the system requirements for the version of Matlab⁷ or Octave that you are using.

In this manual, references to MATLAB usually apply to Octave as well.

2.2 Installation

Note to Matpower users: MIPS and its prerequisite, MP-Test, are included when you install Matpower. There is generally no need to install them separately. You can skip directly to step 3 to verify.

Installation and use of MIPS requires familiarity with the basic operation of MATLAB or Octave, including setting up your MATLAB/Octave path.

Step 1: Clone the repository or download and extract the zip file of the MIPS distribution from the MIPS project page⁸ to the location of your choice. The files in the resulting mips or mipsxxx directory, where xxx depends on the version of MIPS, should not need to be modified, so it is recommended that they be kept separate from your own code. We will use <MIPS> to denote the path to this directory.

⁴Matlab is available from The MathWorks, Inc. (https://www.mathworks.com/). Matlab is a registered trademark of The MathWorks, Inc.

⁵GNU Octave [7] is free software, available online at https://octave.org. MIPS 1.5.2 may work on earlier versions of Octave, but it has not been tested on versions prior to 3.4.

⁶MP-Test is available at https://github.com/MATPOWER/mptest.

⁷https://www.mathworks.com/support/sysreq/previous_releases.html

⁸https://github.com/MATPOWER/mips

Step 2: Add the following directories to your MATLAB or Octave path:

- <MIPS>/lib core MIPS functions
- <MIPS>/lib/t test scripts for MIPS

Step 3: At the MATLAB/Octave prompt, type test_mips to run the test suite and verify that MIPS is properly installed and functioning. The result should resemble the following:

```
>> test_mips
t_mplinsolve.....ok (8 of 180 skipped)
t_mips......ok
t_mips_pardiso....ok (60 of 60 skipped)
t_qps_mips.....ok
All tests successful (304 passed, 68 skipped of 372)
Elapsed time 0.07 seconds.
```

2.3 Documentation

And second is the built-in help command. As with the built-in functions and toolbox routines in Matlab and Octave, you can type help followed by the name of a command or M-file to get help on that particular function. All of the M-files in MIPS have such documentation and this should be considered the main reference for the calling options for each function. See Appendix A for a list of MIPS functions.

⁹The tests require a functioning installation of MP-Test.

3 MIPS – MATPOWER Interior Point Solver

MIPS, that is, the MATPOWER Interior Point Solver, is a primal-dual interior point solver implemented in pure MATLAB code, derived from the MEX implementation of the algorithms included in TSPOPF [1] and described in [2,3].

This solver has application to general nonlinear optimization problems of the following form:

$$\min_{x} f(x) \tag{3.1}$$

subject to

$$g(x) = 0 (3.2)$$

$$h(x) \le 0 \tag{3.3}$$

$$l < Ax < u \tag{3.4}$$

$$x_{\min} \le x \le x_{\max} \tag{3.5}$$

where $f: \mathbb{R}^n \to \mathbb{R}$, $g: \mathbb{R}^n \to \mathbb{R}^m$ and $h: \mathbb{R}^n \to \mathbb{R}^p$.

The solver is implemented by the mips function, which can be called as follows,

```
[x, f, exitflag, output, lambda] = ...
mips(f_fcn, x0, A, l, u, xmin, xmax, gh_fcn, hess_fcn, opt);
```

where the input and output arguments are described in Tables 3-1 and 3-2, respectively. Alternatively, the input arguments can be packaged as fields in a problem struct and passed in as a single argument, where all fields except f_fcn and x0 are optional.

```
[x, f, exitflag, output, lambda] = mips(problem);
```

The calling syntax is nearly identical to that used by fmincon from MATLAB's Optimization Toolbox. The primary difference is that the linear constraints are specified in terms of a single doubly-bounded linear function ($l \le Ax \le u$) as opposed to separate equality constrained ($A_{eq}x = b_{eq}$) and upper bounded ($Ax \le b$) functions. Internally, equality constraints are handled explicitly and determined at run-time based on the values of l and u.

The user-defined functions for evaluating the objective function, constraints and Hessian are identical to those required by fmincon, with one exception described below for the Hessian evaluation function. Specifically, f-fcn should return f as the scalar objective function value f(x), df as an $n \times 1$ vector equal to ∇f and, unless

Table 3-1: Input Arguments for mips[†]

name	description
f_fcn	Handle to a function that evaluates the objective function, its gradients and Hessian [‡] for a given value of x . Calling syntax for this function: [f, df, d2f] = f_fcn(x)
x0	Starting value of optimization vector x .
A, 1, u	Define the optional linear constraints $l \leq Ax \leq u$. Default values for the elements of 1 and u are -Inf and Inf, respectively.
${\tt xmin}, {\tt xmax}$	Optional lower and upper bounds on the x variables, defaults are -Inf and Inf, respectively.
gh_fcn	Handle to function that evaluates the optional nonlinear constraints and their gradients for a given value of x . Calling syntax for this function is: $[h, g, dh, dg] = gh_f cn(x)$
hess_fcn	where the columns of dh and dg are the gradients of the corresponding elements of h and g, i.e. dh and dg are transposes of the Jacobians of h and g, respectively. Handle to function that computes the Hessian of the Lagrangian for given values of x , λ and μ , where λ and μ are the multipliers on the equality and inequality constraints, g and h , respectively. The calling syntax for this function is: Lxx = hess_fcn(x, lam, cost_mult), where λ = lam.eqnonlin, μ = lam.ineqnonlin and cost_mult is a parameter used
opt	to scale the objective function Optional options structure with fields, all of which are also optional, described in Table 3-3.
problem	Alternative, single argument input struct with fields corresponding to arguments above.

[†] All inputs are optional except f_fcn and x0.

gh_fcn is provided and the Hessian is computed by hess_fcn, d2f as an $n \times n$ matrix equal to the Hessian $\frac{\partial^2 f}{\partial x^2}$. Similarly, the constraint evaluation function gh_fcn must return the $m \times 1$ vector of nonlinear equality constraint violations g(x), the $p \times 1$ vector of nonlinear inequality constraint violations h(x) along with their gradients in dg and dh. Here dg is an $n \times m$ matrix whose j^{th} column is ∇g_j and dh is $n \times p$, with j^{th} column equal to ∇h_j . Finally, for cases with nonlinear constraints, hess_fcn returns the $n \times n$ Hessian $\frac{\partial^2 \mathcal{L}}{\partial x^2}$ of the Lagrangian function

$$\mathcal{L}(x,\lambda,\mu,\sigma) = \sigma f(x) + \lambda^{\mathsf{T}} g(x) + \mu^{\mathsf{T}} h(x)$$
(3.6)

for given values of the multipliers λ and μ , where σ is the cost_mult scale factor for the objective function. Unlike fmincon, mips passes this scale factor to the Hessian evaluation function in the 3rd input argument.

[‡] If gh.fcn is provided then hess_fcn is also required. Specifically, if there are nonlinear constraints, the Hessian information must be provided by the hess_fcn function and it need not be computed in f_fcn.

Table 3-2: Output Arguments for mips

name	description			
х	solution vector			
f	final objective function value			
exitflag	exit flag			
	1 - first orde	er optimality conditions satisfied		
	0 - maximur	n number of iterations reached		
	-1 – numerica	ally failed		
output	output struct with fields			
	iterations	number of iterations performed		
	hist	struct array with trajectories of the following: feascond,		
		gradcond, compcond, costcond, gamma, stepsize, obj, alphap,		
		alphad		
	message	exit message		
lambda	struct contain	ing the Langrange and Kuhn-Tucker multipliers on the con-		
	straints, with f			
	eqnonlin	nonlinear equality constraints		
	ineqnonlin	nonlinear inequality constraints		
	$\mathtt{mu_l}$	lower (left-hand) limit on linear constraints		
	mu_u	upper (right-hand) limit on linear constraints		
	lower	lower bound on optimization variables		
	upper	upper bound on optimization variables		

The use of nargout in f_fcn and gh_fcn is recommended so that the gradients and Hessian are only computed when required.

Table 3-3: Options for mips

name	default	description
opt.verbose	0	controls level of progress output displayed 0 – print no progress info 1 – print a little progress info 2 – print a lot of progress info 3 – print all progress info
opt.linsolver	11	linear system solver for solving update steps (3.42), i.e. solver input to mplinsolve '' - default, same as '\' '\' - use built-in \ operator 'LU' - use lu to explicitly factor matrix, followed by back-substitution
<pre>opt.feastol opt.gradtol opt.comptol opt.costtol opt.max_it opt.step_control opt.sc.red_it opt.cost_mult</pre>	$ \begin{array}{c} 10^{-6} \\ 10^{-6} \\ 10^{-6} \\ 10^{-6} \\ 150 \\ 0 \\ 20 \\ 1 \end{array} $	'PARDISO' – use optional third-party PARDISO solver [†] termination tolerance for feasibility condition termination tolerance for gradient condition termination tolerance for complementarity condition termination tolerance for cost condition maximum number of iterations set to 1 to enable step-size control max number of step-size reductions if step-control is on cost multiplier used to scale the objective function for improved conditioning. Note: This value is also passed as the 3 rd argument to the Hessian evaluation function so that it can appropriately scale the objective function term in the Hessian of the
opt.xi opt.sigma opt.z0 opt.alpha_min	0.99995 0.1 1 10^{-8}	Lagrangian. ξ constant used in α updates in (3.43) and (3.44) centering parameter σ used in γ update in (3.49) used to initialize elements of slack variable Z algorithm returns "Numerically Failed" if the α_p or α_d from (3.43) and (3.44) become smaller than this value
<pre>opt.rho_min opt.rho_max opt.mu_threshold opt.max_stepsize</pre>	$0.95 \\ 1.05 \\ 10^{-5} $ 10^{10}	lower bound on ρ_t corresponding to $1 - \eta$ in Fig. 5 in [2] upper bound on ρ_t corresponding to $1 + \eta$ in Fig. 5 in [2] Kuhn-Tucker multipliers smaller than this value for non-binding constraints are forced to zero algorithm returns "Numerically Failed" if the 2-norm of the New-
		ton step $\begin{bmatrix} \Delta X \\ \Delta \lambda \end{bmatrix}$ from (3.42) exceeds this value

[†] Requires the installation of an optional package. See Appendix B for details.

3.1 Example 1

The following code, included as mips_example1.m in <MIPS>lib/t, shows a simple example of using mips to solve a 2-dimensional unconstrained optimization of Rosenbrock's "banana" function¹⁰

$$f(x) = 100(x_2 - x_1^2)^2 + (1 - x_1)^2. (3.7)$$

First, create a MATLAB function that will evaluate the objective function, its gradients and Hessian, for a given value of x. In this case, the coefficient of the first term is defined as a paramter a.

Then, create a handle to the function, defining the value of the paramter **a** to be 100, set up the starting value of x, and call the mips function to solve it.

```
>> f_fcn = @(x)banana(x, 100);
>> x0 = [-1.9; 2];
>> [x, f] = mips(f_fcn, x0)

x =

1
1
1
f =
0
```

¹⁰https://en.wikipedia.org/wiki/Rosenbrock_function

3.2Example 2

The second example¹¹ solves the following 3-dimensional constrained optimization, printing the details of the solver's progress:

$$\min_{x} f(x) = -x_1 x_2 - x_2 x_3 \tag{3.8}$$

subject to

$$x_1^2 - x_2^2 + x_3^2 - 2 \le 0 (3.9)$$

$$x_1^2 - x_2^2 + x_3^2 - 2 \le 0$$
 (3.9)
 $x_1^2 + x_2^2 + x_3^2 - 10 \le 0.$ (3.10)

First, create a MATLAB function to evaluate the objective function and its gradients, 12

```
function [f, df, d2f] = f2(x)
f = -x(1)*x(2) - x(2)*x(3);
if nargout > 1
                          %% gradient is required
    df = -[x(2); x(1)+x(3); x(2)];
    if nargout > 2
                          %% Hessian is required
        d2f = -[0 \ 1 \ 0; \ 1 \ 0 \ 1; \ 0 \ 1 \ 0];
                                          %% actually not used since
                                          %% 'hess_fcn' is provided
    end
end
```

one to evaluate the constraints, in this case inequalities only, and their gradients,

```
function [h, g, dh, dg] = gh2(x)
h = [1 -1 1; 1 1] * x.^2 + [-2; -10];
dh = 2 * [x(1) x(1); -x(2) x(2); x(3) x(3)];
g = []; dg = [];
```

and another to evaluate the Hessian of the Lagrangian.

```
function Lxx = hess2(x, lam, cost_mult)
if nargin < 3, cost_mult = 1; end</pre>
                                     %% allows to be used with 'fmincon'
mu = lam.ineqnonlin;
Lxx = cost_mult * [0 -1 0; -1 0 -1; 0 -1 0] + ...
        [2*[1 1]*mu 0 0; 0 2*[-1 1]*mu 0; 0 0 2*[1 1]*mu];
```

¹¹From https://en.wikipedia.org/wiki/Nonlinear_programming#3-dimensional_example.

¹²Since the problem has nonlinear constraints and the Hessian is provided by hess_fcn, this function will never be called with three output arguments, so the code to compute d2f is actually not necessary.

Then create a problem struct with handles to these functions, a starting value for x and an option to print the solver's progress. Finally, pass this struct to mips to solve the problem and print some of the return values to get the output below.

```
function mips_example2
problem = struct( ...
    'f_fcn', Q(x)f2(x), ...
    'gh_fcn', @(x)gh2(x), ...
    'hess_fcn', @(x, lam, cost_mult)hess2(x, lam, cost_mult), ...
             [1; 1; 0], ...
    'x0',
            struct('verbose', 2) ...
    'opt',
);
[x, f, exitflag, output, lambda] = mips(problem);
fprintf('\nf = %g exitflag = %d\n', f, exitflag);
fprintf('\nx = \n');
fprintf('
           %g\n', x);
fprintf('\nlambda.ineqnonlin =\n');
fprintf('
           %g\n', lambda.ineqnonlin);
```

```
>> mips_example2
MATPOWER Interior Point Solver -- MIPS, Version 1.5.2, 05-Jul-2025
  (using built-in linear solver)
               objective step size feascond gradcond compcond
                                                                                                                                                    {\tt costcond}

        0
        1.5
        5
        0

        1
        -5.3250167
        1.6875
        0
        0.894235
        0.850653
        2.16251

        2
        -7.4708991
        0.97413
        0.129183
        0.00936418
        0.117278
        0.339269

        3
        -7.0553031
        0.10406
        0
        0.00174933
        0.0196518
        0.0490616

        4
        -7.0686267
        0.034574
        0
        0.00041301
        0.0030084
        0.00165402

        5
        -7.0706104
        0.0065191
        0
        1.53531e-05
        0.000337971
        0.0004155

        6
        -7.0710134
        0.00062152
        0
        0.0004150
        0.0004150

                                                                                 0 1.22094e-07 3.41308e-05 4.99387e-05 
0 9.84878e-10 3.41587e-06 6.05875e-06
              -7.0710623 5.7217e-05
-7.0710673 5.6761e-06
    7
                                                                                  0 9.73553e-12 3.41615e-07 6.15483e-07
Converged!
f = -7.07107 exitflag = 1
x =
      1.58114
      2.23607
      1.58114
lambda.ineqnonlin =
       0.707107
```

This example can be found in mips_example2.m. More example problems for mips can be found in t_mips.m, both in <MIPS>lib/t.

3.3 Primal-Dual Interior Point Algorithm

This section provides some details on the primal-dual interior point algorithm used by MIPS and described in [2, 3].

3.3.1 Notation

For a scalar function $f: \mathbb{R}^n \to \mathbb{R}$ of a real vector $X = \begin{bmatrix} x_1 & x_2 & \cdots & x_n \end{bmatrix}^\mathsf{T}$, we use the following notation for the first derivatives (transpose of the gradient):

$$f_X = \frac{\partial f}{\partial X} = \begin{bmatrix} \frac{\partial f}{\partial x_1} & \frac{\partial f}{\partial x_2} & \cdots & \frac{\partial f}{\partial x_n} \end{bmatrix}.$$
 (3.11)

The matrix of second partial derivatives, the Hessian of f, is:

$$f_{XX} = \frac{\partial^2 f}{\partial X^2} = \frac{\partial}{\partial X} \left(\frac{\partial f}{\partial X} \right)^{\mathsf{T}} = \begin{bmatrix} \frac{\partial^2 f}{\partial x_1^2} & \cdots & \frac{\partial^2 f}{\partial x_1 \partial x_n} \\ \vdots & \ddots & \vdots \\ \frac{\partial^2 f}{\partial x_n \partial x_1} & \cdots & \frac{\partial^2 f}{\partial x_n^2} \end{bmatrix}. \tag{3.12}$$

For a vector function $F: \mathbb{R}^n \to \mathbb{R}^m$ of a vector X, where

$$F(X) = \begin{bmatrix} f_1(X) & f_2(X) & \cdots & f_m(X) \end{bmatrix}^\mathsf{T}$$
 (3.13)

the first derivatives form the Jacobian matrix, where row i is the transpose of the gradient of f_i

$$F_X = \frac{\partial F}{\partial X} = \begin{bmatrix} \frac{\partial f_1}{\partial x_1} & \cdots & \frac{\partial f_1}{\partial x_n} \\ \vdots & \ddots & \vdots \\ \frac{\partial f_m}{\partial x_1} & \cdots & \frac{\partial f_m}{\partial x_n} \end{bmatrix}.$$
 (3.14)

In these derivations, the full 3-dimensional set of second partial derivatives of F will not be computed. Instead a matrix of partial derivatives will be formed by computing the Jacobian of the vector function obtained by multiplying the transpose of the Jacobian of F by a vector λ , using the following notation

$$F_{XX}(\lambda) = \frac{\partial}{\partial X} \left(F_X^{\mathsf{T}} \lambda \right). \tag{3.15}$$

Please note also that [A] is used to denote a diagonal matrix with vector A on the diagonal and e is a vector of all ones.

3.3.2 Problem Formulation and Lagrangian

The primal-dual interior point method used by MIPS solves a problem of the form:

$$\min_{X} f(X) \tag{3.16}$$

subject to

$$G(X) = 0 (3.17)$$

$$H(X) < 0 \tag{3.18}$$

where the linear constraints and variable bounds from (3.4) and (3.5) have been incorporated into G(X) and H(X). The approach taken involves converting the n_i inequality constraints into equality constraints using a barrier function and vector of positive slack variables Z.

$$\min_{X} \left[f(X) - \gamma \sum_{m=1}^{n_i} \ln(Z_m) \right] \tag{3.19}$$

subject to

$$G(X) = 0 (3.20)$$

$$H(X) + Z = 0 \tag{3.21}$$

$$Z > 0 \tag{3.22}$$

As the parameter of perturbation γ approaches zero, the solution to this problem approaches that of the original problem.

For a given value of γ , the Lagrangian for this equality constrained problem is

$$\mathcal{L}^{\gamma}(X, Z, \lambda, \mu) = f(X) + \lambda^{\mathsf{T}} G(X) + \mu^{\mathsf{T}} (H(X) + Z) - \gamma \sum_{m=1}^{n_i} \ln(Z_m).$$
 (3.23)

Taking the partial derivatives with respect to each of the variables yields:

$$\mathcal{L}_{X}^{\gamma}(X, Z, \lambda, \mu) = f_{X} + \lambda^{\mathsf{T}} G_{X} + \mu^{\mathsf{T}} H_{X}$$
 (3.24)

$$\mathcal{L}_{Z}^{\gamma}(X, Z, \lambda, \mu) = \mu^{\mathsf{T}} - \gamma e^{\mathsf{T}} [Z]^{-1}$$
(3.25)

$$\mathcal{L}_{\lambda}^{\gamma}(X, Z, \lambda, \mu) = G^{\mathsf{T}}(X) \tag{3.26}$$

$$\mathcal{L}^{\gamma}_{\mu}(X, Z, \lambda, \mu) = H^{\mathsf{T}}(X) + Z^{\mathsf{T}}. \tag{3.27}$$

And the Hessian of the Lagrangian with respect to X is given by

$$\mathcal{L}_{XX}^{\gamma}(X,Z,\lambda,\mu) = f_{XX} + G_{XX}(\lambda) + H_{XX}(\mu). \tag{3.28}$$

3.3.3 First Order Optimality Conditions

The first order optimality (Karush-Kuhn-Tucker) conditions for this problem are satisfied when the partial derivatives of the Lagrangian above are all set to zero:

$$F(X, Z, \lambda, \mu) = 0 \tag{3.29}$$

$$Z > 0 \tag{3.30}$$

$$\mu > 0 \tag{3.31}$$

where

$$F(X, Z, \lambda, \mu) = \begin{bmatrix} \mathcal{L}_X^{\gamma \mathsf{T}} \\ [\mu] Z - \gamma e \\ G(X) \\ H(X) + Z \end{bmatrix} = \begin{bmatrix} f_X^{\mathsf{T}} + G_X^{\mathsf{T}} \lambda + H_X^{\mathsf{T}} \mu \\ [\mu] Z - \gamma e \\ G(X) \\ H(X) + Z \end{bmatrix}. \tag{3.32}$$

3.3.4 Newton Step

The first order optimality conditions are solved using Newton's method. The Newton update step can be written as follows:

$$\begin{bmatrix} F_X & F_Z & F_{\lambda} & F_{\mu} \end{bmatrix} \begin{bmatrix} \Delta X \\ \Delta Z \\ \Delta \lambda \\ \Delta \mu \end{bmatrix} = -F(X, Z, \lambda, \mu)$$
 (3.33)

$$\begin{bmatrix} \mathcal{L}_{XX}^{\gamma} & 0 & G_{X}^{\mathsf{T}} & H_{X}^{\mathsf{T}} \\ 0 & [\mu] & 0 & [Z] \\ G_{X} & 0 & 0 & 0 \\ H_{X} & I & 0 & 0 \end{bmatrix} \begin{bmatrix} \Delta X \\ \Delta Z \\ \Delta \lambda \\ \Delta \mu \end{bmatrix} = - \begin{bmatrix} \mathcal{L}_{X}^{\gamma \mathsf{T}} \\ [\mu] Z - \gamma e \\ G(X) \\ H(X) + Z \end{bmatrix}.$$
(3.34)

This set of equations can be simplified and reduced to a smaller set of equations by solving explicitly for $\Delta \mu$ in terms of ΔZ and for ΔZ in terms of ΔX . Taking the 2^{nd} row of (3.34) and solving for $\Delta \mu$ we get

$$[\mu] \Delta Z + [Z] \Delta \mu = -[\mu] Z + \gamma e$$

$$[Z] \Delta \mu = -[Z] \mu + \gamma e - [\mu] \Delta Z$$

$$\Delta \mu = -\mu + [Z]^{-1} (\gamma e - [\mu] \Delta Z). \tag{3.35}$$

Solving the 4th row of (3.34) for ΔZ yields

$$H_X \Delta X + \Delta Z = -H(X) - Z$$

$$\Delta Z = -H(X) - Z - H_X \Delta X. \tag{3.36}$$

Then, substituting (3.35) and (3.36) into the 1st row of (3.34) results in

$$\mathcal{L}_{XX}^{\gamma} \Delta X + G_{X}^{\mathsf{T}} \Delta \lambda + H_{X}^{\mathsf{T}} \Delta \mu = -\mathcal{L}_{X}^{\gamma\mathsf{T}} \\
\mathcal{L}_{XX}^{\gamma} \Delta X + G_{X}^{\mathsf{T}} \Delta \lambda + H_{X}^{\mathsf{T}} (-\mu + [Z]^{-1} (\gamma e - [\mu] \Delta Z)) = -\mathcal{L}_{X}^{\gamma\mathsf{T}} \\
\mathcal{L}_{XX}^{\gamma} \Delta X + G_{X}^{\mathsf{T}} \Delta \lambda \\
+ H_{X}^{\mathsf{T}} (-\mu + [Z]^{-1} (\gamma e - [\mu] (-H(X) - Z - H_{X} \Delta X))) = -\mathcal{L}_{X}^{\gamma\mathsf{T}} \\
\mathcal{L}_{XX}^{\gamma} \Delta X + G_{X}^{\mathsf{T}} \Delta \lambda - H_{X}^{\mathsf{T}} \mu + H_{X}^{\mathsf{T}} [Z]^{-1} \gamma e \\
+ H_{X}^{\mathsf{T}} [Z]^{-1} [\mu] H(X) + H_{X}^{\mathsf{T}} [Z]^{-1} [Z] \mu + H_{X}^{\mathsf{T}} [Z]^{-1} [\mu] H_{X} \Delta X = -\mathcal{L}_{X}^{\gamma\mathsf{T}} \\
(\mathcal{L}_{XX}^{\gamma} + H_{X}^{\mathsf{T}} [Z]^{-1} [\mu] H_{X}) \Delta X + G_{X}^{\mathsf{T}} \Delta \lambda \\
+ H_{X}^{\mathsf{T}} [Z]^{-1} (\gamma e + [\mu] H(X)) = -\mathcal{L}_{X}^{\gamma\mathsf{T}} \\
M \Delta X + G_{X}^{\mathsf{T}} \Delta \lambda = -N \quad (3.37)$$

where

$$M \equiv \mathcal{L}_{XX}^{\gamma} + H_X^{\mathsf{T}} [Z]^{-1} [\mu] H_X \tag{3.38}$$

$$= f_{XX} + G_{XX}(\lambda) + H_{XX}(\mu) + H_X^{\mathsf{T}}[Z]^{-1}[\mu] H_X$$
 (3.39)

and

$$N \equiv \mathcal{L}_X^{\gamma \mathsf{T}} + H_X^{\mathsf{T}} [Z]^{-1} (\gamma e + [\mu] H(X))$$
(3.40)

$$= f_X^{\mathsf{T}} + G_X^{\mathsf{T}} \lambda + H_X^{\mathsf{T}} \mu + H_X^{\mathsf{T}} [Z]^{-1} (\gamma e + [\mu] H(X)). \tag{3.41}$$

Combining (3.37) and the 3^{rd} row of (3.34) results in a system of equations of reduced size:

$$\begin{bmatrix} M & G_X^{\mathsf{T}} \\ G_X & 0 \end{bmatrix} \begin{bmatrix} \Delta X \\ \Delta \lambda \end{bmatrix} = \begin{bmatrix} -N \\ -G(X) \end{bmatrix}. \tag{3.42}$$

The Newton update can then be computed in the following 3 steps:

- 1. Compute ΔX and $\Delta \lambda$ from (3.42).
- 2. Compute ΔZ from (3.36).
- 3. Compute $\Delta \mu$ from (3.35).

In order to maintain strict feasibility of the trial solution, the algorithm truncates the Newton step by scaling the primal and dual variables by α_p and α_d , respectively,

where these scale factors are computed as follows:

$$\alpha_p = \min\left(\xi \min_{\Delta Z_m < 0} \left(-\frac{Z_m}{\Delta Z_m}\right), 1\right) \tag{3.43}$$

$$\alpha_d = \min\left(\xi \min_{\Delta \mu_m < 0} \left(-\frac{\mu_m}{\Delta \mu_m} \right), 1 \right) \tag{3.44}$$

resulting in the variable updates below.

$$X \leftarrow X + \alpha_p \Delta X \tag{3.45}$$

$$Z \leftarrow Z + \alpha_n \Delta Z$$
 (3.46)

$$\lambda \leftarrow \lambda + \alpha_d \Delta \lambda \tag{3.47}$$

$$\mu \leftarrow \mu + \alpha_d \Delta \mu \tag{3.48}$$

The parameter ξ is a constant scalar with a value slightly less than one. In MIPS, ξ is set to 0.99995.

In this method, during the Newton-like iterations, the perturbation parameter γ must converge to zero in order to satisfy the first order optimality conditions of the original problem. MIPS uses the following rule to update γ at each iteration, after updating Z and μ :

$$\gamma \leftarrow \sigma \frac{Z^{\mathsf{T}} \mu}{n_i} \tag{3.49}$$

where σ is a scalar constant between 0 and 1. In MIPS, σ is set to 0.1.

4 Other Functions

4.1 Linear System Solver - mplinsolve

The mplinsolve function provides a common interface to several different methods for solving a system of linear equations of the form Ax = b.

```
x = mplinsolve(A, b);
x = mplinsolve(A, b, solver);
x = mplinsolve(A, b, solver, opt);
x = mplinsolve(factors, b, ...);
factors = mplinsolve(A);
factors = mplinsolve(A, [], ...);
[x, factors] = mplinsolve(A, b, 'LU' ...);
```

The solver argument can be one of the following:

- '' default, same as '\'
- '\' use built-in \ operator, i.e. $x = A \setminus b$
- 'LU' use built-in 1u function to explicitly factor A, then solve for x via back-substitution
- 'PARDISO' use optional third-party PARDISO solver¹³

See help mplinsolve for more details.

As of version 1.5, mplinsolve can optionally return a struct containing the matrix LU factorization. It can then use these matrix factors to solve systems with different right-hand-sides by passing the struct in place of the A matrix to subsequent calls. Transposed systems can be solved by setting opt.tr to 1, including when providing the matrix factors for the original, non-transposed system.

For example, to solve $Ax_i = b_i$ for x_i for various values of b_i , use the following.

```
factors = mplinsolve(A);
x1 = mplinsolve(factors, b1);
x2 = mplinsolve(factors, b2);
x3 = mplinsolve(factors, b3);
...
```

Similarly, to solve $A^{\mathsf{T}}y_i = c_i$ for y_i for various values of c_i , from the previously computed factors of the original A, use the following.

¹³Requires the installation of an optional package. See Appendix B for details.

```
opt = struct('tr', 1);
y1 = mplinsolve(factors, c1, 'LU', opt);
y2 = mplinsolve(factors, c2, 'LU', opt);
y3 = mplinsolve(factors, c3, 'LU', opt);
...
```

Note that MIPS uses mplinsolve to solve the Newton update step in (3.42).

4.2 Quadratic Programming Solver - qps_mips

A convenience wrapper function called qps_mips is provided to make it trivial to set up and solve linear programming (LP) and quadratic programming (QP) problems of the following form:

$$\min_{x} \frac{1}{2} x^{\mathsf{T}} H x + c^{\mathsf{T}} x \tag{4.1}$$

subject to

$$l \le Ax \le u \tag{4.2}$$

$$x_{\min} \le x \le x_{\max}. \tag{4.3}$$

Instead of a function handle, the objective function is specified in terms of the paramters H and c of quadratic cost coefficients. Internally, qps_mips passes mips the handle of a function that uses these paramters to evaluate the objective function, gradients and Hessian.

The calling syntax for qps_mips is similar to that used by quadprog from the MATLAB Optimization Toolbox.

```
[x, f, exitflag, output, lambda] = qps_mips(H, c, A, 1, u, xmin, xmax, x0, opt);
```

Alternatively, the input arguments can be packaged as fields in a problem struct and passed in as a single argument, where all fields except H, c, A and 1 are optional.

```
[x, f, exitflag, output, lambda] = qps_mips(problem);
```

Aside from H and c, all input and output arguments correspond exactly to the same arguments for mips as described in Tables 3-1 and 3-2.

As with mips and fmincon, the primary difference between the calling syntax for qps_mips and quadprog is that the linear constraints are specified in terms of a single doubly-bounded linear function $(l \le Ax \le u)$ as opposed to separate equality constrained $(A_{eq}x = b_{eq})$ and upper bounded $(Ax \le b)$ functions.

Several examples of using qps_mips to solve LP and QP problems can be found in t_qps_mips.m.

4.3 Private Feature Detection Functions

The following are private functions that implement detection of specific optional functionality. They are not intended to be called directly, but rather are used to extend the capabilities of have_feature, a function included in MP-Test and described in the MP-Test README file.

4.3.1 have_feature_lu_vec

This function implements the 'lu_vec' tag for have_feature to detect support for the lu(..., 'vector') syntax.

4.3.2 have_feature_mips

This function implements the 'mips' tag for have_feature to detect availability/version for mips().

4.3.3 have_feature_pardiso_legacy

This function implements the 'pardiso_legacy' tag for have_feature to detect support for the legacy (v5.x) PARDISO interface, with individual MEX files for factor, solve, etc.

4.3.4 have_feature_pardiso_object

This function implements the 'pardiso_object' tag for have_feature to detect support for the object-oriented (v6.x and later) PARDISO interface.

4.3.5 have_feature_pardiso

This function implements the 'pardiso' tag for have_feature to detect availability/version of PARDISO, Parallel Sparse Direct and Multi-Recursive Iterative Linear Solvers, available from https://pardiso-project.org. See also Appendix B.

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¹⁴Supported in part by the Consortium for Electric Reliability Technology Solutions (CERTS) and the Office of Electricity Delivery and Energy Reliability, Transmission Reliability Program of the U.S. Department of Energy under the National Energy Technology Laboratory Cooperative Agreement No. DE-FC26-09NT43321.

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Appendix A MIPS Files and Functions

This appendix lists all of the files and functions that MIPS provides. In most cases, the function is found in a MATLAB M-file in the lib directory of the distribution, where the .m extension is omitted from this listing. For more information on each, at the MATLAB/Octave prompt, simply type help followed by the name of the function. For documentation and other files, the filename extensions are included.

Table A-1: MIPS Files and Functions

name	description
AUTHORS	list of authors and contributors
CHANGES	MIPS change history
CITATION	info on how to cite MIPS
CONTRIBUTING.md	notes on how to contribute to the MIPS project
LICENSE	MIPS license (3-clause BSD license)
README.md	basic introduction to MIPS
docs/	
MIPS-manual.pdf	MIPS User's Manual
<pre>src/MIPS-manual/</pre>	
MIPS-manual.tex	LaTeX source for MIPS User's Manual
lib/	
${ t have_feature_lu_vec}^*$	support for lu(, 'vector') syntax
${\tt have_feature_pardiso_legacy}^*$	PARDISO v5, individual MEX files for factor, solve, etc.
${\tt have_feature_pardiso_object}^*$	PARDISO v6 and later, object interface
$\mathtt{have_feature_pardiso}^*$	PARDISO, Parallel Sparse Direct & Iterative Linear
	Solver, https://pardiso-project.org
mips	Matpower Interior Point Solver – primal/dual interior
	point solver for NLP
mipsver	prints version information for MIPS
mplinsolve	common linear system solver interface, used by MIPS
qps_mips	common QP/LP solver interface to MIPS-based solver
t/	
${\tt mips_example1}$	implements example 1 from MIPS User's Manual
${\tt mips_example2}$	implements example 2 from MIPS User's Manual
test_mips	runs full MIPS test suite
$ t_{ t mips}$	runs tests for MIPS NLP solver
${\tt t_mips_pardiso}$	runs tests for MIPS NLP solver, using PARDISO as linear solver †
$ t_{ t mplinsolve}$	tests for mplinsolve
t_qps_mips	runs tests for qps_mips

^{*} These functions implement new tags and the detection of the corresponding features for have_feature which is part of MP-Test.

[†] Requires the installation of an optional package. See Appendix B for details.

Appendix B PARDISO – Parallel Sparse Direct and Multi-Recursive Iterative Linear Solvers

The PARDISO package is a thread-safe, high-performance, robust, memory efficient and easy to use software for solving large sparse symmetric and non-symmetric linear systems of equations on shared-memory and distributed-memory multiprocessor systems [10,11]. More information is available at https://pardiso-project.org.

When the Matlab interface to PARDISO is installed, PARDISO's solvers can be used to replace the built-in \setminus operator for solving for the Newton update step in MIPS by setting the linsolver option equal to 'PARDISO'. The mplinsolve function can also be called directly to solve Ax = b problems via PARDISO or the built-in solver, depending on the arguments supplied. This interface also gives access to the full range of PARDISO's options. For details, see help mplinsolve and the PARDISO User's Manual at https://pardiso-project.org/manual/manual.pdf.

Appendix C Release History

The full release history can be found in CHANGES.md or online at https://github.com/MATPOWER/mips/blob/master/CHANGES.md.

C.1 Version 1.0 – released Feb 7, 2011

Documentation found in Appendix A of the MATPOWER 4.0 User's Manual, available online. ¹⁶

Changes

- Licensed under the GNU General Public License (GPL).
- Added compatibility with GNU Octave, a free, open-source Matlab clone.
- MIPS (MATPOWER Interior Point Solver), a new a pure-MATLAB implementation of the primal-dual interior point methods from the optional package TSPOPF.

C.2 Version 1.0.1 – released Apr 30, 2012

Documentation found in Appendix A of the MATPOWER 4.0 User's Manual, available online. 17

Bug Fixed

• Fixed fatal bug in MIPS for unconstrained, scalar problems. Thanks to Han Na Gwon.

C.3 Version 1.0.2 – released Nov 5, 2013

Documentation found in Appendix A of the MATPOWER 4.0 User's Manual, available online. 18

¹⁶https://matpower.org/docs/MATPOWER-manual-4.0.pdf

¹⁷https://matpower.org/docs/MATPOWER-manual-4.0.pdf

¹⁸https://matpower.org/docs/MATPOWER-manual-4.0.pdf

Bug Fixed

• Fixed a bug in MIPS where a near-singular matrix could produce an extremely large Newton step, resulting in incorrectly satisfying the relative feasibility criterion for successful termination.

C.4 Version 1.1 – released Dec 17, 2014

Documentation found in Appendix A of the MATPOWER 5.0 User's Manual, available online. 19

New Features

• Many new user-settable options.

Incompatible Changes

• The name of the mips() option used to specify the maximum number of stepsize reductions with step_control on was changed from max_red to sc.red_it for consistency with other MATPOWER options.

C.5 Version 1.2 – released Mar 20, 2015

Documentation found in Appendix A of the MATPOWER 5.1 User's Manual, available online.²⁰

New License

• Switched to the more permissive 3-clause BSD license from the previously used GNU General Public License (GPL) v3.0.

New Documentation

• Added an online function reference to the MATPOWER website at http://www.pserc.cornell.edu/matpower/docs/ref/.

¹⁹https://matpower.org/docs/MATPOWER-manual-5.0.pdf

²⁰https://matpower.org/docs/MATPOWER-manual-5.1.pdf

New Features

- Added support for using PARDISO (https://pardiso-project.org/) as linear solver for computing interior-point update steps in MIPS, resulting in dramatic improvements in computation time and memory use for very large-scale problems.
- New functions:
 - mplinsolve() provides unified interface for linear system solvers, including PARDISO and built-in backslash operator

C.6 Version 1.2.1 – released Jun 1, 2016

Documentation found in Appendix A of the MATPOWER 6.0b1 User's Manual, available online.²¹

Bug Fixed

• Fixed issue where default value of 'feastol' option was not being set correctly in mips() when called directly (or via qps_mips()) with 'feastol' = 0.

C.7 Version 1.2.2 – released Dec 16, 2016

Documentation found in the MIPS 1.2.2 User's Manual²² or in Appendix A of the MATPOWER 6.0 User's Manual, available online.²³

New Open Development Model

- MIPS development has moved to GitHub! The code repository is now publicly available to clone and submit pull requests.²⁴
- Public issue tracker for reporting bugs, submitting patches, etc.²⁵

```
<sup>21</sup>https://matpower.org/docs/MATPOWER-manual-6.0b1.pdf
```

²²https://matpower.org/docs/MIPS-manual-1.2.2.pdf

²³https://matpower.org/docs/MATPOWER-manual-6.0.pdf

²⁴https://github.com/MATPOWER/mips

²⁵https://github.com/MATPOWER/mips/issues

Other Changes

- Renamed from Matlab Interior Point Solver to Matpower Interior Point Solver.
- Remove dependence of t_mpsolve() on presence of have_fcn() (from MAT-POWER) to detect PARDISO installation.

C.8 Version 1.3 – released Oct 30, 2018

The MIPS 1.3 User's Manual is available online.²⁶

New Features

- Support for PARDISO 6.x.
- New mplinsolve solver option 'LU' for explicit LU decomposition with back substitution, with options in opt.lu for specifying the number of output arguments in call to lu (opt.lu.nout), whether to use permutation vectors or matrices (opt.lu.vec) and pivot threshold options (opt.lu.thresh). The following values for the solver argument act as shortcuts for specifying various combinations of options: 'LU3', 'LU3a', 'LU4', 'LU5', 'LU3m', 'LU3am', 'LU4m', 'LU5m'. See help mplinsolve for details. Thanks to Jose Luis Marín.

Bugs Fixed

• Fix bug preventing pardiso.dparm options from being set.

Other Changes

- LATEX source code for MIPS User's Manual included in docs/src.
- Move mplinsolve PARDISO options to opt.pardiso in preparation for adding options for other solvers.

²⁶https://matpower.org/docs/MIPS-manual-1.3.pdf

C.9 Version 1.3.1 – released Jun 20, 2019

The MIPS 1.3.1 User's Manual is available online.²⁷

Changes

- Add CITATION file.
- Other miscellaneous documentation updates, e.g. MATPOWER website links updated to https://matpower.org.

C.10 Version 1.4 – released Oct 8, 2020

The MIPS 1.4 User's Manual is available online.²⁸

New Features

- Support for have_feature() from MP-Test to detect availability and version information for optional functionality. This is a modular, extensible replacement for have_fcn() from MATPOWER and MP-Opt-Model.
- Feature detection functions for lu() and PARDISO, defining tags 'lu_vec', 'pardiso_legacy', 'pardiso_object' and 'pardiso' for have_feature().
- New functions:
 - have_feature_lu_vec detects support for the lu(..., 'vector') syntax.
 - have_feature_pardiso_legacy detects support for the legacy (v5.x) PAR-DISO interface, with individual MEX files for factor, solve, etc.
 - have_feature_pardiso_object detects support for the object-oriented (v6.x and later) PARDISO interface.
 - have_feature_pardiso detects availability/version of PARDISO.

Bugs Fixed

• Silence inadvertent output from mplinsolve() when called without solver input argument.

²⁷https://matpower.org/docs/MIPS-manual-1.3.1.pdf

²⁸https://matpower.org/docs/MIPS-manual-1.4.pdf

• Fix fatal errors when mplinsolve() is called with 'LU' solver and dense A matrix.

Other Changes

- Requires MP-Test 7.1 or later.
- Remove have_fcn() dependencies in mips(), t_mips_pardiso() and t_qps_mips().

Incompatible Changes

• Calling mips() with opt.linsolver set to 'PARDISO' now results in a fatal error if PARDISO is not installed, rather than warning and continuing with the default linear solver.

C.11 Version 1.5 – released Dec 12, 2022

The MIPS 1.5 User's Manual is available online.²⁹

New Features

- Add to mplinsolve() the ability to return a struct containing the matrix LU factorization, and to reuse this pre-factored matrix to solve additional systems with different right-hand-sides by passing the struct in place of the A matrix to subsequent calls.
- Add option to mplinsolve() to solve transposed systems by setting opt.tr to 1, including when providing the pre-factored matrix for the original, non-transposed system.

C.12 Version 1.5.1 – released May 10, 2024

The MIPS 1.5.1 User's Manual is available online.³⁰

²⁹https://matpower.org/docs/MIPS-manual-1.5.pdf
30https://matpower.org/docs/MIPS-manual-1.5.1.pdf

New Features

- Add Sphinx-based Reference documentation.³¹
- Add full_hist option to enable saving in output.hist trajectories of x, z, g, h, lam, and mu (issue #4).

C.13 Version 1.5.2 – released Jul 5, 2025

The MIPS 1.5.2 User's Manual is available online. 32

New Features

• New feature detection function have_feature_mips(), providing implementation of 'mips' tag for have_feature().

³¹https://matpower.org/doc/mips/

³²https://matpower.org/docs/MIPS-manual-1.5.2.pdf

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