First to Penalty



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Template

```
#include "bits/stdc++.h"
   //assert(x>0) si falla da RTE
   using namespace std;
   #define endl '\n'
   #define DBG(x) cerr<<\#x<< "=" << (x) << endl;
   #define RAYA cerr<<"==========="<<endl;
   #define RAYAS cerr<<"...."<<endl;</pre>
   //#define DBG(x) :
   //#define RAYA ;
   //#define RAYAS ;
11
   int main() {
    ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
14
     int tC;
     cin >> tC;
     while (tC--) {
19
20
21
22
```

Data structures

2.1 Simplified DSU (Stolen from GGDem)

```
int uf [MAXN];
void uf_init(){memset(uf,-1,sizeof(uf));}
   int uf_find(int x){return uf[x]<0?x:uf[x]=uf_find(uf[x]);}</pre>
   bool uf_join(int x, int y){
     x=uf_find(x);y=uf_find(y);
     if(x==y)return false;
     if(uf[x]>uf[y])swap(x,y);
     uf [x] +=uf [y]; uf [y] =x;
     return true;
10 }
```

2.2 Disjoint Set Union

```
class disjSet {
2
     int* sz;
     int* par;
   public:
     int len;
     disjSet(int tam){
            sz = new int[tam + 4]();
           par = new int[tam + 4]();
8
            len = 0;
9
            for(int i = 0; i < = tam; i + +){
10
                par[i] = i;
11
                sz[i] = 1;
12
                len++;
13
            }
14
15
     int finds(int el){
16
            if (el == par[el]) return el;
17
           return par[el] = finds(par[el]);
18
       }
19
     void unions(int a, int b){
20
            a = finds(a);
21
          b = finds(b);
22
            if (a == b) return;
23
            len--;
24
            //se hace que el gde sea padre del pequeno
25
            if (sz[a] > sz[b]) swap(a,b);
26
            par[a] = b;
27
            sz[b] += sz[a];
28
       }
29
      ~disjSet(){
30
            delete[] size;
31
            size = nullptr;
32
            delete[] parent;
33
            parent = nullptr;
34
       }
35
<sub>36</sub> | };
```

3 Graphs

4 Math

4.1 Identities

```
C_n = \frac{2(2n-1)}{n+1}C_{n-1}
C_n = \frac{1}{n+1}\binom{2n}{n}
C_n \sim \frac{4^n}{n^{3/2}\sqrt{\pi}}
\sigma(n) = O(\log(\log(n))) \text{ (number of divisors of } n)
F_{2n+1} = F_n^2 + F_{n+1}^2
F_{2n} = F_{n+1}^2 - F_{n-1}^2
\sum_{i=1}^n F_i = F_{n+2} - 1
F_{n+i}F_{n+j} - F_nF_{n+i+j} = (-1)^n F_i F_j
(Möbius Inv. Formula) Let g(n) = \sum_{d|n} f(d), then f(n) = \sum_{d} d \mid ng(d)\mu\left(\frac{n}{d}\right)).
```

4.2 Sieve Of Eratosthenes

4.3 Sieve-based Factorization

```
#define MAXN 10e6
class soe{
public:
    int smolf[MAXN];
soe(){
    for(int i = 2; i<MAXN; i++) smolf[i] = (i%2==0?2:i);

for(int i = 3; i*i<MAXN; i+=2)</pre>
```

5 Geometry

6 Strings

6.1 Explode by token

```
//#include <sstream>

vector<string> explode(string const& s, char delim) {
 vector<string> result;
 istringstream iss(s);
 for (string token; getline(iss, token, delim); )
 {
 result.push_back(move(token));
 }
 return result;
}
```

6.2 Multiple Hashings DS

```
struct multhash{
       unsigned long long int h1,h2,h3;
2
       unsigned long long int alf[257];
3
       bool operator < (multhash b) const { // override less than operator</pre>
       if (h1 != b.h1) return h1 < other.h1;
5
       if (h2 != b.h2) return h2 < other.h2;
       return h3 < b.h3;
7
8
     bool operator == (multhash b) const { // override equal operator
9
       return (h1== b.h1 && h2== b.h2 && h3== b.h3)
10
11
   public:
12
       string s;
13
       multhash(){
14
           h1 = 0; h2 = 0; h3 = 0; s = "";
15
           for(char l = 'a'; l <= 'z'; l++) alf [l] = l-'a'+1;
16
       }
17
```

```
void innit(){
18
           unsigned long long int inf,p,op;
19
20
           inf = 666666555577777777;
21
           p = 47; op = 47;
22
           for(char 1: s){
23
                h1+=(p*alf[1])%inf;
24
                p*=op;
25
                p%=inf;
26
           }
27
28
           inf = 986143414027351997;
29
           p = 53; op = 53;
30
           for(char 1: s){
31
                h2+=(p*alf[1])%inf;
32
                p*=op;
                p%=inf;
34
           }
35
36
           inf = 909090909090909091;
37
           p = 79; op = 79;
38
           for(char 1: s){
39
                h3+=(p*alf[1])%inf;
40
                p*=op;
41
                p%=inf;
42
43
44
45
   //VALORES POSIBLES DE INF, MIENTRAS MAS CERCANOS A 10^17 MEJOR
    //666666555557777777
   //986143414027351997
48
    //974383618913296759
   //973006384792642181
   //953947941937929919
   //909090909090909091
   //VALORES PARA P, USAR PRIMOS MAYORES A |Alfabeto|
54 //31,47,53,61,79
                           Permute chars of string
void permute(string str){
```

// Sort the string in lexicographically

// ascennding order

```
sort(str.begin(), str.end());
4
5
     // Keep printing next permutation while there
6
     // is next permutation
     do {
8
       cout<<str<<endl;</pre>
9
    } while (next_permutation(str.begin(), str.end()));
10
11 }
                 6.4 Longest common subsequence
   //O(|te|*|pa|)
   //cambiar score para otros problemas, str all match = +2, miss/ins/del =
   //usar char que no este en el alfabeto para denotar del/ins
   string te,pa;
   long long int ninf = -10e13;
   long long int score(char a, char b){
       if(a=='*' || b=='*') return 0:
       if(a==b) return 1;
       return ninf;
9
10
   long long int lcs(){
11
       long long int** dp;te = "*"+te; pa = "*"+pa;
12
       long long int res = 0;
13
14
       dp = new long long int*[te.size()];
15
       for(int i = 0; i<te.size(); i++) dp[i] = new long long int[pa.size()</pre>
16
           ]();
17
       for(int r = 1; r<te.size(); r++){</pre>
18
           for(int c = 1; c<pa.size(); c++){</pre>
19
               dp[r][c] = dp[r-1][c-1] + score(te[r], pa[c]);
20
               dp[r][c] = max(dp[r][c-1]+score(te[r],'*'),dp[r][c]);
21
               dp[r][c] = max(dp[r-1][c]+score('*',pa[c]),dp[r][c]);
22
23
       }
24
25
       return dp[te.size()-1][pa.size()-1];
26
27 }
                                 6.5 KMP
string T,P;
```

```
int bt[MAXN];
   //0(|Text|+|Pattern|)
   void KMPpre(){
       int i = 0, j = 0; bt[0] = -1;
       while(i<P.size()){</pre>
6
            while(j \ge 0 \&\& P[i]!=P[(j \ge 0?j:0)]) j = bt[j];
            i++; j++; bt[i] = j;
8
       }
9
   }
10
   int kmp(){
       int res =0, i = 0, j = 0;
12
       while(i<T.size()){</pre>
13
            while(j \ge 0 \&\& T[i] != P[(j \ge 0?j:0)])  j = bt[j];
14
            i++; j++;
15
            if(j==P.size()){//match, do anything
16
                res++; j = bt[j];
            }
18
       }
19
20
       return res;
21 }
```

7 Flow

8 Miscellaneous

8.1 Bit Manipulation

```
#include "bits/stdc++.h"
   using namespace std;
   #define endl '\n'
4
   int main() {
6
     ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
     //Se representan bitmasks de 30 a 62 bits
8
     //usando signed int y signed long long int
9
     //para evitar problemas con el complemento de dos
10
     signed int a, b;
11
     //para multiplicar un numero por dos solo es necesario aplicar un
12
     // shifteo de sus bits a la izquierda
13
     a = 1:
14
     a= a << 3;
15
     cout << a << endl;</pre>
```

```
//para dividir un numero entre dos es necesario aplicar un
17
     //shifteo a la derecha
18
     a = 32;
19
     a = a >> 3;
20
     cout << a << endl;</pre>
21
     //para encender el bit n de a, solo hay que igualar a = a \mid pow(2,n-1)
     //prende el tercer bit
     a = 1;
24
     b = 1 << 2;
25
     a = a \mid b;
26
     cout << a << endl;</pre>
27
     //para apagar el bit n de a, solo hay que a \ell = \text{pow}(2,n-1)
     //prende el tercer bit
     a = 5;
30
     b = 1 << 2;
31
     a &= ~b;
32
     cout << a << endl;</pre>
33
     //para revisar si el bit n de a esta encendido
34
     //revisa si el tercer bit esta encendido
35
     a = 5;
36
     b = 1 << 2;
37
     a = a \& b;
38
     cout << (a?"SI":"NO") << endl;</pre>
39
     //para volter el bit n de a, solo hay que igualar a = a ^{\circ} pow(2,n-1)
40
     //apaga el tercer bit
41
     a = 5;
42
     b = 1 << 2;
43
     a = a \hat{b};
44
     cout << a << endl;</pre>
45
     //para obtener el bit menos significativo que esta encendido a& -a
46
     a = 12;
47
     cout << log2(a & ((-1) * a))+1 << endl;
48
     //para prender todos los bits hasta n
49
     a = (1 << 4) - 1;
50
     cout << a << endl;</pre>
51
52
        ---------E0S0LUTI0N------
  #include "bits/stdc++.h"
   using namespace std;
   #define endl '\n'
  #pragma GCC optimize("03")
5 #pragma GCC target("popcnt")
```

```
6
7 //no usar con visual c++
  //solo con g++ like compilers
   int main() {
     ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
     signed long long int a, b, n;
     //Obtain the remainder (modulo) of a when it is divided by n (n is a
12
         power of 2)
     a = 15; n = 8-1;
13
     a &= n;
14
     cout << \frac{a}{n}, \frac{a}{a} = 15, \frac{n}{a} = 2^3 << endl;
15
     cout << a << endl;</pre>
     //Apaga el bit menos significativo de a
17
     a = 14:
     b = (a \& ((-1) * a));
     a &= ~b;
     cout << a << endl;</pre>
     //enciende el ultimo cero de a
     a = 9:
23
     b = a;
     b = (b \& ((-1) * b));
     a = a \mid b;
     cout << a<<endl;</pre>
27
     //contar bits encendidos en a
28
     cout << __builtin_popcount(a)<<endl;</pre>
29
     //checar la paridad de a
30
     cout << (__builtin_parity(a) ? "IMPAR" : "PAR") << endl;</pre>
31
     //contar leading zeroes en a
32
     cout << __builtin_clz(a)<<endl;</pre>
33
     //contar 9, trailling zeroes en a
34
     cout << __builtin_ctz(a)<<endl;</pre>
35
   }
36
37 //-----EOSOLUTION-----
```

9 Testing