

# First to Penalty



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## 1 Template

```

1 #include "bits/stdc++.h"
2 //assert(x>0) si falla da RTE
3 using namespace std;
4 #define endl '\n'
5 #define DBG(x) cerr<<#x<< "=" << (x) << endl;
6 #define RAYA cerr<<"===== "<<endl;
7 #define RAYAS cerr<<"..... "<<endl;
8 // #define DBG(x) ;
9 // #define RAYA ;
10 // #define RAYAS ;
11
12 //-----SOLBEGIN-----
13 int main() {
14     ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
15     int tC;
16
17     cin >> tC;
18     while (tC--) {
19
20     }
21 }
22
23 //-----EOSOLUTION-----

```

## 2 Data structures

### 2.1 Simplified DSU (Stolen from GGDem)

```

1 int uf[MAXN];
2 void uf_init(){memset(uf,-1,sizeof(uf));}
3 int uf_find(int x){return uf[x]<0?x:uf[x]=uf_find(uf[x]);}
4 bool uf_join(int x, int y){
5     x=uf_find(x);y=uf_find(y);
6     if(x==y)return false;
7     if(uf[x]>uf[y])swap(x,y);
8     uf[x]+=uf[y];uf[y]=x;
9     return true;
10 }

```

### 2.2 Disjoint Set Union

```

1 class disjSet {
2     int* sz;
3     int* par;
4 public:
5     int len;
6     disjSet(int tam){
7         sz = new int[tam + 4]();
8         par = new int[tam + 4]();
9         len = 0;
10        for(int i = 0; i<=tam; i++){
11            par[i] = i;
12            sz[i] = 1;
13            len++;
14        }
15    }
16    int finds(int el){
17        if (el == par[el]) return el;
18        return par[el] = finds(par[el]);
19    }
20    void unions(int a, int b){
21        a = finds(a);
22        b = finds(b);
23        if (a == b) return;
24        len--;
25        //se hace que el gde sea padre del pequeno
26        if (sz[a] > sz[b]) swap(a,b);
27        par[a] = b;
28        sz[b] += sz[a];
29    }
30    ~disjSet(){
31        delete[] size;
32        size = nullptr;
33        delete[] parent;
34        parent = nullptr;
35    }
36 };

```

### 2.3 Segment tree

```

1 //MAXN = 2^k, n = tam arreglo inicial
2 #define MAXN 262160
3 int stsize; long long int neut;int n;
4 long long int* st = new long long int[2*MAXN-1]();

```

```

5 long long int fst(long long int a, long long int b);
6 long long int build(int sti,int csize){
7     if(csize == 1) return st[sti];
8     return st[sti] = fst(build(sti*2+1,csize/2),build(sti*2+2,csize/2));
9 }
10 void innit(){
11     for(int i = 0; i<stsize; i++) st[i] = neut;
12     /*int d = 0;
13     for(int i = stsize-n; i<stsize && d<n; i++){
14         st[i] = arr[d];d++;
15     }*/
16     build(0,n);
17 }
18 void upd(int ind, long long int val){
19     ind = stsize-n+ind;
20     st[ind] = val;ind--;ind/=2;
21     while(true){
22         st[ind] = fst(st[ind*2+1],st[ind*2+2]);
23         ind--;
24         if(ind<0) break;
25         ind/=2;
26     }
27 }
28 long long int rqu(int l, int r,int sti, int ls, int rs){
29     if(l<=ls && rs<= r) return st[sti];
30     if(r<ls || l>rs) return neut;
31     int m = (rs+ls)/2;
32     return fst(rqu(l,r,sti*2+1,ls,m),rqu(l,r,sti*2+2,m+1,rs));
33 }
34 long long int query(int l, int r){
35     return rqu(l,r,0,0,n-1);
36 }
37 //uso, inicializa neut, n = primera potencia de 2 >= n del problema,
38     stsize = 2*n-1
39 //llena arr de neutros hasta que su tam sea el nuevo n
40 //DEFINE LA FUNCION fst

```

## 2.4 Segment tree Lazy

```

1 //MAXN = 2^k, n = tam arreglo inicial
2 #define MAXN 262160
3 vector<int> arr;
4 int stsize; long long int neut;int n;

```

```

5 long long int* st = new long long int[2*MAXN-1]();
6 long long int* pendientes = new long long int[2*MAXN-1]();
7 long long int fst(long long int a, long long int b){return a+b;}
8 long long int build(int sti,int csize){
9     if(csize == 1) return st[sti];
10    return st[sti] = fst(build(sti*2+1,csize/2),build(sti*2+2,csize/2));
11 }
12 bool hasChildren(int sti){sti*=2;sti++;sti++;return sti<stsize;}
13 void innit(){
14     for(int i = 0; i<stsize; i++) st[i] = neut;
15     int d = 0;
16     for(int i = stsize-n; i<stsize && d<n; i++) {st[i] = arr[d];d++;}
17     build(0,n);
18 }
19 void updrec(int l,int r, int sl, int sr,int sti, long long int val){
20     if(sr<l || r< sl) return;
21     if(l<= sl && sr <=r){
22         st[sti] += val*(sr-sl+1);
23         if(hasChildren(sti)){pendientes[sti*2+1]+=val;pendientes[sti
24             *2+2]+=val;}
25         return;
26     }
27     int sm = (sl+sr)/2;
28     updrec(l,r,sl,sm,sti*2+1,val);
29     updrec(l,r,sm+1,sr,sti*2+2,val);
30     st[sti] = fst(st[sti*2+1]+pendientes[sti*2+1],st[sti*2+2]+pendientes
31         [sti*2+2]);
32 }
33 void upd(int l, int r, long long int val){updrec(l,r,0,n-1,0,val);}
34 long long int rqu(int l, int r,int sti, int ls, int rs){
35     if(r<ls || l>rs) return neut;
36     if(l<=ls && rs<= r){
37         return st[sti]+pendientes[sti]*(rs-ls+1);
38     }
39
40     st[sti] += pendientes[sti]*(rs-ls+1);
41     if(hasChildren(sti)){pendientes[sti*2+1]+=pendientes[sti];pendientes
42         [sti*2+2]+=pendientes[sti];}
43     pendientes[sti] = 0;
44     int m = (rs+ls)/2;

```

```

45     return fst(rqu(l,r,sti*2+1,ls,m),rqu(l,r,sti*2+2,m+1,rs));
46 }
47 long long int query(int l, int r){
48     return rqu(l,r,0,0,n-1);
49 }
50 //uso, inicializa neut, n = primera potencia de 2 >= n del problema,
51     stsize = 2*n-1
52 //llena arr de neutros hasta que su tam sea el nuevo n
53 //DEFINE LA FUNCION fst

```

## 2.5 Trie

```

1 struct triver {
2     char alphabet;
3     bool ter;
4     vector<triver*> child;
5     triver(char a): alphabet(a) { child.assign(26, NULL); ter = false; }
6 };
7 class trie{
8 private:
9     triver* root;
10 public:
11     trie() { root = new triver('!');}
12     void insert(string s){
13         triver* curr = root;
14         for(char l: s){
15             if(curr->child[l-'A'] == NULL) curr->child[l-'A'] = new
16                 triver(l);
17             curr = curr->child[l-'A'];
18         }
19         curr->ter = true;
20     }
21     bool search(string s){
22         triver* curr = root;
23         for(char l: s){
24             if(curr == NULL) break;
25             curr = curr->child[l-'A'];
26         }
27         if(curr == NULL) return false;
28         return curr->ter;
29     }
30 };

```

## 3 Graphs

### 3.1 Graph Transversal

#### 3.1.1 BFS

```

1 #define GS 400040
2 vector<int> graph[GS];
3 bitset <GS> vis;
4 //anchura O(V+E)
5 void dfs(int curr) {
6     queue<int> fringe;
7     fringe.push(curr);
8     while (fringe.size()) {
9         curr = fringe.front(); fringe.pop();
10        if (!vis[curr]) {
11            vis[curr] = 1;
12            for (int h : graph[curr]) fringe.push(h);
13        }
14    }
15 }

```

#### 3.1.2 DFS

```

1 #define GS 400040
2 vector<int> graph[GS];
3 bitset <GS> vis;
4 //profundidad O(V+E)
5 void dfs(int curr) {
6     stack<int> fringe;
7     fringe.push(curr);
8     while (fringe.size()){
9         curr = fringe.top(); fringe.pop();
10        if (!vis[curr]) {
11            vis[curr] = 1;
12            for (int h : graph[curr]) fringe.push(h);
13        }
14    }
15 }

```

### 3.2 Topological Sort

```

1 #define GS 400040
2 vector<int> graph[GS];

```

```

3 bitset <GS> vis;
4 vector<int> topsort;
5 int e,n;
6 //profundidad
7 //O(N+E)
8 //Solo funciona con DAG's, no existe un top sort de un grafo Non-DAG
9 void todfs(int pa) {
10     vis[pa]=1;
11     for(int h: graph[pa]){if(!vis[h]){todfs(h);}}
12     topsort.push_back(pa);
13 }
14 void topologicalSort(){
15     vis.reset();
16     topsort.clear();
17     for(int i = 0; i<n; i++){if(!vis[i]){dfs(i);}}
18     reverse(topsort.begin(),topsort.end());
19 }
    
```

### 3.3 APSP: Floyd Warshall

```

1 #define GS 1000
2 #define INF 100000000
3 //destino, costo
4 int graph[GS][GS];
5 //All Pairs Dist
6 int dist[GS][GS];
7 //Toma en cuenta nodos [0-tam] inclusivo, modificar de acuerdo a las
8 //necesidades
9 //Ten cuidado con el valor que le pones a INF, puede provocar overflows
10 //o puede no ser lo suficientemente grande.
11 void Floyd_Warshall(int tam){
12     for(int i = 0; i<=tam; i++)
13         for(int f = 0; f<=tam; f++)
14             dist[i][f] = INF;
15
16     for(int i = 0; i<=tam; i++)
17         for(int f = 0; f<=tam; f++)
18             dist[i][f] = graph[i][f];
19
20     //para reconstruir el camino solo basta con guardar intermedio como
21     //el padre de ini si el cambio se hizo, -1 otherwise
22     for(int intermedio = 0; intermedio<=tam; intermedio++)
23         for(int ini = 0; ini<=tam; ini++)
    
```

```

21         for(int fin = 0; fin<=tam; fin++)
22             dist[ini][fin] = min(dist[ini][fin],dist[ini][intermedio]
23             ]+dist[intermedio][fin]);
    
```

## 3.4 SSSP

### 3.4.1 Lazy Dijkstra

```

1 #define GS 1000
2 #define INF 100000000
3 //destino, costo
4 vector<pair<int,int>> graph[GS];
5 int dist[GS];
6 void dijkstra(int origen,int tam){
7     for(int i = 0; i<=tam; i++){
8         dist[i] = INF;
9     }
10     priority_queue<pair<int,int>,vector<pair<int,int>>, greater<pair<int
11     ,int>>> pq;
12     pair<int,int> curr;
13
14     pq.push(make_pair(0,origen));
15
16     while(pq.size()){
17         curr = pq.top();pq.pop();
18         if(curr.first >= dist[curr.second]) continue;
19
20         dist[curr.second] = curr.first;
21         for(pair<int,int> h: graph[curr.second]){
22             if((h.second+curr.first)<dist[h.first]) pq.push({h.second+
23             curr.first,h.first});
24         }
25     }
26
27     //Esta es la implementacion huevona
28     //Resuelve Single Source Shortest Paths con aristas positivas
29     //Como es la lazy implementation, si funciona con edges negativos
30     //siempre y cuando no hayan ciclos negativos
31     //Si hay ciclos negativos se va atascar en un ciclo infinito
32     //Si no los hay puede que funcione en O((V+E)log(V)) o puede que se
33     //exponencial, si no jala prueba BellmanFord
    
```

### 3.4.2 Bellman-Ford

```

1 //esta es la implementacion huevona
2 #define GS 1000
3 //cuidado con overflows!!
4 #define INF 100000000
5 #define NINF -100000000
6 //destino, costo
7 vector<pair<int,int>> graph[GS];
8 int dist[GS];
9 struct edge{
10     int from,to,cost;
11 };
12 //Corre en O(VE)
13 void bellmanFord(int origen,int tam){
14     for(int i = 0; i<=tam; i++){
15         dist[i] = INF;
16     }
17     dist[origen] = 0;
18     edge aux;
19     vector<edge> aristas;
20     bool optimal;
21
22     for(int i = 0; i<=tam; i++){
23         for(pair<int,int> h: graph[i]){
24             aux.from = i; aux.to = h.first;aux.cost = h.second;
25             aristas.push_back(aux);
26         }
27     }
28
29     //Si se relajan todas las aristas V-1 veces en un orden arbitrario
30     //Se asegura que la distancia optima para cada vertice sera
31     //alcanzada
32     for(int i = 0; i<tam && !optimal; i++){
33         optimal = true;
34         for(edge elem: aristas){
35             if(dist[elem.from] + elem.cost < dist[elem.to]){
36                 dist[elem.to] = dist[elem.from] + elem.cost;
37                 //si algun vertice fue actualizado significa que puede
38                 //que
39                 //las distancias aun no sean optimas
40                 optimal = false;
41             }
42         }
43     }
44 }

```

```

42
43 //Se corre de nuevo para asegurar encontrar todos los ciclos
44 //negativos
45 for(int i = 0; i<tam && !optimal; i++){
46     optimal = true;
47     for(edge elem: aristas){
48         if(dist[elem.from] + elem.cost < dist[elem.to]){
49             //Si aun despues de correr V-1 veces se puede actualizar
50             //Significa que esta en un ciclo negativo
51             dist[elem.to] = NINF;
52             //si algun vertice fue actualizado significa que puede
53             //que
54             //las distancias aun no sean optimas
55             optimal = false;
56         }
57     }
58 }

```

### 3.5 Strongly Connected Components: Kosaraju

```

1 #define GS 2010
2 vector<int> graph[GS];
3 vector<int> graphI[GS];
4 vector<int> orden;
5 bitset<GS> vis;
6
7 void invertirGrafo(int n){
8     for(int p = 1;p<= n; p++)
9         for(int h: graph[p])graphI[h].push_back(p);
10 }
11 void obtOrd(int p,int n){
12     vis[p] = 1;
13     for(int h: graph[p]){
14         if(!vis[h] && h<=n) obtOrd(h,n);
15     }
16     orden.push_back(p);
17 }
18 int findSCC(int n){
19     int res = 0;
20     invertirGrafo(n);
21     orden.clear();

```

```

22     for(int i = 1; i<=n; i++) vis[i] =0;
23     for(int i = 1; i<=n; i++) if(!vis[i]) obtOrd(i,n);
24     reverse(orden.begin(),orden.end());
25     //cuenta los connected components
26     //vector<int> lscc;
27     stack<int> fringe;
28     int curr;
29     for(int i = 1; i<=n; i++) vis[i] =0;
30     for(int i: orden){
31         //lscc.clear();
32         if(!vis[i]){
33             fringe.push(i);
34             while (fringe.size()){
35                 curr = fringe.top();fringe.pop();
36                 //lscc.push_back(curr);
37                 if (!vis[curr]) {
38                     vis[curr] = 1;
39                     for (int h : graphI[curr]) fringe.push(h);
40                 }
41             }
42             res++;
43         }
44         //hacer lo que sea con lcsc
45     }
46     return res;
47 }
48
49 //OJO esto solo jala con directed graphs
50 //por definicion todas las undirected graphs tienen un solo SCC
51 //NOTAR QUE LOS GRAFOS QUE USA CUMPLEN CON: 0<=VERTICE<=n
    
```

### 3.6 Articulation Points and Bridges: ModTarjan

```

1  #define GS 50
2  vector<int> graph[GS];
3  bitset<GS> vis, isArtic;
4  vector<int> padre;
5  //id por tiempo, menor id accesible
6  //ya sea por descendientes o por back edges
7  vector<int> tId,lId;
8  //cantidad de hijos que tiene en el bfs spanning tree
9  int rootChildren;
10 int cnt;
    
```

```

11 int dfsRoot;
12 void findAP_B(int p){
13     cnt++;vis[p] = 1;tId[p] = cnt;lId[p] = tId[p];
14
15     for(int hijo: graph[p]){
16         if(!vis[hijo]){
17             padre[hijo] = p;
18             if(p == dfsRoot) rootChildren++;
19
20             findAP_B(hijo);
21
22             //esto significa que ni por un back edge el hijo accede al
23             //padre
24             //por lo que si el padre fuese eliminado el hijo quedaria
25             //aislado
26             if(lId[hijo] >= tId[p]) isArtic[p] = 1;
27             if(lId[hijo] > tId[p]){
28                 //esto significa que si se eliminase el camino de padre
29                 //se lograria desconectar el grafo, aka bridge
30             }
31             lId[p] = min(lId[p],lId[hijo]);
32         }else{
33             //si hay un ciclo indirecto, actualiza el valor para el
34             //padre
35             if(hijo != padre[p]) lId[p] = min(lId[p],tId[hijo]);
36         }
37     }
38 }
39 //OJO esto solo jala con Undirected graphs
40 /*
41 MAIN
42 for(int i = 0; i<n; i++){
43     if(!vis[i]){
44         rootChildren = 0;
45         dfsRoot = i;
46         findAP_B(i);
47         //el algoritmo no puede detectar si el nodo que lo origino
48         //es un articulation point, por lo que queda checar si
49         //en el spanning tree que genero tiene mas de un solo hijo
50         isArtic[i] = (rootChildren>1?1:0);
51     }
52 }
    
```

50 `*/`

## 4 Math

### 4.1 Identities

$$C_n = \frac{2(2n-1)}{n+1} C_{n-1}$$

$$C_n = \frac{1}{n+1} \binom{2n}{n}$$

$$C_n \sim \frac{4^n}{n^{3/2}\sqrt{\pi}}$$

$$\sigma(n) = O(\log(\log(n))) \text{ (number of divisors of } n)$$

$$F_{2n+1} = F_n^2 + F_{n+1}^2$$

$$F_{2n} = F_{n+1}^2 - F_{n-1}^2$$

$$\sum_{i=1}^n F_i = F_{n+2} - 1$$

$$F_{n+i}F_{n+j} - F_nF_{n+i+j} = (-1)^n F_i F_j$$

$$\text{(Möbius Inv. Formula) Let } g(n) = \sum_{d|n} f(d), \text{ then } f(n) = \sum_{d|n} d \mu\left(\frac{n}{d}\right).$$

$$\text{Permutaciones objetos repetidos } P(n, k) = \frac{P(n, k)}{n_1! n_2! \dots}$$

$$\text{Separadores, Ecuaciones lineares } a \text{ variables} = b \left( \binom{a}{b} \right) = \binom{a+b-1}{b} = \binom{a+b-1}{a-1}$$

### 4.2 Binary Exponentiation and modArith

```

1 long long int inf = 10000000007;
2 //suma (a+b)%m
3 //resta ((a-b)%m+m)%m
4 //mult (a*b)%m
5 long long binpow(long long b, long long e) {
6     long long res = 1; b%=inf;
7     while (e > 0) {
8         if (e & 1) res = (res * b)%inf;
9         b = (b * b)%inf;
10        e >>= 1;
11    }
12    return res;
13 }
```

### 4.3 Modular Inverse (dividir mod)

```

1 long long int inf = 10000000007;
2 long long int gcd(long long int a, long long int b, long long int& x,
3     long long int& y) {
4     x = 1, y = 0;
5     long long int x1 = 0, y1 = 1, a1 = a, b1 = b;
6     while (b1) {
```

```

6         long long int q = a1 / b1;
7         tie(x, x1) = make_tuple(x1, x - q * x1);
8         tie(y, y1) = make_tuple(y1, y - q * y1);
9         tie(a1, b1) = make_tuple(b1, a1 - q * b1);
10    }
11    return a1;
12 }
13 long long int modinverse(long long int b, long long int m){
14     long long int x,y;
15     long long int d = gcd(b,inf,x,y);
16     if(d!=1) return -1;
17     return ((x%inf)+inf)%inf;
18 }
```

### 4.4 Modular Binomial Coefficient and Permutations

```

1 long long int inf = 10000000007;
2 //cat[n] = bincoef(2*n,n)/(n+1), cat[0] = 1
3 class binCoef{
4     long long int lim;
5     long long int* fact;
6 public:
7     binCoef(long long int l){
8         lim = l; fact = new long long int[l+1];fact[0]= 1;
9         for(long long int i = 1; i<=l; i++) fact[i] = (fact[i-1]*i)%inf;
10    }
11    //perm = (fact[n] * modinverse(fac[n-k],inf)%inf;
12    long long int query(long long int n, long long int k){
13        if(n<k) return 0;
14        return (fact[n] * modinverse((fac[n-k]*fact[k])%inf,inf))%inf;
15    }
16 };
```

### 4.5 Non-Mod Binomial Coefficient and Permutations

```

1 //Solo usar con n<=20
2 //cat[n] = bincoef(2*n,n)/(n+1), cat[0] = 1
3 unsigned long long int bincoef(unsigned long long int n, unsigned long
4     long int k){
5     if(n<k) return 0;
6     unsigned long long int num = 1, den= 1;
7     for(unsigned long long int i = (n-k)+1; i<=n; i++) num*=i;
8     for(unsigned long long int i = 2; i<=k; i++) den*=i;
9     //perm = return num;
```



```

9     return num/den;
10 }
    
```

## 4.6 Modular Catalan Numbers

```

1 long long int inf = 10000000007;
2 class catalan{
3     long long int* cat; long long int lim
4 public:
5     catalan(long long int l){
6         lim = l; cat = new long long int[l+10];cat[0] = 1;
7         for(long long int i = 0;i<=l; i++) cat[i+1] = (((((4LL*i+2)%inf)
8             *cat[i])%inf) *modinverse(n+2))%inf;
9     }
10    long long int query(long long int n){ return cat[n];}
    
```

## 4.7 Ceil Fraccionario

```

1 long long int techo(long long int num, long long int den){ return (num+
    den-1)/den;}
    
```

## 4.8 Numeros de Fibonacci

```

1 //en caso de ser usados mod un m pequeno
2 //recordar que los numeros de fibonacci se repiten por lo menos cada m^2
3 //0(n)
4 unsigned long long int fib(int n){
5     unsigned long long int a = 1,b = 1,aux;
6     if(n<=2){
7         return 1;
8     }
9     for(int i = 3; i<=n; i++){
10        aux = a+b;
11        a = b;
12        b = aux;
13    }
14    return b;
15 }
    
```

```

1 const long long int inf = 10000000007;
2 unordered_map<long long int,long long int> Fib;
3 //0(log n) :DD
4 long long int fib(long long int n)
    
```

```

5 {
6     if(n<2) return 1;
7     if(Fib.find(n) != Fib.end()) return Fib[n];
8     Fib[n] = (fib((n+1) / 2)*fib(n/2) + fib((n-1) / 2)*fib((n-2) / 2)) %
9         inf;
10    return Fib[n];
    }
    
```

## 4.9 Sieve Of Eratosthenes

```

1 #define MAXN 10e6
2 class soe{
3 public:
4     bitset<MAXN> isPrime;
5     soe(){
6         for(int i = 3; i<MAXN; i++) isPrime[i] = (i%2);
7         isPrime[2] = 1;
8         for(int i = 3; i*i<MAXN; i+=2)
9             if(isPrime[i])
10                for(int j = i*i; j<MAXN; j+=i)
11                    isPrime[j] = 0;
12    }
13 };
    
```

## 4.10 Sieve-based Factorization

```

1 #define MAXN 10e6
2 class soe{
3 public:
4     int smolf[MAXN];
5     soe(){
6         for(int i = 2; i<MAXN; i++) smolf[i] = (i%2==0?2:i);
7
8         for(int i = 3; i*i<MAXN; i+=2)
9             if(smolf[i]==i)
10                for(int j = i*i; j<MAXN; j+=i)
11                    smolf[j] = min(smolf[j],smolf[i]);
12    }
13 };
    
```

## 4.11 Cycle Finding

```

1 void cyclef(long long int sem){
2     long long int hare = f(sem),tort=f(sem);hare = f(hare);
    
```

```

3 //liebre avanza dos pasos, tortuga solo uno
4 while(hare!=tort){
5     tort = f(tort); hare = f(f(hare));
6 }
7 //Se detiene en el inicio del ciclo
8 tort = sem;
9 while(hare!=tort){
10     tort = f(tort); hare = f(hare);
11 }
12
13 int len = 1;
14 tort = f(sem);
15 while(hare!=tort){
16     tort=f(tort);
17     len++;
18 }
19 }
    
```

#### 4.12 Berlekamp Massey

```

1 typedef long long int ll;
2 //Obtiene recurrencia lineal dados los primeros elementos en O(n^2)
3 vector<ll> berlekampMassey(const vector<ll> &s) {
4     vector<ll> c;
5     vector<ll> oldC;
6     int f = -1;
7     for (int i=0; i<(int)s.size(); i++) {
8         ll delta = s[i];
9         for (int j=1; j<=(int)c.size(); j++) delta -= c[j-1] * s[i-j];
10        if (delta == 0) continue;
11        if (f == -1) {
12            c.resize(i + 1);
13            mt19937 rng(chrono::steady_clock::now().time_since_epoch().
14                count());
15            for (ll &x : c) x = rng();
16            f = i;
17        } else {
18            vector<ll> d = oldC;
19            for (ll &x : d) x = -x;
20            d.insert(d.begin(), 1);
21            ll df1 = 0;
22            for (int j=1; j<=(int)d.size(); j++) df1 += d[j-1] * s[f+1-j
23                ];
24        }
25    }
26 }
    
```

```

22 assert(df1 != 0);
23 ll coef = delta / df1;
24 for (ll &x : d) x *= coef;
25 vector<ll> zeros(i - f - 1);
26 zeros.insert(zeros.end(), d.begin(), d.end());
27 d = zeros;
28 vector<ll> temp = c;
29 c.resize(max(c.size(), d.size()));
30 for (int j=0; j<(int)d.size(); j++) c[j] += d[j];
31 if (i - (int) temp.size() > f - (int) oldC.size()) {oldC =
32     temp;f = i;}
33 }
34 return c;
35 }
    
```

#### 4.13 Modular Berlekamp Massey

```

1 typedef long long int ll;
2 long long int inf = 1000000007;
3 vector<ll> bermas(vector<ll> x){
4     vector<ll> ls,cur;
5     int lf,ld;
6     for(int i = 0; i<x.size(); i++){
7         long long int t = 0;
8         for(int j = 0; j<cur.size(); j++) t=(t+x[i-j-1]*(long long int)
9             cur[j])%inf;
10        if((t-x[i])%inf==0)continue;
11        if(cur.size()==0){cur.resize(i+1);lf=i;ld=(t-x[i])%inf;continue
12            ;}
13        long long int k = (x[i]-t)*powermod(ld,inf-2)%inf;
14        vector<ll>c(i-lf-1);c.push_back(k);
15        for(int j = 0; j<ls.size(); j++) c.push_back(-ls[j]*k%inf);
16        if(c.size()<cur.size()) c.resize(cur.size());
17        for(int j = 0; j<cur.size();j++) c[j]=(c[j]+cur[j])%inf;
18        if(i-lf+ls.size()>=cur.size())ls=cur,lf=i,ld=(t-x[i])%inf;
19        cur=c;
20    }
21    for(int i =0; i<cur.size(); i++) cur[i]=(cur[i]%inf+inf)%inf;
22    return cur;
23 }
    
```

#### 4.14 Matrix exponentiation

```

1 typedef vector<vector<long long int>> Matrix;
2 long long int inf = 1000000007;
3 Matrix ones(int n) {
4     Matrix r(n,vector<long long int>(n));
5     for(int i= 0; i<n; i++){
6         r[i][i]=1;
7     }
8     return r;
9 }
10 Matrix operator*(Matrix &a, Matrix &b) {
11     int n=a.size(),m=b[0].size(),z=a[0].size();
12     Matrix r(n,vector<long long int>(m));
13     for(int i=0; i<n; i++){
14         for(int j=0; j<m; j++){
15             for(int k=0;k<z; k++){
16                 r[i][j]+=((a[i][k]%inf)*(b[k][j]%inf))%inf;
17                 r[i][j]%=inf;}}}
18     return r;
19 }
20 Matrix be(Matrix b, long long int e) {
21     Matrix r=ones(b.size());
22     while(e){if(e&1LL)r=r*b;b=b*b;e/=2;}
23     return r;
24 }
25
26 //Matrix mat(n,vector<long long int>(n));
    
```

#### 4.15 Ecuaciones Diofantinas

```

1 long long int gcd(long long int a, long long int b, long long int& x,
2     long long int& y) {
3     x = 1, y = 0;
4     long long int x1 = 0, y1 = 1, a1 = a, b1 = b;
5     while (b1) {
6         int q = a1 / b1;
7         tie(x, x1) = make_tuple(x1, x - q * x1);
8         tie(y, y1) = make_tuple(y1, y - q * y1);
9         tie(a1, b1) = make_tuple(b1, a1 - q * b1);
10    }
11    return a1;
12 }
13 long long int d;
14 bool findAnySol(long long int a, long long int& x, long long int b, long
    
```

```

14     long int& y, long long int c) {
15     long long int g = gcd(abs(a), abs(b), x, y);
16     if (c % g != 0) return false;
17     x *= c;
18     y *= c;
19     x /= g;
20     y /= g;
21     d = c / g;
22     if (a < 0) x = -x;
23     if (b < 0) y = -y;
24     return true;
25 }
26 //-----SOLBEGIN-----
27 int main() {
28     ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
29     long long int m, a, k, n;
30     long long int f, h, res;
31     //estira en n, y despues cada m
32     //estira en k+a, y despues cada a
33     cin >> n >> m >> a >> k;
34     while (n != 0 && m != 0 && a != 0 && k != 0) {
35         m = -m;
36         if (!findAnySol(m, f, a, h, k + a - n)) {
37             cout << "Impossible" << endl;
38         }else {
39             res = f * m+n;
40             while (res > 0) res -= m * d;
41             while (res < 0) res += m * d;
42
43             cout << res << endl;
44         }
45         cin >> n >> m >> a >> k;
46     }
47 }
48 //-----EOSOLUTION-----
    
```

#### 4.16 FFT, Stolen from GGDem

```

1 // SPOJ VFMUL - AC
2 // http://www.spoj.com/problems/VFMUL/
3 #include <bits/stdc++.h>
    
```

```

4  #define fst first
5  #define snd second
6  #define fore(i,a,b) for(int i=a,ThxDem=b;i<ThxDem;++i)
7  #define pb push_back
8  #define ALL(s) s.begin(),s.end()
9  #define FIN ios_base::sync_with_stdio(0);cin.tie(0);cout.tie(0)
10 #define SZ(s) int(s.size())
11 using namespace std;
12 typedef long long ll;
13 typedef pair<int,int> ii;
14
15 // MAXN must be power of 2 !!
16 // MOD-1 needs to be a multiple of MAXN !!
17 // big mod and primitive root for NTT:
18 const int MOD=998244353,RT=3,MAXN=1<<20;
19 typedef vector<int> poly;
20 // FFT
21 struct CD {
22     double r,i;
23     CD(double r=0, double i=0):r(r),i(i){}
24     double real()const{return r;}
25     void operator/=(const int c){r/=c, i/=c;}
26 };
27 CD operator*(const CD& a, const CD& b){
28     return CD(a.r*b.r-a.i*b.i,a.r*b.i+a.i*b.r);}
29 CD operator+(const CD& a, const CD& b){return CD(a.r+b.r,a.i+b.i);}
30 CD operator-(const CD& a, const CD& b){return CD(a.r-b.r,a.i-b.i);}
31 const double pi=acos(-1.0);
32 // NTT
33 /*
34 struct CD {
35     int x;
36     CD(int x):x(x){}
37     CD(){}
38     int get()const{return x;}
39 };
40 CD operator*(const CD& a, const CD& b){return CD(mulmod(a.x,b.x));}
41 CD operator+(const CD& a, const CD& b){return CD(addmod(a.x,b.x));}
42 CD operator-(const CD& a, const CD& b){return CD(submod(a.x,b.x));}
43 vector<int> rts(MAXN+9,-1);
44 CD root(int n, bool inv){
45     int r=rts[n]<0?rts[n]=pm(RT,(MOD-1)/n):rts[n];
46     return CD(inv?pm(r,MOD-2):r);

```

```

47 }
48 */
49 CD cp1[MAXN+9],cp2[MAXN+9];
50 int R[MAXN+9];
51 void dft(CD* a, int n, bool inv){
52     fore(i,0,n)if(R[i]<i)swap(a[R[i]],a[i]);
53     for(int m=2;m<=n;m*=2){
54         double z=2*pi/m*(inv?-1:1); // FFT
55         CD wi=CD(cos(z),sin(z)); // FFT
56         // CD wi=root(m,inv); // NTT
57         for(int j=0;j<n;j+=m){
58             CD w(1);
59             for(int k=j,k2=j+m/2;k2<j+m;k++,k2++){
60                 CD u=a[k];CD v=a[k2]*w;a[k]=u+v;a[k2]=u-v;w=w*wi;
61             }
62         }
63     }
64     if(inv)fore(i,0,n)a[i]/=n; // FFT
65     //if(inv){ // NTT
66     // CD z(pm(n,MOD-2)); // pm: modular exponentiation
67     // fore(i,0,n)a[i]=a[i]*z;
68     //}
69 }
70 poly multiply(poly& p1, poly& p2){
71     int n=p1.size()+p2.size()+1;
72     int m=1,cnt=0;
73     while(m<=n)m+=m,cnt++;
74     fore(i,0,m){R[i]=0;fore(j,0,cnt)R[i]=(R[i]<<1)|((i>>j)&1);}
75     fore(i,0,m)cp1[i]=0,cp2[i]=0;
76     fore(i,0,p1.size())cp1[i]=p1[i];
77     fore(i,0,p2.size())cp2[i]=p2[i];
78     dft(cp1,m,false);dft(cp2,m,false);
79     fore(i,0,m)cp1[i]=cp1[i]*cp2[i];
80     dft(cp1,m,true);
81     poly res;
82     n-=2;
83     fore(i,0,n)res.pb((ll)floor(cp1[i].real()+0.5)); // FFT
84     //fore(i,0,n)res.pb(cp1[i].x); // NTT
85     return res;
86 }
87
88 char s[MAXN],t[MAXN],r[MAXN];
89

```

```

90 int main(){
91     int tn;
92     scanf("%d",&tn);
93     while(tn--){
94         vector<int> a,b,c;
95         scanf("%s%s",s,t);
96         for(int i=0;s[i];++i)a.pb(s[i]-'0');reverse(a.begin(),a.end());
97         for(int i=0;t[i];++i)b.pb(t[i]-'0');reverse(b.begin(),b.end());
98         c=multiply(a,b);
99         while(!c.empty()&&!c.back())c.pop_back();
100        if(c.empty()){puts("0");continue;}
101        int n=0;
102        ll x=0;
103        fore(i,0,c.size()){
104            x+=c[i];
105            r[n++]=x%10;
106            x/=10;
107        }
108        while(x){
109            r[n++]=x%10;
110            x/=10;
111        }
112        reverse(r,r+n);
113        bool p=false;
114        fore(i,0,n){
115            putchar(r[i]+'0');
116        }
117        puts("");
118    }
119    return 0;
120 }

```

## 5 Geometry

## 6 Strings

### 6.1 Explode by token

```

1 // #include <sstream>
2
3 vector<string> explode(string const& s, char delim) {
4     vector<string> result;
5     istringstream iss(s);

```

```

6     for (string token; getline(iss, token, delim); )
7     {
8         result.push_back(move(token));
9     }
10    return result;
11 }

```

### 6.2 Multiple Hashings DS

```

1 struct multhash{
2     unsigned long long int h1,h2;
3     unsigned long long int alf[257];
4     bool operator < (multhash b) const {
5         if (h1 != b.h1) return h1 < b.h1;
6         return h2 < b.h2;
7     }
8     bool operator == (multhash b) const { return (h1== b.h1 && h2== b.h2)
9         ;}
10    bool operator != (multhash b) const { return !(h1== b.h1 && h2== b.h2)
11        ;}
12 public:
13     string s;
14     multhash(){
15         h1 = 0; h2 = 0; s = "";
16         for(char l = 'a'; l<='z'; l++) alf[l] = l-'a'+1;
17     }
18     void innit(){
19         unsigned long long int inf,p,op;
20
21         inf = 999727999;
22         p = 325255434; op = 325255434;
23         for(char l: s){
24             h1+=(p*alf[l])%inf;
25             p*=op;
26             p%=inf;
27         }
28
29         inf = 1070777777;
30         p = 10018302; op = 10018302;
31         for(char l: s){
32             h2+=(p*alf[l])%inf;
33             p*=op;
34             p%=inf;

```

```

33     }
34 }
35 };
36 //VALORES ALTERNATIVOS DE INF, LOG 17
37 //6666665555777777
38 //986143414027351997
39 //974383618913296759
40 //973006384792642181
41 //953947941937929919
42 //9090909090909091
43 //VALORES PARA P, USAR PRIMOS MAYORES A |Alfabeto|
44 //31,47,53,61,79
    
```

### 6.3 Permute chars of string

```

1 void permute(string str){
2     // Sort the string in lexicographically
3     // ascennding order
4     sort(str.begin(), str.end());
5
6     // Keep printing next permutation while there
7     // is next permutation
8     do {
9         cout<<str<<endl;
10    } while (next_permutation(str.begin(), str.end()));
11 }
    
```

### 6.4 Longest common subsequence

```

1 //0(|te|*|pa|)
2 //cambiar score para otros problemas, str all match = +2, miss/ins/del =
   -1
3 //usar char que no este en el alfabeto para denotar del/ins
4 string te,pa;
5 long long int ninf = -10e13;
6 long long int score(char a, char b){
7     if(a=='*' || b=='*') return 0;
8     if(a==b) return 1;
9     return ninf;
10 }
11 long long int lcs(){
12     long long int** dp;te = "*" + te; pa = "*" + pa;
13     long long int res = 0;
14
    
```

```

15 dp = new long long int*[te.size()];
16 for(int i = 0; i<te.size(); i++) dp[i] = new long long int[pa.size()
   ]();
17
18 for(int r = 1; r<te.size(); r++){
19     for(int c = 1; c<pa.size(); c++){
20         dp[r][c] = dp[r-1][c-1]+score(te[r],pa[c]);
21         dp[r][c] = max(dp[r][c-1]+score(te[r],'*'),dp[r][c]);
22         dp[r][c] = max(dp[r-1][c]+score('*',pa[c]),dp[r][c]);
23     }
24 }
25
26 return dp[te.size()-1][pa.size()-1];
27 }
    
```

### 6.5 KMP

```

1 string T,P;
2 int bt[MXN];
3 //0(|Text|+|Pattern|)
4 void KMPpre(){
5     int i = 0,j = -1; bt[0] = -1;
6     while(i<P.size()){
7         while(j>=0 && P[i]!=P[(j>=0?j:0)]) j = bt[j];
8         i++;j++; bt[i] = j;
9     }
10 }
11 int kmp(){
12     int res =0, i = 0, j = 0;
13     while(i<T.size()){
14         while(j>=0 && T[i] != P[(j>=0?j:0)]) j = bt[j];
15         i++; j++;
16         if(j==P.size()){//match, do anything
17             res++;j = bt[j];
18         }
19     }
20     return res;
21 }
    
```

### 6.6 Suffix Array

```

1 //se asume que la longitud de la cadena sera menor a 10**6, modificar el
   ub a discrecion
2 #define ub 1000000LL
    
```

```

3 //pot de ub times two
4 #define ccd 12
5
6 //metodos y structs auxiliares para el suffix array
7 struct sufd{int id;long long int t;};
8 int getndigit(long long int num, int d){
9     while(d--) num/=10LL;
10    return (int) (num%10LL);
11 }
12 void radixSort(vector<sufd>& arr){
13     int count[10]; int n = arr.size();
14     vector<sufd> aux(n);
15     for(int d = 0; d<ccd; d++){
16         for(int i = 0; i<10; i++) count[i] = 0;
17         for(int i = 0; i<n; i++) count[getndigit(arr[i].t,d)]++;
18         for(int i = 1; i<10; i++) count[i]+=count[i-1];
19         for(int i = n-1; i>=0; i--){
20             count[getndigit(arr[i].t,d)]--;
21             aux[count[getndigit(arr[i].t,d)]] = arr[i];
22         }
23         for(int i = 0; i<n; i++) arr[i] = aux[i];
24     }
25 }
26 //El suffix array mismo, agregar caracter menor al alfabeto al final de
    T
27 string T,P;
28 int* sa,*lcest;
29 int stsize;
30 void makesa(){
31     int n = T.size();
32     sa = new int[n+1](); int* ra = new int[2*n+2]();
33     for(int i = 0; i<n; i++){sa[i] = i; ra[i] = T[i];}
34
35     sufd aux;vector<sufd> arr(n);
36     for(int k = 1; k<n;k*=2){
37         arr.clear();
38         for(int i = 0; i<n; i++){
39             aux.id = sa[i]; aux.t = ra[sa[i]];aux.t*=ub;aux.t += ra[sa[i]
                ]+k];
40             arr.push_back(aux);
41         }
42         //en caso de TLE calar con STL sort
43         radixSort(arr);
    
```

```

44     sa[0] = arr[0].id; ra[sa[0]] = 0;
45     for(int i = 1; i<n; i++){
46         sa[i] = arr[i].id;
47         ra[sa[i]] = ra[sa[i-1]]+1;
48         if(arr[i].t == arr[i-1].t) ra[sa[i]]--;
49     }
50     if(ra[sa[n-1]]==n-1) break;
51 }
52 delete[]ra;
53 }
54 void makelce(){
55     int n = T.size();
56     int* lce = new int[n+2]();
57     int* rank = new int[n+2]();
58     for(int i = 0; i<n; i++) rank[sa[i]] = i;
59
60     int curr = 0;
61     for(int i= 0; i<n; i++){
62         if(rank[i]==0) continue;
63         for(int j = max(curr-1,0); j+max(i,sa[rank[i]-1])<n; j++){
64             if(T[i+j] == T[sa[rank[i]-1]+j]) curr = j;
65             if(T[i+j]!=T[sa[rank[i]-1]+j]){curr = j-1; break;}
66         }
67         curr++;lce[i] = curr;
68     }
69
70     int p = 1; while(p<=n) p*=2; stsize = 2*p-1;
71     lcest = new int[stsize+2]();
72     for(int i= p-1; i-(p-1)<n; i++) lcest[i] = lce[sa[i-(p-1)]];
73     for(int i = p-2; i>=0; i--) lcest[i] = min(lcest[2*i+1],lcest[2*i +
        2]);
74     delete[] lce; delete[] rank;
75 }
76 int recque(int l, int r, int sti, int stil, int stir){
77     if(stir<l || stil>r) return ub;
78     if(l<=stil && stir<=r) return lcest[sti];
79     int stim = stil+stir; stim/=2;
80     return min(recque(l,r,sti*2+1,stil,stim),recque(l,r,sti*2+2,stim+1,
        stir));
81 }
82 int getlce(int l, int r){
83     if(l>r) return 0;
84     return recque(l,r,0,0,stsize/2);
    
```

```

85 }
86 int buscarRec(int l, int r,int lcp,int eas){
87     if(l>r) return -1;
88     int m = (l+r)/2;
89     //string curr = T.substr(sa[m],T.size()-sa[m]);
90     int lce = (eas>m?getlce(m+1,eas):getlce(eas+1,m));
91     if(lce>lcp){
92         if(eas<m) return buscarRec(m+1,r,lcp,eas);
93         if(eas>m) return buscarRec(l,m-1,lcp,eas);
94     }
95     if(lce<lcp){
96         if(eas>m) return buscarRec(m+1,r,lcp,eas);
97         if(eas<m) return buscarRec(l,m-1,lcp,eas);
98     }
99
100     for(int i = lcp,n = T.size(); sa[m]+i<n && i<P.size(); i++){if(P[i]
101         !=T[sa[m]+i]) break; lcp++;}
102     if(lcp == P.size()) return m;
103     if(l==r) return -1;
104     return (P[lcp]>T[sa[m]+lcp]?buscarRec(m+1,r,lcp,m):buscarRec(l,m-1,
105         lcp,m));
106 }
107 int buscar(){
108     int n = T.size();
109     if(P.size()>n) return -1;
110     return buscarRec(1,n-1,0,0);
111 }
112 //CODIGO DE 100 LINEAS, TE HE FALLADO MarcosK
113 //Uso: lee T, agregar signo dolar, llama makesa(); makelce(); lee P para
114     despues buscar()
115 //delete[] sa; delete[] lcest; cuando leas de nuevo T
116 //O(|T| log(|T|)) preprocesamiento, O(|P|+log**2(|T|)) cada busqueda
117 //Buscar devuelve un indice cualquiera de sa tal que el sufijo denotado
118     tenga P como prefijo
119 //Se puede hacer mas corto?

```

## 6.7 STL Suffix Array

```

1 //se asume que la longitud de la cadena sera menor a 10**6, modificar el
2     ub a discrecion
3 #define ub 1000000LL
4 //pot de ub times two
5 #define ccd 12

```

```

5 //metodos y structs auxiliares para el suffix array
6 struct sufd{int id;long long int t;
7     bool operator<(const sufd b) const{return t<b.t;}}
8 };
9 //El suffix array mismo, agregar caracter menor al alfabeto al final de
10     T
11 string T,P;
12 int* sa,*lcest;
13 int stsize;
14 void makesa(){
15     int n = T.size();
16     sa = new int[n+1](); int* ra = new int[2*n+2]();
17     for(int i = 0; i<n; i++){sa[i] = i; ra[i] = T[i];}
18
19     sufd aux;vector<sufd> arr(n);
20     for(int k = 1; k<n;k*=2){
21         arr.clear();
22         for(int i = 0; i<n; i++){
23             aux.id = sa[i]; aux.t = ra[sa[i]];aux.t*=ub;aux.t += ra[sa[i]
24                 ]+k];
25             arr.push_back(aux);
26         }
27         //en caso de TLE calar con STL sort
28         sort(arr.begin(),arr.end());
29         sa[0] = arr[0].id; ra[sa[0]] = 0;
30         for(int i = 1; i<n; i++){
31             sa[i] = arr[i].id;
32             ra[sa[i]] = ra[sa[i-1]]+1;
33             if(arr[i].t == arr[i-1].t) ra[sa[i]]--;
34         }
35         if(ra[sa[n-1]]==n-1) break;
36     }
37     delete[]ra;
38 }
39 void makelce(){
40     int n = T.size();
41     int* lce = new int[n+2]();
42     int* rank = new int[n+2]();
43     for(int i = 0; i<n; i++) rank[sa[i]] = i;
44
45     int curr = 0;
46     for(int i= 0; i<n; i++){
47         if(rank[i]==0) continue;

```



```

46     for(int j = max(curr-1,0); j+max(i,sa[rank[i]-1])<n; j++){
47         if(T[i+j] == T[sa[rank[i]-1]+j]) curr = j;
48         if(T[i+j] != T[sa[rank[i]-1]+j]){curr = j-1; break;}
49     }
50     curr++;lce[i] = curr;
51 }
52
53 int p = 1; while(p<=n) p*=2; stsize = 2*p-1;
54 lcest = new int[stsize+2]();
55 for(int i = p-1; i-(p-1)<n; i++) lcest[i] = lce[sa[i-(p-1)]];
56 for(int i = p-2; i>=0; i--) lcest[i] = min(lcest[2*i+1],lcest[2*i +
57     2]);
58 delete[] lce; delete[] rank;
59 }
60 int recque(int l, int r, int sti, int stil, int stir){
61     if(stir<l || stil>r) return ub;
62     if(l<=stil && stir<=r) return lcest[sti];
63     int stim = stil+stir; stim/=2;
64     return min(recque(l,r,sti*2+1,stil,stim),recque(l,r,sti*2+2,stim+1,
65         stir));
66 }
67 int getlce(int l, int r){
68     if(l>r) return 0;
69     return recque(l,r,0,0,stsize/2);
70 }
71 int buscarRec(int l, int r,int lcp,int eas){
72     if(l>r) return -1;
73     int m = (l+r)/2;
74     //string curr = T.substr(sa[m],T.size()-sa[m]);
75     int lce = (eas>m?getlce(m+1,eas):getlce(eas+1,m));
76     if(lce>lcp){
77         if(eas<m) return buscarRec(m+1,r,lcp,eas);
78         if(eas>m) return buscarRec(l,m-1,lcp,eas);
79     }
80     if(lce<lcp){
81         if(eas>m) return buscarRec(m+1,r,lcp,eas);
82         if(eas<m) return buscarRec(l,m-1,lcp,eas);
83     }
84     for(int i = lcp,n = T.size(); sa[m]+i<n && i<P.size(); i++){if(P[i
85         ]!=T[sa[m]+i]) break; lcp++;}
86     if(lcp == P.size()) return m;
87     if(l==r) return -1;

```

```

86     return (P[lcp]>T[sa[m]+lcp]?buscarRec(m+1,r,lcp,m):buscarRec(l,m-1,
87         lcp,m));
88 }
89 int buscar(){
90     int n = T.size();
91     if(P.size()>n) return -1;
92     return buscarRec(1,n-1,0,0);
93 }
94 pair<int,int> primeraYUltimaOc(){
95     int sai = buscar();
96     pair<int,int>res = {sai,sai};
97     if(sai==-1) return res;
98
99     int l,r,m;
100
101     r = sai-1; l = 0;
102     while(l<=r){
103         m = (l+r)/2;
104         if(getlce(m+1,sai)>=P.size()){
105             res.first = m; r = m-1;
106         }else{
107             l = m+1;
108         }
109     }
110     l = sai+1;r = T.size()-1;
111     while(l<=r){
112         m = (l+r)/2;
113         if(getlce(sai+1,m)>=P.size()){
114             res.second = m; l = m+1;
115         }else{
116             r = m-1;
117         }
118     }
119     return res;
120 }
121 //CODIGO DE 100 LINEAS, TE HE FALLADO MarcosK
122 //Uso: lee T, agregar signo dolar, llama makesa(); makelce(); lee P para
123 //despues buscar()
124 //delete[] sa; delete[] lcest; cuando leas de nuevo T
125 //0(|T| log(|T|)) preprocesamiento, 0(|P|+log**2(|T|)) cada busqueda
126 //Buscar devuelve un indice cualquiera de sa tal que el sufijo denotado
127 //tenga P como prefijo
128 //Se puede hacer mas corto?

```

## 7 Clasicos

### 7.1 Job scheduling

#### 7.1.1 One machine, linear penalty

```

1 //cuando se tiene que encontrar un orden optimo
2 //para trabajos con una funcion lineal de penalty, basta con hacer un
  sort en  $O(n \log n)$ 
3 struct trabajo{
4     long long int penalty, tiempo;
5     int ind;
6 };
7 bool comp(const trabajo a, const trabajo b){
8     if (a.tiempo * b.penalty == a.penalty * b.tiempo) return a.ind < b.ind
9     ;
10    return a.tiempo * b.penalty < a.penalty * b.tiempo;
11 }

```

#### 7.1.2 One machine, deadlines

```

1 //calcula la maxima cantidad de jobs que se pueden hacer dados sus
  deadlines y duraciones en  $O(n \log n)$ 
2 struct Job {
3     int deadline, duration, idx;
4
5     bool operator<(Job o) const {
6         return deadline < o.deadline;
7     }
8 };
9 vector<int> compute_schedule(vector<Job> jobs) {
10     sort(jobs.begin(), jobs.end());
11
12     set<pair<int, int>> s;
13     vector<int> schedule;
14     for (int i = jobs.size()-1; i >= 0; i--) {
15         int t = jobs[i].deadline - (i ? jobs[i-1].deadline : 0);
16         s.insert(make_pair(jobs[i].duration, jobs[i].idx));
17         while (t && !s.empty()) {
18             auto it = s.begin();
19             if (it->first <= t) {
20                 t -= it->first;
21                 schedule.push_back(it->second);
22             } else {

```

```

23         s.insert(make_pair(it->first - t, it->second));
24         t = 0;
25     }
26     s.erase(it);
27 }
28 }
29 return schedule;
30 }

```

#### 7.1.3 One machine, profit

```

1 // Dado n Jobs y su profit, calcula cual es el mayor profit que se puede
  obtener en  $O(n^2)$ 
2 struct Job{int start, finish, profit;};
3 bool jobComparataor(Job s1, Job s2){return (s1.finish < s2.finish);}
4 // Find the latest job (in sorted array) that doesn't
5 // conflict with the job[i]. If there is no compatible job,
6 // then it returns -1.
7 vector <Job> arr;
8 int* memo;
9 int latestNonConflict( int i){
10     for (int j = i - 1; j >= 0; j--)
11         if (arr[j].finish <= arr[i - 1].start)
12             return j;
13     return -1;
14 }
15 // A recursive function that returns the maximum possible
16 // profit from given array of jobs. The array of jobs must
17 // be sorted according to finish time.
18 int findMaxProfitRec( int n){
19     // Base case
20     if (n == 1) return arr[n - 1].profit;
21     if (memo[n]>=0) return memo[n];
22     // Find profit when current job is included
23     int inclProf = arr[n - 1].profit;
24     int i = latestNonConflict(n);
25     if (i != -1) inclProf += findMaxProfitRec( i + 1);
26
27     // Find profit when current job is excluded
28     int exclProf = findMaxProfitRec( n - 1);
29
30     return memo[n]=max(inclProf, exclProf);
31 }

```

```

32
33 // The main function that returns the maximum possible
34 // profit from given array of jobs
35 int findMaxProfit( int n){
36     sort(arr.begin(),arr.end(), jobComparataor);
37     return findMaxProfitRec(n);
38 }

```

#### 7.1.4 Two machines, min time

```

1 //Obtiene el ordenamiento optimo de Jobs en dos maquinas en O(n log n)
2 struct Job {
3     int a, b, idx;
4     bool operator<(Job o) const {return min(a, b) < min(o.a, o.b);}
5 };
6 vector<Job> johnsons_rule(vector<Job> jobs) {
7     sort(jobs.begin(), jobs.end());
8     vector<Job> a, b;
9     for (Job j : jobs) {
10         if (j.a < j.b)
11             a.push_back(j);
12         else
13             b.push_back(j);
14     }
15     a.insert(a.end(), b.rbegin(), b.rend());
16     return a;
17 }
18
19 pair<int, int> finish_times(vector<Job> const& jobs) {
20     int t1 = 0, t2 = 0;
21     for (Job j : jobs) {
22         t1 += j.a;
23         t2 = max(t2, t1) + j.b;
24     }
25     return make_pair(t1, t2);
26 }

```

## 8 Flow

### 8.1 Dinic, thx GGDem

```

1 #define pb push_back
2 #define mp make_pair
3 #define fst first

```

```

4 #define snd second
5 #define ALL(s) s.begin(),s.end()
6 #define SZ(x) int((x).size())
7 #define fore(i,a,b) for(int i=a,to=b;i<to;++i)
8 using namespace std;
9 typedef long long ll;
10
11 #define INF (1LL<<62)
12 // Min cut: nodes with dist>=0 vs nodes with dist<0
13 // Matching MVC: left nodes with dist<0 + right nodes with dist>0
14 struct Dinic{
15     int nodes,src,dst;
16     vector<int> dist,q,work;
17     struct edge {int to,rev;ll f,cap;};
18     vector<vector<edge>> g;
19     Dinic(int x):nodes(x),g(x),dist(x),q(x),work(x){}
20     void add_edge(int s, int t, ll cap){
21         g[s].pb((edge){t,SZ(g[t]),0,cap});
22         g[t].pb((edge){s,SZ(g[s])-1,0,0});
23     }
24     bool dinic_bfs(){
25         fill(ALL(dist),-1);dist[src]=0;
26         int qt=0;q[qt++]=src;
27         for(int qh=0;qh<qt;qh++){
28             int u=q[qh];
29             fore(i,0,SZ(g[u])){
30                 edge &e=g[u][i];int v=g[u][i].to;
31                 if(dist[v]<0&&e.f<e.cap)dist[v]=dist[u]+1,q[qt++]=v;
32             }
33         }
34         return dist[dst]>=0;
35     }
36     ll dinic_dfs(int u, ll f){
37         if(u==dst)return f;
38         for(int &i=work[u];i<SZ(g[u]);i++){
39             edge &e=g[u][i];
40             if(e.cap<=e.f)continue;
41             int v=e.to;
42             if(dist[v]==dist[u]+1){
43                 ll df=dinic_dfs(v,min(f,e.cap-e.f));
44                 if(df>0){e.f+=df;g[v][e.rev].f-=df;return df;}
45             }
46         }

```

```

47     return 0;
48 }
49 ll max_flow(int _src, int _dst){
50     src=_src;dst=_dst;
51     ll result=0;
52     while(dinic_bfs()){
53         fill(ALL(work),0);
54         while(ll delta=dinic_dfs(src,INF))result+=delta;
55     }
56     return result;
57 }
58 };
59
60 //-----SOLBEGIN-----
61 int main() {
62     ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
63     //l set,r set
64     int n,m;
65     cin>>n>>m;
66     m+=n;
67     Dinic d(n+m+2);
68     for(int i = 1; i<=n; i++) d.add_edge(0,i,1);
69     for(int i = n+1; i<=m; i++) d.add_edge(i,m+1,1);
70
71     int fin,q;
72     for(int i = 1; i<=n; i++){
73         cin>>q;
74         while(q--){
75             cin>>fin;
76             d.add_edge(i,n+fin,1);
77         }
78     }
79     int res =d.max_flow(0,m+1);
80     m-=n;
81     //how many were left unmatched
82     cout<<m-res<<endl;
83 }
84 //-----EOSOLUTION-----

```

## 9 Miscellaneous

### 9.1 Bit Manipulation

```

1  #include "bits/stdc++.h"
2  using namespace std;
3  #define endl '\n'
4
5
6  int main() {
7      ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
8      //Se representan bitmasks de 30 a 62 bits
9      //usando signed int y signed long long int
10     //para evitar problemas con el complemento de dos
11     signed int a, b;
12     //para multiplicar un numero por dos solo es necesario aplicar un
13     // shifteo de sus bits a la izquierda
14     a = 1;
15     a= a << 3;
16     cout << a << endl;
17     //para dividir un numero entre dos es necesario aplicar un
18     //shifteo a la derecha
19     a = 32;
20     a = a >> 3;
21     cout << a << endl;
22     //para encender el bit n de a, solo hay que igualar a = a | pow(2,n-1)
23     //prende el tercer bit
24     a = 1;
25     b = 1 << 2;
26     a = a | b;
27     cout << a << endl;
28     //para apagar el bit n de a, solo hay que a &= ~pow(2,n-1)
29     //prende el tercer bit
30     a = 5;
31     b = 1 << 2;
32     a &= ~b;
33     cout << a << endl;
34     //para revisar si el bit n de a esta encendido
35     //revisa si el tercer bit esta encendido
36     a = 5;
37     b = 1 << 2;
38     a = a & b;
39     cout << (a?"SI":"NO") << endl;
40     //para volter el bit n de a, solo hay que igualar a = a ^ pow(2,n-1)
41     //apaga el tercer bit
42     a = 5;
43     b = 1 << 2;

```

```

44  a = a ^ b;
45  cout << a << endl;
46  //para obtener el bit menos significativo que esta encendido a& -a
47  a = 12;
48  cout << log2(a & ((-1) * a))+1 << endl;
49  //para prender todos los bits hasta n
50  a = (1<<4)-1;
51  cout << a << endl;
52  }
53  //-----EOSOLUTION-----

1  #include "bits/stdc++.h"
2  using namespace std;
3  #define endl '\n'
4  #pragma GCC optimize("O3")
5  #pragma GCC target("popcnt")
6
7  //no usar con visual c++
8  //solo con g++ like compilers
9  int main() {
10     ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
11     signed long long int a, b, n;
12     //Obtain the remainder (modulo) of a when it is divided by n (n is a
        power of 2)
13     a = 15; n = 8-1;
14     a &= n;
15     cout << "a%n, a=15, n=2^3" << endl;
16     cout << a << endl;
17     //Apaga el bit menos significativo de a
18     a = 14;
19     b = (a & ((-1) * a));
20     a &= ~b;
21     cout << a << endl;
22     //enciende el ultimo cero de a
23     a = 9;
24     b = ~a;
25     b = (b & ((-1) * b));
26     a = a | b;
27     cout << a<<endl;
28     //contar bits encendidos en a
29     cout << __builtin_popcount(a)<<endl;
30     //checar la paridad de a
31     cout << (__builtin_parity(a) ? "IMPAR" : "PAR") << endl;

```

```

32  //contar leading zeroes en a
33  cout << __builtin_clz(a)<<endl;
34  //contar 9,trailling zeroes en a
35  cout << __builtin_ctz(a)<<endl;
36  }
37  //-----EOSOLUTION-----

```

## 10 Testing

### 10.1 Highly Composite Numbers

Particularly useful when testing number theoretical solutions.

1	1	1
2	2	2
3	4	2 <sup>2</sup>
4	6	2*3
5	12	2 <sup>2</sup> *3
6	24	2 <sup>3</sup> *3
7	36	2 <sup>2</sup> *3 <sup>2</sup>
8	48	2 <sup>4</sup> *3
9	60	2 <sup>2</sup> *3*5
10	120	2 <sup>3</sup> *3*5
11	180	2 <sup>2</sup> *3 <sup>2</sup> *5
12	240	2 <sup>4</sup> *3*5
13	360	2 <sup>3</sup> *3 <sup>2</sup> *5
14	720	2 <sup>4</sup> *3 <sup>2</sup> *5
15	840	2 <sup>3</sup> *3*5*7
16	1260	2 <sup>2</sup> *3 <sup>2</sup> *5*7
17	1680	2 <sup>4</sup> *3*5*7
18	2520	2 <sup>3</sup> *3 <sup>2</sup> *5*7
19	5040	2 <sup>4</sup> *3 <sup>2</sup> *5*7
20	7560	2 <sup>3</sup> *3 <sup>3</sup> *5*7
21	10080	2 <sup>5</sup> *3 <sup>2</sup> *5*7
22	15120	2 <sup>4</sup> *3 <sup>3</sup> *5*7
23	20160	2 <sup>6</sup> *3 <sup>2</sup> *5*7
24	25200	2 <sup>4</sup> *3 <sup>2</sup> *5 <sup>2</sup> *7
25	27720	2 <sup>3</sup> *3 <sup>2</sup> *5*7*11
26	45360	2 <sup>4</sup> *3 <sup>4</sup> *5*7
27	50400	2 <sup>5</sup> *3 <sup>2</sup> *5 <sup>2</sup> *7
28	55440	2 <sup>4</sup> *3 <sup>2</sup> *5*7*11
29	83160	2 <sup>3</sup> *3 <sup>3</sup> *5*7*11
30	110880	2 <sup>5</sup> *3 <sup>2</sup> *5*7*11
31	166320	2 <sup>4</sup> *3 <sup>3</sup> *5*7*11

32	221760	168	2`6*3`2*5*7*11	75	5587021440	2048	2`7*3`3*5*7*11*13*17*19
33	277200	180	2`4*3`2*5`2*7*11	76	6983776800	2304	2`5*3`3*5`2*7*11*13*17*19
34	332640	192	2`5*3`3*5*7*11	77	10475665200	2400	2`4*3`4*5`2*7*11*13*17*19
35	498960	200	2`4*3`4*5*7*11	78	13967553600	2688	2`6*3`3*5`2*7*11*13*17*19
36	554400	216	2`5*3`2*5`2*7*11	79	20951330400	2880	2`5*3`4*5`2*7*11*13*17*19
37	665280	224	2`6*3`3*5*7*11	80	27935107200	3072	2`7*3`3*5`2*7*11*13*17*19
38	720720	240	2`4*3`2*5*7*11*13	81	41902660800	3360	2`6*3`4*5`2*7*11*13*17*19
39	1081080	256	2`3*3`3*5*7*11*13	82	48886437600	3456	2`5*3`3*5`2*7`2*11*13*17*19
40	1441440	288	2`5*3`2*5*7*11*13	83	64250746560	3584	2`6*3`3*5*7*11*13*17*19*23
41	2162160	320	2`4*3`3*5*7*11*13	84	73329656400	3600	2`4*3`4*5`2*7`2*11*13*17*19
42	2882880	336	2`6*3`2*5*7*11*13	85	80313433200	3840	2`4*3`3*5`2*7*11*13*17*19*23
43	3603600	360	2`4*3`2*5`2*7*11*13	86	97772875200	4032	2`6*3`3*5`2*7`2*11*13*17*19
44	4324320	384	2`5*3`3*5*7*11*13	87	128501493120	4096	2`7*3`3*5*7*11*13*17*19*23
45	6486480	400	2`4*3`4*5*7*11*13	88	146659312800	4320	2`5*3`4*5`2*7`2*11*13*17*19
46	7207200	432	2`5*3`2*5`2*7*11*13	89	160626866400	4608	2`5*3`3*5`2*7*11*13*17*19*23
47	8648640	448	2`6*3`3*5*7*11*13	90	240940299600	4800	2`4*3`4*5`2*7*11*13*17*19*23
48	10810800	480	2`4*3`3*5`2*7*11*13	91	293318625600	5040	2`6*3`4*5`2*7`2*11*13*17*19
49	14414400	504	2`6*3`2*5`2*7*11*13	92	321253732800	5376	2`6*3`3*5`2*7*11*13*17*19*23
50	17297280	512	2`7*3`3*5*7*11*13	93	481880599200	5760	2`5*3`4*5`2*7*11*13*17*19*23
51	21621600	576	2`5*3`3*5`2*7*11*13	94	642507465600	6144	2`7*3`3*5`2*7*11*13*17*19*23
52	32432400	600	2`4*3`4*5`2*7*11*13	95	963761198400	6720	2`6*3`4*5`2*7*11*13*17*19*23
53	36756720	640	2`4*3`3*5*7*11*13*17	96	1124388064800	6912	2`5*3`3*5`2*7`2*11*13*17*19*23
54	43243200	672	2`6*3`3*5`2*7*11*13	97	1606268664000	7168	2`6*3`3*5`3*7*11*13*17*19*23
55	61261200	720	2`4*3`2*5`2*7*11*13*17	98	1686582097200	7200	2`4*3`4*5`2*7`2*11*13*17*19*23
56	73513440	768	2`5*3`3*5*7*11*13*17	99	1927522396800	7680	2`7*3`4*5`2*7*11*13*17*19*23
57	110270160	800	2`4*3`4*5*7*11*13*17	100	2248776129600	8064	2`6*3`3*5`2*7`2*11*13*17*19*23
58	122522400	864	2`5*3`2*5`2*7*11*13*17	101	3212537328000	8192	2`7*3`3*5`3*7*11*13*17*19*23
59	147026880	896	2`6*3`3*5*7*11*13*17	102	3373164194400	8640	2`5*3`4*5`2*7`2*11*13*17*19*23
60	183783600	960	2`4*3`3*5`2*7*11*13*17	103	4497552259200	9216	2`7*3`3*5`2*7`2*11*13*17*19*23
61	245044800	1008	2`6*3`2*5`2*7*11*13*17	104	6746328388800	10080	2`6*3`4*5`2*7`2*11*13*17*19*23
62	294053760	1024	2`7*3`3*5*7*11*13*17	105	8995104518400	10368	2`8*3`3*5`2*7`2*11*13*17*19*23
63	367567200	1152	2`5*3`3*5`2*7*11*13*17	106	9316358251200	10752	2`6*3`3*5`2*7*11*13*17*19*23*29
64	551350800	1200	2`4*3`4*5`2*7*11*13*17	107	13492656777600	11520	2`7*3`4*5`2*7`2*11*13*17*19*23
65	698377680	1280	2`4*3`3*5*7*11*13*17*19	108	18632716502400	12288	2`7*3`3*5`2*7*11*13*17*19*23*29
66	735134400	1344	2`6*3`3*5`2*7*11*13*17	109	26985313555200	12960	2`8*3`4*5`2*7`2*11*13*17*19*23
67	1102701600	1440	2`5*3`4*5`2*7*11*13*17	110	27949074753600	13440	2`6*3`4*5`2*7*11*13*17*19*23*29
68	1396755360	1536	2`5*3`3*5*7*11*13*17*19	111	32607253879200	13824	2`5*3`3*5`2*7`2*11*13*17*19*23*29
69	2095133040	1600	2`4*3`4*5*7*11*13*17*19	112	46581791256000	14336	2`6*3`3*5`3*7*11*13*17*19*23*29
70	2205403200	1680	2`6*3`4*5`2*7*11*13*17	113	48910880818800	14400	2`4*3`4*5`2*7`2*11*13*17*19*23*29
71	2327925600	1728	2`5*3`2*5`2*7*11*13*17*19	114	55898149507200	15360	2`7*3`4*5`2*7*11*13*17*19*23*29
72	2793510720	1792	2`6*3`3*5*7*11*13*17*19	115	65214507758400	16128	2`6*3`3*5`2*7`2*11*13*17*19*23*29
73	3491888400	1920	2`4*3`3*5`2*7*11*13*17*19	116	93163582512000	16384	2`7*3`3*5`3*7*11*13*17*19*23*29
74	4655851200	2016	2`6*3`2*5`2*7*11*13*17*19	117	97821761637600	17280	2`5*3`4*5`2*7`2*11*13*17*19*23*29

118	130429015516800	18432	2^7*3^3*5^2*7^2*11*13*17*19*23*29
119	195643523275200	20160	2^6*3^4*5^2*7^2*11*13*17*19*23*29
120	260858031033600	20736	2^8*3^3*5^2*7^2*11*13*17*19*23*29
121	288807105787200	21504	2^6*3^3*5^2*7*11*13*17*19*23*29*31
122	391287046550400	23040	2^7*3^4*5^2*7^2*11*13*17*19*23*29
123	577614211574400	24576	2^7*3^3*5^2*7*11*13*17*19*23*29*31
124	782574093100800	25920	2^8*3^4*5^2*7^2*11*13*17*19*23*29
125	866421317361600	26880	2^6*3^4*5^2*7*11*13*17*19*23*29*31
126	1010824870255200	27648	2^5*3^3*5^2*7^2*11*13*17*19*23*29*31
127	1444035528936000	28672	2^6*3^3*5^3*7*11*13*17*19*23*29*31
128	1516237305382800	28800	2^4*3^4*5^2*7^2*11*13*17*19*23*29*31
129	1732842634723200	30720	2^7*3^4*5^2*7*11*13*17*19*23*29*31
130	2021649740510400	32256	2^6*3^3*5^2*7^2*11*13*17*19*23*29*31
131	2888071057872000	32768	2^7*3^3*5^3*7*11*13*17*19*23*29*31
132	3032474610765600	34560	2^5*3^4*5^2*7^2*11*13*17*19*23*29*31
133	4043299481020800	36864	2^7*3^3*5^2*7^2*11*13*17*19*23*29*31
134	6064949221531200	40320	2^6*3^4*5^2*7^2*11*13*17*19*23*29*31
135	8086598962041600	41472	2^8*3^3*5^2*7^2*11*13*17*19*23*29*31
136	10108248702552000	43008	2^6*3^3*5^3*7^2*11*13*17*19*23*29*31
137	12129898443062400	46080	2^7*3^4*5^2*7^2*11*13*17*19*23*29*31
138	18194847664593600	48384	2^6*3^5*5^2*7^2*11*13*17*19*23*29*31
139	20216497405104000	49152	2^7*3^3*5^3*7^2*11*13*17*19*23*29*31
140	24259796886124800	51840	2^8*3^4*5^2*7^2*11*13*17*19*23*29*31
141	30324746107656000	53760	2^6*3^4*5^3*7^2*11*13*17*19*23*29*31
142	36389695329187200	55296	2^7*3^5*5^2*7^2*11*13*17*19*23*29*31
143	48519593772249600	57600	2^9*3^4*5^2*7^2*11*13*17*19*23*29*31
144	60649492215312000	61440	2^7*3^4*5^3*7^2*11*13*17*19*23*29*31
145	72779390658374400	62208	2^8*3^5*5^2*7^2*11*13*17*19*23*29*31
146	74801040398884800	64512	2^6*3^3*5^2*7^2*11*13*17*19*23*29*31*37
147	106858629141264000	65536	2^7*3^3*5^3*7*11*13*17*19*23*29*31*37
148	112201560598327200	69120	2^5*3^4*5^2*7^2*11*13*17*19*23*29*31*37
149	149602080797769600	73728	2^7*3^3*5^2*7^2*11*13*17*19*23*29*31*37
150	224403121196654400	80640	2^6*3^4*5^2*7^2*11*13*17*19*23*29*31*37
151	299204161595539200	82944	2^8*3^3*5^2*7^2*11*13*17*19*23*29*31*37
152	374005201994424000	86016	2^6*3^3*5^3*7^2*11*13*17*19*23*29*31*37
153	448806242393308800	92160	2^7*3^4*5^2*7^2*11*13*17*19*23*29*31*37
154	673209363589963200	96768	2^6*3^5*5^2*7^2*11*13*17*19*23*29*31*37
155	748010403988848000	98304	2^7*3^3*5^3*7^2*11*13*17*19*23*29*31*37
156	897612484786617600	103680	2^8*3^4*5^2*7^2*11*13*17*19*23*29*31*37