# First to Penalty

# -12

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## 1 Template

```
#include "bits/stdc++.h"
  //assert(x>0) si falla da RTE
  using namespace std;
  #define endl '\n'
  #define DBG(x) cerr<<\#x<< "=" << (x) << endl:
  #define RAYA cerr<<"========"<<endl:
  #define RAYAS cerr<<"...."<<endl;</pre>
  //#define DBG(x) :
   //#define RAYA ;
  //#define RAYAS ;
11
   //----SOLBEGIN-----
  int main() {
    ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
14
    int tC;
15
16
    cin >> tC;
17
    while (tC--) {
18
19
    }
20
21
^{22}
         -----EOSOLUTION-----
```

#### 2 Data structures

# 2.1 Simplified DSU (Stolen from GGDem)

```
int uf[MAXN];
void uf_init(){memset(uf,-1,sizeof(uf));}
int uf_find(int x){return uf[x]<0?x:uf[x]=uf_find(uf[x]);}
bool uf_join(int x, int y){
    x=uf_find(x);y=uf_find(y);
    if(x==y)return false;
    if(uf[x]>uf[y])swap(x,y);
    uf[x]+=uf[y];uf[y]=x;
    return true;
}
```

## 2.2 Disjoint Set Union

```
class disjSet {
     int* sz;
     int* par;
   public:
     int len;
     disjSet(int tam){
           sz = new int[tam + 4]();
           par = new int[tam + 4]();
           len = 0;
           for(int i = 0; i<=tam; i++){</pre>
               par[i] = i;
11
                sz[i] = 1;
12
               len++;
13
           }
       }
15
     int finds(int el){
16
           if (el == par[el]) return el;
17
           return par[el] = finds(par[el]);
18
       }
19
     void unions(int a, int b){
20
           a = finds(a);
21
         b = finds(b);
22
           if (a == b) return;
23
           len--;
24
           //se hace que el gde sea padre del pequeno
25
           if (sz[a] > sz[b]) swap(a,b);
           par[a] = b;
27
           sz[b] += sz[a];
28
       }
29
      ~disjSet(){
30
           delete[] size;
31
           size = nullptr;
32
           delete[] parent;
33
           parent = nullptr;
34
35
36 };
                            2.3 Segment tree
```

```
//MAXN = 2^k, n = tam arreglo inicial
int stsize; long long int neut;int n;
long long int* st = new long long int[2*MAXN-1]();
long long int fst(long long int a, long long int b);
```

vis[pa]=1;

```
5 long long int build(int sti,int csize){
       if(csize == 1) return st[sti];
6
       return st[sti] = fst(build(sti*2+1,csize/2),build(sti*2+2,csize/2));
8
   void innit(){
9
       for(int i = 0; i<stsize; i++) st[i] = neut;</pre>
10
       /*int d = 0;
11
       for(int i = stsize-n; i<stsize && d<n; i++){</pre>
^{12}
           st[i] = arr[d];d++;
13
       }*/
14
       build(0,n);
15
16
   void upd(int ind, long long int val){
17
       ind = stsize-n+ind:
18
       st[ind] = val;ind--;ind/=2;
19
       while(true){
20
           st[ind] = fst(st[ind*2+1],st[ind*2+2]);
21
           ind--;
22
           if(ind<0) break;</pre>
23
           ind/=2;
24
       }
25
26
   long long int rqu(int 1, int r, int sti, int ls, int rs){
27
       if(l<=ls && rs<= r) return st[sti];</pre>
28
       if(r<ls || l>rs) return neut;
29
       int m = (rs+ls)/2;
30
       return fst(rqu(1,r,sti*2+1,ls,m),rqu(1,r,sti*2+2,m+1,rs));
31
32
   long long int query(int 1, int r){
33
       return rqu(1,r,0,0,n-1);
34
35
   //uso, inicializa neut, determina n (asegurate que sea una potencia de
       2), define fst para determinar
37 //la opracion del segment tree
```

## 3 Graphs

#### 3.1 Graph Transversal

#### 3.1.1 BFS

```
#define GS 400040
vector<int> graph[GS];
```

```
3 | bitset <GS> vis:
   //anchura O(V+E)
   void dfs(int curr) {
     queue<int> fringe;
     fringe.push(curr);
     while (fringe.size()) {
       curr = fringe.front(); fringe.pop();
       if (!vis[curr]) {
         vis[curr] = 1;
11
         for (int h : graph[curr]) fringe.push(h);
13
    }
14
15 }
                                 3.1.2 DFS
   #define GS 400040
   vector<int> graph[GS];
   bitset <GS> vis;
   //profundidad O(V+E)
   void dfs(int curr) {
     stack<int> fringe;
     fringe.push(curr);
7
     while (fringe.size()){
8
       curr = fringe.top(); fringe.pop();
9
       if (!vis[curr]) {
10
         vis[curr] = 1;
11
         for (int h : graph[curr]) fringe.push(h);
12
13
    }
14
15 }
                               Topological Sort
   #define GS 400040
  vector<int> graph[GS];
   bitset <GS> vis;
   vector<int> topsort;
   int e,n;
   //profundidad
   //O(N+E)
   //Solo funciona con DAG's, no existe un top sort de un grafo Non-DAG
  void todfs(int pa) {
```

```
for(int h: graph[pa]){if(!vis[h]){todfs(h);}}
11
     topsort.push_back(pa);
12
   }
13
   void topologicalSort(){
14
     vis.reset();
15
     topsort.clear();
16
     for(int i = 0; i<n; i++){if(!vis[i]){dfs(i);}}</pre>
     reverse(topsort.begin(),topsort.end());
  |}
19
```

#### 4 Math

#### 4.1 Identities

$$C_n = \frac{2(2n-1)}{n+1}C_{n-1}$$

$$C_n = \frac{1}{n+1}\binom{2n}{n}$$

$$C_n \sim \frac{4^n}{n^{3/2}\sqrt{\pi}}$$

$$\sigma(n) = O(\log(\log(n))) \text{ (number of divisors of } n)$$

$$F_{2n+1} = F_n^2 + F_{n+1}^2$$

$$F_{2n} = F_{n+1}^2 - F_{n-1}^2$$

$$\sum_{i=1}^n F_i = F_{n+2} - 1$$

$$F_{n+i}F_{n+j} - F_nF_{n+i+j} = (-1)^n F_i F_j$$
(Möbius Inv. Formula) Let  $g(n) = \sum_{d|n} f(d)$ , then  $f(n) = \sum_{d} d \mid ng(d)\mu\left(\frac{n}{d}\right)$ ).

#### 4.2 Binary Exponentiation and modArith

```
long long int inf = 10000000007;
   //suma (a+b)%m
   //resta ((a-b)\m+m)\m
   //mult (a*b)%m
   long long binpow(long long b, long long e) {
       long long res = 1; b%=inf;
       while (e > 0) {
           if (e \& 1) res = (res * b)\%inf;
           b = (b * b)\%inf:
9
           e >>= 1;
10
       }
11
       return res:
12
13 }
```

#### 4.3 Modular Inverse (dividir mod)

```
long long int inf = 10000000007;
```

```
2 long long int gcd(long long int a, long long int b, long long int& x,
       long long int& y) {
      x = 1, y = 0;
      long long int x1 = 0, y1 = 1, a1 = a, b1 = b;
       while (b1) {
           long long int q = a1 / b1;
           tie(x, x1) = make_tuple(x1, x - q * x1);
          tie(y, y1) = make_tuple(y1, y - q * y1);
          tie(a1, b1) = make_tuple(b1, a1 - q * b1);
10
      return a1;
11
12
  long long int modinverse(long long int b, long long int m){
       long long int x,y;
      long long int d = extEuclid(b,inf,x,y);
      if(d!=1) return -1;
      return ((x%inf)+inf)%inf;
17
18 }
```

#### 4.4 Modular Binomial Coeficient and Permutations

```
long long int inf = 10000000007;
   //cat[n] = bincoef(2*n,n)/(n+1), cat[0] = 1
   class binCoef{
       long long int lim;
5
       long long int* fact;
   public:
6
       binCoef(long long int 1){
           lim = 1; fact = new long long int[l+1];fact[0]= 1;
           for(long long int i = 1; i<=1; i++) fact[i] = (fact[i-1]*i)%inf;</pre>
9
10
       //perm = (fact[n] * modinverse(fac[n-k],inf)%inf;
11
       long long int query(long long int n, long long int k){
           if(n<k) return 0;
13
           return (fact[n] * modinverse((fac[n-k]*fact[k])%inf,inf))%inf;
14
       }
15
<sub>16</sub> };
```

#### 4.5 Non-Mod Binomial Coeficient and Permutations

```
//Solo usar con n<=20
//cat[n] = bincoef(2*n,n)/(n+1), cat[0] = 1
unsigned long long int bincoef(unsigned long long int n, unsigned long long int k){</pre>
```

```
if(n<k) return 0:
4
       unsigned long long int num = 1, den= 1;
5
       for(unsigned long long int i = (n-k)+1; i<=n; i++) num*=i;</pre>
6
       for(unsigned long long int i = 2; i<=k; i++) den*=i;
       //perm = return num;
8
       return num/den;
9
10 }
                        Modular Catalan Numbers
  long long int inf = 10000000007;
   class catalan{
       long long int* cat; long long int lim
   public:
4
       catalan(long long int 1){
5
           \lim = 1; cat = new long long int[1+10]; cat[0] = 1;
6
           for(long long int i = 0; i <= 1; i++) cat[i+1] = ((((4LL*i+2)%inf)))
7
                *cat[i])%inf) *modinverse(n+2))%inf;
8
       long long int query(long long int n){ return cat[n];}
9
10 | };
                         4.7 Ceil Fraccionario
1 long long int techo(long long int num, long long int den){ return (num+
       den-1)/den;}
                      4.8 Sieve Of Eratosthenes
   #define MAXN 10e6
   class soe{
   public:
3
       bitset<MAXN> isPrime;
4
       soe(){
5
           for(int i = 3; i<MAXN; i++) isPrime[i] = (i%2);</pre>
6
           isPrime[2] = 1;
7
           for(int i = 3; i*i<MAXN; i+=2)</pre>
8
               if(isPrime[i])
9
                   for(int j = i*i; j<MAXN; j+=i)</pre>
10
                       isPrime[j] = 0;
11
12
13 };
                          Sieve-based Factorization
```

```
#define MAXN 10e6
   class soef
   public:
3
       int smolf[MAXN];
       soe(){
5
           for(int i = 2; i < MAXN; i++) smolf[i] = (i \% 2 = = 0.72 : i);
6
           for(int i = 3; i*i<MAXN; i+=2)</pre>
                if(smolf[i]==i)
                    for(int j = i*i; j<MAXN; j+=i)</pre>
                        smolf[j] = min(smolf[j],smolf[i]);
11
       }
12
13 | };
                        4.10 Berlekamp Massey
typedef long long int 11;
   //Obtiene recurrencia lineal dados los primeros elementos en O(n^2)
   vector<ll> berlekampMassey(const vector<ll> &s) {
       vector<ll> c;
       vector<ll> oldC;
       int f = -1;
6
       for (int i=0; i<(int)s.size(); i++) {</pre>
           ll delta = s[i]:
8
           for (int j=1; j<=(int)c.size(); j++) delta -= c[j-1] * s[i-j];
           if (delta == 0) continue:
10
           if (f == -1) {
11
                c.resize(i + 1);
12
                mt19937 rng(chrono::steady_clock::now().time_since_epoch().
13
                    count());
                for (ll &x : c) x = rng();
14
                f = i;
15
           } else {
16
                vector<ll> d = oldC;
17
                for (11 &x : d) x = -x;
18
                d.insert(d.begin(), 1);
19
                11 df1 = 0;
20
                for (int j=1; j <= (int)d.size(); j++) df1 += d[j-1] * s[f+1-j]
21
                    ];
                assert(df1 != 0);
22
                11 coef = delta / df1:
23
                for (ll &x : d) x *= coef;
24
```

vector<ll> zeros(i - f - 1);

25

```
zeros.insert(zeros.end(), d.begin(), d.end());
26
                d = zeros;
27
                vector<ll> temp = c;
28
                c.resize(max(c.size(), d.size()));
29
                for (int j=0; j<(int)d.size(); j++) c[j] += d[j];</pre>
30
                if (i - (int) temp.size() > f - (int) oldC.size()) {oldC =
31
                    temp;f = i;
           }
32
       }
33
       return c;
34
35 | }
```

#### 4.11 Modular Berlekamp Massey

```
typedef long long int 11;
  long long int inf = 1000000007;
   vector<ll> bermas(vector<ll> x){
       vector<ll> ls,cur;
4
       int lf,ld;
5
       for(int i = 0; i<x.size(); i++){</pre>
6
            long long int t = 0;
7
           for(int j = 0; j < cur.size(); j++) t=(t+x[i-j-1]*(long long int)
8
                cur[j])%inf;
            if((t-x[i])%inf==0)continue;
9
           if(cur.size()==0){cur.resize(i+1);lf=i;ld=(t-x[i])%inf;continue
10
            long long int k = (x[i]-t)*powermod(ld,inf-2)%inf;
11
            vector<ll>c(i-lf-1);c.push_back(k);
12
           for(int j = 0; j<ls.size(); j++) c.push_back(-ls[j]*k%inf);</pre>
13
           if(c.size()<cur.size()) c.resize(cur.size());</pre>
14
           for(int j = 0; j<cur.size(); j++) c[j]=(c[j]+cur[j])%inf;</pre>
15
            if(i-lf+ls.size()>=cur.size())ls=cur,lf=i,ld=(t-x[i])%inf;
16
                cur=c:
17
18
       for(int i =0; i < cur.size(); i++) cur[i] = (cur[i] % inf + inf) % inf;</pre>
19
     return cur;
20
  |}
21
```

# 5 Geometry

# 6 Strings

#### 6.1 Explode by token

```
//#include <sstream>

vector<string> explode(string const& s, char delim) {
 vector<string> result;
 istringstream iss(s);
 for (string token; getline(iss, token, delim); )
 {
 result.push_back(move(token));
 }
 return result;
}
```

#### 6.2 Multiple Hashings DS

```
1 struct multhash{
       unsigned long long int h1,h2,h3;
       unsigned long long int alf[257];
       bool operator < (multhash b) const { // override less than operator
       if (h1 != b.h1) return h1 < other.h1;</pre>
5
       if (h2 != b.h2) return h2 < other.h2;</pre>
6
       return h3 < b.h3;
7
8
     bool operator == (multhash b) const { // override equal operator
9
       return (h1== b.h1 && h2== b.h2 && h3== b.h3)
10
11
   public:
12
13
       string s;
       multhash(){
14
           h1 = 0; h2 = 0; h3 = 0; s = "";
15
           for(char l = 'a'; l <= 'z'; l++) alf[l] = l-'a'+1;
16
       }
17
       void innit(){
18
           unsigned long long int inf,p,op;
19
20
           inf = 666666555557777777;
21
22
           p = 47; op = 47;
           for(char 1: s){
23
```

```
h1+=(p*alf[1])%inf;
24
               p*=op;
^{25}
               p%=inf;
26
27
28
           inf = 986143414027351997;
29
           p = 53; op = 53;
30
           for(char 1: s){
31
               h2+=(p*alf[1])%inf;
32
               p*=op;
33
               p%=inf;
34
           }
35
36
           inf = 909090909090909091:
37
           p = 79; op = 79;
38
           for(char 1: s){
39
               h3+=(p*alf[1])%inf;
40
               p*=op;
41
               p%=inf;
42
43
       }
44
45
    //VALORES POSIBLES DE INF, MIENTRAS MAS CERCANOS A 10^17 MEJOR
    //666666555557777777
   //986143414027351997
   //974383618913296759
   //973006384792642181
   //953947941937929919
   //909090909090909091
   //VALORES PARA P, USAR PRIMOS MAYORES A |Alfabeto|
  //31,47,53,61,79
                     6.3 Permute chars of string
   void permute(string str){
     // Sort the string in lexicographically
2
     // ascennding order
3
     sort(str.begin(), str.end());
5
     // Keep printing next permutation while there
     // is next permutation
```

7

9

do {

cout<<str<<endl;</pre>

```
} while (next_permutation(str.begin(), str.end()));
11 }
                  6.4 Longest common subsequence
1 //O(|te|*|pa|)
   //cambiar score para otros problemas, str all match = +2, miss/ins/del =
   //usar char que no este en el alfabeto para denotar del/ins
   string te,pa;
   long long int ninf = -10e13;
   long long int score(char a, char b){
       if(a=='*' || b=='*') return 0;
       if(a==b) return 1;
       return ninf;
9
   }
10
   long long int lcs(){
       long long int** dp;te = "*"+te; pa = "*"+pa;
12
       long long int res = 0;
13
14
       dp = new long long int*[te.size()];
15
       for(int i = 0; i<te.size(); i++) dp[i] = new long long int[pa.size()</pre>
16
           ]();
17
       for(int r = 1; r < te.size(); r + + ){
18
           for(int c = 1; c<pa.size(); c++){</pre>
19
               dp[r][c] = dp[r-1][c-1]+score(te[r],pa[c]);
20
               dp[r][c] = max(dp[r][c-1]+score(te[r],'*'),dp[r][c]);
21
               dp[r][c] = max(dp[r-1][c]+score('*',pa[c]),dp[r][c]);
22
23
       }
24
25
       return dp[te.size()-1][pa.size()-1];
27 }
                                 6.5
                                      KMP
string T,P;
2 | int bt[MAXN]:
   //O(|Text|+|Pattern|)
4 void KMPpre(){
       int i = 0, j = 0; bt[0] = -1;
5
       while(i<P.size()){</pre>
6
7
           while(j \ge 0 \&\& P[i]!=P[(j \ge 0?i:0)]) j = bt[j];
```

```
i++; j++; bt[i] = j;
       }
9
   }
10
   int kmp(){
11
        int res =0, i = 0, j = 0;
12
        while(i<T.size()){</pre>
13
            while(j \ge 0 \&\& T[i] != P[(j \ge 0?j:0)]) j = bt[j];
14
            i++; j++;
15
            if(j==P.size()){//match, do anything
16
                 res++; j = bt[j];
17
18
       }
19
       return res;
20
21 | }
```

#### 7 Flow

#### 8 Miscellaneous

#### 8.1 Bit Manipulation

```
#include "bits/stdc++.h"
   using namespace std;
   #define endl '\n'
5
   int main() {
6
     ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
7
     //Se representan bitmasks de 30 a 62 bits
8
     //usando signed int y signed long long int
9
     //para evitar problemas con el complemento de dos
10
     signed int a, b;
11
     //para multiplicar un numero por dos solo es necesario aplicar un
12
     // shifteo de sus bits a la izquierda
13
     a = 1;
14
     a = a << 3;
15
     cout << a << endl;</pre>
16
     //para dividir un numero entre dos es necesario aplicar un
17
     //shifteo a la derecha
18
     a = 32:
19
     a = a >> 3;
20
     cout << a << endl;</pre>
21
     //para encender el bit n de a, solo hay que igualar a = a | pow(2,n-1)
22
```

```
//prende el tercer bit
     a = 1;
24
     b = 1 << 2;
25
     a = a \mid b;
     cout << a << endl;</pre>
     //para apagar el bit n de a, solo hay que a &= \text{pow}(2,n-1)
     //prende el tercer bit
29
     a = 5;
     b = 1 << 2;
     a &= ~b;
     cout << a << endl;</pre>
33
     //para revisar si el bit n de a esta encendido
34
     //revisa si el tercer bit esta encendido
35
     a = 5:
     b = 1 << 2;
     a = a \& b;
     cout << (a?"SI":"NO") << endl;</pre>
     //para volter el bit n de a, solo hay que igualar a = a \cdot pow(2,n-1)
     //apaga el tercer bit
41
     a = 5;
     b = 1 << 2;
     a = a \hat{b};
     cout << a << endl;</pre>
45
     //para obtener el bit menos significativo que esta encendido a& -a
46
     a = 12;
47
     cout << \log_2(a \& ((-1) * a))+1 << \text{endl};
    //para prender todos los bits hasta n
49
     a = (1 << 4) - 1;
50
     cout << a << endl;</pre>
51
   }
52
         -----EOSOLUTION-----
#include "bits/stdc++.h"
   using namespace std;
   #define endl '\n'
   #pragma GCC optimize("03")
   #pragma GCC target("popcnt")
   //no usar con visual c++
   //solo con g++ like compilers
   int main() {
     ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
     signed long long int a, b, n;
```

```
//{\tt Obtain} the remainder (modulo) of a when it is divided by n (n is a
12
          power of 2)
     a = 15; n = 8-1;
13
     a &= n;
14
     cout << a_n, a_n = 15, n_n = 2^3 << endl;
     cout << a << endl;</pre>
     //Apaga el bit menos significativo de a
     a = 14;
18
     b = (a & ((-1) * a));
19
     a &= ~b;
20
     cout << a << endl;</pre>
21
     //enciende el ultimo cero de a
22
     a = 9;
23
     b = a;
24
     b = (b & ((-1) * b));
     a = a \mid b;
26
     cout << a<<endl;</pre>
27
     //contar bits encendidos en a
28
     cout << __builtin_popcount(a)<<endl;</pre>
29
     //checar la paridad de a
30
     cout << (__builtin_parity(a) ? "IMPAR" : "PAR") << endl;</pre>
31
     //contar leading zeroes en a
32
     cout << __builtin_clz(a)<<endl;</pre>
33
     //contar 9, trailling zeroes en a
34
     cout << __builtin_ctz(a)<<endl;</pre>
35
36
                  -----EOSOLUTION--
37
```

9 Testing