## First to Penalty

# -12

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## 1 Template

```
#include "bits/stdc++.h"
  //assert(x>0) si falla da RTE
  using namespace std;
  #define endl '\n'
  #define DBG(x) cerr<<\#x<< "=" << (x) << endl:
  #define RAYA cerr<<"========"<<endl:
  #define RAYAS cerr<<"...."<<endl;</pre>
  //#define DBG(x) :
   //#define RAYA ;
  //#define RAYAS ;
11
   //----SOLBEGIN-----
  int main() {
    ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
14
    int tC;
15
16
    cin >> tC;
17
    while (tC--) {
18
19
    }
20
21
^{22}
         -----EOSOLUTION-----
```

## 2 Data structures

## 2.1 Simplified DSU (Stolen from GGDem)

```
int uf[MAXN];
void uf_init(){memset(uf,-1,sizeof(uf));}
int uf_find(int x){return uf[x]<0?x:uf[x]=uf_find(uf[x]);}
bool uf_join(int x, int y){
    x=uf_find(x);y=uf_find(y);
    if(x==y)return false;
    if(uf[x]>uf[y])swap(x,y);
    uf[x]+=uf[y];uf[y]=x;
    return true;
}
```

## 2.2 Disjoint Set Union

```
class disjSet {
     int* sz;
     int* par;
   public:
     int len;
     disjSet(int tam){
           sz = new int[tam + 4]();
           par = new int[tam + 4]();
           len = 0;
           for(int i = 0; i<=tam; i++){</pre>
               par[i] = i;
11
                sz[i] = 1;
12
               len++;
13
           }
       }
15
     int finds(int el){
16
           if (el == par[el]) return el;
17
           return par[el] = finds(par[el]);
18
       }
19
     void unions(int a, int b){
20
           a = finds(a);
21
         b = finds(b);
22
           if (a == b) return;
23
           len--;
24
           //se hace que el gde sea padre del pequeno
25
           if (sz[a] > sz[b]) swap(a,b);
           par[a] = b;
27
           sz[b] += sz[a];
28
       }
29
      ~disjSet(){
30
           delete[] size;
31
           size = nullptr;
32
           delete[] parent;
33
           parent = nullptr;
34
35
36 };
                                 Segment tree
```

```
//MAXN = 2^k, n = tam arreglo inicial
#define MAXN 262160
int stsize; long long int neut;int n;
long long int* st = new long long int[2*MAXN-1]();
```

```
5 long long int fst(long long int a, long long int b);
                                                                                   5 long long int* st = new long long int[2*MAXN-1]();
  long long int build(int sti,int csize){
                                                                                   6 long long int* pendientes = new long long int[2*MAXN-1]();
                                                                                     long long int fst(long long int a, long long int b){return a+b;}
       if(csize == 1) return st[sti];
       return st[sti] = fst(build(sti*2+1,csize/2),build(sti*2+2,csize/2));
                                                                                      long long int build(int sti,int csize){
8
   }
                                                                                          if(csize == 1) return st[sti];
9
                                                                                   9
                                                                                          return st[sti] = fst(build(sti*2+1,csize/2),build(sti*2+2,csize/2));
   void innit(){
                                                                                   10
       for(int i = 0; i<stsize; i++) st[i] = neut;</pre>
                                                                                      }
                                                                                   11
11
       /*int d = 0:
                                                                                      bool hasChildren(int sti){sti*=2;sti++;sti++;return sti<stsize;}</pre>
12
       for(int i = stsize-n; i<stsize && d<n; i++){</pre>
                                                                                      void innit(){
13
           st[i] = arr[d];d++;
                                                                                          for(int i = 0; i<stsize; i++) st[i] = neut;</pre>
14
                                                                                          int d = 0:
15
                                                                                  15
                                                                                          for(int i = stsize-n; i<stsize && d<n; i++) {st[i] = arr[d];d++;}</pre>
       build(0,n);
16
                                                                                   16
                                                                                          build(0.n):
17
                                                                                   17
   void upd(int ind, long long int val){
                                                                                      }
                                                                                   18
       ind = stsize-n+ind:
                                                                                      void updrec(int 1,int r, int s1, int sr,int sti, long long int val){
                                                                                   19
19
       st[ind] = val;ind--;ind/=2;
                                                                                          if(sr<l | r< sl) return:
20
                                                                                  20
       while(true){
                                                                                          if(l<= sl && sr <=r){
21
                                                                                  21
           st[ind] = fst(st[ind*2+1],st[ind*2+2]);
                                                                                              st[sti] += val*(sr-sl+1);
22
                                                                                              if(hasChildren(sti)){pendientes[sti*2+1]+=val;pendientes[sti
           ind--:
                                                                                  23
23
           if(ind<0) break;
                                                                                                  *2+2]+=val;}
24
           ind/=2;
                                                                                              return;
                                                                                  24
25
       }
                                                                                          }
26
                                                                                   25
                                                                                  26
27
                                                                                          int sm = (sl+sr)/2;
   long long int rqu(int 1, int r, int sti, int ls, int rs){
                                                                                  27
28
                                                                                          updrec(l,r,sl,sm,sti*2+1,val);
       if(l<=ls && rs<= r) return st[sti];</pre>
                                                                                  28
29
       if(r<ls || l>rs) return neut;
                                                                                          updrec(l,r,sm+1,sr,sti*2+2,val);
                                                                                  29
30
                                                                                          st[sti] = fst(st[sti*2+1],st[sti*2+2]);
       int m = (rs+ls)/2;
                                                                                   30
31
       return fst(rqu(1,r,sti*2+1,ls,m),rqu(1,r,sti*2+2,m+1,rs));
                                                                                   31
32
                                                                                      void upd(int 1, int r, long long int val){updrec(1,r,0,n-1,0,val);}
33
   long long int query(int 1, int r){
       return rqu(1,r,0,0,n-1);
                                                                                      long long int rqu(int 1, int r, int sti, int ls, int rs){
35
                                                                                          if(r<ls || l>rs) return neut;
                                                                                  35
36
   //uso, inicializa neut, n = primera potencia de 2 >= n del problema,
                                                                                          if(1<=1s && rs<= r){
                                                                                  36
                                                                                              return st[sti]+pendientes[sti]*(rs-ls+1);
       stsize = 2*n-1
                                                                                  37
   //llena arr de neutros hasta que su tam sea el nuevo n
                                                                                          }
                                                                                  38
39 //DEFINE LA FUNCION fst
                                                                                   39
                                                                                          st[sti] += pendientes[sti]*(rs-ls+1);
                                                                                   40
                        2.4 Segment tree Lazy
                                                                                          if(hasChildren(sti)){pendientes[sti*2+1]+=pendientes[sti];pendientes
                                                                                  41
                                                                                              [sti*2+2]+=pendientes[sti];}
                                                                                          pendientes[sti] = 0;
1 //MAXN = 2^k, n = tam arreglo inicial
                                                                                  42
  #define MAXN 262160
                                                                                  43
                                                                                          int m = (rs+ls)/2;
                                                                                  44
  vector<int> arr;
                                                                                          return fst(rqu(1,r,sti*2+1,ls,m),rqu(1,r,sti*2+2,m+1,rs));
4 | int stsize; long long int neut; int n;
                                                                                  45
```

```
d6   }
long long int query(int 1, int r){
    return rqu(1,r,0,0,n-1);
49   }
50   //uso, inicializa neut, n = primera potencia de 2 >= n del problema,
        stsize = 2*n-1
51   //llena arr de neutros hasta que su tam sea el nuevo n
52   //DEFINE LA FUNCION fst
```

#### 2.5 Trie

```
struct triver {
       char alphabet;
2
       bool ter;
3
       vector<triver*> child;
4
       triver(char a): alphabet(a) { child.assign(26, NULL); ter = false; }
5
6
   class trie{
   private:
       triver* root;
   public:
10
       trie() { root = new triver('!');}
11
       void insert(string s){
12
           triver* curr = root;
13
           for(char 1: s){
14
                if(curr->child[1-'A'] == NULL) curr->child[1-'A'] = new
15
                    triver(1);
                curr = curr->child[l-'A'];
16
           }
17
            curr->ter = true;
18
       }
19
       bool search(string s){
20
           triver* curr = root;
^{21}
           for(char 1: s){
^{22}
                if(curr == NULL) break;
23
                curr = curr->child[1-'A'];
24
25
           if(curr == NULL) return false;
26
           return curr->ter;
27
28
29 | };
```

## 3 Graphs

## 3.1 Graph Transversal

#### 3.1.1 BFS

```
#define GS 400040
  vector<int> graph[GS];
   bitset <GS> vis;
   //anchura O(V+E)
   void dfs(int curr) {
     queue<int> fringe;
     fringe.push(curr);
     while (fringe.size()) {
       curr = fringe.front(); fringe.pop();
       if (!vis[curr]) {
10
         vis[curr] = 1:
         for (int h : graph[curr]) fringe.push(h);
12
13
    }
14
15 }
                                 3.1.2 DFS
  #define GS 400040
```

```
vector<int> graph[GS];
   bitset <GS> vis;
   //profundidad O(V+E)
   void dfs(int curr) {
     stack<int> fringe;
     fringe.push(curr);
     while (fringe.size()){
       curr = fringe.top(); fringe.pop();
       if (!vis[curr]) {
         vis[curr] = 1;
11
         for (int h : graph[curr]) fringe.push(h);
12
13
     }
14
15 }
```

## 3.2 Topological Sort

```
#define GS 400040
vector<int> graph[GS];
```

//para reconstruir el camino solo basta con guardar intermedio como

el padre de ini si el cambio se hizo, -1 otherwise

for(int intermedio = 0; intermedio<=tam; intermedio++)</pre>

for(int ini = 0; ini<=tam; ini++)</pre>

18

19

20

```
3 | bitset <GS> vis;
                                                                                                  for(int fin = 0; fin<=tam; fin++)</pre>
                                                                                  21
                                                                                                       dist[ini][fin] = min(dist[ini][fin],dist[ini][intermedio
   vector<int> topsort;
                                                                                   22
                                                                                                           ]+dist[intermedio][fin]);
   int e,n;
   //profundidad
                                                                                   23 }
   //O(N+E)
                                                                                                                    3.4 SSSP
   //Solo funciona con DAG's, no existe un top sort de un grafo Non-DAG
   void todfs(int pa) {
                                                                                                               3.4.1 Lazy Dijkstra
     vis[pa]=1;
10
     for(int h: graph[pa]){if(!vis[h]){todfs(h);}}
                                                                                   1 #define GS 1000
11
     topsort.push_back(pa);
                                                                                      #define INF 100000000
12
13
                                                                                      //destino, costo
   void topologicalSort(){
                                                                                      vector<pair<int,int>> graph[GS];
     vis.reset():
                                                                                      int dist[GS];
15
     topsort.clear();
                                                                                      void dijkstra(int origen,int tam){
     for(int i = 0; i<n; i++){if(!vis[i]){dfs(i);}}</pre>
                                                                                          for(int i = 0; i<=tam; i++){</pre>
     reverse(topsort.begin(),topsort.end());
                                                                                              dist[i] = INF;
                                                                                   8
19 }
                                                                                   9
                                                                                          priority_queue<pair<int,int>,vector<pair<int,int>>, greater<pair<int</pre>
                                                                                   10
                      3.3 APSP: Floyd Warshall
                                                                                               ,int>>> pq;
                                                                                          pair<int,int> curr;
                                                                                   11
  #define GS 1000
                                                                                   12
   #define INF 100000000
                                                                                          pq.push(make_pair(0,origen));
                                                                                   13
   //destino, costo
                                                                                   14
   int graph[GS][GS];
                                                                                          while(pq.size()){
                                                                                   15
                                                                                              curr = pq.top();pq.pop();
   //All Pairs Dist
                                                                                   16
   int dist[GS][GS]:
                                                                                              if(curr.first >= dist[curr.second]) continue:
                                                                                   17
  //Toma en cuenta nodos [0-tam] inclusivo, modificar de acuerdo a las
                                                                                   18
       necesidades
                                                                                              dist[curr.second] = curr.first;
                                                                                   19
                                                                                              for(pair<int,int> h: graph[curr.second]){
  //Ten cuidado con el valor que le pones a INF, puede provocar overflows
                                                                                   20
                                                                                                  if((h.second+curr.first)<dist[h.first]) pq.push({h.second+</pre>
       o puede no ser lo suficientemente grande.
                                                                                  21
   void Floyd_Warshall(int tam){
                                                                                                       curr.first,h.first});
       for(int i = 0; i<=tam; i++)</pre>
                                                                                              }
10
                                                                                  22
           for(int f = 0; f<=tam; f++)</pre>
                                                                                   23
11
               dist[i][f] = INF;
                                                                                      }
                                                                                   24
12
                                                                                      //Esta es la implementacion huevona
13
       for(int i = 0; i<=tam; i++)
                                                                                      //Resuelve Single Source Shortest Paths con aristas positivas
14
           for(int f = 0; f < = tam; f + +)
                                                                                      //Como es la lazy implementation, si funciona con edges negativos
15
               dist[i][f] = graph[i][f];
                                                                                          siempre y cuando no hayan ciclos negativos
16
                                                                                  28 //Si hay ciclos negativos se va atascar en un ciclo infinito
17
```

29 //Si no los hay puede que funcione en O((V+E)log(V)) o puede que se

3.4.2 Bellman-Ford

exponencial, si no jala prueba BellmanFord

```
1 //esta es la implementacion huevona
   #define GS 1000
2
   //cuidado con overflows!!
   #define INF 100000000
   #define NINF -10000000
   //destino, costo
   vector<pair<int,int>> graph[GS];
   int dist[GS];
   struct edge{
       int from, to, cost;
10
   };
11
   //Corre en O(VE)
   void bellmanFord(int origen,int tam){
       for(int i = 0; i<=tam; i++){</pre>
14
           dist[i] = INF;
15
       }
16
       dist[origen] = 0;
17
       edge aux;
18
       vector<edge> aristas;
19
       bool optimal;
20
21
       for(int i = 0; i<=tam; i++){</pre>
22
           for(pair<int,int> h: graph[i]){
23
                aux.from = i; aux.to = h.first;aux.cost = h.second;
24
                aristas.push_back(aux);
25
26
       }
27
28
       //Si se relajan todos las aristas V-1 veces en un orden arbitrario
29
       //Se asegura que la distancia optima para cada vertice sera
30
           alcanzada
       for(int i = 0; i<tam && !optimal; i++){</pre>
31
           optimal = true;
32
           for(edge elem: aristas){
33
                if(dist[elem.from] + elem.cost < dist[elem.to]){</pre>
34
                    dist[elem.to] = dist[elem.from] + elem.cost;
35
                    //si algun vertice fue actualizado significa que puede
36
                    //las distancias aun no sean optimas
37
                    optimal = false;
38
39
           }
40
41
```

```
42
       //Se corre de nuevo para asegurar encontrar todos los ciclos
43
            negativos
       for(int i = 0; i<tam && !optimal; i++){</pre>
44
            optimal = true;
45
            for(edge elem: aristas){
46
                if(dist[elem.from] + elem.cost < dist[elem.to]){</pre>
47
                    //Si aun despues de correr V-1 veces se puede actualizar
48
                    //Significa que esta en un ciclo negativo
49
                    dist[elem.to] = NINF;
                    //si algun vertice fue actualizado significa que puede
51
                    //las distancias aun no sean optimas
52
                    optimal = false;
53
                }
54
            }
55
       }
56
57
58 }
```

## 3.5 Strongly Connected Components: Kosaraju

```
1 #define GS 2010
   vector<int> graph[GS];
   vector<int> graphI[GS];
   vector<int> orden;
   bitset<GS> vis;
6
   void invertirGrafo(int n){
       for(int p = 1; p <= n; p++)
8
           for(int h: graph[p])graphI[h].push_back(p);
9
10
   void obtOrd(int p,int n){
11
       vis[p] = 1;
12
       for(int h: graph[p]){
13
           if(!vis[h] && h<=n) obtOrd(h,n);</pre>
14
15
       orden.push_back(p);
16
   }
17
   int findSCC(int n){
18
       int res = 0;
19
       invertirGrafo(n);
20
       orden.clear();
21
```

```
for(int i = 1; i<=n; i++) vis[i] =0;
22
       for(int i = 1; i<=n; i++) if(!vis[i]) obtOrd(i,n);</pre>
23
       reverse(orden.begin(),orden.end());
^{24}
       //cuenta los connected components
25
       //vector<int> lscc;
26
       stack<int> fringe;
27
       int curr;
28
       for(int i = 1; i<=n; i++) vis[i] =0;</pre>
29
       for(int i: orden){
30
           //lscc.clear();
31
           if(!vis[i]){
32
                fringe.push(i);
33
                while (fringe.size()){
34
                    curr = fringe.top();fringe.pop();
35
                    //lscc.push_back(curr);
36
                    if (!vis[curr]) {
37
                        vis[curr] = 1:
38
                        for (int h : graphI[curr]) fringe.push(h);
39
                    }
40
                }
41
                res++;
42
43
           //hacer lo que sea con lcss
44
       }
45
       return res;
46
47
48
    //OJO esto solo jala con directed graphs
   //por definicion todas las undirected graphs tienen un solo SCC
   //NOTAR QUE LOS GRAFOS QUE USA CUMPLEN CON: O<=VERTICE<=n
```

## 3.6 Articulation Points and Bridges: ModTarjan

```
#define GS 50
vector<int> graph[GS];
bitset<GS> vis, isArtic;
vector<int> padre;
//id por tiempo, menor id accesible
//ya sea por descendientes o por back edges
vector<int> tId, lId;
//cantidad de hijos que tiene en el bfs spanning tree
int rootChildren;
int cnt;
```

```
int dfsRoot;
   void findAP_B(int p){
       cnt++;vis[p] = 1;tId[p] = cnt;lId[p] = tId[p];
13
14
       for(int hijo: graph[p]){
15
           if(!vis[hijo]){
16
                padre[hijo] = p;
17
                if(p == dfsRoot) rootChildren++;
18
19
                findAP_B(hijo);
20
21
                //esto significa que ni por un back edge el hijo accede al
22
                    padre
                //por lo que si el padre fuese eliminado el hijo quedaria
23
                    aislado
                if(lId[hijo] >= tId[p]) isArtic[p] = 1;
24
                if(lId[hijo] > tId[p]){
25
                    //esto significa que si se eliminase el camino de padre
26
                        ->hiio
                    //se lograria desconectar el grafo, aka bridge
27
                }
28
                lId(p) = min(lId(p),lId(hijo));
29
           }else{
30
                //si hay un ciclo indirecto, actualiza el valor para el
31
                if(hijo != padre[p]) lId[p] = min(lId[p],tId[hijo]);
32
33
       }
34
35
    //OJO esto solo jala con Undirected graphs
   /*
37
       MAIN
38
       for(int i = 0; i < n; i++){
39
           if(!vis[i]){
40
                rootChildren = 0;
41
                dfsRoot = i:
42
                findAP_B(i);
43
                //el algoritmo no puede detectar si el nodo que lo origino
44
                //es un articulation point, por lo que queda checar si
45
                //en el spanning tree que genero tiene mas de un solo hijo
46
               isArtic[i] = (rootChildren>1?1:0);
47
48
49
```

```
50 */
```

## 4 Math

#### 4.1 Identities

```
C_n = \frac{2(2n-1)}{n+1}C_{n-1} C_n = \frac{1}{n+1}\binom{2n}{n} C_n \sim \frac{4^n}{n^{3/2}\sqrt{\pi}} \sigma(n) = O(\log(\log(n))) \text{ (number of divisors of } n) F_{2n+1} = F_n^2 + F_{n+1}^2 F_{2n} = F_{n+1}^2 - F_{n-1}^2 \sum_{i=1}^n F_i = F_{n+2} - 1 F_{n+i}F_{n+j} - F_nF_{n+i+j} = (-1)^n F_i F_j (Möbius Inv. Formula) Let g(n) = \sum_{d|n} f(d), then f(n) = \sum_{d} d \mid ng(d)\mu\left(\frac{n}{d}\right)). Permutaciones objetos repetidos P(n,k) = \frac{P(n,k)}{n_1!n_2!\dots} Separadores, Ecuaciones lineares a variables = b \left(\binom{a}{b}\right) = \binom{a+b-1}{b} = \binom{a+b-1}{a-1}
```

## 4.2 Binary Exponentiation and modArith

```
long long int inf = 10000000007;
   //suma (a+b)%m
   //resta ((a-b)\m+m)\m
   //mult (a*b)%m
   long long binpow(long long b, long long e) {
       long long res = 1; b%=inf;
6
       while (e > 0) {
           if (e \& 1) res = (res * b)\%inf;
8
           b = (b * b)\%inf:
9
           e >>= 1:
10
       }
11
       return res;
12
13 }
```

## 4.3 Modular Inverse (dividir mod)

```
long long int q = a1 / b1;
           tie(x, x1) = make_tuple(x1, x - q * x1);
           tie(y, y1) = make_tuple(y1, y - q * y1);
           tie(a1, b1) = make_tuple(b1, a1 - q * b1);
10
       return a1;
11
12
   long long int modinverse(long long int b, long long int m){
       long long int x,y;
14
       long long int d = gcd(b, inf, x, y);
       if(d!=1) return -1;
16
       return ((x%inf)+inf)%inf;
17
18 }
```

### 4.4 Modular Binomial Coeficient and Permutations

```
long long int inf = 10000000007;
  //\text{cat}[n] = \text{bincoef}(2*n,n)/(n+1), \text{cat}[0] = 1
   class binCoef{
4
       long long int lim;
       long long int* fact;
  public:
6
       binCoef(long long int 1){
           lim = 1; fact = new long long int[1+1];fact[0]= 1;
           for(long long int i = 1; i<=1; i++) fact[i] = (fact[i-1]*i)%inf;</pre>
9
10
       //perm = (fact[n] * modinverse(fac[n-k],inf)%inf;
11
       long long int query(long long int n, long long int k){
12
           if(n<k) return 0;
13
           return (fact[n] * modinverse((fac[n-k]*fact[k])%inf,inf))%inf;
14
       }
15
16 };
```

#### 4.5 Non-Mod Binomial Coefficient and Permutations

```
//Solo usar con n<=20
//cat[n] = bincoef(2*n,n)/(n+1), cat[0] = 1
unsigned long long int bincoef(unsigned long long int n, unsigned long long int k){
   if(n<k) return 0;
   unsigned long long int num = 1, den= 1;
   for(unsigned long long int i = (n-k)+1; i<=n; i++) num*=i;
   for(unsigned long long int i = 2; i<=k; i++) den*=i;
//perm = return num;</pre>
```

```
return num/den;
9
10 }
                        Modular Catalan Numbers
  long long int inf = 10000000007;
   class catalan{
       long long int* cat; long long int lim
3
   public:
4
       catalan(long long int 1){
5
           lim = 1; cat = new long long int[l+10];cat[0] = 1;
6
           for(long long int i = 0; i \le 1; i++) cat[i+1] = ((((4LL*i+2)%inf))
7
                *cat[i])%inf) *modinverse(n+2))%inf;
8
       long long int query(long long int n){ return cat[n];}
9
10 | };
                               Ceil Fraccionario
  long long int techo(long long int num, long long int den){ return (num+
       den-1)/den;}
                           Numeros de Fibonacci
   //en caso de ser usados mod un m pequeno
   //recordar que los numeros de fibonacci se repiten por lo menos cada m^2
   //O(n)
3
   unsigned long long int fib(int n){
     unsigned long long int a = 1,b = 1,aux;
5
     if(n \le 2)
6
       return 1;
8
     for(int i = 3; i <= n; i++){
9
       aux = a+b;
10
       a = b;
11
       b = aux;
12
13
     return b;
14
15
  const long long int inf = 1000000007;
```

unordered\_map<long long int,long long int> Fib;

long long int fib(long long int n)

 $//O(\log n) : DD$ 

```
5 | {
       if(n<2) return 1;
6
       if(Fib.find(n) != Fib.end()) return Fib[n];
       Fib[n] = (fib((n+1) / 2)*fib(n/2) + fib((n-1) / 2)*fib((n-2) / 2)) %
            inf;
       return Fib[n];
9
10 }
                             Sieve Of Eratosthenes
1 #define MAXN 10e6
   class soe{
   public:
       bitset<MAXN> isPrime;
4
       soe(){
5
           for(int i = 3; i<MAXN; i++) isPrime[i] = (i\(^2\));</pre>
6
           isPrime[2] = 1;
7
           for(int i = 3; i*i<MAXN; i+=2)</pre>
                if(isPrime[i])
9
                    for(int j = i*i; j<MAXN; j+=i)</pre>
10
                        isPrime[j] = 0;
11
12
13 };
                    4.10 Sieve-based Factorization
1 #define MAXN 10e6
   class soe{
   public:
       int smolf[MAXN];
       soe(){
           for(int i = 2; i<MAXN; i++) smolf[i] = (i\( 2 == 0 ? 2 : i );
7
           for(int i = 3; i*i<MAXN; i+=2)</pre>
8
                if(smolf[i]==i)
                    for(int j = i*i; j<MAXN; j+=i)</pre>
                        smolf[j] = min(smolf[j],smolf[i]);
11
12
13 };
                           4.11 Cycle Finding
void cyclef(long long int sem){
       long long int hare = f(sem),tort=f(sem);hare = f(hare);
```

```
//liebre avanza dos pasos, tortuga solo uno
3
       while(hare!=tort){
4
           tort = f(tort); hare = f(f(hare));
5
       }
6
       //Se detiene en el inicio del ciclo
       tort = sem;
8
       while(hare!=tort){
9
           tort = f(tort); hare = f(hare);
10
       }
11
12
       int len = 1;
13
       tort = f(sem);
14
       while(hare!=tort){
15
           tort=f(tort):
16
           len++;
17
       }
18
19 }
```

## 4.12 Berlekamp Massey

```
typedef long long int 11;
   //Obtiene recurrencia lineal dados los primeros elementos en O(n^2)
   vector<ll> berlekampMassey(const vector<ll> &s) {
       vector<ll> c:
4
       vector<ll> oldC:
5
       int f = -1:
6
       for (int i=0; i<(int)s.size(); i++) {</pre>
7
           ll delta = s[i];
8
           for (int j=1; j<=(int)c.size(); j++) delta -= c[j-1] * s[i-j];</pre>
9
           if (delta == 0) continue;
10
           if (f == -1) {
11
               c.resize(i + 1);
12
               mt19937 rng(chrono::steady_clock::now().time_since_epoch().
13
                    count());
               for (11 &x : c) x = rng();
14
               f = i;
15
           } else {
16
               vector<11> d = oldC:
17
               for (11 &x : d) x = -x;
18
               d.insert(d.begin(), 1);
19
               11 df1 = 0:
20
               for (int j=1; j <= (int)d.size(); j++) df1 += d[j-1] * s[f+1-j]
21
                    ];
```

```
assert(df1 != 0):
22
                ll coef = delta / df1;
23
                for (11 &x : d) x *= coef;
24
                vector<ll> zeros(i - f - 1);
25
                zeros.insert(zeros.end(), d.begin(), d.end());
26
                d = zeros;
27
                vector<ll> temp = c;
28
                c.resize(max(c.size(), d.size()));
29
                for (int j=0; j<(int)d.size(); j++) c[j] += d[j];</pre>
                if (i - (int) temp.size() > f - (int) oldC.size()) {oldC =
31
                    temp;f = i;}
           }
32
       }
33
       return c;
34
35 }
```

### 4.13 Modular Berlekamp Massey

```
typedef long long int 11;
  long long int inf = 1000000007;
   vector<ll> bermas(vector<ll> x){
       vector<ll> ls,cur;
4
       int lf,ld;
5
       for(int i = 0; i<x.size(); i++){</pre>
6
            long long int t = 0;
7
            for(int j = 0; j < cur.size(); j++) t=(t+x[i-j-1]*(long long int)
8
                cur[i])%inf:
           if((t-x[i])%inf==0)continue;
9
           if(cur.size()==0){cur.resize(i+1);lf=i;ld=(t-x[i])%inf;continue
10
                ;}
            long long int k = (x[i]-t)*powermod(ld,inf-2)%inf;
11
           vector<ll>c(i-lf-1);c.push_back(k);
12
           for(int j = 0; j<ls.size(); j++) c.push_back(-ls[j]*k%inf);</pre>
13
           if(c.size()<cur.size()) c.resize(cur.size());</pre>
14
           for(int j = 0; j<cur.size();j++) c[j]=(c[j]+cur[j])%inf;</pre>
15
            if(i-lf+ls.size()>=cur.size())ls=cur,lf=i,ld=(t-x[i])%inf;
16
                cur=c:
17
     }
18
       for(int i =0; i < cur.size(); i++) cur[i] = (cur[i]%inf+inf)%inf;</pre>
     return cur;
21 }
```

## 4.14 Matrix exponentiation

13 bool findAnySol(long long int a, long long int& x, long long int b, long

```
typedef vector<vector<long long int>> Matrix;
                                                                                      long int& y, long long int c) {
   long long int inf = 1000000007;
                                                                                   long long int g = gcd(abs(a), abs(b), x, y);
   Matrix ones(int n) {
                                                                                   if (c % g != 0) return false;
     Matrix r(n,vector<long long int>(n));
                                                                                   x *= c;
    for(int i= 0; i<n; i++){
                                                                                   v *= c;
          r[i][i]=1;
                                                                                   x /= g;
      }
                                                                                   y /= g;
    return r;
                                                                                   d = c / g;
8
                                                                                   if (a < 0) x = -x;
9
   Matrix operator*(Matrix &a, Matrix &b) {
     int n=a.size(),m=b[0].size(),z=a[0].size();
                                                                                   if (b < 0) y = -y;
                                                                              23
     Matrix r(n,vector<long long int>(m));
                                                                                   return true;
12
                                                                              24
     for(int i=0: i<n: i++){
                                                                              25
          for(int j=0; j<m; j++){
                                                                                  //----SOLBEGIN-----
              for(int k=0; k< z; k++){
                                                                                 int main() {
                                                                              27
15
                  r[i][j] += ((a[i][k]\%inf)*(b[k][j]\%inf))\%inf;
                                                                                   ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
16
                  r[i][j]%=inf;}}}
                                                                                   long long int m, a, k, n;
17
                                                                              29
     return r;
                                                                                   long long int f, h,res;
18
                                                                                   //estira en n, y despues cada m
19
                                                                              31
   Matrix be(Matrix b, long long int e) {
                                                                                   //estira en k+a, y despues cada a
     Matrix r=ones(b.size());
                                                                                   cin >> n >> m >> a >> k;
21
     while(e){if(e&1LL)r=r*b;b=b*b;e/=2;}
                                                                                   while (n != 0 \&\& m != 0 \&\& a != 0 \&\& k != 0) {
22
                                                                                     m = -m;
     return r;
                                                                              35
23
                                                                                     if (!findAnySol(m, f, a, h, k + a - n)) {
^{24}
                                                                                       cout << "Impossible" << endl;</pre>
                                                                              37
25
   //Matrix mat(n,vector<long long int>(n));
                                                                                     }else {
                                                                                       res = f * m+n;
                    4.15 Ecuaciones Diofantinas
                                                                                       while (res > 0) res -= m * d;
                                                                                       while (res < 0) res += m * d;
                                                                              41
  long long int gcd(long long int a, long long int b, long long int& x,
                                                                                       cout << res << endl;</pre>
      long long int& y) {
                                                                              43
     x = 1, y = 0;
                                                                                     cin >> n >> m >> a >> k:
     long long int x1 = 0, y1 = 1, a1 = a, b1 = b;
                                                                              45
3
     while (b1) {
                                                                              46
                                                                              47
      int q = a1 / b1;
                                                                              48
      tie(x, x1) = make_tuple(x1, x - q * x1);
6
                                                                              49 //-----EOSOLUTION------
      tie(y, y1) = make_tuple(y1, y - q * y1);
      tie(a1, b1) = make_tuple(b1, a1 - q * b1);
                                                                                                4.16 FFT, Stolen from GGDem
9
    return a1:
                                                                               1 // SPOJ VFMUL - AC
11
                                                                              2 // http://www.spoj.com/problems/VFMUL/
  long long int d;
```

3 #include <bits/stdc++.h>

```
4 | #define fst first
   #define snd second
   #define fore(i,a,b) for(int i=a,ThxDem=b;i<ThxDem;++i)</pre>
   #define pb push_back
   #define ALL(s) s.begin(),s.end()
   #define FIN ios_base::sync_with_stdio(0);cin.tie(0);cout.tie(0)
   #define SZ(s) int(s.size())
   using namespace std;
   typedef long long 11;
   typedef pair<int,int> ii;
   // MAXN must be power of 2 !!
   // MOD-1 needs to be a multiple of MAXN !!
   // big mod and primitive root for NTT:
   const int MOD=998244353,RT=3,MAXN=1<<20;
   typedef vector<int> poly;
   // FFT
20
   struct CD {
     double r.i:
22
     CD(double r=0, double i=0):r(r),i(i){}
23
     double real()const{return r;}
24
     void operator/=(const int c){r/=c, i/=c;}
25
26
   CD operator*(const CD& a, const CD& b){
27
     return CD(a.r*b.r-a.i*b.i,a.r*b.i+a.i*b.r);}
28
   CD operator+(const CD& a, const CD& b){return CD(a.r+b.r,a.i+b.i);}
   CD operator-(const CD& a, const CD& b){return CD(a.r-b.r,a.i-b.i);}
   const double pi=acos(-1.0);
   // NTT
32
   /*
33
   struct CD {
34
     int x;
35
     CD(int x):x(x)
36
     CD(){}
37
     int get()const{return x;}
38
39
   CD operator*(const CD& a, const CD& b){return CD(mulmod(a.x,b.x));}
40
   CD operator+(const CD& a, const CD& b){return CD(addmod(a.x,b.x));}
   CD operator-(const CD& a, const CD& b){return CD(submod(a.x,b.x));}
   vector<int> rts(MAXN+9,-1);
   CD root(int n, bool inv){
44
     int r=rts[n]<0?rts[n]=pm(RT,(MOD-1)/n):rts[n];</pre>
45
    return CD(inv?pm(r,MOD-2):r);
46
```

```
47 }
   */
48
   CD cp1[MAXN+9],cp2[MAXN+9];
49
   int R[MAXN+9];
   void dft(CD* a, int n, bool inv){
     fore(i,0,n)if(R[i]<i)swap(a[R[i]],a[i]);</pre>
     for(int m=2;m<=n;m*=2){
53
       double z=2*pi/m*(inv?-1:1); // FFT
54
       CD wi=CD(cos(z),sin(z)); // FFT
55
       // CD wi=root(m,inv); // NTT
       for(int j=0;j<n;j+=m){
57
         CD w(1);
         for(int k=j,k2=j+m/2;k2<j+m;k++,k2++){
59
           CD u=a[k];CD v=a[k2]*w;a[k]=u+v;a[k2]=u-v;w=w*wi;
60
         }
61
       }
62
     }
63
     if(inv)fore(i,0,n)a[i]/=n; // FFT
     //if(inv){ // NTT
65
     // CD z(pm(n,MOD-2)); // pm: modular exponentiation
     // fore(i,0,n)a[i]=a[i]*z;
67
     //}
68
69
   poly multiply(poly& p1, poly& p2){
     int n=p1.size()+p2.size()+1;
71
     int m=1,cnt=0;
72
     while(m<=n)m+=m,cnt++;</pre>
73
     fore(i,0,m){R[i]=0;fore(j,0,cnt)R[i]=(R[i]<<1)|((i>>j)&1);}
74
     fore(i,0,m)cp1[i]=0,cp2[i]=0;
75
     fore(i,0,p1.size())cp1[i]=p1[i];
76
     fore(i,0,p2.size())cp2[i]=p2[i];
77
     dft(cp1,m,false);dft(cp2,m,false);
78
     fore(i,0,m)cp1[i]=cp1[i]*cp2[i];
79
     dft(cp1,m,true);
80
     poly res;
81
     n-=2:
82
     fore(i,0,n)res.pb((ll)floor(cp1[i].real()+0.5)); // FFT
83
     //fore(i,0,n)res.pb(cp1[i].x); // NTT
84
     return res;
85
86
87
   char s[MAXN],t[MAXN],r[MAXN];
89
```

```
int main(){
      int tn;
91
      scanf("%d", &tn);
92
      while(tn--){
93
        vector<int> a,b,c;
94
        scanf("%s%s",s,t);
95
        for(int i=0;s[i];++i)a.pb(s[i]-'0');reverse(a.begin(),a.end());
96
        for(int i=0;t[i];++i)b.pb(t[i]-'0');reverse(b.begin(),b.end());
97
        c=multiply(a,b);
98
        while(!c.empty()&&!c.back())c.pop_back();
99
        if(c.empty()){puts("0");continue;}
100
        int n=0;
101
        11 x=0:
102
        fore(i,0,c.size()){
103
          x+=c[i]:
104
          r[n++]=x%10;
105
          x/=10;
106
        }
107
        while(x){
108
          r[n++]=x%10;
109
          x/=10;
110
        }
111
        reverse(r,r+n);
112
        bool p=false;
113
        fore(i,0,n){
114
          putchar(r[i]+'0');
115
        }
116
        puts("");
117
      }
118
      return 0;
119
120 }
                                    Geometry
```

## 6 Strings

## 6.1 Explode by token

```
//#include <sstream>
vector<string> explode(string const& s, char delim) {
   vector<string> result;
   istringstream iss(s);
```

```
for (string token; getline(iss, token, delim); )

{
    result.push_back(move(token));
    }

return result;
}
```

## 6.2 Multiple Hashings DS

```
struct multhash{
       unsigned long long int h1,h2;
       unsigned long long int alf[257];
       bool operator < (multhash b) const {</pre>
       if (h1 != b.h1) return h1 < b.h1;
       return h2 < b.h2;
6
7
     bool operator == (multhash b) const { return (h1== b.h1 && h2== b.h2)
     bool operator != (multhash b) const { return ! (h1== b.h1 && h2== b.h2)
          ;}
   public:
       string s;
       multhash(){
           h1 = 0: h2 = 0:s = "":
13
           for(char 1 = 'a'; 1 <= 'z'; 1++) alf[1] = 1-'a'+1;
14
       }
15
       void innit(){
16
           unsigned long long int inf,p,op;
17
18
           inf = 999727999;
19
           p = 325255434; op = 325255434;
20
           for(char 1: s){
21
                h1+=(p*alf[1])%inf;
22
                p*=op;
23
                p\%=inf;
24
           }
25
26
           \inf = 1070777777:
27
           p = 10018302; op = 10018302;
28
           for(char 1: s){
29
                h2+=(p*alf[1])%inf;
30
                p*=op;
31
                p\%=inf;
32
```

14

```
}
                                                                                          dp = new long long int*[te.size()];
33
                                                                                  15
                                                                                         for(int i = 0; i<te.size(); i++) dp[i] = new long long int[pa.size()</pre>
       }
                                                                                  16
34
   };
                                                                                              ]();
35
   //VALORES ALTERNATIVOS DE INF, LOG 17
                                                                                  17
                                                                                          for(int r = 1; r < te.size(); r + + ){
   //666666555557777777
                                                                                  18
                                                                                             for(int c = 1; c<pa.size(); c++){</pre>
   //986143414027351997
                                                                                  19
                                                                                                  dp[r][c] = dp[r-1][c-1]+score(te[r],pa[c]);
   //974383618913296759
                                                                                                  dp[r][c] = max(dp[r][c-1]+score(te[r],'*'),dp[r][c]);
   //973006384792642181
                                                                                  21
   //953947941937929919
                                                                                                  dp[r][c] = max(dp[r-1][c]+score('*',pa[c]),dp[r][c]);
                                                                                  22
   //9090909090909091
                                                                                  23
                                                                                          }
   //VALORES PARA P, USAR PRIMOS MAYORES A |Alfabeto|
                                                                                  24
44 //31,47,53,61,79
                                                                                  25
                                                                                         return dp[te.size()-1][pa.size()-1];
                                                                                  26
                     6.3 Permute chars of string
                                                                                  27 }
                                                                                                                   6.5 KMP
   void permute(string str){
     // Sort the string in lexicographically
     // ascennding order
                                                                                   string T,P;
     sort(str.begin(), str.end());
                                                                                     int bt[MAXN];
4
                                                                                     //O(|Text|+|Pattern|)
5
     // Keep printing next permutation while there
                                                                                     void KMPpre(){
6
     // is next permutation
                                                                                          int i = 0, j = -1; bt[0] = -1;
7
                                                                                   5
     do ſ
                                                                                          while(i<P.size()){</pre>
8
                                                                                   6
       cout<<str<<endl:
                                                                                              while(j \ge 0 \&\& P[i]!=P[(j \ge 0?j:0)]) j = bt[j];
9
     } while (next_permutation(str.begin(), str.end()));
                                                                                              i++; j++; bt[i] = j;
                                                                                   8
                                                                                          }
  |}
11
                                                                                   9
                                                                                     }
                                                                                  10
                 6.4 Longest common subsequence
                                                                                     int kmp(){
                                                                                  11
                                                                                          int res =0, i = 0, j = 0;
                                                                                  12
   //O(|te|*|pa|)
                                                                                          while(i<T.size()){</pre>
                                                                                  13
   //cambiar score para otros problemas, str all match = +2, miss/ins/del =
                                                                                              while(j \ge 0 \&\& T[i] != P[(j \ge 0?j:0)]) j = bt[j];
                                                                                  14
                                                                                              i++; j++;
                                                                                  15
   //usar char que no este en el alfabeto para denotar del/ins
                                                                                              if(j==P.size()){//match, do anything
                                                                                  16
   string te,pa;
                                                                                                  res++; j = bt[j];
                                                                                  17
   long long int ninf = -10e13;
                                                                                              }
                                                                                  18
   long long int score(char a, char b){
                                                                                         }
                                                                                  19
       if(a=='*' || b=='*') return 0;
                                                                                  20
                                                                                         return res;
       if(a==b) return 1;
8
                                                                                  21 }
       return ninf:
9
                                                                                                               6.6 Suffix Array
10
   long long int lcs(){
11
                                                                                   1 //se asume que la longitud de la cadena sera menor a 10**6, modificar el
       long long int** dp;te = "*"+te; pa = "*"+pa;
12
       long long int res = 0;
                                                                                           ub a discrecion
13
```

2 #define ub 1000000LL

```
3 //pot de ub times two
                                                                                               radixSort(arr):
                                                                                    44
   #define ccd 12
                                                                                               sa[0] = arr[0].id; ra[sa[0]] = 0;
                                                                                    45
                                                                                               for(int i = 1; i < n; i++){
                                                                                    46
   //metodos y structs auxiliares para el suffix array
                                                                                                    sa[i] = arr[i].id;
                                                                                                    ra[sa[i]] = ra[sa[i-1]]+1;
   struct sufd{int id;long long int t;};
   int getndigit(long long int num, int d){
                                                                                                    if(arr[i].t == arr[i-1].t) ra[sa[i]]--;
       long long int p = 1; while(d--) p*=10LL;
       num/=p;
                                                                                               if(ra[sa[n-1]]==n-1) break;
                                                                                    51
10
       return (int) num%10LL;
11
                                                                                    52
                                                                                           delete[]ra;
12
   void radixSort(vector<sufd>& arr){
                                                                                       }
13
                                                                                    54
       int count[10]; int n = arr.size();
                                                                                       void makelce(){
14
       vector<sufd> aux(n):
                                                                                           int n = T.size():
15
       for(int d = 0: d < ccd: d++){
                                                                                           int* lce = new int[n+2]():
16
           for(int i = 0; i<10; i++) count[i] = 0;
                                                                                           int* rank = new int[n+2]():
17
           for(int i = 0; i<n; i++) count[getndigit(arr[i].t,d)]++;</pre>
                                                                                           for(int i = 0; i<n; i++) rank[sa[i]] = i;</pre>
18
           for(int i = 1; i<10; i++) count[i]+=count[i-1];</pre>
19
           for(int i = n-1; i>=0; i--){
                                                                                           int curr = 0;
20
               count[getndigit(arr[i].t,d)]--;
                                                                                           for(int i= 0: i<n-1: i++){
21
                                                                                               for(int j = max(curr-1,0); j+max(i,sa[rank[i]-1])<n; j++){</pre>
               aux[count[getndigit(arr[i].t,d)]] = arr[i];
22
                                                                                                    if(T[i+j] == T[sa[rank[i]-1]+j]) curr = j;
23
                                                                                                    if(T[i+j]!=T[sa[rank[i]-1]+j]){curr = j-1; break;}
           for(int i = 0; i<n; i++) arr[i] = aux[i];</pre>
24
       }
                                                                                    66
25
                                                                                               curr++;lce[i] = curr;
                                                                                    67
26
   //El suffix array mismo, agregar caracter menor al alfabeto al final de
                                                                                           }
                                                                                    68
                                                                                    69
                                                                                           int p = 1; while(p<n) p*=2; stsize = 2*p-1;</pre>
   string T,P;
                                                                                    70
   int* sa,*lcest;
                                                                                           lcest = new int[stsize+2]();
                                                                                           for(int i= p-1; i-(p-1) < n; i++) lcest[i] = lce[sa[i-(p-1)]];
   int stsize;
                                                                                    72
   void makesa(){
                                                                                           for(int i = p-2; i>=0; i--) lcest[i] = min(lcest[2*i+1],lcest[2*i +
31
       int n = T.size();
                                                                                               2]);
32
       sa = new int[n+1](); int* ra = new int[2*n+2]();
                                                                                           delete[] lce; delete[] rank;
                                                                                    74
33
       for(int i = 0; i < n; i++){sa[i] = i; ra[i] = T[i];}
                                                                                    75
34
                                                                                       int recque(int 1, int r, int sti, int stil, int stir){
35
                                                                                           if(stir<l || stil>r) return ub;
       sufd aux;vector<sufd> arr(n);
                                                                                    77
36
       for(int k = 1; k < n; k = 2){
                                                                                           if(l<=stil && stir<=r) return lcest[sti];</pre>
37
           arr.clear():
                                                                                           int stim = stil+stir; stim/=2;
38
                                                                                    79
           for(int i = 0: i < n: i++){
                                                                                           return min(recque(1,r,sti*2+1,stil,stim),recque(1,r,sti*2+2,stim+1,
                                                                                    80
39
               aux.id = sa[i]; aux.t = ra[sa[i]];aux.t*=ub;aux.t += ra[sa[i]]
                                                                                               stir));
40
                    ]+k];
                                                                                    81
               arr.push_back(aux);
                                                                                       int getlce(int 1, int r){
41
                                                                                           if(l==r) return T.size()-sa[1];
42
           //en caso de TLE calar con STL sort
                                                                                           return recque(l+1,r,0,0,stsize/2);
43
                                                                                    84
```

```
85 }
   int buscarRec(int 1, int r,int lcpl, int lcpr, bool izq){
86
       int m = (1+r)/2; int n = T.size();
87
        int lce = (izq?getlce(m+1,r):getlce(1,m));
88
       int lcpm = min(lcpl,lcpr);
89
        if(lcpm<lce && 1!=r) return buscarRec(m+1,r,lcpm,lcpr,false);</pre>
90
        if(lcpm>lce && 1!=r) return buscarRec(l,m-1,lcpm,lcpr,true);
91
       for(int i = lcpm; sa[m]+i < n && i < P.size(); i++){if(P[i]!=T[sa[m]+i])}
92
             break; lcpm++;}
        if(lcpm == P.size()) return m;
93
        if(l==r) return -1:
94
       return (P[lcpm]>T[sa[m]+lcpm]?buscarRec(m+1,r,lcpm,lcpr,false):
95
            buscarRec(1,m,lcpm,lcpr,true));
96
   int buscar(){
97
        int 1 = 0; int n = T.size();
98
       for(int i = 0; i < P.size() && i + sa[n-1] < n; i + + ){}
99
            if(T[i+sa[T.size()-1]] != P[i]) break;
100
            1++:
101
       }
102
        return buscarRec(0,n-1,0,1,false);
103
104
    //CODIGO DE 100 LINEAS, TE HE FALLADO MarcosK
105
    //Uso: lee T, agregar signo dolar, llama makesa(); makelce(); lee P para
106
         despues buscar()
    //delete[] sa; delete[] lcest; cuando leas de nuevo T
    //O(|T| \log(|T|)) preprocesamiento, O(|P|+\log**2(|T|)) cada busqueda
    //Buscar devuelve un indice cualquiera de sa tal que el sufijo denotado
        tenga P como prefijo
110 //Se puede hacer mas corto?
```

## 7 Clasicos

## 7.1 Job scheduling

## 7.1.1 One machine, linear penalty

```
//cuando se tiene que encontrar un orden optimo
//para trabajos con una funcion lineal de penalty, basta con hacer un
sort en O(n log n)
struct trabajo{
long long int penalty,tiempo;
int ind;
```

```
6 };
  |bool comp(const trabajo a, const trabajo b){
       if (a.tiempo * b.penalty == a.penalty * b.tiempo) return a.ind<b.ind</pre>
       return a.tiempo * b.penalty < a.penalty * b.tiempo;</pre>
9
10 }
                        7.1.2 One machine, deadlines
1 //calcula la maxima cantidad de jobs que se pueden hacer dados sus
       deadlines y duraciones en O(n log n)
2 | struct Job {
       int deadline, duration, idx;
4
       bool operator<(Job o) const {</pre>
5
           return deadline < o.deadline:
6
7
   };
8
   vector<int> compute_schedule(vector<Job> jobs) {
       sort(jobs.begin(), jobs.end());
10
11
       set<pair<int,int>> s;
12
       vector<int> schedule;
13
       for (int i = jobs.size()-1; i >= 0; i--) {
14
            int t = jobs[i].deadline - (i ? jobs[i-1].deadline : 0);
15
           s.insert(make_pair(jobs[i].duration, jobs[i].idx));
16
           while (t && !s.empty()) {
17
                auto it = s.begin();
18
                if (it->first <= t) {</pre>
19
                    t -= it->first;
20
                    schedule.push_back(it->second);
21
                } else {
                    s.insert(make_pair(it->first - t, it->second));
23
                    t = 0;
24
25
                s.erase(it);
26
           }
27
28
       return schedule;
29
30 }
```

#### 7.1.3 One machine, profit

1 // Dado n Jobs y su profit, calcula cual es el mayor profit que se puede

```
obtener en O(n^2)
  struct Job{int start, finish, profit;};
   bool jobComparataor(Job s1, Job s2){return (s1.finish < s2.finish);}</pre>
   // Find the latest job (in sorted array) that doesn't
   // conflict with the job[i]. If there is no compatible job,
   // then it returns -1.
   vector <Job> arr;
   int* memo:
   int latestNonConflict( int i){
     for (int j = i - 1; j \ge 0; j--)
10
       if (arr[j].finish <= arr[i - 1].start)</pre>
         return j;
12
     return -1;
13
14
   // A recursive function that returns the maximum possible
   // profit from given array of jobs. The array of jobs must
   // be sorted according to finish time.
   int findMaxProfitRec( int n){
     // Base case
19
     if (n == 1) return arr[n - 1].profit;
20
       if (memo[n]>=0) return memo[n];
21
     // Find profit when current job is included
22
     int inclProf = arr[n - 1].profit;
23
     int i = latestNonConflict(n);
24
     if (i != -1) inclProf += findMaxProfitRec( i + 1);
25
26
     // Find profit when current job is excluded
27
     int exclProf = findMaxProfitRec( n - 1);
28
29
     return memo[n]=max(inclProf, exclProf);
30
31
32
   // The main function that returns the maximum possible
   // profit from given array of jobs
   int findMaxProfit( int n){
     sort(arr.begin(),arr.end(), jobComparataor);
     return findMaxProfitRec(n);
37
38 | }
                      7.1.4 Two machines, min time
1 //Obtiene el ordenamiento optimo de Jobs en dos maquinas en O(n log n)
2 | struct Job {
```

```
int a, b, idx;
3
       bool operator<(Job o) const {return min(a, b) < min(o.a, o.b);}</pre>
4
   };
5
   vector<Job> johnsons_rule(vector<Job> jobs) {
6
       sort(jobs.begin(), jobs.end());
       vector<Job> a, b;
       for (Job j : jobs) {
9
           if (j.a < j.b)
                a.push_back(j);
11
           else
                b.push_back(j);
13
14
       a.insert(a.end(), b.rbegin(), b.rend());
15
       return a;
16
   }
17
   pair<int, int> finish_times(vector<Job> const& jobs) {
19
       int t1 = 0, t2 = 0;
20
       for (Job j : jobs) {
21
           t1 += j.a;
           t2 = max(t2, t1) + j.b;
23
24
       return make_pair(t1, t2);
25
```

## 8 Flow

## 8.1 Dinic, thx GGDem

```
#define pb push_back
#define mp make_pair
#define fst first
#define snd second
#define ALL(s) s.begin(),s.end()
#define SZ(x) int((x).size())
#define fore(i,a,b) for(int i=a,to=b;i<to;++i)
using namespace std;
#typedef long long ll;

#define INF (1LL<<62)
// Min cut: nodes with dist>=0 vs nodes with dist<0
// Matching MVC: left nodes with dist<0 + right nodes with dist>0
struct Dinic{
```

```
int nodes,src,dst;
15
     vector<int> dist,q,work;
16
     struct edge {int to,rev;ll f,cap;};
17
     vector<vector<edge>> g;
18
     Dinic(int x):nodes(x),g(x),dist(x),q(x),work(x){}
19
     void add_edge(int s, int t, ll cap){
20
       g[s].pb((edge){t,SZ(g[t]),0,cap});
21
       g[t].pb((edge){s,SZ(g[s])-1,0,0});
22
23
     bool dinic_bfs(){
24
       fill(ALL(dist),-1);dist[src]=0;
25
       int qt=0;q[qt++]=src;
26
       for(int qh=0;qh<qt;qh++){</pre>
27
         int u=q[qh];
28
         fore(i,0,SZ(g[u])){
29
            edge &e=g[u][i];int v=g[u][i].to;
30
           if(dist[v]<0&&e.f<e.cap)dist[v]=dist[u]+1,q[qt++]=v;</pre>
31
         }
32
       }
33
       return dist[dst]>=0;
34
35
     11 dinic_dfs(int u, ll f){
36
       if(u==dst)return f;
37
       for(int &i=work[u];i<SZ(g[u]);i++){</pre>
38
         edge &e=g[u][i];
39
         if(e.cap<=e.f)continue;</pre>
40
          int v=e.to;
41
         if(dist[v]==dist[u]+1){
42
           11 df=dinic_dfs(v,min(f,e.cap-e.f));
43
            if(df>0){e.f+=df;g[v][e.rev].f-=df;return df;}
44
         }
45
       }
46
       return 0:
47
48
     ll max_flow(int _src, int _dst){
49
       src=_src;dst=_dst;
50
       11 result=0;
51
       while(dinic bfs()){
52
         fill(ALL(work),0);
53
         while(ll delta=dinic_dfs(src,INF))result+=delta;
54
       }
55
       return result;
56
57
```

```
<sub>58</sub> };
59
   //----SOLBEGIN-----
60
   int main() {
61
    ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
62
      //l set,r set
63
      int n,m;
64
      cin>>n>>m;
      m+=n;
      Dinic d(n+m+2);
      for(int i = 1; i<=n; i++) d.add_edge(0,i,1);</pre>
      for(int i = n+1; i<=m; i++) d.add_edge(i,m+1,1);</pre>
70
      int fin,q;
      for(int i = 1; i<=n; i++){
72
          cin>>q;
73
          while(q--){
74
              cin>>fin;
              d.add_edge(i,n+fin,1);
76
          }
77
      }
78
      int res =d.max_flow(0,m+1);
      m-=n;
80
      //how many were left unmatched
      cout<<m-res<<endl;
82
  }
83
               -----EOSOLUTION-----
```

## 9 Miscellaneous

## 9.1 Bit Manipulation

```
#include "bits/stdc++.h"
using namespace std;

#define endl '\n'

int main() {
   ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);

//Se representan bitmasks de 30 a 62 bits
//usando signed int y signed long int
//para evitar problemas con el complemento de dos
signed int a, b;
```

```
//para multiplicar un numero por dos solo es necesario aplicar un
     // shifteo de sus bits a la izquierda
13
     a = 1;
14
     a = a << 3;
15
     cout << a << endl;</pre>
     //para dividir un numero entre dos es necesario aplicar un
     //shifteo a la derecha
     a = 32;
19
     a = a >> 3;
20
     cout << a << endl;</pre>
21
     //para encender el bit n de a, solo hay que igualar a = a \mid pow(2,n-1)
22
     //prende el tercer bit
23
     a = 1:
     b = 1 << 2;
     a = a \mid b;
     cout << a << endl;</pre>
     //para apagar el bit n de a, solo hay que a \&= \text{pow}(2,n-1)
28
     //prende el tercer bit
     a = 5:
30
     b = 1 << 2;
31
     a &= ~b;
32
     cout << a << endl;</pre>
33
     //para revisar si el bit n de a esta encendido
34
     //revisa si el tercer bit esta encendido
35
     a = 5;
36
     b = 1 << 2;
37
     a = a \& b;
38
     cout << (a?"SI":"NO") << endl;</pre>
39
     //para volter el bit n de a, solo hay que igualar a = a ^{\circ} pow(2,n-1)
40
     //apaga el tercer bit
41
     a = 5;
42
     b = 1 << 2;
43
     a = a \hat{b};
44
     cout << a << endl;</pre>
45
     //para obtener el bit menos significativo que esta encendido a& -a
46
47
     cout << \log 2(a \& ((-1) * a)) + 1 << endl;
48
     //para prender todos los bits hasta n
49
     a = (1 << 4) - 1;
     cout << a << endl;</pre>
51
52
       -----EOSOLUTION-----
```

```
#include "bits/stdc++.h"
  using namespace std;
   #define endl '\n'
   #pragma GCC optimize("03")
  #pragma GCC target("popcnt")
  //no usar con visual c++
   //solo con g++ like compilers
  int main() {
    ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
     signed long long int a, b, n;
    //Obtain the remainder (modulo) of a when it is divided by n (n is a
12
        power of 2)
    a = 15: n = 8-1:
13
    a &= n;
    cout << a << endl;</pre>
16
    //Apaga el bit menos significativo de a
    a = 14:
18
    b = (a \& ((-1) * a));
    a &= ~b;
    cout << a << endl;</pre>
    //enciende el ultimo cero de a
    a = 9;
    b = a;
24
    b = (b \& ((-1) * b));
    a = a \mid b;
    cout << a<<endl;</pre>
27
    //contar bits encendidos en a
28
     cout << __builtin_popcount(a)<<endl;</pre>
    //checar la paridad de a
30
     cout << (__builtin_parity(a) ? "IMPAR" : "PAR") << endl;</pre>
31
    //contar leading zeroes en a
32
     cout << __builtin_clz(a)<<endl;</pre>
    //contar 9, trailling zeroes en a
     cout << __builtin_ctz(a)<<endl;</pre>
35
36
37 //-----EOSOLUTION-----
```

#### Testing

## 10.1 Highly Composite Numbers

Particularly useful when testing number theoretical solutions.

		rarricularly useful when testing	number theoretical solutions.
1	1	1	
2	2	2	2
3	4	3	2^2
4	6	4	2*3
5	12	6	2^2*3
6	24	8	2^3*3
7	36	9	2^2*3^2
8	48	10	2^4*3
9	60	12	2^2*3*5
10	120	16	2^3*3*5
11	180	18	2^2*3^2*5
12	240	20	2^4*3*5
13	360	24	2^3*3^2*5
14	720	30	2^4*3^2*5
15	840	32	2^3*3*5*7
16	1260	36	2^2*3^2*5*7
17	1680	40	2^4*3*5*7
18	2520	48	2^3*3^2*5*7
19	5040	60	2^4*3^2*5*7
20	7560	64	2^3*3^3*5*7
21	10080	72	2^5*3^2*5*7
22	15120	80	2^4*3^3*5*7
23	20160	84	2^6*3^2*5*7
24	25200	90	2^4*3^2*5^2*7
25	27720	96	2^3*3^2*5*7*11
26	45360	100	2^4*3^4*5*7
27	50400	108	2^5*3^2*5^2*7
28	55440	120	2^4*3^2*5*7*11
29	83160	128	2^3*3^3*5*7*11
30	110880	144	2^5*3^2*5*7*11
31	166320	160	2^4*3^3*5*7*11
32	221760	168	2^6*3^2*5*7*11
33	277200	180	2^4*3^2*5^2*7*11
34	332640	192	2^5*3^3*5*7*11
35	498960	200	2^4*3^4*5*7*11
36	554400	216	2^5*3^2*5^2*7*11
37	665280	224	2^6*3^3*5*7*11
38	720720	240	2^4*3^2*5*7*11*13

82	48886437600	3456	2^5*3^3*5^2*7^2*11*13*17*19
83	64250746560	3584	2^6*3^3*5*7*11*13*17*19*23
84	73329656400	3600	2^4*3^4*5^2*7^2*11*13*17*19
85	80313433200	3840	2^4*3^3*5^2*7*11*13*17*19*23
86	97772875200	4032	2^6*3^3*5^2*7^2*11*13*17*19
87	128501493120	4096	2^7*3^3*5*7*11*13*17*19*23
88	146659312800	4320	2^5*3^4*5^2*7^2*11*13*17*19
89	160626866400	4608	2^5*3^3*5^2*7*11*13*17*19*23
90	240940299600	4800	2^4*3^4*5^2*7*11*13*17*19*23
91	293318625600	5040	2^6*3^4*5^2*7^2*11*13*17*19
92	321253732800	5376	2^6*3^3*5^2*7*11*13*17*19*23
93	481880599200	5760	2^5*3^4*5^2*7*11*13*17*19*23
94	642507465600	6144	2^7*3^3*5^2*7*11*13*17*19*23
95	963761198400	6720	2^6*3^4*5^2*7*11*13*17*19*23
96	1124388064800	6912	2^5*3^3*5^2*7^2*11*13*17*19*23
97	1606268664000	7168	2^6*3^3*5^3*7*11*13*17*19*23
98	1686582097200	7200	2^4*3^4*5^2*7^2*11*13*17*19*23
99	1927522396800	7680	2^7*3^4*5^2*7*11*13*17*19*23
100	2248776129600	8064	2^6*3^3*5^2*7^2*11*13*17*19*23
101	3212537328000	8192	2^7*3^3*5^3*7*11*13*17*19*23
102	3373164194400	8640	2^5*3^4*5^2*7^2*11*13*17*19*23
103	4497552259200	9216	2^7*3^3*5^2*7^2*11*13*17*19*23
104	6746328388800	10080	2^6*3^4*5^2*7^2*11*13*17*19*23
105	8995104518400	10368	2^8*3^3*5^2*7^2*11*13*17*19*23
106	9316358251200	10752	2^6*3^3*5^2*7*11*13*17*19*23*29
107	13492656777600	11520	2^7*3^4*5^2*7^2*11*13*17*19*23
108	18632716502400	12288	2^7*3^3*5^2*7*11*13*17*19*23*29
109	26985313555200	12960	2^8*3^4*5^2*7^2*11*13*17*19*23
110	27949074753600	13440	2^6*3^4*5^2*7*11*13*17*19*23*29
111	32607253879200	13824	2^5*3^3*5^2*7^2*11*13*17*19*23*29
112	46581791256000	14336	2^6*3^3*5^3*7*11*13*17*19*23*29
113	48910880818800	14400	2^4*3^4*5^2*7^2*11*13*17*19*23*29
114	55898149507200	15360	2^7*3^4*5^2*7*11*13*17*19*23*29
115	65214507758400	16128	2^6*3^3*5^2*7^2*11*13*17*19*23*29
116	93163582512000	16384	2^7*3^3*5^3*7*11*13*17*19*23*29
117	97821761637600	17280	2^5*3^4*5^2*7^2*11*13*17*19*23*29
118	130429015516800	18432	2^7*3^3*5^2*7^2*11*13*17*19*23*29
119	195643523275200	20160	2^6*3^4*5^2*7^2*11*13*17*19*23*29
120	260858031033600	20736	2^8*3^3*5^2*7^2*11*13*17*19*23*29
121	288807105787200	21504	2^6*3^3*5^2*7*11*13*17*19*23*29*31
122	391287046550400	23040	2^7*3^4*5^2*7^2*11*13*17*19*23*29
123	577614211574400	24576	2^7*3^3*5^2*7*11*13*17*19*23*29*31
124	782574093100800	25920	2^8*3^4*5^2*7^2*11*13*17*19*23*29