First to Penalty

-12

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1 Template

```
#include "bits/stdc++.h"
  //assert(x>0) si falla da RTE
  using namespace std;
  #define endl '\n'
  #define DBG(x) cerr<<\#x<< "=" << (x) << endl:
  #define RAYA cerr<<"========"<<endl:
  #define RAYAS cerr<<"...."<<endl;</pre>
  //#define DBG(x) :
   //#define RAYA ;
  //#define RAYAS ;
11
   //----SOLBEGIN-----
  int main() {
    ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
14
    int tC;
15
16
    cin >> tC;
17
    while (tC--) {
18
19
    }
20
21
^{22}
         -----EOSOLUTION-----
```

2 Data structures

2.1 Simplified DSU (Stolen from GGDem)

```
int uf[MAXN];
void uf_init(){memset(uf,-1,sizeof(uf));}
int uf_find(int x){return uf[x]<0?x:uf[x]=uf_find(uf[x]);}
bool uf_join(int x, int y){
    x=uf_find(x);y=uf_find(y);
    if(x==y)return false;
    if(uf[x]>uf[y])swap(x,y);
    uf[x]+=uf[y];uf[y]=x;
    return true;
}
```

2.2 Disjoint Set Union

```
class disjSet {
     int* sz;
     int* par;
   public:
     int len;
     disjSet(int tam){
           sz = new int[tam + 4]();
           par = new int[tam + 4]();
           len = 0;
           for(int i = 0; i<=tam; i++){</pre>
               par[i] = i;
11
                sz[i] = 1;
12
               len++;
13
           }
       }
15
     int finds(int el){
16
           if (el == par[el]) return el;
17
           return par[el] = finds(par[el]);
18
       }
19
     void unions(int a, int b){
20
           a = finds(a);
21
         b = finds(b);
22
           if (a == b) return;
23
           len--;
24
           //se hace que el gde sea padre del pequeno
25
           if (sz[a] > sz[b]) swap(a,b);
           par[a] = b;
27
           sz[b] += sz[a];
28
       }
29
      ~disjSet(){
30
           delete[] size;
31
           size = nullptr;
32
           delete[] parent;
33
           parent = nullptr;
34
35
36 };
                                 Segment tree
```

```
//MAXN = 2^k, n = tam arreglo inicial
#define MAXN 262160
int stsize; long long int neut;int n;
long long int* st = new long long int[2*MAXN-1]();
```

```
5 long long int fst(long long int a, long long int b);
                                                                                   5 long long int* st = new long long int[2*MAXN-1]();
  long long int build(int sti,int csize){
                                                                                     long long int* pendientes = new long long int[2*MAXN-1]();
                                                                                     long long int fst(long long int a, long long int b){return a+b;}
       if(csize == 1) return st[sti];
       return st[sti] = fst(build(sti*2+1,csize/2),build(sti*2+2,csize/2));
                                                                                      long long int build(int sti,int csize){
8
   }
                                                                                          if(csize == 1) return st[sti];
9
                                                                                   9
                                                                                          return st[sti] = fst(build(sti*2+1,csize/2),build(sti*2+2,csize/2));
   void innit(){
                                                                                   10
       for(int i = 0; i<stsize; i++) st[i] = neut;</pre>
                                                                                      }
                                                                                   11
11
       /*int d = 0:
                                                                                      bool hasChildren(int sti){sti*=2;sti++;sti++;return sti<stsize;}</pre>
12
       for(int i = stsize-n; i<stsize && d<n; i++){</pre>
                                                                                      void innit(){
13
           st[i] = arr[d];d++;
                                                                                          for(int i = 0; i<stsize; i++) st[i] = neut;</pre>
14
                                                                                          int d = 0:
15
                                                                                  15
                                                                                          for(int i = stsize-n; i<stsize && d<n; i++) {st[i] = arr[d];d++;}</pre>
       build(0,n);
16
                                                                                   16
                                                                                          build(0.n):
   | }
17
                                                                                   17
   void upd(int ind, long long int val){
                                                                                      }
                                                                                   18
       ind = stsize-n+ind:
                                                                                      void updrec(int 1,int r, int s1, int sr,int sti, long long int val){
                                                                                   19
19
       st[ind] = val;ind--;ind/=2;
                                                                                          if(sr<l | r< sl) return:
20
                                                                                  20
       while(true){
                                                                                          if(l<= sl && sr <=r){
21
                                                                                  21
           st[ind] = fst(st[ind*2+1],st[ind*2+2]);
                                                                                              st[sti] += val*(sr-sl+1);
22
                                                                                              if(hasChildren(sti)){pendientes[sti*2+1]+=val;pendientes[sti
           ind--:
                                                                                  23
23
           if(ind<0) break;
                                                                                                  *2+2]+=val;}
24
           ind/=2;
                                                                                              return;
                                                                                  24
25
       }
                                                                                          }
26
                                                                                   25
                                                                                  26
27
                                                                                          int sm = (sl+sr)/2;
   long long int rqu(int 1, int r, int sti, int ls, int rs){
                                                                                  27
28
                                                                                          updrec(1,r,sl,sm,sti*2+1,val);
       if(l<=ls && rs<= r) return st[sti];</pre>
                                                                                  28
29
       if(r<ls || l>rs) return neut;
                                                                                          updrec(l,r,sm+1,sr,sti*2+2,val);
                                                                                  29
30
                                                                                          st[sti] = fst(st[sti*2+1]+pendientes[sti*2+1],st[sti*2+2]+pendientes
       int m = (rs+ls)/2;
                                                                                   30
31
       return fst(rqu(1,r,sti*2+1,ls,m),rqu(1,r,sti*2+2,m+1,rs));
                                                                                              [sti*2+2]);
32
                                                                                  31
33
   long long int query(int 1, int r){
                                                                                      void upd(int 1, int r, long long int val){updrec(1,r,0,n-1,0,val);}
       return rqu(1,r,0,0,n-1);
35
                                                                                   33
                                                                                      long long int rqu(int 1, int r, int sti, int ls, int rs){
36
   //uso, inicializa neut, n = primera potencia de 2 >= n del problema,
                                                                                          if(r<ls || l>rs) return neut;
                                                                                  35
       stsize = 2*n-1
                                                                                          if(1<=1s && rs<= r){
                                                                                  36
   //llena arr de neutros hasta que su tam sea el nuevo n
                                                                                              return st[sti]+pendientes[sti]*(rs-ls+1);
                                                                                  37
39 //DEFINE LA FUNCION fst
                                                                                          }
                                                                                  38
                                                                                  39
                        2.4 Segment tree Lazy
                                                                                          st[sti] += pendientes[sti]*(rs-ls+1);
                                                                                  40
                                                                                          if(hasChildren(sti)){pendientes[sti*2+1]+=pendientes[sti];pendientes
                                                                                  41
                                                                                              [sti*2+2]+=pendientes[sti];}
1 //MAXN = 2^k, n = tam arreglo inicial
                                                                                          pendientes[sti] = 0;
  #define MAXN 262160
                                                                                  42
  vector<int> arr;
                                                                                   43
                                                                                          int m = (rs+ls)/2;
  int stsize; long long int neut; int n;
                                                                                  44
```

```
return fst(rqu(l,r,sti*2+1,ls,m),rqu(l,r,sti*2+2,m+1,rs));

long long int query(int l, int r){
    return rqu(l,r,0,0,n-1);
}

//uso, inicializa neut, n = primera potencia de 2 >= n del problema,
    stsize = 2*n-1

//llena arr de neutros hasta que su tam sea el nuevo n

//DEFINE LA FUNCION fst

2.5 Trie
```

```
struct triver {
       char alphabet;
2
       bool ter;
3
       vector<triver*> child;
4
       triver(char a): alphabet(a) { child.assign(26, NULL); ter = false; }
5
6
   class trie{
   private:
       triver* root;
   public:
10
       trie() { root = new triver('!');}
11
       void insert(string s){
12
           triver* curr = root;
13
           for(char 1: s){
14
                if(curr->child[l-'A'] == NULL) curr->child[l-'A'] = new
15
                    triver(1);
                curr = curr->child[l-'A'];
16
           }
17
            curr->ter = true;
18
       }
19
       bool search(string s){
20
           triver* curr = root;
^{21}
           for(char 1: s){
^{22}
                if(curr == NULL) break;
23
                curr = curr->child[1-'A'];
24
25
           if(curr == NULL) return false;
26
           return curr->ter;
27
28
  |};
29
```

3 Graphs

3.1 Graph Transversal

3.1.1 BFS

```
#define GS 400040
  vector<int> graph[GS];
   bitset <GS> vis;
   //anchura O(V+E)
   void dfs(int curr) {
     queue<int> fringe;
     fringe.push(curr);
     while (fringe.size()) {
       curr = fringe.front(); fringe.pop();
9
       if (!vis[curr]) {
10
         vis[curr] = 1:
         for (int h : graph[curr]) fringe.push(h);
12
13
    }
14
15 }
                                 3.1.2 DFS
```

```
#define GS 400040
   vector<int> graph[GS];
   bitset <GS> vis;
   //profundidad O(V+E)
   void dfs(int curr) {
     stack<int> fringe;
     fringe.push(curr);
     while (fringe.size()){
       curr = fringe.top(); fringe.pop();
       if (!vis[curr]) {
10
         vis[curr] = 1;
11
         for (int h : graph[curr]) fringe.push(h);
12
13
     }
14
15 }
```

3.2 Topological Sort

```
#define GS 400040
vector<int> graph[GS];
```

```
3 | bitset <GS> vis;
   vector<int> topsort;
  int e,n;
   //profundidad
   //O(N+E)
   //Solo funciona con DAG's, no existe un top sort de un grafo Non-DAG
   void todfs(int pa) {
     vis[pa]=1;
10
    for(int h: graph[pa]){if(!vis[h]){todfs(h);}}
11
     topsort.push_back(pa);
12
13
   void topologicalSort(){
     vis.reset():
15
     topsort.clear();
     for(int i = 0; i<n; i++){if(!vis[i]){dfs(i);}}</pre>
     reverse(topsort.begin(),topsort.end());
19 }
                     3.3 APSP: Floyd Warshall
  #define GS 1000
```

```
#define INF 100000000
   //destino, costo
   int graph[GS] [GS];
   //All Pairs Dist
   int dist[GS][GS]:
  //Toma en cuenta nodos [0-tam] inclusivo, modificar de acuerdo a las
       necesidades
  //Ten cuidado con el valor que le pones a INF, puede provocar overflows
       o puede no ser lo suficientemente grande.
   void Floyd_Warshall(int tam){
       for(int i = 0; i<=tam; i++)</pre>
10
           for(int f = 0; f<=tam; f++)</pre>
11
                dist[i][f] = INF;
12
13
       for(int i = 0; i<=tam; i++)
14
           for(int f = 0; f < = tam; f + +)
15
                dist[i][f] = graph[i][f];
16
17
       //para reconstruir el camino solo basta con guardar intermedio como
18
            el padre de ini si el cambio se hizo, -1 otherwise
       for(int intermedio = 0; intermedio<=tam; intermedio++)</pre>
19
           for(int ini = 0; ini<=tam; ini++)</pre>
20
```

```
for(int fin = 0; fin<=tam; fin++)</pre>
21
                    dist[ini][fin] = min(dist[ini][fin],dist[ini][intermedio
22
                        ]+dist[intermedio][fin]);
23 | }
                                 3.4 SSSP
                             3.4.1 Lazy Dijkstra
1 #define GS 1000
   #define INF 100000000
   //destino, costo
   vector<pair<int,int>> graph[GS];
   int dist[GS];
   void dijkstra(int origen,int tam){
       for(int i = 0; i<=tam; i++){</pre>
           dist[i] = INF;
8
9
       priority_queue<pair<int,int>,vector<pair<int,int>>, greater<pair<int</pre>
10
            ,int>>> pq;
       pair<int,int> curr;
11
12
       pq.push(make_pair(0,origen));
13
14
       while(pq.size()){
15
           curr = pq.top();pq.pop();
16
           if(curr.first >= dist[curr.second]) continue:
17
18
           dist[curr.second] = curr.first;
19
           for(pair<int,int> h: graph[curr.second]){
20
               if((h.second+curr.first)<dist[h.first]) pq.push({h.second+</pre>
21
                    curr.first,h.first});
           }
22
23
   }
24
   //Esta es la implementacion huevona
   //Resuelve Single Source Shortest Paths con aristas positivas
   //Como es la lazy implementation, si funciona con edges negativos
       siempre y cuando no hayan ciclos negativos
28 //Si hay ciclos negativos se va atascar en un ciclo infinito
29 //Si no los hay puede que funcione en O((V+E)log(V)) o puede que se
```

3.4.2 Bellman-Ford

exponencial, si no jala prueba BellmanFord

```
1 //esta es la implementacion huevona
   #define GS 1000
2
   //cuidado con overflows!!
   #define INF 100000000
   #define NINF -10000000
   //destino, costo
   vector<pair<int,int>> graph[GS];
   int dist[GS];
   struct edge{
       int from, to, cost;
10
   };
11
   //Corre en O(VE)
   void bellmanFord(int origen,int tam){
       for(int i = 0; i<=tam; i++){</pre>
14
           dist[i] = INF;
15
       }
16
       dist[origen] = 0;
17
       edge aux;
18
       vector<edge> aristas;
19
       bool optimal;
20
21
       for(int i = 0; i<=tam; i++){</pre>
22
           for(pair<int,int> h: graph[i]){
23
                aux.from = i; aux.to = h.first;aux.cost = h.second;
24
                aristas.push_back(aux);
25
26
       }
27
28
       //Si se relajan todos las aristas V-1 veces en un orden arbitrario
29
       //Se asegura que la distancia optima para cada vertice sera
30
           alcanzada
       for(int i = 0; i<tam && !optimal; i++){</pre>
31
           optimal = true;
32
           for(edge elem: aristas){
33
                if(dist[elem.from] + elem.cost < dist[elem.to]){</pre>
34
                    dist[elem.to] = dist[elem.from] + elem.cost;
35
                    //si algun vertice fue actualizado significa que puede
36
                    //las distancias aun no sean optimas
37
                    optimal = false;
38
39
           }
40
41
```

```
42
       //Se corre de nuevo para asegurar encontrar todos los ciclos
43
            negativos
       for(int i = 0; i<tam && !optimal; i++){</pre>
44
            optimal = true;
45
            for(edge elem: aristas){
46
                if(dist[elem.from] + elem.cost < dist[elem.to]){</pre>
47
                    //Si aun despues de correr V-1 veces se puede actualizar
48
                    //Significa que esta en un ciclo negativo
49
                    dist[elem.to] = NINF;
                    //si algun vertice fue actualizado significa que puede
51
                    //las distancias aun no sean optimas
52
                    optimal = false;
53
                }
54
            }
55
       }
56
57
58 }
```

3.5 Strongly Connected Components: Kosaraju

```
1 #define GS 2010
   vector<int> graph[GS];
   vector<int> graphI[GS];
   vector<int> orden;
   bitset<GS> vis;
6
   void invertirGrafo(int n){
       for(int p = 1; p <= n; p++)
8
           for(int h: graph[p])graphI[h].push_back(p);
9
10
   void obtOrd(int p,int n){
11
       vis[p] = 1;
12
       for(int h: graph[p]){
13
           if(!vis[h] && h<=n) obtOrd(h,n);</pre>
14
15
       orden.push_back(p);
16
   }
17
   int findSCC(int n){
18
       int res = 0;
19
       invertirGrafo(n);
20
       orden.clear();
21
```

```
for(int i = 1; i<=n; i++) vis[i] =0;
22
       for(int i = 1; i<=n; i++) if(!vis[i]) obtOrd(i,n);</pre>
23
       reverse(orden.begin(),orden.end());
^{24}
       //cuenta los connected components
25
       //vector<int> lscc;
26
       stack<int> fringe;
27
       int curr;
28
       for(int i = 1; i<=n; i++) vis[i] =0;</pre>
29
       for(int i: orden){
30
           //lscc.clear();
31
           if(!vis[i]){
32
                fringe.push(i);
33
                while (fringe.size()){
34
                    curr = fringe.top();fringe.pop();
35
                    //lscc.push_back(curr);
36
                    if (!vis[curr]) {
37
                        vis[curr] = 1:
38
                        for (int h : graphI[curr]) fringe.push(h);
39
                    }
40
                }
41
                res++;
42
43
           //hacer lo que sea con lcss
44
       }
45
       return res;
46
47
48
    //OJO esto solo jala con directed graphs
   //por definicion todas las undirected graphs tienen un solo SCC
   //NOTAR QUE LOS GRAFOS QUE USA CUMPLEN CON: O<=VERTICE<=n
```

3.6 Articulation Points and Bridges: ModTarjan

```
#define GS 50
vector<int> graph[GS];
bitset<GS> vis, isArtic;
vector<int> padre;
//id por tiempo, menor id accesible
//ya sea por descendientes o por back edges
vector<int> tId, lId;
//cantidad de hijos que tiene en el bfs spanning tree
int rootChildren;
int cnt;
```

```
int dfsRoot;
   void findAP_B(int p){
       cnt++;vis[p] = 1;tId[p] = cnt;lId[p] = tId[p];
13
14
       for(int hijo: graph[p]){
15
           if(!vis[hijo]){
16
                padre[hijo] = p;
17
                if(p == dfsRoot) rootChildren++;
18
19
                findAP_B(hijo);
20
21
                //esto significa que ni por un back edge el hijo accede al
22
                    padre
                //por lo que si el padre fuese eliminado el hijo quedaria
23
                    aislado
                if(lId[hijo] >= tId[p]) isArtic[p] = 1;
24
                if(lId[hijo] > tId[p]){
25
                    //esto significa que si se eliminase el camino de padre
26
                        ->hiio
                    //se lograria desconectar el grafo, aka bridge
27
                }
28
                lId(p) = min(lId(p),lId(hijo));
29
           }else{
30
                //si hay un ciclo indirecto, actualiza el valor para el
31
                if(hijo != padre[p]) lId[p] = min(lId[p],tId[hijo]);
32
33
       }
34
35
    //OJO esto solo jala con Undirected graphs
   /*
37
       MAIN
38
       for(int i = 0; i < n; i++){
39
           if(!vis[i]){
40
                rootChildren = 0;
41
                dfsRoot = i;
42
                findAP_B(i);
43
                //el algoritmo no puede detectar si el nodo que lo origino
44
                //es un articulation point, por lo que queda checar si
45
                //en el spanning tree que genero tiene mas de un solo hijo
46
               isArtic[i] = (rootChildren>1?1:0);
47
48
49
```

```
50 */
```

4 Math

4.1 Identities

```
C_n = \frac{2(2n-1)}{n+1}C_{n-1} C_n = \frac{1}{n+1}\binom{2n}{n} C_n \sim \frac{4^n}{n^{3/2}\sqrt{\pi}} \sigma(n) = O(\log(\log(n))) \text{ (number of divisors of } n) F_{2n+1} = F_n^2 + F_{n+1}^2 F_{2n} = F_{n+1}^2 - F_{n-1}^2 \sum_{i=1}^n F_i = F_{n+2} - 1 F_{n+i}F_{n+j} - F_nF_{n+i+j} = (-1)^n F_i F_j (Möbius Inv. Formula) Let g(n) = \sum_{d|n} f(d), then f(n) = \sum_{d} d \mid ng(d)\mu\left(\frac{n}{d}\right)). Permutaciones objetos repetidos P(n,k) = \frac{P(n,k)}{n_1!n_2!\dots} Separadores, Ecuaciones lineares a variables = b \left(\binom{a}{b}\right) = \binom{a+b-1}{b} = \binom{a+b-1}{a-1}
```

4.2 Binary Exponentiation and modArith

```
long long int inf = 10000000007;
   //suma (a+b)%m
   //resta ((a-b)\m+m)\m
   //mult (a*b)%m
   long long binpow(long long b, long long e) {
       long long res = 1; b%=inf;
6
       while (e > 0) {
           if (e \& 1) res = (res * b)\%inf;
8
           b = (b * b)\%inf:
9
           e >>= 1:
10
       }
11
       return res;
12
13 }
```

4.3 Modular Inverse (dividir mod)

```
long long int q = a1 / b1;
           tie(x, x1) = make_tuple(x1, x - q * x1);
           tie(y, y1) = make_tuple(y1, y - q * y1);
           tie(a1, b1) = make_tuple(b1, a1 - q * b1);
10
       return a1;
11
12
   long long int modinverse(long long int b, long long int m){
       long long int x,y;
14
       long long int d = gcd(b, inf, x, y);
       if(d!=1) return -1;
16
       return ((x%inf)+inf)%inf;
17
18 }
```

4.4 Modular Binomial Coeficient and Permutations

```
long long int inf = 10000000007;
  //\text{cat}[n] = \text{bincoef}(2*n,n)/(n+1), \text{cat}[0] = 1
   class binCoef{
4
       long long int lim;
       long long int* fact;
  public:
6
       binCoef(long long int 1){
           lim = 1; fact = new long long int[1+1];fact[0]= 1;
           for(long long int i = 1; i<=1; i++) fact[i] = (fact[i-1]*i)%inf;</pre>
9
10
       //perm = (fact[n] * modinverse(fac[n-k],inf)%inf;
11
       long long int query(long long int n, long long int k){
12
           if(n<k) return 0;
13
           return (fact[n] * modinverse((fac[n-k]*fact[k])%inf,inf))%inf;
14
       }
15
16 };
```

4.5 Non-Mod Binomial Coefficient and Permutations

```
//Solo usar con n<=20
//cat[n] = bincoef(2*n,n)/(n+1), cat[0] = 1
unsigned long long int bincoef(unsigned long long int n, unsigned long long int k){
   if(n<k) return 0;
   unsigned long long int num = 1, den= 1;
   for(unsigned long long int i = (n-k)+1; i<=n; i++) num*=i;
   for(unsigned long long int i = 2; i<=k; i++) den*=i;
//perm = return num;</pre>
```

```
return num/den;
9
10 }
                        Modular Catalan Numbers
  long long int inf = 10000000007;
   class catalan{
       long long int* cat; long long int lim
3
   public:
4
       catalan(long long int 1){
5
           lim = 1; cat = new long long int[l+10];cat[0] = 1;
6
           for(long long int i = 0; i \le 1; i++) cat[i+1] = ((((4LL*i+2)%inf))
7
                *cat[i])%inf) *modinverse(n+2))%inf;
8
       long long int query(long long int n){ return cat[n];}
9
10 | };
                               Ceil Fraccionario
  long long int techo(long long int num, long long int den){ return (num+
       den-1)/den;}
                           Numeros de Fibonacci
   //en caso de ser usados mod un m pequeno
   //recordar que los numeros de fibonacci se repiten por lo menos cada m^2
   //O(n)
3
   unsigned long long int fib(int n){
     unsigned long long int a = 1,b = 1,aux;
5
     if(n \le 2)
6
       return 1;
8
     for(int i = 3; i <= n; i++){
9
       aux = a+b;
10
       a = b;
11
       b = aux;
12
13
     return b;
14
15
  const long long int inf = 1000000007;
```

unordered_map<long long int,long long int> Fib;

long long int fib(long long int n)

 $//O(\log n) : DD$

```
5 | {
       if(n<2) return 1;
6
       if(Fib.find(n) != Fib.end()) return Fib[n];
       Fib[n] = (fib((n+1) / 2)*fib(n/2) + fib((n-1) / 2)*fib((n-2) / 2)) %
            inf;
       return Fib[n];
9
10 }
                             Sieve Of Eratosthenes
1 #define MAXN 10e6
   class soe{
   public:
       bitset<MAXN> isPrime;
4
       soe(){
5
           for(int i = 3; i<MAXN; i++) isPrime[i] = (i\(^2\));</pre>
6
           isPrime[2] = 1;
7
           for(int i = 3; i*i<MAXN; i+=2)</pre>
               if(isPrime[i])
9
                    for(int j = i*i; j<MAXN; j+=i)</pre>
10
                        isPrime[j] = 0;
11
12
13 };
                    4.10 Sieve-based Factorization
1 #define MAXN 10e6
   class soe{
   public:
       int smolf[MAXN];
       soe(){
           for(int i = 2; i<MAXN; i++) smolf[i] = (i\( 2==0?2:i );
7
           for(int i = 3; i*i<MAXN; i+=2)</pre>
8
               if(smolf[i]==i)
                    for(int j = i*i; j<MAXN; j+=i)</pre>
                        smolf[j] = min(smolf[j],smolf[i]);
11
12
13 };
                           4.11 Cycle Finding
void cyclef(long long int sem){
       long long int hare = f(sem),tort=f(sem);hare = f(hare);
```

```
//liebre avanza dos pasos, tortuga solo uno
3
       while(hare!=tort){
4
           tort = f(tort); hare = f(f(hare));
5
       }
6
       //Se detiene en el inicio del ciclo
       tort = sem;
8
       while(hare!=tort){
9
           tort = f(tort); hare = f(hare);
10
       }
11
12
       int len = 1;
13
       tort = f(sem);
14
       while(hare!=tort){
15
           tort=f(tort):
16
           len++;
17
       }
18
19 }
```

4.12 Berlekamp Massey

```
typedef long long int 11;
   //Obtiene recurrencia lineal dados los primeros elementos en O(n^2)
   vector<ll> berlekampMassey(const vector<ll> &s) {
       vector<ll> c:
4
       vector<ll> oldC:
5
       int f = -1:
6
       for (int i=0; i<(int)s.size(); i++) {</pre>
7
           ll delta = s[i];
8
           for (int j=1; j<=(int)c.size(); j++) delta -= c[j-1] * s[i-j];</pre>
9
           if (delta == 0) continue;
10
           if (f == -1) {
11
               c.resize(i + 1);
12
               mt19937 rng(chrono::steady_clock::now().time_since_epoch().
13
                    count());
               for (11 &x : c) x = rng();
14
               f = i;
15
           } else {
16
               vector<11> d = oldC:
17
               for (11 &x : d) x = -x;
18
               d.insert(d.begin(), 1);
19
               11 df1 = 0:
20
               for (int j=1; j <= (int)d.size(); j++) df1 += d[j-1] * s[f+1-j]
21
                    ];
```

```
assert(df1 != 0):
22
                ll coef = delta / df1;
23
                for (11 &x : d) x *= coef;
24
                vector<ll> zeros(i - f - 1);
25
                zeros.insert(zeros.end(), d.begin(), d.end());
26
                d = zeros;
27
                vector<ll> temp = c;
28
                c.resize(max(c.size(), d.size()));
29
                for (int j=0; j<(int)d.size(); j++) c[j] += d[j];</pre>
                if (i - (int) temp.size() > f - (int) oldC.size()) {oldC =
31
                    temp;f = i;}
           }
32
       }
33
       return c;
34
35 }
```

4.13 Modular Berlekamp Massey

```
typedef long long int 11;
  long long int inf = 1000000007;
   vector<ll> bermas(vector<ll> x){
       vector<ll> ls,cur;
4
       int lf,ld;
5
       for(int i = 0; i<x.size(); i++){</pre>
6
            long long int t = 0;
7
            for(int j = 0; j < cur.size(); j++) t=(t+x[i-j-1]*(long long int)
8
                cur[i])%inf:
           if((t-x[i])%inf==0)continue;
9
           if(cur.size()==0){cur.resize(i+1);lf=i;ld=(t-x[i])%inf;continue
10
                ;}
            long long int k = (x[i]-t)*powermod(ld,inf-2)%inf;
11
           vector<ll>c(i-lf-1);c.push_back(k);
12
           for(int j = 0; j<ls.size(); j++) c.push_back(-ls[j]*k%inf);</pre>
13
           if(c.size()<cur.size()) c.resize(cur.size());</pre>
14
           for(int j = 0; j<cur.size();j++) c[j]=(c[j]+cur[j])%inf;</pre>
15
            if(i-lf+ls.size()>=cur.size())ls=cur,lf=i,ld=(t-x[i])%inf;
16
                cur=c:
17
     }
18
       for(int i =0; i < cur.size(); i++) cur[i] = (cur[i]%inf+inf)%inf;</pre>
     return cur;
21 }
```

4.14 Matrix exponentiation

```
typedef vector<vector<long long int>> Matrix;
   long long int inf = 1000000007;
   Matrix ones(int n) {
     Matrix r(n,vector<long long int>(n));
     for(int i= 0; i<n; i++){
           r[i][i]=1;
       }
     return r;
8
9
   Matrix operator*(Matrix &a, Matrix &b) {
     int n=a.size(),m=b[0].size(),z=a[0].size();
                                                                                  23
     Matrix r(n,vector<long long int>(m));
12
                                                                                  24
     for(int i=0: i<n: i++){
                                                                                  25
           for(int j=0; j<m; j++){
               for(int k=0; k< z; k++){
                                                                                  27
15
                   r[i][j] += ((a[i][k]\%inf)*(b[k][j]\%inf))\%inf;
16
                   r[i][j]%=inf;}}}
17
     return r;
18
19
                                                                                  31
   Matrix be(Matrix b, long long int e) {
     Matrix r=ones(b.size());
21
     while(e){if(e&1LL)r=r*b;b=b*b;e/=2;}
22
     return r;
                                                                                  35
23
^{24}
                                                                                  37
25
   //Matrix mat(n,vector<long long int>(n));
                     4.15 Ecuaciones Diofantinas
                                                                                  41
  long long int gcd(long long int a, long long int b, long long int& x,
                                                                                  42
       long long int& y) {
                                                                                  43
     x = 1, y = 0;
     long long int x1 = 0, y1 = 1, a1 = a, b1 = b;
                                                                                  45
     while (b1) {
                                                                                  46
                                                                                  47
       int q = a1 / b1;
                                                                                  48
       tie(x, x1) = make_tuple(x1, x - q * x1);
6
      tie(y, y1) = make_tuple(y1, y - q * y1);
       tie(a1, b1) = make_tuple(b1, a1 - q * b1);
9
```

13 bool findAnySol(long long int a, long long int& x, long long int b, long

return a1:

long long int d;

11

```
long int& y, long long int c) {
    long long int g = gcd(abs(a), abs(b), x, y);
    if (c % g != 0) return false;
    x *= c;
    v *= c;
    x /= g;
    y /= g;
    d = c / g;
    if (a < 0) x = -x;
    if (b < 0) y = -y;
    return true;
   //----SOLBEGIN-----
  int main() {
    ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
    long long int m, a, k, n;
    long long int f, h,res;
    //estira en n, y despues cada m
    //estira en k+a, y despues cada a
    cin >> n >> m >> a >> k;
    while (n != 0 \&\& m != 0 \&\& a != 0 \&\& k != 0) {
      m = -m;
      if (!findAnySol(m, f, a, h, k + a - n)) {
        cout << "Impossible" << endl;</pre>
      }else {
        res = f * m+n;
        while (res > 0) res -= m * d;
        while (res < 0) res += m * d;
        cout << res << endl;</pre>
      cin >> n >> m >> a >> k:
49 //-----EOSOLUTION-----
```

4.16 Pollard-Rho, Stolen from GGDem

```
long long int gcd(long long int a, long long int b){return a?gcd(b%a,a):
    b;}
long long int mulmod(long long int a, long long int b, long long int m)
```

```
{
     long long int r=a*b-(long long int)((long double)a*b/m+.5)*m;
3
     return (r<0?r+m:r);</pre>
4
5
   long long int expmod(long long int b, long long int e, long long int m){
     if(!e)return 1;
     long long int q=expmod(b,e/2,m);q=mulmod(q,q,m);
     return (e&1?mulmod(b,q,m):q);
10
   bool is_prime_prob(ll n, int a){
11
     if(n==a)return true;
12
     long long int s=0,d=n-1;
13
     while(d\%2==0)s++,d/=2:
     long long int x=expmod(a,d,n);
15
     if((x==1)||(x+1==n))return true:
16
     for(int i = 0; i < s-1; i++){
17
       x=mulmod(x,x,n);
18
       if(x==1)return false;
19
       if(x+1==n)return true:
20
21
     return false;
22
23
   bool rabin(long long int n){ // true iff n is prime
24
     if(n==1)return false;
25
     int A[]=\{2,3,5,7,11,13,17,19,23\};
26
       for(int a: A) if(!is_prime_prob(n,a))return false;
27
     return true;
28
29
   long long int rho(long long int n){
30
       if(!(n&1))return 2;
31
       long long int x=2,y=2,d=1;
32
       long long int c=rand()%n+1;
33
       while(d==1){
34
           x=(\text{mulmod}(x,x,n)+c)%n;
35
           y=(mulmod(y,y,n)+c)%n;
36
           y=(\text{mulmod}(y,y,n)+c)%n;
37
           if(x>=y)d=gcd(x-y,n);
38
           else d=gcd(y-x,n);
39
       }
40
       return d==n?rho(n):d;
41
42
   void fact(long long int n, map<long long int,int>& f){ //0 (lg n)^3
     if(n==1)return;
```

```
if(rabin(n)){f[n]++;return;}
long long int q=rho(n);
fact(q,f);fact(n/q,f);
}
```

4.17 FFT, Stolen from GGDem

```
1 // SPOJ VFMUL - AC
   // http://www.spoj.com/problems/VFMUL/
   #include <bits/stdc++.h>
   #define fst first
   #define snd second
   #define fore(i,a,b) for(int i=a,ThxDem=b;i<ThxDem;++i)</pre>
   #define pb push_back
   #define ALL(s) s.begin(),s.end()
   #define FIN ios_base::sync_with_stdio(0);cin.tie(0);cout.tie(0)
   #define SZ(s) int(s.size())
   using namespace std;
   typedef long long 11;
   typedef pair<int,int> ii;
   // MAXN must be power of 2 !!
   // MOD-1 needs to be a multiple of MAXN !!
   // big mod and primitive root for NTT:
   const int MOD=998244353,RT=3,MAXN=1<<20;
   typedef vector<int> poly;
   // FFT
20
   struct CD {
21
     double r,i;
22
     CD(double r=0, double i=0):r(r),i(i){}
23
     double real()const{return r;}
24
     void operator/=(const int c){r/=c, i/=c;}
25
26
   CD operator*(const CD& a, const CD& b){
27
     return CD(a.r*b.r-a.i*b.i,a.r*b.i+a.i*b.r);}
   CD operator+(const CD& a, const CD& b){return CD(a.r+b.r,a.i+b.i);}
   CD operator-(const CD& a, const CD& b){return CD(a.r-b.r,a.i-b.i);}
   const double pi=acos(-1.0);
   // NTT
32
33
   struct CD {
     int x;
35
     CD(int x):x(x){}
36
```

```
CD(){}
37
     int get()const{return x;}
38
39
   CD operator*(const CD& a, const CD& b){return CD(mulmod(a.x,b.x));}
40
   CD operator+(const CD& a, const CD& b){return CD(addmod(a.x,b.x));}
   CD operator-(const CD& a, const CD& b){return CD(submod(a.x,b.x));}
    vector<int> rts(MAXN+9,-1);
   CD root(int n, bool inv){
     int r=rts[n]<0?rts[n]=pm(RT,(MOD-1)/n):rts[n];</pre>
     return CD(inv?pm(r,MOD-2):r);
47
48
   CD cp1[MAXN+9],cp2[MAXN+9];
   int R[MAXN+9]:
   void dft(CD* a, int n, bool inv){
     fore(i,0,n)if(R[i]<i)swap(a[R[i]],a[i]);</pre>
     for(int m=2;m<=n;m*=2){</pre>
53
       double z=2*pi/m*(inv?-1:1); // FFT
54
       CD wi=CD(cos(z),sin(z)): // FFT
55
       // CD wi=root(m,inv); // NTT
56
       for(int j=0; j<n; j+=m){
57
         CD w(1);
58
         for(int k=j,k2=j+m/2;k2<j+m;k++,k2++){</pre>
59
           CD u=a[k]; CD v=a[k2]*w; a[k]=u+v; a[k2]=u-v; w=w*wi;
60
         }
61
       }
62
63
     if(inv)fore(i,0,n)a[i]/=n; // FFT
64
     //if(inv){ // NTT
65
     // CD z(pm(n,MOD-2)); // pm: modular exponentiation
66
     // fore(i,0,n)a[i]=a[i]*z;
67
     //}
68
69
   poly multiply(poly& p1, poly& p2){
     int n=p1.size()+p2.size()+1;
71
     int m=1,cnt=0;
72
     while(m<=n)m+=m,cnt++;</pre>
73
     fore(i,0,m){R[i]=0;fore(j,0,cnt)R[i]=(R[i]<<1)|((i>>j)&1);}
74
     fore(i,0,m)cp1[i]=0,cp2[i]=0;
75
     fore(i,0,p1.size())cp1[i]=p1[i];
76
     fore(i,0,p2.size())cp2[i]=p2[i];
77
     dft(cp1,m,false);dft(cp2,m,false);
78
     fore(i,0,m)cp1[i]=cp1[i]*cp2[i];
79
```

```
dft(cp1,m,true);
80
      poly res;
81
      n-=2:
82
      fore(i,0,n)res.pb((11)floor(cp1[i].real()+0.5)); // FFT
83
      //fore(i,0,n)res.pb(cp1[i].x); // NTT
84
      return res;
85
    }
86
87
    char s[MAXN],t[MAXN],r[MAXN];
89
    int main(){
90
      int tn;
91
      scanf("%d",&tn);
92
      while(tn--){
93
        vector<int> a,b,c;
94
        scanf("%s%s",s,t);
95
        for(int i=0;s[i];++i)a.pb(s[i]-'0');reverse(a.begin(),a.end());
        for(int i=0;t[i];++i)b.pb(t[i]-'0');reverse(b.begin(),b.end());
        c=multiply(a,b);
98
        while(!c.empty()&&!c.back())c.pop_back();
        if(c.empty()){puts("0");continue;}
        int n=0;
101
        11 x=0;
102
        fore(i,0,c.size()){
103
          x+=c[i];
104
          r[n++]=x%10;
105
          x/=10;
106
        }
107
        while(x){
108
109
          r[n++]=x%10;
          x/=10;
110
111
        reverse(r.r+n):
112
        bool p=false;
113
        fore(i,0,n){
114
          putchar(r[i]+'0');
115
        }
116
        puts("");
117
118
119
      return 0;
120 }
```

5 Geometry

6 Strings

6.1 Explode by token

```
//#include <sstream>
2
   vector<string> explode(string const& s, char delim) {
3
     vector<string> result;
4
     istringstream iss(s);
5
     for (string token; getline(iss, token, delim); )
6
7
       result.push_back(move(token));
8
     }
9
     return result;
10
11 }
```

6.2 Multiple Hashings DS

```
struct multhash{
       unsigned long long int h1,h2;
2
       unsigned long long int alf[257];
3
       bool operator < (multhash b) const {</pre>
       if (h1 != b.h1) return h1 < b.h1;</pre>
5
       return h2 < b.h2:
6
7
     bool operator == (multhash b) const { return (h1== b.h1 && h2== b.h2)
8
     bool operator != (multhash b) const { return !(h1== b.h1 && h2== b.h2)
9
          ;}
   public:
10
       string s;
11
       multhash(){
12
           h1 = 0; h2 = 0; s = "";
13
           for(char 1 = 'a'; 1 <= 'z'; 1++) alf [1] = 1-'a'+1;
14
       }
15
       void innit(){
16
           unsigned long long int inf,p,op;
17
18
           inf = 999727999;
19
           p = 325255434; op = 325255434;
20
           for(char 1: s){
21
```

```
h1+=(p*alf[1])%inf;
22
               p*=op;
23
               p%=inf;
^{24}
           }
25
26
           inf = 1070777777;
27
           p = 10018302; op = 10018302;
28
           for(char 1: s){
29
               h2+=(p*alf[1])%inf;
               p*=op;
31
               p%=inf;
32
33
       }
34
35
   //VALORES ALTERNATIVOS DE INF, LOG 17
   //666666555557777777
   //986143414027351997
   //974383618913296759
   //973006384792642181
   //953947941937929919
   //909090909090909091
   //VALORES PARA P, USAR PRIMOS MAYORES A |Alfabeto|
44 //31,47,53,61,79
                     6.3 Permute chars of string
void permute(string str){
     // Sort the string in lexicographically
     // ascennding order
     sort(str.begin(), str.end());
4
5
     // Keep printing next permutation while there
6
     // is next permutation
7
     do {
       cout<<str<<endl;</pre>
    } while (next_permutation(str.begin(), str.end()));
11 }
                 6.4 Longest common subsequence
1 //O(|te|*|pa|)
  //cambiar score para otros problemas, str all match = +2, miss/ins/del =
3 //usar char que no este en el alfabeto para denotar del/ins
```

i++; j++;

15

```
if(j==P.size()){//match, do anything
4 string te,pa;
                                                                                     16
  long long int ninf = -10e13;
                                                                                                     res++; j = bt[j];
                                                                                    17
   long long int score(char a, char b){
                                                                                                }
                                                                                     18
       if(a=='*' || b=='*') return 0;
                                                                                            }
                                                                                     19
       if(a==b) return 1;
                                                                                            return res;
                                                                                     20
                                                                                    21 }
       return ninf;
9
10
                                                                                                                  6.6 Suffix Array
   long long int lcs(){
11
       long long int** dp;te = "*"+te; pa = "*"+pa;
12
       long long int res = 0;
                                                                                     1 //se asume que la longitud de la cadena sera menor a 10**6, modificar el
13
14
                                                                                             ub a discrecion
       dp = new long long int*[te.size()];
15
                                                                                       #define ub 1000000LL
       for(int i = 0; i<te.size(); i++) dp[i] = new long long int[pa.size()</pre>
                                                                                       //pot de ub times two
16
           ]();
                                                                                        #define ccd 12
17
                                                                                     5
       for(int r = 1; r < te.size(); r + + ){
                                                                                        //metodos y structs auxiliares para el suffix array
18
           for(int c = 1; c<pa.size(); c++){</pre>
19
                                                                                        struct sufd{int id;long long int t;};
                dp[r][c] = dp[r-1][c-1] + score(te[r], pa[c]);
20
                                                                                        int getndigit(long long int num, int d){
                dp[r][c] = max(dp[r][c-1]+score(te[r], '*'), dp[r][c]);
                                                                                            while(d--) num/=10LL;
21
                dp[r][c] = max(dp[r-1][c]+score('*',pa[c]),dp[r][c]);
                                                                                            return (int) (num%10LL);
22
                                                                                     10
23
                                                                                    11
       }
24
                                                                                        void radixSort(vector<sufd>& arr){
                                                                                            int count[10]; int n = arr.size();
25
                                                                                    13
       return dp[te.size()-1][pa.size()-1];
                                                                                            vector<sufd> aux(n):
26
                                                                                    14
27 }
                                                                                            for(int d = 0: d < ccd: d++){
                                                                                    15
                                                                                                for(int i = 0; i<10; i++) count[i] = 0;
                                                                                    16
                                 6.5 KMP
                                                                                                for(int i = 0; i<n; i++) count[getndigit(arr[i].t,d)]++;</pre>
                                                                                    17
                                                                                                for(int i = 1; i<10; i++) count[i]+=count[i-1];</pre>
                                                                                    18
                                                                                                for(int i = n-1; i>=0; i--){
string T,P;
                                                                                    19
                                                                                                    count[getndigit(arr[i].t,d)]--;
  int bt[MAXN];
                                                                                    20
                                                                                                    aux[count[getndigit(arr[i].t,d)]] = arr[i];
   //O(|Text|+|Pattern|)
                                                                                    21
   void KMPpre(){
                                                                                    22
4
       int i = 0, j = -1; bt[0] = -1;
                                                                                                for(int i = 0; i<n; i++) arr[i] = aux[i];</pre>
                                                                                    23
5
       while(i<P.size()){</pre>
                                                                                    24
6
           while(j \ge 0 \&\& P[i]!=P[(j \ge 0?j:0)]) j = bt[j];
7
                                                                                    25
           i++; j++; bt[i] = j;
                                                                                        //El suffix array mismo, agregar caracter menor al alfabeto al final de
8
       }
9
   }
                                                                                    27 string T.P:
10
                                                                                    28 int* sa,*lcest;
   int kmp(){
11
       int res =0, i = 0, j = 0;
                                                                                    29 int stsize;
12
       while(i<T.size()){</pre>
                                                                                        void makesa(){
13
           while(j \ge 0 \&\& T[i] != P[(j \ge 0?j:0)])  j = bt[j];
                                                                                            int n = T.size();
                                                                                    31
14
```

32

sa = new int[n+1](); int* ra = new int[2*n+2]();

```
for(int i = 0; i<n; i++){sa[i] = i; ra[i] = T[i];}
                                                                                           delete[] lce; delete[] rank;
33
                                                                                   74
                                                                                      1
                                                                                   75
34
       sufd aux;vector<sufd> arr(n);
                                                                                      int recque(int 1, int r, int sti, int stil, int stir){
                                                                                   76
35
       for(int k = 1; k < n; k = 2){
                                                                                           if(stir<l || stil>r) return ub;
36
           arr.clear();
                                                                                           if(l<=stil && stir<=r) return lcest[sti];</pre>
                                                                                   78
37
           for(int i = 0; i < n; i++){
                                                                                           int stim = stil+stir; stim/=2;
38
                                                                                   79
                                                                                           return min(recque(1,r,sti*2+1,stil,stim),recque(1,r,sti*2+2,stim+1,
               aux.id = sa[i]; aux.t = ra[sa[i]];aux.t*=ub;aux.t += ra[sa[i
                                                                                   80
39
                    ]+k]:
                                                                                               stir));
               arr.push_back(aux);
                                                                                       }
                                                                                   81
40
                                                                                       int getlce(int 1, int r){
41
           //en caso de TLE calar con STL sort
                                                                                           if(1>r) return 0;
42
           radixSort(arr):
                                                                                           return recque(1,r,0,0,stsize/2);
43
                                                                                   84
           sa[0] = arr[0].id; ra[sa[0]] = 0;
                                                                                       }
44
                                                                                   85
           for(int i = 1: i < n: i++){
                                                                                       int buscarRec(int 1, int r,int lcp,int eas){
               sa[i] = arr[i].id;
                                                                                           if(l>r) return -1;
                                                                                   87
               ra[sa[i]] = ra[sa[i-1]]+1;
                                                                                           int m = (1+r)/2;
               if(arr[i].t == arr[i-1].t) ra[sa[i]]--;
                                                                                           //string curr = T.substr(sa[m],T.size()-sa[m]);
48
                                                                                           int lce = (eas>m?getlce(m+1,eas):getlce(eas+1,m));
49
           if(ra[sa[n-1]]==n-1) break:
                                                                                           if(lce>lcp){
50
                                                                                               if(eas<m) return buscarRec(m+1,r,lcp,eas);</pre>
       }
51
       delete[]ra;
                                                                                               if(eas>m) return buscarRec(1,m-1,lcp,eas);
52
                                                                                           }
53
   void makelce(){
                                                                                           if(lce<lcp){</pre>
                                                                                   95
54
       int n = T.size();
                                                                                               if(eas>m) return buscarRec(m+1,r,lcp,eas);
55
       int* lce = new int[n+2]();
                                                                                               if(eas<m) return buscarRec(1,m-1,lcp,eas);</pre>
                                                                                   97
56
       int* rank = new int[n+2]();
                                                                                           }
                                                                                   98
57
       for(int i = 0; i<n; i++) rank[sa[i]] = i;</pre>
                                                                                   99
58
                                                                                           for(int i = lcp,n = T.size(); sa[m]+i<n && i<P.size(); i++){if(P[i</pre>
                                                                                   100
59
                                                                                               ]!=T[sa[m]+i]) break; lcp++;}
       int curr = 0;
60
       for(int i= 0; i<n; i++){
                                                                                           if(lcp == P.size()) return m;
                                                                                   101
61
           if(rank[i]==0) continue;
                                                                                           if(l==r) return -1;
                                                                                   102
62
           for(int j = max(curr-1,0); j+max(i,sa[rank[i]-1])<n; j++){</pre>
                                                                                           return (P[lcp]>T[sa[m]+lcp]?buscarRec(m+1,r,lcp,m):buscarRec(1,m-1,
                                                                                   103
63
               if(T[i+j] == T[sa[rank[i]-1]+j]) curr = j;
                                                                                               lcp,m));
64
               if(T[i+j]!=T[sa[rank[i]-1]+j]){curr = j-1; break;}
                                                                                   104
65
           }
                                                                                   int buscar(){
66
           curr++;lce[i] = curr;
                                                                                   106
                                                                                           int n = T.size();
67
       }
                                                                                           if(P.size()>n) return -1;
                                                                                   107
68
                                                                                           return buscarRec(1,n-1,0,0);
                                                                                   108
69
       int p = 1; while(p \le n) p = 2; stsize = 2 p - 1;
                                                                                   109
70
       lcest = new int[stsize+2]();
                                                                                       //CODIGO DE 100 LINEAS, TE HE FALLADO MarcosK
71
       for(int i= p-1; i-(p-1)<n; i++) lcest[i] = lce[sa[i-(p-1)]];</pre>
                                                                                   //Uso: lee T, agregar signo dolar, llama makesa(); makelce(); lee P para
72
       for(int i = p-2; i>=0; i--) lcest[i] = min(lcest[2*i+1],lcest[2*i +
                                                                                            despues buscar()
73
                                                                                  //delete[] sa; delete[] lcest; cuando leas de nuevo T
           2]);
```

32

33

if(ra[sa[n-1]]==n-1) break;

```
\frac{1}{1} \frac{1}
                                                                                                                                                                                      }
                                                                                                                                                                       34
     //Buscar devuelve un indice cualquiera de sa tal que el sufijo denotado
                                                                                                                                                                                      delete[]ra;
                                                                                                                                                                       35
               tenga P como prefijo
                                                                                                                                                                             }
                                                                                                                                                                       36
115 //Se puede hacer mas corto?
                                                                                                                                                                              void makelce(){
                                                                                                                                                                                      int n = T.size();
                                                                                                                                                                       38
                                                              STL Suffix Array
                                                                                                                                                                                      int* lce = new int[n+2]();
                                                                                                                                                                                      int* rank = new int[n+2]();
                                                                                                                                                                       40
                                                                                                                                                                                      for(int i = 0; i<n; i++) rank[sa[i]] = i;</pre>
  1 //se asume que la longitud de la cadena sera menor a 10**6, modificar el
                  ub a discrecion
                                                                                                                                                                       42
                                                                                                                                                                                      int curr = 0;
      #define ub 1000000LL
                                                                                                                                                                       43
                                                                                                                                                                                      for(int i= 0; i<n; i++){
       //pot de ub times two
                                                                                                                                                                       44
                                                                                                                                                                                              if(rank[i]==0) continue;
       #define ccd 12
                                                                                                                                                                       45
                                                                                                                                                                                              for(int j = max(curr-1,0); j+max(i,sa[rank[i]-1]) < n; j++){
       //metodos y structs auxiliares para el suffix array
                                                                                                                                                                       46
                                                                                                                                                                                                       if(T[i+j] == T[sa[rank[i]-1]+j]) curr = j;
       struct sufd{int id;long long int t;
                                                                                                                                                                       47
                                                                                                                                                                                                       if(T[i+j]!=T[sa[rank[i]-1]+j]){curr = j-1; break;}
               bool operator<(const sufd b) const{return t<b.t;}</pre>
                                                                                                                                                                       48
       };
  8
                                                                                                                                                                                              curr++;lce[i] = curr;
        //El suffix array mismo, agregar caracter menor al alfabeto al final de
                                                                                                                                                                       50
                                                                                                                                                                                      }
      string T,P;
                                                                                                                                                                       52
                                                                                                                                                                                      int p = 1; while(p \le n) p = 2; stsize = 2 \cdot p - 1;
      int* sa,*lcest;
                                                                                                                                                                                      lcest = new int[stsize+2]();
      int stsize:
                                                                                                                                                                                      for(int i= p-1; i-(p-1) < n; i++) lcest[i] = lce[sa[i-(p-1)]];
       void makesa(){
                                                                                                                                                                                      for(int i = p-2; i>=0; i--) lcest[i] = min(lcest[2*i+1],lcest[2*i +
               int n = T.size();
                                                                                                                                                                       56
 14
                                                                                                                                                                                              2]);
               sa = new int[n+1](): int* ra = new int[2*n+2]():
 15
               for(int i = 0; i<n; i++){sa[i] = i; ra[i] = T[i];}
                                                                                                                                                                                      delete[] lce; delete[] rank;
                                                                                                                                                                       57
 16
                                                                                                                                                                       58
 17
                                                                                                                                                                              int recque(int 1, int r, int sti, int stil, int stir){
               sufd aux;vector<sufd> arr(n);
 18
                                                                                                                                                                                      if(stir<l || stil>r) return ub;
               for(int k = 1; k < n; k = 2){
 19
                                                                                                                                                                                      if(l<=stil && stir<=r) return lcest[sti];</pre>
                       arr.clear();
                                                                                                                                                                       61
20
                                                                                                                                                                                      int stim = stil+stir; stim/=2;
                       for(int i = 0; i < n; i + +){
21
                                                                                                                                                                                      return min(recque(1,r,sti*2+1,stil,stim),recque(1,r,sti*2+2,stim+1,
                                aux.id = sa[i]; aux.t = ra[sa[i]];aux.t*=ub;aux.t += ra[sa[i
                                                                                                                                                                       63
22
                                                                                                                                                                                              stir));
                                        ]+k];
                                arr.push_back(aux);
                                                                                                                                                                       64
23
                                                                                                                                                                             int getlce(int 1, int r){
                       }
24
                                                                                                                                                                                      if(l>r) return 0;
                        //en caso de TLE calar con STL sort
25
                                                                                                                                                                                      return recque(1,r,0,0,stsize/2);
                                                                                                                                                                       67
                        sort(arr.begin(),arr.end());
26
                        sa[0] = arr[0].id; ra[sa[0]] = 0;
                                                                                                                                                                       68
27
                                                                                                                                                                             int buscarRec(int 1, int r,int lcp,int eas){
                       for(int i = 1; i < n; i++){}
28
                                                                                                                                                                                      if(l>r) return -1;
                                sa[i] = arr[i].id:
                                                                                                                                                                       70
29
                                                                                                                                                                                      int m = (1+r)/2;
                                ra[sa[i]] = ra[sa[i-1]]+1;
30
                                                                                                                                                                                     //string curr = T.substr(sa[m],T.size()-sa[m]);
                                if(arr[i].t == arr[i-1].t) ra[sa[i]]--;
31
```

int lce = (eas>m?getlce(m+1,eas):getlce(eas+1,m));

if(lce>lcp){

74

```
if(eas<m) return buscarRec(m+1,r,lcp,eas);</pre>
75
            if(eas>m) return buscarRec(1,m-1,lcp,eas);
76
        }
77
        if(lce<lcp){</pre>
78
            if(eas>m) return buscarRec(m+1,r,lcp,eas);
79
            if(eas<m) return buscarRec(1,m-1,lcp,eas);</pre>
80
        }
81
82
        for(int i = lcp,n = T.size(); sa[m]+i<n && i<P.size(); i++){if(P[i</pre>
83
            ]!=T[sa[m]+i]) break; lcp++;}
        if(lcp == P.size()) return m;
84
        if(l==r) return -1;
85
        return (P[lcp]>T[sa[m]+lcp]?buscarRec(m+1,r,lcp,m):buscarRec(1,m-1,
            lcp,m));
87
    int buscar(){
        int n = T.size();
89
        if(P.size()>n) return -1;
90
        return buscarRec(1,n-1,0,0);
91
92
    pair<int,int> primeraYUltimaOc(){
93
        int sai = buscar();
94
        pair<int,int>res = {sai,sai};
95
        if(sai==-1) return res;
96
97
        int l,r,m;
98
99
        r = sai-1; l = 0;
100
        while(l<=r){</pre>
101
            m = (1+r)/2:
102
            if(getlce(m+1,sai)>=P.size()){
103
                 res.first = m; r = m-1;
104
            }else{
105
                 1 = m+1:
106
            }
107
108
        l = sai+1; r = T.size()-1;
109
        while(l<=r){</pre>
110
            m = (1+r)/2;
111
            if(getlce(sai+1,m)>=P.size()){
112
                 res.second = m; l = m+1;
113
            }else{
114
                 r = m-1;
115
```

7 Clasicos

7.1 Job scheduling

7.1.1 One machine, linear penalty

7.1.2 One machine, deadlines

```
//calcula la maxima cantidad de jobs que se pueden hacer dados sus
    deadlines y duraciones en O(n log n)
struct Job {
    int deadline, duration, idx;

    bool operator<(Job o) const {
        return deadline < o.deadline;
    }
};
vector<int> compute_schedule(vector<Job> jobs) {
```

```
sort(jobs.begin(), jobs.end());
10
11
       set<pair<int,int>> s;
12
       vector<int> schedule;
13
       for (int i = jobs.size()-1; i >= 0; i--) {
14
           int t = jobs[i].deadline - (i ? jobs[i-1].deadline : 0);
15
           s.insert(make_pair(jobs[i].duration, jobs[i].idx));
16
           while (t && !s.empty()) {
17
                auto it = s.begin();
18
                if (it->first <= t) {</pre>
19
                    t -= it->first;
20
                    schedule.push_back(it->second);
21
                } else {
22
                    s.insert(make_pair(it->first - t, it->second));
23
                    t = 0:
24
25
                s.erase(it);
26
           }
27
       }
28
       return schedule;
29
30 }
```

7.1.3 One machine, profit

```
1 // Dado n Jobs y su profit, calcula cual es el mayor profit que se puede
        obtener en O(n^2)
struct Job{int start, finish, profit;};
  bool jobComparataor(Job s1, Job s2){return (s1.finish < s2.finish);}</pre>
   // Find the latest job (in sorted array) that doesn't
  // conflict with the job[i]. If there is no compatible job,
   // then it returns -1.
  vector <Job> arr;
   int* memo:
  int latestNonConflict( int i){
9
    for (int j = i - 1; j >= 0; j--)
10
       if (arr[j].finish <= arr[i - 1].start)</pre>
11
         return j;
12
    return -1:
13
14
   // A recursive function that returns the maximum possible
   // profit from given array of jobs. The array of jobs must
  // be sorted according to finish time.
  int findMaxProfitRec( int n){
```

```
// Base case
19
     if (n == 1) return arr[n - 1].profit;
20
       if (memo[n]>=0) return memo[n];
21
     // Find profit when current job is included
22
     int inclProf = arr[n - 1].profit;
23
     int i = latestNonConflict(n);
24
     if (i != -1) inclProf += findMaxProfitRec( i + 1);
25
26
     // Find profit when current job is excluded
27
     int exclProf = findMaxProfitRec( n - 1);
28
29
     return memo[n]=max(inclProf, exclProf);
30
31
32
   // The main function that returns the maximum possible
   // profit from given array of jobs
   int findMaxProfit( int n){
     sort(arr.begin(),arr.end(), jobComparataor);
     return findMaxProfitRec(n);
38 }
```

7.1.4 Two machines, min time

```
1 //Obtiene el ordenamiento optimo de Jobs en dos maquinas en O(n log n)
   struct Job {
       int a, b, idx;
3
       bool operator<(Job o) const {return min(a, b) < min(o.a, o.b);}</pre>
4
   };
5
   vector<Job> johnsons_rule(vector<Job> jobs) {
       sort(jobs.begin(), jobs.end());
       vector<Job> a, b;
8
       for (Job j : jobs) {
9
           if (j.a < j.b)
10
                a.push_back(j);
11
           else
12
                b.push_back(j);
13
14
       a.insert(a.end(), b.rbegin(), b.rend());
15
       return a:
16
   }
17
18
  pair<int, int> finish_times(vector<Job> const& jobs) {
19
       int t1 = 0, t2 = 0;
```

```
for (Job j : jobs) {
    t1 += j.a;
    t2 = max(t2, t1) + j.b;
}
return make_pair(t1, t2);
}
```

8 Flow

8.1 Dinic, thx GGDem

```
#define pb push_back
   #define mp make_pair
   #define fst first
   #define snd second
   #define ALL(s) s.begin(),s.end()
   #define SZ(x) int((x).size())
   #define fore(i,a,b) for(int i=a,to=b;i<to;++i)</pre>
   using namespace std;
   typedef long long 11;
   #define INF (1LL<<62)
   // Min cut: nodes with dist>=0 vs nodes with dist<0
   // Matching MVC: left nodes with dist<0 + right nodes with dist>0
   struct Dinic{
     int nodes,src,dst;
15
     vector<int> dist,q,work;
16
     struct edge {int to,rev;ll f,cap;};
17
     vector<vector<edge>> g;
18
     Dinic(int x):nodes(x),g(x),dist(x),q(x),work(x){}
19
     void add_edge(int s, int t, ll cap){
20
       g[s].pb((edge){t,SZ(g[t]),0,cap});
21
       g[t].pb((edge){s,SZ(g[s])-1,0,0});
^{22}
23
     bool dinic_bfs(){
24
       fill(ALL(dist),-1);dist[src]=0;
25
       int qt=0;q[qt++]=src;
26
       for(int qh=0;qh<qt;qh++){</pre>
27
         int u=q[qh];
28
         fore(i,0,SZ(g[u])){
29
           edge &e=g[u][i];int v=g[u][i].to;
30
           if(dist[v]<0&&e.f<e.cap)dist[v]=dist[u]+1,q[qt++]=v;</pre>
31
32
```

```
}
33
       return dist[dst]>=0;
34
35
     11 dinic_dfs(int u, ll f){
36
       if(u==dst)return f;
37
       for(int &i=work[u];i<SZ(g[u]);i++){</pre>
38
          edge &e=g[u][i];
39
          if(e.cap<=e.f)continue;</pre>
40
          int v=e.to;
          if(dist[v]==dist[u]+1){
            11 df=dinic_dfs(v,min(f,e.cap-e.f));
43
            if(df>0){e.f+=df;g[v][e.rev].f-=df;return df;}
44
         }
45
       }
46
       return 0;
47
     }
48
     11 max_flow(int _src, int _dst){
49
       src=_src;dst=_dst;
50
       11 result=0:
51
       while(dinic_bfs()){
         fill(ALL(work),0);
53
          while(ll delta=dinic_dfs(src,INF))result+=delta;
54
       }
55
       return result;
56
57
   };
58
59
                ----SOLBEGIN----
60
   int main() {
61
     ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
       //l set,r set
63
       int n,m;
64
       cin>>n>>m:
65
       m+=n;
66
       Dinic d(n+m+2);
67
       for(int i = 1; i \le n; i++) d.add_edge(0,i,1);
68
       for(int i = n+1; i<=m; i++) d.add_edge(i,m+1,1);</pre>
69
70
       int fin,q;
71
       for(int i = 1; i \le n; i++){
72
            cin>>q;
73
            while(q--){
74
                cin>>fin;
75
```

```
d.add_edge(i,n+fin,1);
76
          }
77
      }
78
      int res =d.max_flow(0,m+1);
79
      m-=n;
80
      //how many were left unmatched
81
      cout<<m-res<<endl;</pre>
82
83
                  -----EOSOLUTION------
```

9 Miscellaneous

9.1 pbds

```
| #include "bits/stdc++.h"
  #include <bits/extc++.h>
   using namespace __gnu_pbds;
   using namespace std;
   typedef tree<pair<int,int>, null_type,less<pair<int,int>>, rb_tree_tag,
       tree_order_statistics_node_update> ost;
  using namespace std;
   int main(){
       ost arbol;
       int n = 5;
9
       for(int id = 1; id<=n; id++)
10
           for(int val = 0; val<n; val++)</pre>
11
               arbol.insert({val,id});
12
       //te da el valor mas pequenio, en caso de empate te da el del id mas
13
       cout<<(*arbol.find_by_order(0)).first<<"u"<<(*arbol.find_by_order(0))</pre>
14
           ).second<<endl:
       //te da el indice (base 0) de la primera ocurrencia de .first
15
       cout<<arbol.order_of_key({1,-1})<<endl;;</pre>
16
17 }
```

9.2 Bit Manipulation

```
#include "bits/stdc++.h"
using namespace std;
#define endl '\n'

int main() {
```

```
ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
     //Se representan bitmasks de 30 a 62 bits
8
     //usando signed int y signed long long int
     //para evitar problemas con el complemento de dos
     signed int a, b;
11
     //para multiplicar un numero por dos solo es necesario aplicar un
     // shifteo de sus bits a la izquierda
13
     a = 1;
14
     a= a << 3;
     cout << a << endl;</pre>
     //para dividir un numero entre dos es necesario aplicar un
17
     //shifteo a la derecha
18
     a = 32:
19
     a = a >> 3;
20
     cout << a << endl;</pre>
     //para encender el bit n de a, solo hay que igualar a = a \mid pow(2,n-1)
     //prende el tercer bit
     a = 1;
     b = 1 << 2:
     a = a \mid b;
     cout << a << endl;</pre>
27
     //para apagar el bit n de a, solo hay que a &= ~pow(2,n-1)
     //prende el tercer bit
29
     a = 5;
     b = 1 << 2;
31
     a &= ~b;
     cout << a << endl;</pre>
33
     //para revisar si el bit n de a esta encendido
     //revisa si el tercer bit esta encendido
35
     a = 5:
36
     b = 1 << 2;
37
     a = a \& b;
38
     cout << (a?"SI":"NO") << endl;</pre>
39
     //para volter el bit n de a, solo hay que igualar a = a ^{\circ} pow(2,n-1)
40
     //apaga el tercer bit
41
     a = 5;
42
     b = 1 << 2;
43
     a = a ^ b;
     cout << a << endl;</pre>
     //para obtener el bit menos significativo que esta encendido a& -a
46
     cout << log2(a & ((-1) * a))+1 << endl;
     //para prender todos los bits hasta n
```

```
a = (1 << 4) - 1:
     cout << a << endl;</pre>
51
52
          -----EOSOLUTION-----
   #include "bits/stdc++.h"
   using namespace std;
   #define endl '\n'
   #pragma GCC optimize("03")
   #pragma GCC target("popcnt")
   //no usar con visual c++
   //solo con g++ like compilers
   int main() {
     ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
     signed long long int a, b, n;
11
     //Obtain the remainder (modulo) of a when it is divided by n (n is a
12
         power of 2)
     a = 15; n = 8-1;
     a &= n:
     cout << \frac{a}{n}, \frac{a}{2} = 15, \frac{n}{2} = 2^3 << endl;
     cout << a << endl:</pre>
16
     //Apaga el bit menos significativo de a
17
     a = 14:
18
     b = (a & ((-1) * a));
19
     a &= ~b:
20
     cout << a << endl:</pre>
21
     //enciende el ultimo cero de a
     a = 9;
23
     b = a;
24
     b = (b & ((-1) * b));
25
     a = a \mid b;
26
     cout << a<<endl:</pre>
27
     //contar bits encendidos en a
28
     cout << __builtin_popcount(a)<<endl;</pre>
29
     //checar la paridad de a
30
     cout << (_builtin_parity(a) ? "IMPAR" : "PAR") << endl;</pre>
31
     //contar leading zeroes en a
32
     cout << __builtin_clz(a)<<endl;</pre>
33
     //contar 9, trailling zeroes en a
     cout << __builtin_ctz(a)<<endl;</pre>
35
36
                -----EOSOLUTION-----
```

10 Testing

10.1 Gen and AutoRun testcases

10.1.1 Gen.cpp

```
1 #include <iostream>
   #include <string.h>
   #include <random>
   #include <chrono>
   using namespace std;
   //args nombreDelEjecutable, seed, len
   int main (int argc, char **argv) {
       // argv is an array of strings
       // atoi is a C function for converting a string into an int
       mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());
       srand(atoi(argv[1])); // srand sets the random seed
11
       int n = atoi(argv[2]);
12
       int d = rng()\%n; d++;
13
       string test = "";
       for (int i = 0; i < n; i++) {
15
           test+= \frac{a}{(rng())(26)};
16
17
       cout<<test<<""<<d<<endl;
18
19 }
```

10.1.2 Stress testing

```
g++ -std=c++14 gen.cpp -o gen
g++ -std=c++14 lazy.cpp -v -o lazy
   g++ -std=c++14 lazyn.cpp -v -o lazyn
  for i in 'seq 1 $1'; do
       # prints the current test number
       # I like to do this so I can see progress is being made
6
       #chmod +x test.sh
7
       echo $i
8
       ./gen $i $((1 + i%14)) > input.txt #pasa al generador una longitud
9
           entre 1 y 14, para hacer operaciones matematicas, usar $((a+b))
       ./lazy < input.txt > output.txt
10
       ./lazyn < input.txt > answer.txt
11
12
13
       diff output.txt answer.txt || break
14 done
```

g++ -std=c++14 gen.cpp -o gen g++ -std=c++14 lazy.cpp -v -o lazy for i in 'seq 1 \$1'; do # prints the current test number # I like to do this so I can see progress is being made 5 #chmod +x test.sh 6 echo \$i 7 8 ./gen i ((1 + i/14)) > input.txt9 ./lazy < i\${i}.txt > o\${i}.txt 11 diff a\${i}.txt o\${i}.txt || break 13 done

10.2 Highly Composite Numbers

10.1.3 Autorun

Particularly useful when testing number theoretical solutions.

1	1	1	
2	2	2	2
3	4	3	2^2
4	6	4	2*3
5	12	6	2^2*3
6	24	8	2^3*3
7	36	9	2^2*3^2
8	48	10	2^4*3
9	60	12	2^2*3*5
10	120	16	2^3*3*5
11	180	18	2^2*3^2*5
12	240	20	2^4*3*5
13	360	24	2^3*3^2*5
14	720	30	2^4*3^2*5
15	840	32	2^3*3*5*7
16	1260	36	2^2*3^2*5*7
17	1680	40	2^4*3*5*7
18	2520	48	2^3*3^2*5*7
19	5040	60	2^4*3^2*5*7
20	7560	64	2^3*3^3*5*7
21	10080	72	2^5*3^2*5*7
22	15120	80	2^4*3^3*5*7
23	20160	84	2^6*3^2*5*7
24	25200	90	2^4*3^2*5^2*7

25	27720	96
26	45360	100
27	50400	108
28	55440	120
29	83160	128
30	110880	144
31	166320	160
32	221760	168
33	277200	180
34	332640	192
35	498960	200
36	554400	216
37	665280	224
38	720720	240
39	1081080	256
40	1441440	288
41	2162160	320
42	2882880	336
43	3603600	360
44	4324320	384
45	6486480	400
46	7207200	432
47	8648640	448
48	10810800	480
49	14414400	504
50	17297280	512
51	21621600	576
52	32432400	600
53	36756720	640 672
54	43243200 61261200	720
55	73513440	768
56	110270160	800
57	122522400	864
58 59	147026880	896
60	183783600	960
61	245044800	1008
62	294053760	1003
62	20-1000100	IUZT

1152

1200

1280

1344

1440

367567200

551350800

698377680

735134400

67 1102701600

2^3*3^2*5*7*11 2^4*3^4*5*7

2^5*3^2*5^2*7

2^4*3^2*5*7*11

2^3*3^3*5*7*11

2^5*3^2*5*7*11

2^4*3^3*5*7*11

2^6*3^2*5*7*11

2^5*3^3*5*7*11

2^4*3^4*5*7*11

2^6*3^3*5*7*11

2^5*3^2*5^2*7*11

2^4*3^2*5*7*11*13

2^3*3^3*5*7*11*13

2^5*3^2*5*7*11*13

2^4*3^3*5*7*11*13

2^6*3^2*5*7*11*13

2^5*3^3*5*7*11*13

2^4*3^4*5*7*11*13

2^6*3^3*5*7*11*13

2^7*3^3*5*7*11*13

2^4*3^2*5^2*7*11*13

2^5*3^2*5^2*7*11*13

2^4*3^3*5^2*7*11*13

2^6*3^2*5^2*7*11*13

2^5*3^3*5^2*7*11*13

2^4*3^4*5^2*7*11*13

2^4*3^3*5*7*11*13*17

2^6*3^3*5^2*7*11*13

2^5*3^3*5*7*11*13*17

2^4*3^4*5*7*11*13*17

2^6*3^3*5*7*11*13*17

2^7*3^3*5*7*11*13*17

2^4*3^2*5^2*7*11*13*17

2^5*3^2*5^2*7*11*13*17

2^4*3^3*5^2*7*11*13*17

2^6*3^2*5^2*7*11*13*17

2^5*3^3*5^2*7*11*13*17

2^4*3^4*5^2*7*11*13*17

2^6*3^3*5^2*7*11*13*17

2^5*3^4*5^2*7*11*13*17

2^4*3^3*5*7*11*13*17*19

2^4*3^2*5^2*7*11

68	1396755360	1536	2^5*3^3*5*7*11*13*17*19	111	32607253879200	13824	2^5*3^3*5^2*7^2*11*13*17*19*23*29
69	2095133040	1600	2^4*3^4*5*7*11*13*17*19	112	46581791256000	14336	2^6*3^3*5^3*7*11*13*17*19*23*29
70	2205403200	1680	2^6*3^4*5^2*7*11*13*17	113	48910880818800	14400	2^4*3^4*5^2*7^2*11*13*17*19*23*29
71	2327925600	1728	2^5*3^2*5^2*7*11*13*17*19	114	55898149507200	15360	2^7*3^4*5^2*7*11*13*17*19*23*29
72	2793510720	1792	2^6*3^3*5*7*11*13*17*19	115	65214507758400	16128	2^6*3^3*5^2*7^2*11*13*17*19*23*29
73	3491888400	1920	2^4*3^3*5^2*7*11*13*17*19	116	93163582512000	16384	2^7*3^3*5^3*7*11*13*17*19*23*29
74	4655851200	2016	2^6*3^2*5^2*7*11*13*17*19	117	97821761637600	17280	2^5*3^4*5^2*7^2*11*13*17*19*23*29
75	5587021440	2048	2^7*3^3*5*7*11*13*17*19	118	130429015516800	18432	2^7*3^3*5^2*7^2*11*13*17*19*23*29
76	6983776800	2304	2^5*3^3*5^2*7*11*13*17*19	119	195643523275200	20160	2^6*3^4*5^2*7^2*11*13*17*19*23*29
77	10475665200	2400	2^4*3^4*5^2*7*11*13*17*19	120	260858031033600	20736	2^8*3^3*5^2*7^2*11*13*17*19*23*29
78	13967553600	2688	2^6*3^3*5^2*7*11*13*17*19	121	288807105787200	21504	2^6*3^3*5^2*7*11*13*17*19*23*29*31
79	20951330400	2880	2^5*3^4*5^2*7*11*13*17*19	122	391287046550400	23040	2^7*3^4*5^2*7^2*11*13*17*19*23*29
80	27935107200	3072	2^7*3^3*5^2*7*11*13*17*19	123	577614211574400	24576	2^7*3^3*5^2*7*11*13*17*19*23*29*31
81	41902660800	3360	2^6*3^4*5^2*7*11*13*17*19	124	782574093100800	25920	2^8*3^4*5^2*7^2*11*13*17*19*23*29
82	48886437600	3456	2^5*3^3*5^2*7^2*11*13*17*19	125	866421317361600	26880	2^6*3^4*5^2*7*11*13*17*19*23*29*31
83	64250746560	3584	2^6*3^3*5*7*11*13*17*19*23	126	1010824870255200	27648	2^5*3^3*5^2*7^2*11*13*17*19*23*29*31
84	73329656400	3600	2^4*3^4*5^2*7^2*11*13*17*19	127	1444035528936000	28672	2^6*3^3*5^3*7*11*13*17*19*23*29*31
85	80313433200	3840	2^4*3^3*5^2*7*11*13*17*19*23	128	1516237305382800	28800	2^4*3^4*5^2*7^2*11*13*17*19*23*29*31
86	97772875200	4032	2^6*3^3*5^2*7^2*11*13*17*19	129	1732842634723200	30720	2^7*3^4*5^2*7*11*13*17*19*23*29*31
87	128501493120	4096	2^7*3^3*5*7*11*13*17*19*23	130	2021649740510400	32256	2^6*3^3*5^2*7^2*11*13*17*19*23*29*31
88	146659312800	4320	2^5*3^4*5^2*7^2*11*13*17*19	131	2888071057872000	32768	2^7*3^3*5^3*7*11*13*17*19*23*29*31
89	160626866400	4608	2^5*3^3*5^2*7*11*13*17*19*23	132	3032474610765600	34560	2^5*3^4*5^2*7^2*11*13*17*19*23*29*31
90	240940299600	4800	2^4*3^4*5^2*7*11*13*17*19*23	133	4043299481020800	36864	2^7*3^3*5^2*7^2*11*13*17*19*23*29*31
91	293318625600	5040	2^6*3^4*5^2*7^2*11*13*17*19	134	6064949221531200	40320	2^6*3^4*5^2*7^2*11*13*17*19*23*29*31
92	321253732800	5376	2^6*3^3*5^2*7*11*13*17*19*23	135	8086598962041600	41472	2^8*3^3*5^2*7^2*11*13*17*19*23*29*31
93	481880599200	5760	2^5*3^4*5^2*7*11*13*17*19*23	136	10108248702552000	43008	2^6*3^3*5^3*7^2*11*13*17*19*23*29*31
94	642507465600	6144	2^7*3^3*5^2*7*11*13*17*19*23	137	12129898443062400	46080	2^7*3^4*5^2*7^2*11*13*17*19*23*29*31
95	963761198400	6720	2^6*3^4*5^2*7*11*13*17*19*23	138	18194847664593600	48384	2^6*3^5*5^2*7^2*11*13*17*19*23*29*31
96	1124388064800	6912	2^5*3^3*5^2*7^2*11*13*17*19*23	139	20216497405104000	49152	2^7*3^3*5^3*7^2*11*13*17*19*23*29*31
97	1606268664000	7168	2^6*3^3*5^3*7*11*13*17*19*23	140	24259796886124800	51840	2^8*3^4*5^2*7^2*11*13*17*19*23*29*31
98	1686582097200	7200	2^4*3^4*5^2*7^2*11*13*17*19*23	141	30324746107656000	53760	2^6*3^4*5^3*7^2*11*13*17*19*23*29*31
99	1927522396800	7680	2^7*3^4*5^2*7*11*13*17*19*23	142	36389695329187200	55296	2^7*3^5*5^2*7^2*11*13*17*19*23*29*31
100	2248776129600	8064	2^6*3^3*5^2*7^2*11*13*17*19*23	143	48519593772249600	57600	2^9*3^4*5^2*7^2*11*13*17*19*23*29*31
101	3212537328000	8192	2^7*3^3*5^3*7*11*13*17*19*23	144	60649492215312000	61440	2^7*3^4*5^3*7^2*11*13*17*19*23*29*31
102	3373164194400	8640	2^5*3^4*5^2*7^2*11*13*17*19*23	145	72779390658374400	62208	2^8*3^5*5^2*7^2*11*13*17*19*23*29*31
103	4497552259200	9216	2^7*3^3*5^2*7^2*11*13*17*19*23	146	74801040398884800	64512	2^6*3^3*5^2*7^2*11*13*17*19*23*29*31*37
104	6746328388800	10080	2^6*3^4*5^2*7^2*11*13*17*19*23	147	106858629141264000	65536	2^7*3^3*5^3*7*11*13*17*19*23*29*31*37
105	8995104518400	10368	2^8*3^3*5^2*7^2*11*13*17*19*23	148	112201560598327200	69120	2^5*3^4*5^2*7^2*11*13*17*19*23*29*31*37
106	9316358251200	10752	2^6*3^3*5^2*7*11*13*17*19*23*29	149	149602080797769600	73728	2^7*3^3*5^2*7^2*11*13*17*19*23*29*31*37
107	13492656777600	11520	2^7*3^4*5^2*7^2*11*13*17*19*23	150	224403121196654400	80640	2^6*3^4*5^2*7^2*11*13*17*19*23*29*31*37
108	18632716502400	12288	2^7*3^3*5^2*7*11*13*17*19*23*29	151	299204161595539200	82944	2^8*3^3*5^2*7^2*11*13*17*19*23*29*31*37
109	26985313555200	12960	2^8*3^4*5^2*7^2*11*13*17*19*23	152	374005201994424000	86016	2^6*3^3*5^3*7^2*11*13*17*19*23*29*31*37
110	27949074753600	13440	2^6*3^4*5^2*7*11*13*17*19*23*29	153	448806242393308800	92160	2^7*3^4*5^2*7^2*11*13*17*19*23*29*31*37

 154
 673209363589963200
 96768
 2^6*3^5*5^2*7^2*11*13*17*19*23*29*31*37

 155
 748010403988848000
 98304
 2^7*3^3*5^3*7^2*11*13*17*19*23*29*31*37

 156
 897612484786617600
 103680
 2^8*3^4*5^2*7^2*11*13*17*19*23*29*31*37