

$$1) \bullet 155,4087104999 \rightarrow 155,41$$

$$\bullet 0,754910899 \rightarrow 0,75491$$

$$\bullet 709,430999997 \rightarrow 709,43$$

$$\bullet 637,9980000009 \rightarrow 638$$

$$\bullet 4,999599999 \rightarrow 4,9996$$

$$2). \tilde{x} = 0,5 \quad \Delta \tilde{x} = 0,001 \quad f(x) = 3 \operatorname{sen}(x^2 - 1)$$

$$f'(x) = 6x \cos(x^2 - 1)$$

$$f(\tilde{x}) = |6(0,5) \cos(0,5^2 - 1)| \cdot 0,001$$

$$= ~~6,2997 \times 10^{-3}~~ 2,1950 \times 10^{-3}$$

$$f(x) \in [0,010893, 0,0152840]$$

$$3). f(x) = 0,75x^4 - 1,25x^3 + 2,5x + 0,5 \quad x = 3$$

$$~~f(3,001) = 35,001~~$$

$$* f'(x) = 3x^3 - 3,75x^2 + 2,5$$

$$h = 3,001 - 3$$

$$h = 0,001$$

$$* f''(x) = 9x^2 - 7,5x$$

$$* f'''(x) = 18x - 7,5$$

Orden 0

$$~~f(3,001) = 35~~ \quad f(3,001) = 35$$

Orden 1

$$~~f(3,001) = 35,001~~$$

→ Orden 1.

$$f(3,001) \approx 35,04 (49,75 \cdot 0,001) = \boxed{35,08975}$$

→ Orden 2

$$f(3,001) \approx \text{orden 1} + \left(\frac{f''(3)}{2!} \right) \cdot h^2$$

$$= 35,08975 + \left(\frac{58,5}{2!} \right) \cdot (0,001)^2 = \boxed{35,08977925}$$

→ Orden 3

$$f(3,001) = \text{orden 2} + \left(\frac{f'''(3)}{3!} \right) \cdot h^3$$

$$= 35,08977925 + \left(\frac{46,5}{3!} \right) \cdot (0,001)^3 = \boxed{35,08977926}$$

$$4). f(x) = 0,2x^5 + 0,1x^4 - 0,5x^3 - 0,2x^2 + x + 2$$

$$x = 3$$

$$\text{tamaño incremento} = 0,001$$

$$f(x) = 48,6 + 8,1 - 13,5 - 1,8 + 3 + 2 \quad f(x_{i+1}) = 46,47815472$$

$$= 46,4$$

$$f'(x) = x^4 + 0,4x^3 - 1,5x^2 - 0,4x + 1 \quad f(x_{i-1}) = 46,32195468$$

$$f''(x) = 4x^3 + 1,2x^2 - 3x - 0,4$$

→ Diferencia finita hacia adelante

$$f'(x_i) = \frac{f(x_{i+1}) - f(x_i)}{h} = \frac{46,47815472 - 46,4}{0,001} = 78,15472$$

$$f''(x_i) = \frac{f(x_{i+2}) - 2f(x_{i+1}) + f(x_i)}{h^2} = \frac{46,55641895 - 2(46,47815472) + 46,4}{0,001^2}$$

$$= \frac{46,55641895 - 2(46,47815472) + 46,4}{0,001^2} = 109,51$$

→ Diferencia finita hacia atrás

$$f'(x_i) = \frac{f(x_i) - f(x_{i-1})}{h} = \frac{46,4 - 46,32195468}{0,001}$$

$$= 78,04532$$

$$f''(x_i) = \frac{f(x_i) - 2f(x_{i-1}) + f(x_{i-2}))}{h^2}$$

$$= \frac{46,4 - 2(46,32195468) + 46,24401865}{0,001^2} = 109,29$$

→ Diferencia finita centrada

$$f'(x_i) = \frac{f(x_{i+1}) - f(x_{i-1}))}{2h} = \frac{46,47815472 - 46,32195468}{2 \cdot 0,001}$$

$$= 78,10002$$

$$f''(x_i) = \frac{f(x_{i+1}) - 2f(x_i) + f(x_{i-1}))}{h^2}$$

$$= \frac{46,47815472 - 2(46,4) + 46,32195468}{0,001^2} = 109,4$$

• Valores verdaderos

$$f'(3) = 78,1$$

$$f''(3) = 109,4$$