

Computer Organization (Revision)-Assignment-1

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Q-1 Simplify the following expressions using Boolean algebra.

a. $A + AB$

b. $AB + AB'$

c. $A'BC + AC$

d. $A'B + ABC' + ABC$

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Ans-1 ★ (a) $A + AB$
 $\Rightarrow A(1+B)$
 $= A \cdot 1$
 $= A$

So, $A + AB = A$

★ (b) $AB + AB'$
 $\Rightarrow A(B+B')$
 $= A \cdot 1$
 $= A$

So, $AB + AB' = A$

★ (c) $A'BC + AC$
 $\Rightarrow (A'B + A) \cdot C$
 $\Rightarrow (A' + A) \cdot (B + A) \cdot C$ (AND Distributive Law)
 $\Rightarrow 1 \cdot (B + A) \cdot C$
 $\Rightarrow (B + A) \cdot C$

So, $A'BC + AC = BC + AC$

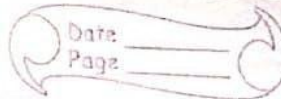
★ (d) $A'B + ABC' + ABC$
 $\Rightarrow A'B + A \cdot B \cdot (C' + C)$
 $\Rightarrow A'B + A \cdot B \cdot 1$
 $\Rightarrow (A' + A) \cdot B$
 $= 1 \cdot B = B$

So, $A'B + ABC' + ABC = B$

Q-2 Given the Boolean function $F = xy'z + x'y'z + xyz$

- List the truth table of the function.
- Draw the logic diagram using the original Boolean expression.
- Simplify the algebraic expression using Boolean algebra.

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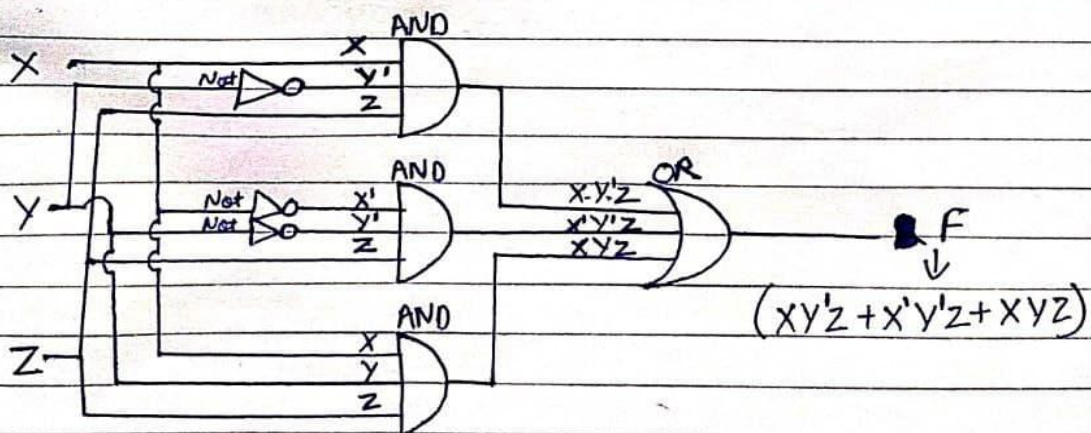
Q-2

Ans-2 Given :- $F = XY'Z + X'Y'Z + XYZ$

(a) Truth table

$\begin{matrix} 3 \\ 2 \\ 1 \\ \downarrow \end{matrix}$	X	Y	Z	X'	Y'	Z'	$XY'Z$	$X'Y'Z$	XYZ	$F = XY'Z + X'Y'Z + XYZ$
1	0	0	0	1	1	1	0	0	0	0
2	0	0	1	1	1	0	0	1	0	1
3	0	1	0	1	0	1	0	0	0	0
4	0	1	1	1	0	0	0	0	0	0
5	1	0	0	0	1	1	0	0	0	0
6	1	0	1	0	1	0	1	0	0	1
7	1	1	0	0	0	1	0	0	0	0
8	1	1	1	0	0	0	0	0	1	1

b Logic Diagram



Simplification

$$F = XY'Z + X'Y'Z + XYZ$$

$$= (X+X')(Y'Z) + XYZ$$

$$= Y'Z + XYZ$$

$$= (Y' + XY)Z$$

$$= (Y' + X)(Y' + Y)Z$$

$$= (Y' + X)Z$$

$$= Y'Z + XZ$$

Q-3 Simplify the following Boolean functions using three-variable maps.

a. $F(x,y,z) = (0, 1, 5, 7)$

b. $F(x,y,z) = (1, 2, 3, 6, 7)$

c. $F(x, y, z) = (3, 5, 6, 7)$

d. $F(A,B,C) = (0, 2, 3, 4, 6)$

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Ans-3 (a) $F(x,y,z) = (0, 1, 5, 7)$
 $= x'y'z' + x'y'z + xy'z + xyz$

		$y'z'$	$y'z$	yz	yz'
x'	(1)	(1)	0	0	
x	0	(1)	(1)	0	

(i)

from (i) $\rightarrow x'y'$

from (ii) $\rightarrow xz$

So,

$(x'y' + xz)$

(b) $F(x,y,z) = (1, 2, 3, 6, 7)$
 $= x'y'z + x'yz' + x'yz + xyz' + xyz$

	$y'z'$	$y'z$	yz	yz'
x'	0	(1)	(1)	(1)
x	0	0	(1)	(1)

(ii)

from (i) $x'z$

from (ii) y

So, $(x'z + y)$

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$$(c) \quad f(x, y, z) = (3, 5, 6, 7)$$

$$= x'yz + xy'z + xyz' + xyz$$

	$y'z'$	$y'z$	yz	yz'	
x'	0	0	1	0	(i)
x	0	1	1	1	(ii)
			(iii)		

from (i) $\rightarrow yz$

from (ii) $\rightarrow xy$ So, $(yz + xy + xz)$

from (iii) $\rightarrow xz$

$\underline{\underline{=}}$

$$(d) \quad f(A, B, C) = (0, 2, 3, 4, 6)$$

$$f(x, y, z) = x'y'z' + x'yz' + x'yz + xy'z' + xyz'$$

$x \backslash yz$	$y'z'$	$y'z$	yz	yz'	
x'	1	0	1	1	(i)
x	1	0	0	1	(ii)

from (i) $\rightarrow x'y$ So, $(x'y + z')$

from (ii) $\rightarrow z'$

\downarrow

$$(A'B + C')$$

$\underline{\underline{=}}$

Q-4 Decode the following ASCII code:

1001010 1001111 1001000 1001110 0100000 1000100 1001111 1000101

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Ans - 4

1001010 1001111 1001000 1001110 0100000
1000100 1001111 1000101

2^6 2^5 2^4 2^3 2^2 2^1 2^0	Decimal equivalent	ASCII Char at Decimal Position
(1001010) ₂	$\rightarrow 64+8+2 = (74)_{10} \rightarrow$	J
(1001111) ₂	$\rightarrow 64+8+4+2+1 = (79)_{10} \rightarrow$	O
(1001000) ₂	$\rightarrow 64+8 = (72)_{10} \rightarrow$	H
(1001110) ₂	$\rightarrow 64+8+4+2 = (78)_{10} \rightarrow$	N
(0100000) ₂	$\rightarrow 32 = (32)_{10} \rightarrow$	() \rightarrow space
(1000100) ₂	$\rightarrow 64+4 = (68)_{10} \rightarrow$	D
(1001111) ₂	$\rightarrow 64+8+4+2+1 = (79)_{10} \rightarrow$	O
(1000101) ₂	$\rightarrow 64+4+1 = (69)_{10} \rightarrow$	E

So, Code is JOHN DOE

≡

Q-5 Convert the following binary numbers to decimal:

a. 101110

b. 1110101

c. 110110100

Ans-5 (1) $(101110)_2 \rightarrow 1 \times 2^5 + 0 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0$
 $= 32 + 0 + 8 + 4 + 2 + 0$
 $= (46)_{10}$

(2) $(1110101)_2 \rightarrow 1 \times 2^6 + 1 \times 2^5 + 1 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0$
 $\Rightarrow 64 + 32 + 16 + 0 + 4 + 0 + 1$
 $\Rightarrow (117)_{10}$

(3) $(110110100)_2 \rightarrow 1 \times 2^8 + 1 \times 2^7 + 0 \times 2^6 + 1 \times 2^5 + 1 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 0 \times 2^0$
 $\Rightarrow 256 + 128 + 0 + 32 + 16 + 0 + 4 + 0 + 0$
 $\Rightarrow (436)_{10}$

Q-6 Convert the following decimal numbers to binary:

- a. 1231
- b. 673
- c. 1998

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Ans-6 (a) $(1231)_{10} \Rightarrow$

2		1231		1	↑
		615		1	
		307		1	
		153		1	
		76		0	
		38		0	
		19		1	
		9		1	
		4		0	↑
		2		0	
		1			

$(1231)_{10} \Rightarrow (10011001111)_2$

(b) $(673)_{10} \Rightarrow$

2		673		1	↑
		336		0	
		168		0	
		84		0	
		42		0	
		21		1	↑
		10		0	
		5		1	
		2		0	
		1			

$(673)_{10} \Rightarrow (1010100001)_2$

(c) $(1998)_{10} \Rightarrow$

2	1998	0	↑
	999	1	
	499	1	
	249	1	
	124	0	
	62	0	
	31	1	
	15	1	↑
	7	1	
	3	1	
	1		

$(1998)_{10} \Rightarrow (11111001110)_2$

Q-7 Convert the following decimal numbers to the bases indicated.

a. 7562 to octal

b. 1938 to hexadecimal

c. 175 to binary

Ans-7 (a) 7562 to octal

$$\begin{array}{r|l} 8 & 7562 \\ \hline & 945 \\ & 118 \\ & 14 \\ & 1 \end{array} \begin{array}{l} 2 \\ 1 \\ 6 \\ 6 \\ 1 \end{array}$$

$$\text{So, } (7562)_{10} = (16612)_8$$

(b) 1938 to hexadecimal

$$\begin{array}{r|l} 16 & 1938 \\ \hline & 121 \\ & 7 \end{array} \begin{array}{l} 2 \\ 9 \\ 7 \end{array}$$

$$\text{So, } (1938)_{10} = (792)_{16}$$

(c) 175 to binary

$$\begin{array}{r|l} 2 & 175 \\ \hline & 87 \\ & 43 \\ & 21 \\ & 10 \\ & 5 \\ & 2 \\ & 1 \end{array} \begin{array}{l} 1 \\ 1 \\ 1 \\ 0 \\ 1 \\ 0 \\ 1 \end{array}$$

$$\text{So, } (175)_{10} = (10101111)_2$$

Q-8 Convert the hexadecimal number F3A7C2 to

a. Binary

b. Octal

Ans-8 (a) $(F3A7C2)_{16}$ to binary

\swarrow	\downarrow	\downarrow	\downarrow	\downarrow	\downarrow
15 15	3	10	7	12	2
\downarrow	\downarrow	\downarrow	\downarrow	\downarrow	\downarrow
1111	0011	1010	0111	1100	0010

So, $(F3A7C2)_{16} = (111100111010011111000010)_2$

(b) $(F3A7C2)_{16}$ to Octal

F 3 A 7 C 2					
\swarrow	\downarrow	\downarrow	\downarrow	\downarrow	\downarrow
15	3	10	7	12	2
\downarrow	\downarrow	\downarrow	\downarrow	\downarrow	\downarrow
1111	0011	1010	0111	1100	0010
\downarrow	\downarrow	\downarrow	\downarrow	\downarrow	\downarrow
111	100	111	010	011	111
7	4	7	2	3	7

So, $(F3A7C2)_{16}$

$(74723702)_8$