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Massimo Torquati Computer Science Department University of Pisa, Italy. Email: torquati@di.unipi.it

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Massimo Torquati
Computer Science Department
University of Pisa, Italy.
Email: torquati@di.unipi.it

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Abstract

Using efficient point-to-point communication channels is critical for implementing fine grained parallel program on modern shared cache multi-core architectures.

This report discusses in detail several implementations of wait-free Single-Producer/Single-Consumer queue (SPSC), and presents a novel and efficient algorithm for the implementation of an unbounded wait-free SPSC queue (uSPSC). The correctness proof of the new algorithm, and several performance measurements based on simple synthetic benchmark and microbenchmark, are also discussed.

1 Introduction

This report focuses on Producer-Consumer coordination, and in particular on Single-Producer/Single-Consumer (SPSC) coordination. The producer and the consumer are concurrent entities, i.e. processes or threads. The first one produces items placing them in a shared structure, whereas the the second one consumes these items by removing them from the shared structure. Different kinds of shared data structures provide different fairness guarantees. Here, we consider a queue data structure that provides First-In-First-Out fairness (FIFO queue), and we assume that Producer and Consumer share a common address space, that is, we assume threads as concurrent entities.

In the end of '70s, Leslie Lamport proved that, under Sequential Consistency memory model [10], a Single-Producer/Single-Consumer circular buffer ¹ can be implemented without using explicit synchronization mechanisms between the producer and the consumer [9]. Lamport's circular buffer is a wait-free

 $^{^1\}mathrm{A}$ circular buffer can be used to implement a FIFO queue

algorithm. A wait-free algorithm is guaranteed to complete after a finite number of steps, regardless of the timing behavior of other operations. Differently, a lock-free algorithm guarantees only that after a finite number of steps, some operation completes. Wait-freedom is a stronger condition than lock-freedom and both conditions are strong enough to preclude the use of blocking constructs such as locks.

With minimal modification to Lamport's wait-free SPSC algorithm, it results correct also under Total-Store-Order and others weaker consistency models, but it fails under weakly ordered memory model such as those used in IBM's Power and Intel's Itanium architectures. On such systems, expensive memory barrier (also known as memory fence) instructions are needed in order to ensure correct load/store instructions ordering.

Maurice Herlihy in his seminal paper [5] formally proves that few simple HW atomic instructions are enough for building any wait-free data structure for any number of concurrent entities. The simplest and widely used primitive is the compare-and-swap (CAS). Over the years, many works have been proposed with focus on lock-free/wait-free Multiple-Producer/Multiple-Consumer (MPMC) queue [13, 8, 12]. They use CAS-like primitives in order to guarantee correct implementation.

Unfortunately, the CAS-like hardware primitives used in the implementations, introduce non-negligible overhead on modern shared-cache architectures, so even the best MPMC queue implementation, is not able to obtain better performance than Lamport's circular buffer in cases with just 1 producer and 1 consumer.

FIFO queues are typically used to implement streaming networks [2, 14]. Streams are directional channels of communication that behave as a FIFO queue. In many cases streams are implemented using circular buffer instead of a pointer-based dynamic queue in order to avoid excessive memory usage. Hoverer, when complex streaming networks have to be implemented, which have multiple nested cycles, the use of bounded-size queues as basic data structure requires more complex and costly communication protocols in order to avoid deadlock situations.

Unbounded size queue are particularly interesting in these complex cases, and in all the cases where it is extremely difficult to choose a suitable queue size. As we shall see, it is possible to implement a wait-free unbounded SPSC queue by using Lamport's algorithm and dynamic memory allocation. Unfortunately, dynamic memory allocation/deallocation is costly because they use locks to protect internal data structures, hence introduces costly memory barriers.

In this report it is presented an efficient implementation of an unbounded wait-free SPSC FIFO queue which makes use only of a modified version of the Lamport's circular buffer without requiring any additional memory barrier, and, at the same time, minimizes the use of dynamic memory allocation. The novel unbounded queue implementation presented here, is able to speed up producer-consumer coordination, and, in turn, provides the basic mechanisms for implementing complex streaming networks of cooperating entities.

The remainder of this paper is organized as follows. Section 2 reminds

```
1 bool push(data) {
                                                8 bool pop(data) {
   if ((tail+1 mod N)==head)
                                                    if (head==tail)
     return false; // buffer full
                                                      return false; // buffer empty
                                               10
    buffer [tail]=data;
                                                    data = buffer[head];
                                               11
   tail = tail +1 mod N;
                                                    head = head + 1 \mod N;
5
                                               12
   return true:
                                                    return true:
6
                                               13
                                               14
```

Figure 1: Lamport's circular buffer push and pop methods pseudo-code. At the beginning head=tail=0.

```
1 bool push(data) {
                                               10 bool pop(data) {
   if (buffer [tail] == BOTTOM) {
                                                   if (buffer [head]!=BOTTOM) {
                                                     data = buffer[head];
     buffer [tail]=data;
                                               12
     tail = tail + 1 \mod N;
                                                     buffer [head] = BOTTOM;
                                               13
                                                     head = head+1 \mod N;
     return true;
                                               14
6
                                               15
                                                     return true:
   return false; // buffer full
                                                   }
                                               16
                                                   return false; // buffer empty
                                               17
```

Figure 2: P_1C_1 -buffer buffer pseudocode. Modified version of the code presented in [6]. The buffer is initialized to BOTTOM and head=tail=0 at the beginning.

Lamport's algorithm and also shows the necessary modifications to make it work efficiently on modern shared-cache multiprocessors. Section 3 discuss the extension of the Lamport's algorithm to the unbounded case. Section 4 presents the new implementations with a proof of correctness. Section 5 presents some performance results, and Sec. 6 concludes.

2 Lamport's circular buffer

In Fig. 1 the pseudocode of the push and pop methods of the Lamport's circular buffer algorithm, is sketched. The buffer is implemented as an array of N entries.

Lamport proved that, under Sequential Consistency [10], no locks are needed around pop and push methods, thus resulting in a concurrent wait-free queue implementation. If Sequential Consistency requirement is released, it is easy to see that Lamport's algorithm fails. This happens for example with the PowerPC architecture where write to write relaxation is allowed ($W \to W$ using the same notation used in [1]), i.e. 2 distinct writes at different memory locations may be executed not in program order. In fact, the consumer may pop out of the buffer a value before the data is effectively written in it, this is because the update of the tail pointer (modified only by the producer) can be seen by the consumer before the producer writes in the tail position of the buffer. In this case, the test at line §1.9 would be passed even though buffer[head] contains stale data.

Few simple modifications to the basic Lamport's algorithm, allow the correct execution even under weakly ordered memory consistency model. To the best of our knowledge such modifications have been presented and formally proved

correct for the first time by Higham and Kavalsh in [6]. The idea mainly consists in tightly coupling control and data information into a single buffer operation by using a know value (called BOTTOM), which cannot be used by the application. The BOTTOM value is used to indicate whether there is an empty buffer slot, which in turn indicates an available room in the buffer to the producer and the empty buffer condition to the consumer.

With the circular buffer implementation sketched in Fig. 2, the consistency problem described for the Lamport's algorithm cannot occur provided that the generic store buffer[i]=data is seen in its entirety by a processor, or not at all, i.e. a single memory store operation is executed atomically. To the best of our knowledge, this condition is satisfied in any modern general-purpose processor for aligned memory word stores.

As shown by Giacomoni et all. in [3], Lamport's circular buffer algorithm results in cache line thrashing on shared-cache multiprocessors, as the head and tail buffer pointers are shared between consumer and producer. Modifications of pointers, at lines §1.5 and §1.12, turn out in cache-line invalidation (or update) traffic among processors, thus introducing unexpected overhead. With the implementation in Fig. 2, the head and the tail buffer pointers are always in the local cache of the consumer and the producer respectively, without incurring in cache-coherence overhead since they are not shared.

When transferring references through the buffer rather than plain data values, a memory fence is required on processors with weakly memory consistency model, in which stores can be executed out of program order. In fact, without a memory fence, the write of the reference in the buffer could be visible to the consumer before the referenced data has been committed in memory. In the code in Fig. 2, a write-memory-barrier (WMB) must be inserted between line §1.2 and line §1.3.

The complete code of the SPSC circular buffer is shown in Fig. 3.

2.1 Cache optimizations

Avoiding cache-line thrashing due to false-sharing is a critical aspect in shared-cache multiprocessors. Consider the case where two threads sharing a SPSC buffer are working in lock step. The producer produces one task at a time while the consumer immediately consumes the task in the buffer. When a buffer entry is accessed, the system reads a portion of memory containing the data being accessed placing it in a cache line. The cache line containing the buffer entry is read by the consumer thread which only consumes one single task. The producer than produces the next task pushing the task into a subsequent entry into the buffer. Since, in general, a single cache line contains several buffer entries (a typical cache line is 64bytes, whereas a memory pointer on a 64bit architecture is 8 bytes) the producer's write operation changes the cache line status invalidating the whole contents in the line. When the consumer tries to consumer the next task the entire cache line is reloaded again even if the consumer tries to access a different buffer location. This way, during the entire computation the cache lines containing the buffer entries bounce between the

```
1 class SPSC_buffer {
 2 private:
     volatile unsigned long pread;
     long padding1[longxCacheLine-1]
     volatile unsigned long pwrite;
     long padding2[longxCacheLine-1];
              size_t
                             ** buf;
9 public:
    SWSR_Ptr_Buffer(size_t n, const bool=true):
10
       pread(0),pwrite(0), size(n),buf(0) {
11
12
     SWSR_Ptr_Buffer() { if (buf)::free(buf); }
13
14
     bool init() {
15
        if (buf) return false;
16
          buf = (void **)::malloc(size*sizeof(void*));
17
          if (!buf) return false;
18
          bzero(buf, size*sizeof(void*));
19
          return true;
20
21
22
                       { return (buf[pread]==NULL);}
     bool empty()
23
     bool available() { return (buf[pwrite]==NULL);}
24
25
     bool push(void * const data) {
26
        if (available()) {
27
          WMB();
28
          buf[pwrite] = data;
29
          pwrite += (pwrite+1 >= size) ? (1-size): 1;
30
31
          return true:
32
        return false:
33
34
    \hat{\mathbf{bool}} \operatorname{pop}(\mathbf{void} ** \operatorname{data}) {
35
36
        if (empty()) return false;
37
        *data = buf[pread];
        buf[pread]=NULL;
38
        pread += (pread+1 >= size) ? (1-size): 1;
39
40
        return true;
41
42 };
```

Figure 3: SPSC circular buffer implementation.

producer and the consumer private caches incurring in extra overhead due to cache coherence traffic. The problem arises because the cache coherence protocol works at cache line granularity and because the "distance" between the producer and the consumer (i.e. |pwrite-pread|) is less than or equal to the number of tasks which fill a cache line (on a 64bit machine with 64bytes of cache line size the critical distance is 8). In order to avoid false sharing between the head and tail pointers in the SPSC queue, a proper amount of padding in required to force the two pointers to reside in different cache lines (see for example Fig. 3). In general, the thrashing behavior can be alleviated if the producer and the consumer are forced to work on different cache lines, that is, augmenting the "distance".

The FastForward SPSC queue implementation presented in [3] improves Lamport's circular buffer implementation by optimizing cache behavior and preventing cache line thrashing. FastForward temporally slips the producer and the consumer in such a way that push and pop methods operate on different cache lines. The consumer, upon receiving its first task, spins until an appropriate amount of slip (that is the number of tasks in the queue reach a fixed value) is established. During the computation, if necessary, the temporal slipping is maintained by the consumer through local spinning. FastForward obtains a performance improvement of 3.7 over Lamport's circular buffer when temporal slipping optimization is used.

A different approach named cache line protection has been used in MCRing-Buffer [11]. The producer and consumer thread update private copies of the head and tail buffer pointer for several iterations before updating a shared copy. Furthermore, MCRingBuffer performs batch update of control variables thus reducing the frequency of writing the shared control variables to main memory.

A variation of the MCRingBuffer approach is used in Liberty Queue [7]. Liberty Queue shifts most of the overhead to the consumer end of the queue. Such customization is useful in situations where the producer is expected to be slower than the consumer.

Multipush method. Here we present a sligtly different approach for reducing cache-line trashing which is very simple and effective, and does not introduce any significant modification to the basic SPSC queue implementation. The basic idea is the following: instead of enqueuing just one item at a time directly into the SPSC buffer, we can enqueue the items in a temporary array and then submit the entire array of tasks in the buffer using a proper insertion order. We added a new method called mpush to the SPSC buffer implementation (see Fig.12), which has the same interface of the push method but inserts the data items in a temporary buffer of fixed size. The elements in the buffer are written in the SPSC buffer only if the local buffer is full or if the flush method is called. The multipush method gets in input an array of items, and writes the items into the SPSC buffer in backward order. The backward order insertions, is particularly important to reduce cache trashing, in fact, in this way, we enforce a distance between the pread and the pwrite pointers thus reducing the cache invalidation ping-pong. Furthermore, writing in backward order does not require any other control variables or synchronisation.

This simple approach increase cache locality by reducing the cache trashing. However, there may be two drawbacks:

- 1. we pay an extra copy for each element to push into the SPSC buffer
- 2. we could increase the latency of the computation if the consumer is much faster than the producer.

The first point, in reality, is not an issue because the cost of extra copies are typically amortized by the better cache utilization. The second point might represent an issue for applications exhibiting very strict latency requirements that cannot be balanced by an increased throughput (note however that this is a rare requirement in a streaming application). In section 5, we try to evaluate experimentally the benefits of the proposed approach.

```
1 bool multipush(void * const data[], int len) {
    unsigned long last = pwrite + ((pwrite+ -
                                                 -len >= size) ? (len-size): len);
     unsigned long r = len-(last+1), l=last, i;
     if (buf[last]==NULL) {
       if (last < pwrite) {
        for(i=len;i>r;-
          \operatorname{buf}[1] = \operatorname{data}[i];
         for(i=(size-1);i>=pwrite;--i,--r)
          buf[i] = data[r];
10
         for(register int i=len;i>=0;--i)
11
           buf[pwrite+i] = data[i];
12
13
       WMB();
14
       pwrite = (last+1 >= size) ? 0 : (last+1);
15
       ment = 0; // reset mpush counter
16
      return true;
17
18
    return false;
19
20 }
21
22 bool flush() {
    return (mcnt ? multipush(multipush_buf,mcnt) : true);
23
24 }
25
26 bool mpush(void * const data) -
     if (mcnt==MULTIPUSH_BUFFER_SIZE)
27
       return multipush(multipush_buf,MULTÍPUSH_BUFFER_SIZE);
28
29
    multipush_buf[mcnt++]=data:
30
31
    if (mcnt==MULTIPUSH_BUFFER_SIZE)
32
       \textbf{return} \ \ \text{multipush\_buf,MULTIPUSH\_BUFFER\_SIZE)};
33
34
35
    return true:
36 }
37
```

Figure 4: Methods added to the SPSC buffer to reduce cache trashing.

3 Unbounded List-Based Wait-Free SPSC Queue

Using the same idea of the Lamport's circular buffer algorithm, it is possible to implement an unbounded wait-free SPSC queue using a list-based algorithm and dynamic memory allocation/deallocation. The implementation presented here has been inspired by the work of Hendler and Shavit in [4], although it is different in several aspects. The pseudocode is sketched in Fig. 5.

The algorithm is very simple: the push method allocates a new Node data structure containing the real value to push into the queue and a pointer to the next Node structure. The tail pointer is adjusted to point to the current Node. The pop method gets the current head Node, sets the data value, adjusts the head pointer and, before exiting, deallocates the head Node.

In the general case, the main problem with the list-based implementation of queues is the dynamic memory allocation/deallocation of the Node structure. In fact, dynamic memory management operations, typically, use lock to enforce mutual exclusion to protect internal shared data structures, so, much of the

```
if (head->next != NULL) {
                                                11
2 bool push(data) {
                                                12
                                                       Node * n = (Node *)head;
    Node * n = allocnode(data):
                                                       data
                                                               = (head - > next) - > data:
                                                13
    WMB();
                                                               = head -> next;
                                                14
                                                      head
    tail -> next = n:
                                                       deallocnode(n):
                                                15
    tail
6
              = n:
                                                16
                                                      return true:
    return true;
                                                17
                                                     return false; // queue empty
                                                18
10 bool pop(data) {
```

Figure 5: Unbounded list-based SPSC queue implementation.

```
ı class SPSC_dynBuffer {
    \mathbf{struct}\ \mathrm{Node}\ \{
                                                           ~SPSC_dynBuffer() { ... }
                                                     25
       void
                    * data:
                                                     26
        struct Node * next;
                                                          bool push(void * const data) {
                                                              Node * n = allocnode();
     volatile Node * head;
                                                              n->data = data; n->next = NULL;
     long pad1[longxCacheLine-sizeof(Node *)];
                                                              WMB();
     volatile Node * tail;
                                                              tail - > next = n;
     \textbf{long} \ \mathrm{pad2}[longxCacheLine} - \mathbf{sizeof}(Node*)];
                                                              tail
     SPSC_Buffer
                                                              return true;
10
11 private:
     Node * allocnode() {
                                                          bool pop(void ** data) {
       Node * n = NULL
                                                              if (head->next) {
       if (cache.pop((void **)&n)) return n;
                                                                Node * n = (Node *)head;
14
                                                                         = (head - > next) -
15
         n = (Node *)malloc(sizeof(Node));
                                                     38
16
                                                                         = head -> next;
17
                                                     40
                                                                 \  \  \, \textbf{if} \  \  \, (!\, cache.push(n)) \  \, free(n); \\
18 public:
    SPSC_dynBuffer(int size):cache(size) {
19
                                                     42
      Node * n=(Node *)::malloc(sizeof(Node)); 43
                                                              return false;
20
       n->data = NULL; n->next = NULL;
21
       head=tail=n; cache.init();
                                                     45 };
22
```

Figure 6: Unbounded list-based SPSC queue implementation with Node(s) caching (dSPSC).

benefits gained using lock-free implementation of the queue are eventually lost. To mitigate such overhead, it is possible to use caching of list's internal structure (e.g. Node) [4]. The cache is by definition bounded in the number of elements and so it can be efficiently implemented using a wait-free SPSC circular buffer presented in the previous sections. Figure 6 shows the complete implementation of the list-based SPSC queue when Node caching is used. In the following we will refer to this implementation with the name dSPSC.

As we shall see in Sec. 5, caching strategies help in improving the performance but are not sufficient to obtain optimal figures. This is mainly due to the poor cache locality caused by lots of memory indirections. Note that the number of elementary instruction per push/pop operation is greater than the ones needed in the SPSC implementation.

4 Unbounded Wait-Free SPSC Queue

We now describe an implementation of the unbounded wait-free SPSC queue combining the ideas described in the previous sections. We refer to the implementation with the name uSPSC.

The key idea is quite simple: the unbounded queue is based on a pool of wait-free SPSC circular buffers (see Sec. 2). The pool of buffers automatically grows and shrinks on demand. The implementation of the pool of buffers carefully try to minimize the impact of dynamic memory allocation/deallocation by using caching techniques like in the list-based SPSC queue. Furthermore, the use of SPSC circular buffers as basic uSPSC data structure, enforce cache locality hence provides better performance.

The unbounded queue uses two pointers: buf_w that points to writer's buffer (the same of the tail pointer in the circular buffer), and a buf_r that points to reader's buffer (the same of the head pointer). Initially both buf_w and buf_r point to the same SPSC circular buffer. The push method works as follow. The producer first checks whether there is an available room in the current buffer (line §7.52) and then push the data. If the current buffer is full, asks the pool for a new buffer (line §7.53), set the buf_w pointer and push the data into the new buffer.

The consumer first checks whether the current buffer is not empty and in case pops the data. If the current buffer is empty, there are 2 possibilities:

- 1. there are no items to consume, i.e. the unbounded queue is really empty;
- 2. the current buffer is empty (i.e. the one pointed by buf_r), but there may be some items in the next buffer.

For the consumer point of view, the queue is really empty when the current buffer is empty and both the read and write pointers point to the same buffer. If the read and writer queue pointers differ, the consumer have to re-check the current queue emptiness because in the meantime (i.e. between the execution of the instruction §7.61 and §7.62) the producer could have written some new elements into the current buffer before switching to a new one. This is the most subtle condition, if we switch to the next buffer but the current one is not really empty, we definitely loose data. If the queue is really empty for the consumer, the consumer switch to a new buffer releasing the current one in order to be recycled by the buffer pool (lines §7.64–§7.67).

4.1 Correctness proof

Here we provide a proof of correctness for the uSPSC queue implementation described in the previous section. By correctness, we mean that the consumer extracts elements from the queue in the same order in which they were inserted by the producer. The proof is based on the only assumption that the SPSC circular buffer algorithm is correct. A formal proof of the correctness of the SPSC buffer can be found in [6] and [3]. Furthermore, the previous assumption,

```
1 class BufferPool {
                                                             : buf_r(0), buf_w(0), size(size),
                                                     38
                                                              pool(CACHE_SIZE) {}
    SPSC_dynBuffer inuse;
                                                     39
                                                            uSPSC_Buffer() { ... }
     SPSC_Buffer
                    bufcache:
                                                      40
 4 public:
                                                      41
     BufferPool(int cachesize)
                                                           bool init() {
                                                      42
                                                             buf_r = new SPSC_Buffer(size);
      :inuse(cachesize), bufcache(cachesize) {
6
                                                      43
        bufcache.init();
                                                             if (buf_r->init()<0) return false;
                                                      44
                                                             buf_w = buf_r:
                                                      45
     BufferPool() {...}
                                                             return true:
9
                                                      46
10
                                                      47
     SPSC_Buffer * const next_w(size_t size) {
11
                                                      48
                                                           bool empty() {return buf_r->empty();}
       SPSC Buffer * buf:
                                                           bool available() {return buf_w->available()
12
                                                      49
13
       if (!bufcache.pop(&buf)) {
         buf = new SPSC_Buffer(size);
14
                                                      50
                                                           \mathbf{bool} \ \mathrm{push}(\mathbf{void} * \mathbf{const} \ \mathrm{data}) \ \{
         if (buf->init()<0) return NULL;</pre>
15
                                                     51
                                                             if (! available ()) {
16
                                                      52
       inuse.push(buf);
                                                               SPSC_Buffer * t = pool.next_w(size);
17
                                                      53
18
       return buf;
                                                      54
                                                               if (!t) return false;
19
                                                      55
                                                               buf_w = t;
    SPSC_Buffer * const next_r() {
20
                                                      56
       SPSC_Buffer * buf:
                                                             buf_w->push(data);
21
                                                      57
       return (inuse.pop(&buf)? buf : NULL);
22
                                                      58
                                                             return true:
23
                                                      59
     void release(SPSC_Buffer * const buf) {
24
                                                      60
                                                           bool pop(void ** data) {
25
       buf->reset();
                                                      61
                                                             if (buf_r->empty()) {
       if (!bufcache.push(buf)) delete buf;
26
                                                      62
                                                                if (buf_r == buf_w) return false;
27
                                                      63
                                                                \mathbf{if}\ (\mathrm{buf\_r}{-}{>}\mathrm{empty}(\dot{)})\ \{
28 };
                                                                  SPSC_Buffer * tmp = pool.next_r();
                                                      64
29 class uSPSC_Buffer {
                                                                  if (tmp) {
    SPSC_Buffer * buf_r;
                                                                    pool.release(buf_r);
30
     \textbf{long} \ \mathrm{padding1}[\mathrm{longxCacheLine-1}];
                                                                    buf_r = tmp;
     SPSC_Buffer * buf_w;
     long padding2[longxCacheLine-1];
     size_t
     BufferPool
                    pool;
                                                             return buf_r->pop(data);
36 public:
    uSPSC_Buffer(size_t n)
```

Figure 7: Unbounded wait-free SPSC queue implementation.

implies that memory word read and write are executed atomically. This is one of the main assumption for the proof of correctness for the SPSC wait-free circular buffer [3]. To the best of our knowledge, this condition is satisfied in any modern CPUs.

The proof is straightforward. If buf_r differs from buf_w, the execution is correct because there is no data sharing between producer and consumer (the push method uses only the buf_w pointer, whereas the pop method uses only the buf_r pointer), since the producer and the consumer use different SPSC buffer. If buf_r is equal to buf_w (both the producer and the consumer use the same SPSC buffer) and the buffer is neither seen full nor empty by the producer and the consumer, the execution is correct because of the correctness of the SPSC circular buffer. So, we have to prove that if buf_r is equal to buf_w and the buffer is seen full or empty by the producer and/or by the consumer respectively, the execution of the push and pop methods are always correct.

The previous sentence has only one subtle condition worth proving: buf_r is equal to buf_w and the producer sees the buffer full whereas the consumer sees the buffer empty. This sound strange but it is not.

Suppose that the internal SPSC buffers used in the implementation of the uSPSC queue has only a single slot (size=1). Suppose also that the consumer try to pop one element out of the queue, and the queue is empty. Before checking the condition at line §7.62, the producer inserts an item in the queue and try to insert a second one. At the second insert operation, the producer gets a new buffer because the current buffer is full (line §7.53), so, the buf_w pointer changes pointing to the new buffer (line §7.55). Since we have not assumed anything about read after write memory ordering $(R \to W \text{ using the same notation as in})$ [1]), we might suppose that the write of the buf_w pointer is immediately visible to the consumer end such that for the consumer results buf_r different from buf_w at line §7.62. In this case, if the consumer sees the buffer empty in the next test (line §7.63), the algorithm fails because the first element pushed by the produces is definitely lost. So, depending on the memory consistency model, we could have different scenarios. Consider a memory consistency model in which $W \to W$ program order is respected. In this case, the emptiness check at line §7.63 could never fail because a write in the internal SPSC buffer (line §3.29) cannot bypass the update of the buf_w pointer (line §7.55). Instead, if $W \to W$ memory ordering is relaxed, the algorithm fails if the SPSC buffer has size 1, but it works if SPSC internal buffer has size greater than 1. In fact, if the SPSC internal buffer has size 1 it is possible that the write in the buffer is not seen at line §7.63 because writes can be committed out-of-order in memory, and also, the Write Memory Barrier (WMB) at line §3.28 is not sufficient, because it ensures that only the previous writes are committed in memory. On the other hand if the size of the SPSC buffer is at least 2 the first of the 2 writes will be visible at line §7.63 because of the WMB instruction, thus the emptiness check could never fail. From the above reasoning follows two theorems:

Theorem 4.1 The uSPSC queue is correct under any memory consistency model that ensure $W \to W$ program order.

Theorem 4.2 The uSPSC queue is correct under any memory consistency model provided that the size of the internal circular buffer is greater than 1.

5 Experiments

All reported experiments have been executed on an Intel workstation with 2 quad-core Xeon E5520 Nehalem (16 HyperThreads) @2.26GHz with 8MB L3 cache and 24 GBytes of main memory with Linux x86_64. The Nehalem processor uses Simultaneous MultiThreading (SMT, a.k.a. HyperThreading) with 2 contexts per core and the Quickpath interconnect equipped with a distributed cache coherency protocol. SMT technology makes a single physical processor appear as two logical processors for the operating system, but all execution resources are shared between the two contexts. We have 2 CPUs each one with 4 physical cores. The operating system (Linux kernel 2.6.20) sees the two per core contexts as two distinct cores assigning to each one a different id whose topology is sketched in Fig. 8.

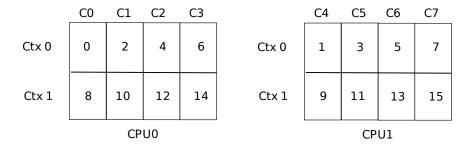


Figure 8: Core's topology on the Intel Xeon E5520 workstation used for the tests.

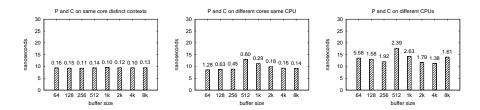


Figure 9: Average latency time and standard deviation (in nanoseconds) of a push/pop operation for the SPSC queue using different buffer size. The producer (P) and the consumer (C) are pinned: on the same core (left), on different core (middle), on different CPUs (right).

The methodology used in this paper to evaluate performance consists in plotting the results obtained by running a simple synthetic benchmarks and a very simple microkernel.

The first test is a 2-stage pipeline in which the first stage (P) pushes 1 million tasks (a task is just a memory pointer) into a FIFO queue and the second stage (C) pops tasks from the queue and checks for correct values. Neither additional memory operations nor additional computation in the producer or consumer stage is executed. With this simple test we are able to measure the raw performance of a single push/pop operation by computing the average value of 100 runs and the standard deviation.

In Fig. 9 are reported the values obtained running the first benchmark for the SPSC queue, varying the buffer size. We tested 3 distinct cases obtained by changing the physical mapping of the 2 threads corresponding to the 2 stages of the pipeline: 1) the first and second stage of the pipeline are pinned on the same physical core but on different HW contexts (P on core 0 and C on core 8), 2) are pinned on the same CPU but on different physical cores (P on core 0 and C on core 2), and 3) are pinned on two cores of two distinct CPUs (P on core

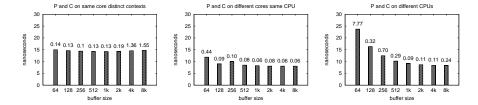


Figure 10: Average latency time and standard deviation (in nanoseconds) of a push/pop operation for the unbounded SPSC queue (uSPSC) using different internal buffer size. The producer (P) and the consumer (C) are pinned: on the same core (left), on different core (middle), on different CPUs (right).

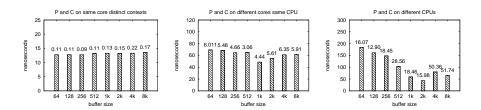


Figure 11: Average latency time and standard deviation (in nanoseconds) of a push/pop operation for the dynamic list-based SPSC queue (dSPSC) using different internal cache size. The producer (P) and the consumer (C) are pinned: on the same core (left), on different core (middle), on different CPUs (right).

0 and C on core 1). In Fig. 10 and in Fig. 11 are reported the values obtained running the same benchmark using the unbounded SPSC (uSPSC) queue and the dynamic list-based SPSC queue (dSPSC) respectively. On top of each bar is reported the standard deviation in nanoseconds computed over 100 runs.

The SPSC queue is insensitive to buffer size in all cases. It takes on average 10–12 ns per queue operation with standard deviations less than 1 ns when the producer and the consumer are on the same CPU, and takes on average 11–15 ns if the producer and the consumer are on separate CPUs. The unbounded SPSC queue (Fig. 10) is more sensitive to the internal buffer size especially if the producer and the consumer are pinned into separate CPUs. The values obtained are extremely good if compared with the ones obtained for the dynamic list-based queue (Fig. 11), and are almost the same if compared with the bounded SPSC queue when using an internal buffer size greater than or equal to 512 entries.

The dynamic list-based SPSC queue is sensitive to the internal cache size (implemented with a single SPSC queue). It is almost 6 times slower than the uSPSC version if the producer and the consumer are not pinned on the same core. In this case in fact, producer and consumer works in lock steps as

	L1 accesses	L1 misses	L2 accesses	L2 misses
push	9,845,321	249,789	544,882	443,387
mpush	4,927,934	148,011	$367,\!129$	$265,\!509$

Table 1: push vs. mpush cache miss obtained using a SPSC of size 1024 and performing 1 million push/pop operations.

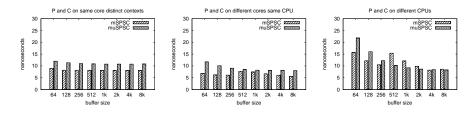


Figure 12: Average latency time of a multi-push/pop operation for the bounded and unbounded SPSC buffer. The multi-push internal buffer size is statically set to 16 entries. The producer (P) and the consumer (C) are pinned: on the same core (left), on different core (middle), on different CPUs (right).

they share the same ALUs and so dynamic memory allocation is reduced with performance improvement. Another point in this respect, is that the dynamic list-based SPSC queue uses memory indirection to link together queue's elements thus not fully exploiting cache locality. The bigger the internal cache the better performance is obtained. It is worth to note that caching strategies for dynamic list-based SPSC queue implementation, significantly improve performance but are not enough to obtain optimal figures like those obtained in the SPSC implementation.

We want now to evaluate the benefit of the cache optimization presented in Sec. 2.1 for the SPSC and for the uSPSC queue. We refer to mSPSC and to muSPSC the version of the SPSC queue and of the uSPSC queue which use the mpush instead of the push method. Table 1 reports the L1 and L2 cache accesses and misses for the push and mpush methods using a specific buffer size. As can be noticed, the mpush method greatly reduce cache accesses and misses. The reduced number of misses, and accesses in general, leads to better overall performance. The average latency of a push/pop operation, decreases from 10–11ns of the SPSC queue, to 6–9ns for the multi-push version. The comparison of the push and mpush methods for both the SPSC and uSPSC queue, distinguishing the three mapping scenario for the producer and the consumer, are shown in Fig. 12. The muSPSC queue is less sensitive to the cache optimization introduced with the mpush method with respect to the uSPSC queue.

In order to test a simple but real application kernel we consider the code in Fig. 13. The sequential execution of such code on a single core of the tested architecture is 94.6ms. We parallelize the code into a pipeline of 2 stages, P

```
 \begin{array}{ll} \mathbf{int\ main}() \ \{ \\ \mathbf{2} & \mathbf{double\ x} = 0.12345678, \, y{=}0.654321012; \\ \mathbf{3} & \mathbf{for(int\ i{=}0;i{<}1000000; +{+}i)} \ \{ \\ \mathbf{4} & \mathbf{x} = 3.1415*\sin(\mathbf{x}); \\ \mathbf{5} & \mathbf{y} +{=} \mathbf{x} - \cos(\mathbf{y}); \\ \mathbf{6} & \mathbf{\}} \\ \mathbf{7} & \mathbf{return\ 0}; \\ \mathbf{8} \ \} \end{array}
```

Figure 13: Microbenchmark: sequential code.

ls

```
1 void P() {
                                                 8 void C() {
   double x = 0.12345678;
                                                     double x, y=0.654321012;
   for(int i=0;i<1000000;++i) {
                                                     for(int i=0;i<1000000;++i) {
     x = 3.1415 * \sin(x);
                                                       Q.pop(&x);
                                                11
      Q.push(x);
5
                                                12
                                                         += x - \cos(y);
6
7 }
                                                13
                                                14 }
```

Figure 14: Microbenchmark: pipeline implementation.

and C, as shown in Fig. 14. The 2 stages are connected by a FIFO queue. The results obtained considering for the queue the mSPSC, dSPSC and muSPSC implementations are shown in Fig 15. As can be noticed the unbounded multipush implementation (muSPSC) obtain the best performance reaching a maximum speedup of 1.4, whereas the bounded multipush implementation (mSPSC) reaches a maximum speedup of 1.28 and finally the dynamic list-based queue (dSPSC) does not obtain any performance improvement reaching a maximum speedup of 0.98. This simple test, proves the effectiveness of the uSPSC queue implementation with respect to the list-based FIFO queue implementation when used in real case scenario.

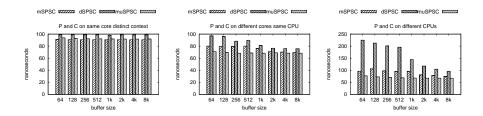


Figure 15: Average latency time (in nanoseconds) of the pipeline microbench-mark implementation when using the mSPSC, dSPSC and muSPSC queue. P and C are pinned: on the same core (left), on different core (middle), on different CPUs (right).

6 Conclusions

In this report we reviewed several possible implementations of fast wait-free Single-Producer/Single-Consumer (SPSC) queue for shared cache multi-core starting from the well-known Lamport's circular buffer algorithm. A novel implementation of unbounded wait-free SPSC queue has been introduced with a formal proof of correctness. The new implementation is able to minimize dynamic memory allocation/deallocation and increases cache locality thus obtaining very good performance figures on modern shared cache multi-core. We believe that the unbounded SPSC algorithm presented here can be used as an efficient alternative to the widely used list-based FIFO queue.

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