

# IFM 2014 Lecture 3

## Uncovered interest parity and flex-price monetary models of the exchange rate

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## Lecture 3

- Uncovered interest parity (UIP)
- Introduction to monetary models of exchange rates
- The flex-price monetary model of the exchange rate
- Implications of the flex-price monetary model

# Uncovered interest parity

- UIP is a theory about interest rates that relies on **bond market arbitrage**
- More specifically, UIP states that

$$i = i^* + \frac{\Delta S^e}{S}$$

where

$i$  = nominal interest rate on domestic bonds

$i^*$  = nominal interest rate on foreign bonds

$\frac{\Delta S^e}{S}$  = expected rate of depreciation of the home currency

- That is, 
$$i = i^* + \text{Expected capital gain on } S$$

# Uncovered interest parity

- The UIP formulas on the previous slide state that the return on home bonds is equal to the expected return on foreign bonds
- The latter includes the **expected** capital gain (or loss) on the exchange rate because exchange rates are **uncertain**
- An expected depreciation in the exchange rate is an expected capital gain from holding foreign bonds. An expected appreciation is an expected capital loss.
- Because it makes good economic sense for returns to be equalised across bonds, many models of exchange rates include UIP as one of the equations that must hold

# UIP: a UK-China example

- Suppose Chinese interest rates are 4% and UK interest rates are 0.5%
- That is,  $0.5\% = 4\% + \frac{\Delta S^e}{S} \implies \frac{\Delta S^e}{S} = -3.5\%$
- So UK investors will be indifferent between home bonds and Chinese bonds if the Pound is expected to strengthen against the Yuan by 3.5% over the next year
- This is because they will receive 4% on Chinese bonds in a year's time, but this is expected to be worth less in terms of Pounds
- Investors expect to 'lose' 3.5% when they convert Yuan back into Pounds to spend their return in the UK

# UIP assumptions

- Several assumptions are required for UIP to hold
  - ① Perfect mobility of capital
  - ② Bonds are not risky –  $i$  and  $i^*$  known with certainty
  - ③ Home and foreign bonds are viewed by investors as *perfect substitutes*
- Assumption 1 ensures that there is unrestricted **arbitrage**
- Assumptions 2 and 3 ensure that investors see home and foreign bonds as **identical**
- Monetary models with UIP are making assumptions 1, 2, 3

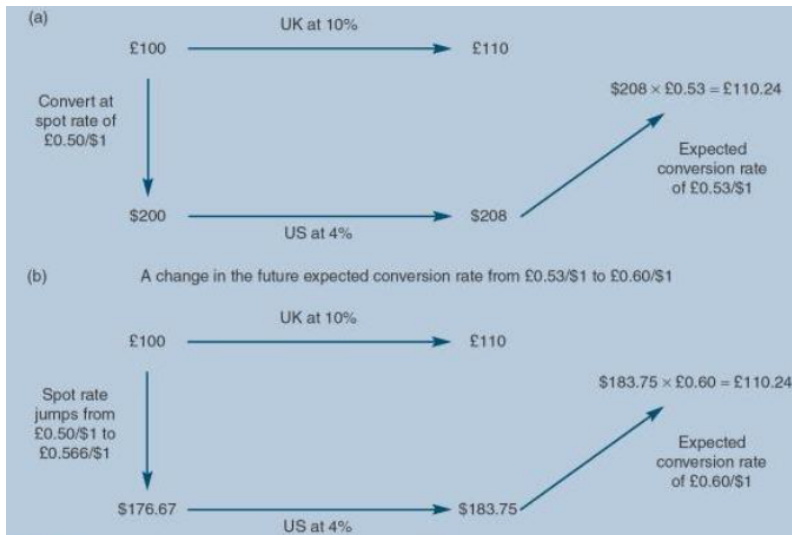
# UIP and expectations

- The UIP condition implies future expectations about exchange rates can have a significant impact on the current spot rate  $S$
- We can see this by rearranging the UIP condition for  $S$ :

$$S = \frac{\Delta S^e}{i - i^*}$$

- Pilbeam Box 7.1 gives an excellent discussion of the impact of changes in exchange rate expectations on the spot rate
- UIP is an 'asset approach' to exchange rates because it recognises the importance of expectations about the future for exchange rates today

# UIP and expectations (Pilbeam Box 7.1)





# Intro to monetary models of exchange rates

- In monetary models of exchange rates money supply and money demand are important determinants of exchange rate movements
- The UIP condition is assumed to hold – ie this is a separate equation in the model
- Some of the models have perfectly flexible prices, but others have 'sticky' prices
- In monetary models with flexible prices, PPP will hold at all points in time – ie short run and long run. But in models with sticky prices, PPP will hold only in the long run.

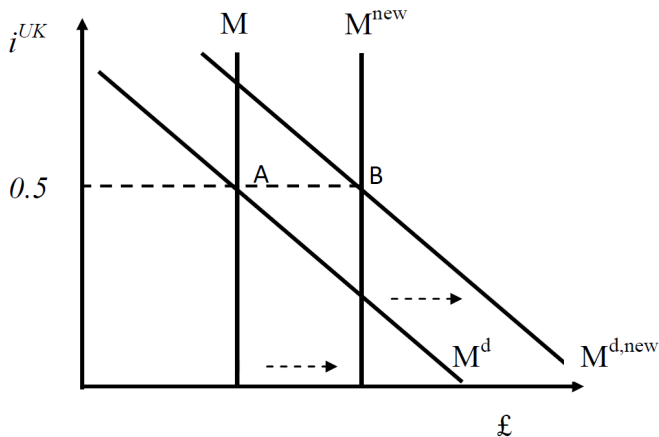
# Intro to monetary models of exchange rates

- All monetary models start from a definition of money demand
- Money demand is negatively related to interest rates – the **opportunity cost** of holding money
- Since money supply and money demand must be equal in equilibrium, interest rates can be related back to the money supply
- Since interest rates affect exchange rates by UIP, the exchange rate will depend upon the money supply

# Monetary example: BoE

- Suppose the Bank of England wishes to maintain interest rates at 0.5% well into the recovery
- As the economy recovers, the demand for money will rise because households will wish to carry out more transactions
- The BoE will therefore have to increase money supply in pace with money demand in order to keep interest rates at 0.5%
- If it doesn't do this, the likely outcome is that interest rates will rise
- Monetary models of exchange rates are consistent with these predictions

# Monetary example: BoE



- $M$  = money supply and  $M^d$  = money demand

# The flex-price monetary model of the exchange rate

- The flex-price monetary model of the exchange rate has perfectly flexible prices
- As discussed in Lecture 1, this is a reasonable assumption only in times of high inflation or hyperinflation, or in the long run
- Nevertheless, the simple flex-price model is important because it attempts to explain nominal exchange rate movements by relating the exchange rate to money supplies
- For example, it can help to explain why countries with high money supply growth tend to have depreciating currencies

# The flex-price monetary model of the exchange rate

## Assumption 1

- The domestic demand for real money balances is

$$m^d - p = \eta y - \sigma i$$

where

$i$  = nominal interest rate on domestic bonds

$y$  = domestic real GDP (expressed in logs)

$m^d - p$  = real domestic demand for money (in logs)

- In the foreign country,

$$m^{d*} - p^* = \eta y^* - \sigma i^*$$

where 'starred' variables are foreign prices or quantities

# The flex-price monetary model of the exchange rate

## Assumption 2

- There is equilibrium in the money market:

$$\text{Money demand} = \text{Money supply}$$

- Mathematically,  $m^d = m$  in the home country, where  $m$  is the domestic money supply (in nominal terms)
- Likewise, we have  $m^{d*} = m^*$  in the foreign country, where  $m^*$  is the foreign money supply
- We can therefore say that

$$(1) \quad m - p = \eta y - \sigma i \quad \text{and} \quad (2) \quad m^* - p^* = \eta y^* - \sigma i^*$$

# The flex-price monetary model of the exchange rate

## Assumption 3

- Purchasing power parity holds:

$$\text{PPP: } s = p - p^*$$

- Now, subtract (2) from (1) to get

$$m - m^* - (p - p^*) = \eta(y - y^*) - \sigma(i - i^*)$$

- Rearranging this equation gives

$$p - p^* = m - m^* - \eta(y - y^*) + \sigma(i - i^*)$$



# The flex-price monetary model of the exchange rate

- Now, substitute for  $p - p^*$  using PPP:

$$\text{FPMM: } s = m - m^* - \eta(y - y^*) + \sigma(i - i^*)$$

- This equation predicts that the nominal exchange rate is affected by
  - ① Relative money supplies
  - ② Relative levels of real GDP
  - ③ Nominal interest rate differential
- Both (1) and (3) have a positive effect on the exchange rate, but a rise in relative GDPs lowers the exchange rate (ie an appreciation)

# The flex-price monetary model of the exchange rate

## Assumption 4 – UIP holds

- The FPMM equation is known as a '**reduced-form**' equation
- This is because it contains variables on the RHS which are determined inside the model
- In particular, the interest rate differential is given by **UIP in logs**:

$$i - i^* = \Delta s^e$$

where  $\Delta s^e$  is the expected rate of depreciation

- Substituting in the FPMM equation we have a **forward-looking** equation:

$$s = m - m^* - \eta(y - y^*) + \sigma \Delta s^e$$

# Implications of the FPMM (1)

- Suppose for simplicity that GDPs and interest rates are constant
- The rate of depreciation in the home currency is then

$$\Delta s = \Delta m - \Delta m^*$$

- **Rate of dep. = home money growth – foreign money growth**
- **Example:** if UK money growth is 10% and US money growth is 2%, what rate of depreciation in the Pound does FPMM predict?

# Implications of the FPMM (2)

- Now suppose instead that money supplies and interest rates are constant but GDPs are growing
- The FPMM predicts that

$$\Delta s = -\eta(\Delta y - \Delta y^*)$$

- **Example:** if Chinese growth is 7%, US growth is 2% and  $\eta = 0.5$ , what is the rate of appreciation of the RNB against the Dollar?

# Implications of the FPMM (3)

- Our forward-looking equation for the nominal exchange rate predicts that the expected future rate of depreciation affects the current exchange rate
- **Example:** suppose that the expected rate of depreciation rises from zero to  $\Delta s^e = 5\%$
- The predicted impact on the exchange rate is  $\Delta s = \sigma \times 5\%$ . Notice that the impact of expectations on the current exchange rate depends crucially on  $\sigma$ .
- The parameter  $\sigma$  determines the sensitivity of money demand to the nominal interest rate

# Implications of the FPMM (4)

- The variables on the RHS of the FPMM equation are **economic fundamentals**
- The FPMM predicts that only economic fundamentals and the parameters of the money demand function matter for exchange rates
- Consequently, there is no allowance for the potential impact of 'bubbles' or currency speculation for the exchange rate
- The fact that the exchange rate is the outcome of trading on FOREX markets is also ignored
- However, the FPMM does allow exchange rate expectations to affect the current exchange rate – albeit that these expectations are assumed to be **rational expectations**

# Testing the FPMM

- In order to test the flex-price monetary model, we can compare its predictions against data
- Data is readily available for exchange rates, money supplies, GDPs and interest rates
- The basic idea of these tests is to see whether the models can explain real-world movements in exchange rates over various horizons
- In Lecture 5 we will consider how well the flex-price monetary model does in these tests
- We will also look at the empirical performance of the sticky price monetary model, which we will discuss in the next lecture

# Next time...

- We will look at the sticky-price monetary model of the exchange rate, ie the Dornbusch 'overshooting' model
- In addition, we will study the implications of Frankel's real interest rate differential model
- This is a general monetary exchange rate model that incorporates the flex-price model and the Dornbusch model as special cases
- **Advance reading:**
  - ① The same as last week, if you haven't already read it!
  - ② Pilbeam, Ch. 7.5 to 7.13 or Rogoff (2001) from the Reading List