

IFM 2014 Lecture 2

Purchasing Power Parity (PPP)

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Lecture 2

- PPP and the law of one price (LOOP)
- Empirical evidence on PPP and LOOP
- The PPP puzzle
- Explanations for the PPP puzzle

Purchasing Power Parity (PPP)

- PPP predicts that national price levels will be equal when converted to a common currency
- \implies **Purchasing power** should be equalised across countries
- Example: \$100 should buy the same basket of goods in US and China
- PPP is built upon the international law of one price (LOOP), which applies to internationally traded goods
- Goods market **arbitrage** is crucial for LOOP...

The law of one price (LOOP)

- LOOP is basically PPP at the micro level of individual goods
- It states that the domestic and foreign prices of an identical good should be equal when expressed in terms of a common currency
- LOOP implies that for any good j

$$P_j = SP_j^*$$

where

P_j = domestic price of good j

P_j^* = foreign price of good j

S = bilateral nominal exchange rate

LOOP example: iPhones in UK and US

- LOOP requires that

$$P_{iPhone}^{UK} = SP_{iPhone}^{US} \implies 500GBP = S \times \$750$$

- LOOP therefore predicts

$$S = \frac{500GBP}{\$750} = 0.66 \text{ pounds per dollar}$$

- Now suppose that $P_{iPhone}^{UK} = 500GBP$ still, but the Pound weakens to $S = 0.80$ pounds per dollar
- For LOOP to hold we now require that

$$P_{iPhone}^{US} = \frac{500GBP}{0.80GBP \text{ per } \$} = \$625$$

- US price is pushed down by arbitrage – cheap UK iPhones imported

LOOP and PPP

- Suppose there are N goods in total and α_j is the weight given to good j in the Consumer Prices Index (CPI)
- CPIs at home and abroad are

$$P = \sum_{j=1}^N \alpha_j P_j \quad \text{and} \quad P^* = \sum_{j=1}^N \alpha_j P_j^*$$

- Multiplying LOOP by α_j on both sides gives $\alpha_j P_j = S \alpha_j P_j^*$
- Summing on both sides implies PPP

$$\sum_{j=1}^N \alpha_j P_j = S \sum_{j=1}^N \alpha_j P_j^* \quad \text{or} \quad P = SP^*$$

LOOP and PPP: a simple 2-good example

- With 2 goods the home and foreign CPIs are

$$P = \alpha_1 P_1 + \alpha_2 P_2 \quad \text{and} \quad P^* = \alpha_1 P_1^* + \alpha_2 P_2^*$$

- LOOP implies that $P_1 = SP_1^*$ and $P_2 = SP_2^*$

- Therefore,

$$\alpha_1 P_1 = \alpha_1 SP_1^* \quad \text{and} \quad \alpha_2 P_2 = \alpha_2 SP_2^*$$

- Add these equations together: $\alpha_1 P_1 + \alpha_2 P_2 = S(\alpha_1 P_1^* + \alpha_2 P_2^*)$
- In other words,

$$P = SP^*$$

Absolute PPP

- The equation $P = SP^*$ is known as **Absolute PPP**
- It states that **national price levels are equal** when expressed in terms of a common currency
- APPP requires several **assumptions**:
 - 1 Perfect competition
 - 2 Identical goods and tastes across countries
 - 3 All goods must be traded
 - 4 No transport costs
 - 5 No barriers to trade (e.g. tariffs or quotas)

APPP and the real exchange rate

- We define the **real exchange rate** as $Q = \frac{SP^*}{P}$
- The log real exchange rate is $\ln Q = \ln\left(\frac{SP^*}{P}\right)$, or more compactly

$$q = s + p^* - p$$

where lowercase letters are **natural logarithms** (e.g. $q = \ln Q$)

- If APPP is correct, then $Q = 1$ and $q = \ln(1) = 0$
- **We can test whether these predictions hold true using data**

APPP and trade costs

- If $q \neq 0$ then arbitrage opportunities exist and APPP does not hold. This could be due to transport costs or other trade costs (e.g. tariffs).
- Suppose these costs are equal to some positive constant τ
- Within the 'neutral band' $-\tau$ to $+\tau$, arbitrage will not be profitable
- But outside the band arbitrage will take place, causing q to revert to the neutral band
- MacDonald illustrates this concept in Figure 2.1 (p. 42)

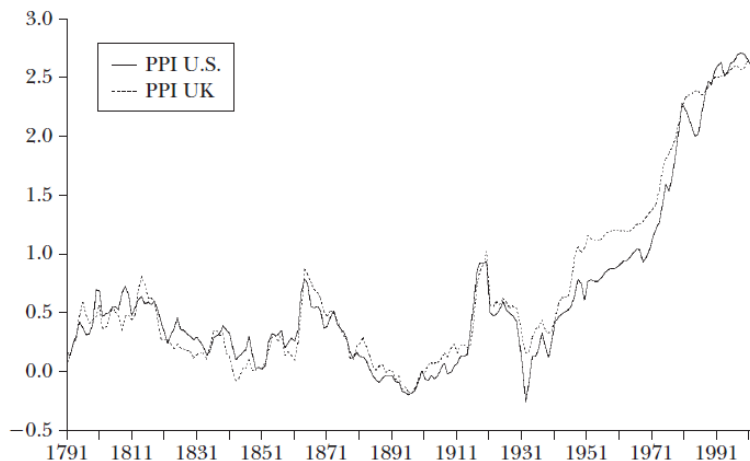
- It is clear from data that APPP does not hold as an exact relationship
- This is hardly surprising given that trade costs are not zero in reality
- Even if they were, we would get deviations from APPP since
 - 1 Different countries have different price index weights
 - 2 Goods are not exactly identical across countries
 - 3 Different baskets of goods in different countries
- Relative PPP makes allowance for these differences, but it does require that they be stable over time

- Suppose that $s = \tau + p - p^*$, where τ = deviation from APPP
- The real exchange rate is then $q = \tau$
- But because τ is constant by assumption, the **change in S DOES NOT** depend on τ :

$$\text{RPPP: } \Delta s = \pi - \pi^*$$

- **Rate of depreciation = home inflation – foreign inflation**
- We can test whether this more realistic PPP theory holds in the data

Empirical evidence on APPP: US vs UK



Source: Taylor and Taylor (2004), Fig 1

Empirical evidence on APPP

- The graph on the last page shows that APP does not hold perfectly and continuously
- Deviations from APPP often last several years – and after 1940 the deviations are rather large
- But overall there is a clear relationship between the two series, so APPP may hold in the long run
- **What can econometrics tell us about whether APPP holds?**

Empirical evidence on APPP

- We can use econometrics to test whether APPP holds as a long run relationship
- **That is: do deviations from APPP ‘die out’, or are they permanent?**
- To find out we can run a regression of the real exchange rate q on its past value q_{-1} :

$$q = \beta + \rho q_{-1} + \varepsilon$$

- **Two cases:**
 - ① $\rho < 1$: Mean-reversion – APPP holds in long run
 - ② $\rho = 1$: Unit root – q a random walk so long run APPP rejected

Empirical evidence on APPP

- The extent of mean reversion can be measured using **half-life**:

$$\text{Half-life} = \frac{\ln(0.5)}{\ln(\hat{\rho})}$$

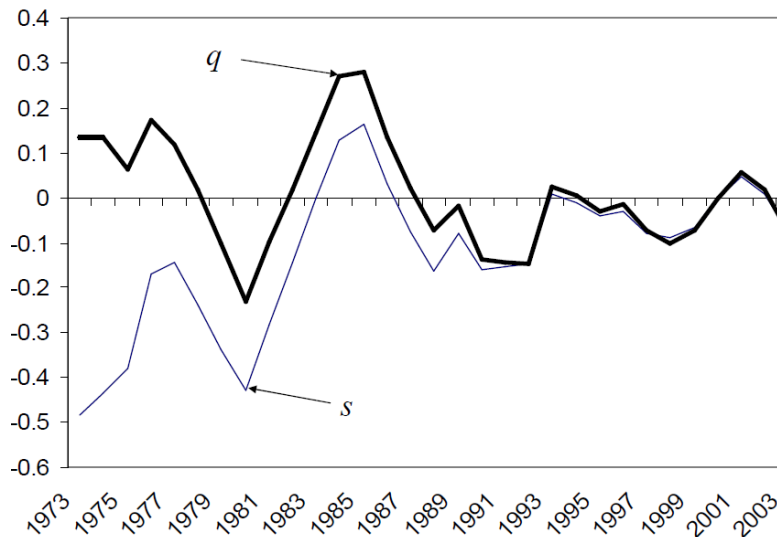
where $\hat{\rho}$ is the regression estimate of ρ

- The half-life is the number of years it takes for one-half of a real exchange rate deviation to 'die out'
- Typically, we find $\hat{\rho}$ between 0.80 and 0.87 in annual data, implying a half-life of 3 to 5 years
- Therefore, we conclude that APPP holds in the long run

Empirical evidence on APPP

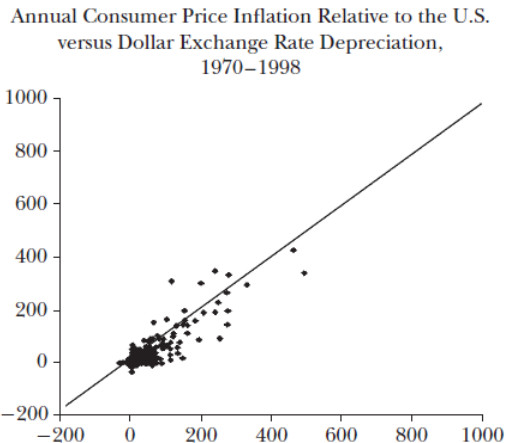
- APPP predicts that real exchange rates are constant, but they are actually very volatile
- For example, real (and nominal) exchange rates are far more volatile than interest rates
- We can see this volatility on the next slide
- We can also see how real exchange rates tend to revert back to mean, as suggested by the half-life results we discussed above

Log exchange rates (GBP per USD)



Source: OECD

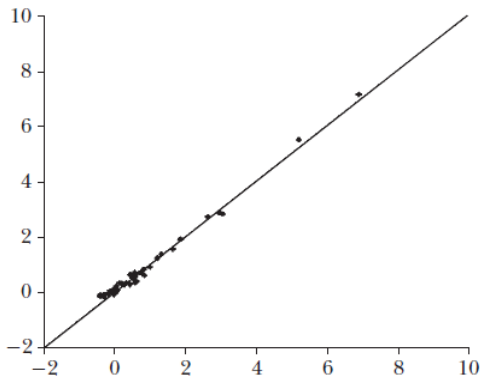
Empirical evidence on RPPP (short run)



Source: Taylor and Taylor (2004), Fig 2

Empirical evidence on RPPP (long run)

Consumer Price Inflation Relative to the U.S. versus
Dollar Exchange Rate Depreciation,
29-Year Average, 1970–1998



Source: Taylor and Taylor (2004), Fig 2

Empirical evidence on RPPP

- There are substantial deviations from RPPP at a yearly horizon, but when we look at a 29-year average it holds almost exactly
- Taylor and Taylor (2004, pp. 138-9) report that the results for a 10-year average are very similar
- So, although RPPP clearly does not hold at a short horizon, it does appear to hold (at least approximately) at longer horizons such as 10+ years
- This conclusion is not just true for the US – it holds for other industrialised economies as well

Starbucks Tall Latte Index^a (price differentials in US\$ terms)

Country	Difference
UK	+17
Euro Area	+33
Japan	+13

(a) The Economist (2004). Figures are % differences.

- The Latte Index and the Big Mac Index indicate substantial deviations from LOOP
- Economic studies reach the same conclusion (see MacDonald p. 48)
- LOOP appears to hold only for a small number of commodities such as gold (see Rogoff 1996, Table 2)

The PPP Puzzle

- It is difficult to explain why deviations from PPP last as long as suggested by a half-life of 3-5 years. Rogoff (1996) therefore argues that there is a **‘PPP puzzle’**.
- Price stickiness and unexpected changes in monetary policy could explain large short-term deviations from PPP
- But why do these deviations persist for so long when most prices are changed at least once a year?
- If we can answer that question convincingly we will have a solution to the PPP puzzle
- Let's consider some possible explanations...

PPP Puzzle explanations

- We will look at the following explanations for the PPP puzzle:
 - 1 Border effects
 - 2 Pricing to market
 - 3 The Balassa-Samuelson hypothesis
 - 4 Aggregation bias
- There are some additional explanations, but these 4 are considered to be some of the most important

Explanation 1: Border effects

- Rogoff (1996, pp. 664-5) concludes that the large and persistent deviations from PPP that we observe must be due to international goods markets being less integrated than domestic markets
- He argues that this could be due to trade costs, additional information costs of exploiting international arbitrage opportunities, or lack of labour mobility between countries
- It may be that real exchange rates only revert to mean after large deviations from PPP because at such times the profits available from arbitrage dominate these costs
- In support of this argument, Engel and Rogers (1996) find that the Canadian-US border is important for explaining price differentials

Explanation 1: Border effects

Engel and Rogers (1996): How wide is the border?

- Consumer prices from US and Canadian cities in USD
- Monthly data: 1978-1994
- If transport costs are an important factor, then price differentials should be large between distant cities **in the same country**
- They are – but borders are much more important, with the same impact upon price differentials as a **distance of 75,000 miles!**
- It is not clear why the border is so important, but this may be due to country-specific productivity shocks or pricing to market

Explanation 2: Pricing to market (PTM)

- In our iPhone example, a depreciation in Sterling made UK iPhones cheaper to US citizens, which in turn drove down USD prices
- This is because under perfect competition there is **full exchange rate pass through**
- But with imperfect competition and differentiated products UK exporters may not reduce the USD price at all – **zero exchange rate pass through!**
- This is because firms with market power can practice price discrimination
- Partial exchange rate pass-through is also a possibility...

Explanation 2: Pricing to market (PTM)

- PTM example: Lindauer in UK and NZ
- **Krugman (1986)** gives the example of European automobile prices in fact rising in USD when European currencies were depreciating
- Krugman also finds formal evidence of PTM by German exporters in the 1980s, albeit that this is confined mainly to machinery and transport equipment
- In a survey of the literature, Goldberg and Knetter (1997) conclude that pass-through from the exchange rate to import prices in the US has been partial – **around 60%**
- There is also evidence that exchange rate pass-through is partial in other economies (see MacDonald p. 84)

Explanation 3: The Balassa-Samuelson hypothesis

- The B-S hypothesis is built on several assumptions:
 - 1 PPP is assumed to hold in the traded goods sector
 - 2 Countries with high GDP per capita have higher relative productivity in the traded goods sector
 - 3 Capital and labour can move freely between sectors in the home country
 - 4 Capital is mobile internationally, but labour is not
- Suppose the home price index is a weighted average of the price levels in the non-traded and traded sectors:

$$P = \alpha P^{NT} + (1 - \alpha) P^T$$

Explanation 3: The Balassa-Samuelson hypothesis

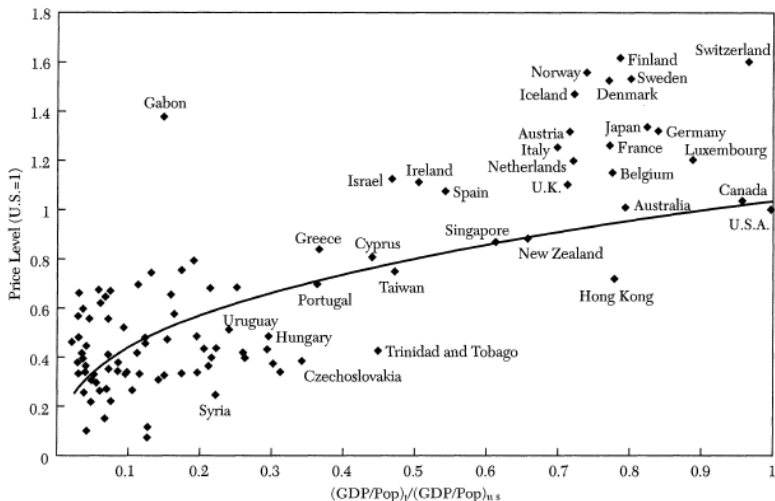
- The simplest possible statement of B-S is

$$P^{NT} = \frac{A^T}{A^{NT}}$$

where $\frac{A^T}{A^{NT}}$ is relative productivity in the traded goods sector

- Therefore, by Assumption 2, the B-S hypothesis predicts the price level in the non-traded goods sector will be higher in rich countries
- With P^T fixed by PPP (Assumption 1), a rise in P^{NT} raises P
- \implies Richer countries will have higher price levels and their real exchange rates will appreciate

International price levels vs GDP per head



Source: Rogoff (1996), Fig 3

Explanation 3: The Balassa-Samuelson hypothesis

- But the link between productivity and real exchange rates is less clear
- Japan is often cited as an example where the B-S hypothesis may apply (see Rogoff 1996, pp. 661-2). But the B-S hypothesis does not seem to work as well for other industrialised economies.
- For example, under B-S, productivity in the traded and non-traded sectors should have equal but opposite effects on the real exchange rate, but MacDonald and Ricci (2001) conclusively reject this using OECD sectoral data (MacDonald, pp. 76-77)
- In addition, because technology diffuses across borders, poor countries may be able to adopt rich country technologies over time, but the B-S hypothesis does not allow for this

Explanation 4: Aggregation bias

- Imbs et al. (2002): if the prices of different goods revert to mean at different speeds, then aggregating across prices will introduce a positive bias into estimated half-lives (MacDonald, p. 64-66)
- So, using aggregate data will **overstate the true half-life**
- Using Eurostat data, Imbs et al. find significantly lower half-lives for real exchange rates once the upward bias is removed (e.g. 11 months). They conclude that **AB largely solves the PPP puzzle**.
- Parsley and Wei (2003) use the Big Mac Index and the prices of tradable Big Mac components to avoid the aggregation bias issue
- They find that the half-life of Big Mac deviations is less than 2 years, which provides further support for the findings of Imbs et al.

Explanation 4: Aggregation bias

- Chen and Engel (2005) argue that the analysis of Imbs et al. is flawed and that **“aggregation bias does not explain the PPP puzzle”** (MacDonald, p. 66)
- They argue that **measurement error** in tradables prices was an issue in the original analysis. When they correct for this, they find even higher half-lives than the 3-5 years reported in Rogoff (1996).
- However, Imbs et al. have argued that it is in fact CE who are mistaken, and they refuse to budge from their original conclusion
- In summary, aggregation bias is a possible explanation for the PPP puzzle, albeit a rather controversial one!

Next time...

- In the next lecture we will look at monetary models of exchange rates and their predictions
- You will also be introduced to the concept of uncovered interest parity (UIP)
- **Advance reading:**
 - ① Pilbeam Ch. 7.2 or Copeland Ch. 3.1
 - ② MacDonald Ch. 4.1 and 5.2 (except 5.2.2)