

Assignment #4: 排序、栈、队列和树

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说明:

1) The complete process to learn DSA from scratch can be broken into 4 parts:

Learn about Time complexities, learn the basics of individual Data Structures, learn the basics of Algorithms, and practice Problems.

2) 请把每个题目解题思路（可选），源码Python, 或者C++（已经在Codeforces/Openjudge上AC），截图（包含Accepted），填写到下面作业模版中（推荐使用 typora <https://typoraio.cn>，或者用 word）。AC 或者没有AC，都请标上每个题目大致花费时间。

3) 提交时候先提交pdf文件，再把md或者doc文件上传到右侧“作业评论”。Canvas需要有同学清晰头像、提交文件有pdf、“作业评论”区有上传的md或者doc附件。

4) 如果不能在截止前提交作业，请写明原因。

编程环境

操作系统: Windows 11 23H2

Python编程环境: Visual Studio Code 1.86.2

1. 题目

05902: 双端队列

<http://cs101.openjudge.cn/practice/05902/>

思路: 利用pop(0)删除左侧元素，思路简单。

代码

```
1 class deque(object):
2     dequeList:list
3
4     def __init__(self):
5         self.dequeList = []
6     def __str__(self):
7         if self.dequeList:
8             return (' '.join(str(T) for T in self.dequeList))
9         else:
10            return "NULL"
11     def append(self, T):
```

```
12         self.dequeList.append(T)
13     def appendLeft(self, T):
14         self.dequeList.insert(0, T)
15     def pop(self):
16         self.dequeList.pop()
17     def popLeft(self):
18         self.dequeList.pop(0)
19
20 def op(dequeIn:deque, operatorType:int, t:int):
21     if operatorType == 1:
22         dequeIn.append(t)
23     elif t == 0:
24         dequeIn.popLeft()
25     else:
26         dequeIn.pop()
27
28 for _ in range(int(input())):
29     dequeI = deque()
30     for __ in range(int(input())):
31         operatorType, t = map(int, input().split())
32         op(dequeI, operatorType, t)
33     print(dequeI)
```

代码运行截图

状态: Accepted

源代码

```
class deque(object):
    dequeList:list

    def __init__(self):
        self.dequeList = []
    def __str__(self):
        if self.dequeList:
            return (' '.join(str(T) for T in self.dequeList))
        else:
            return "NULL"
    def append(self, T):
        self.dequeList.append(T)
    def appendLeft(self, T):
        self.dequeList.insert(0, T)
    def pop(self):
        self.dequeList.pop()
    def popLeft(self):
        self.dequeList.pop(0)

def op(dequeIn:deque, operatorType:int, t:int):
    if operatorType == 1:
        dequeIn.append(t)
    elif t == 0:
        dequeIn.popLeft()
    else:
        dequeIn.pop()

for _ in range(int(input())):
    dequeI = deque()
    for __ in range(int(input())):
        operatorType, t = map(int, input().split())
        op(dequeI, operatorType, t)
    print(dequeI)
```

02694: 波兰表达式

<http://cs101.openjudge.cn/practice/02694/>

思路：反向读取，将数字入栈，遇到符号就计算并去掉用于计算的数字，最后在读完（IndexError）时输出最终结果。

代码

```
1 operatorSet = {'+', '-', '*', '/'}
2 def isOp(t):
3     global operatorSet
```

```

4     return t in operatorSet
5 def op(op, i, j):
6     if op == '+':
7         return i + j
8     elif op == '-':
9         return i - j
10    elif op == '*':
11        return i * j
12    else:
13        return i / j
14 def useable(i):
15     global operatorSet
16     if i in operatorSet:
17         return(i)
18     else:
19         return((float(i)))
20
21 l = list(map(useable, input().split()))
22 stack = []
23 i = -1
24 while 1:
25     try:
26         x = l[i]
27         if isOp(x):
28             stack.append(op(x, stack[-1], stack[-2]))
29             stack.pop(-2)
30             stack.pop(-2)
31         else:
32             stack.append(x)
33         i -= 1
34     except IndexError:
35         print("%.6f\n"%stack[-1])
36         break

```

代码运行截图

状态: Accepted

源代码

```
operatorSet = {'+', '-', '*', '/'}
def isOp(t):
    global operatorSet
    return t in operatorSet
def op(op, i, j):
    if op == '+':
        return i + j
    elif op == '-':
        return i - j
    elif op == '*':
        return i * j
    else:
        return i / j
def useable(i):
    global operatorSet
    if i in operatorSet:
        return(i)
    else:
        return((float(i)))

l = list(map(useable, input().split()))
stack = []
i = -1
while 1:
    try:
        x = l[i]
        if isOp(x):
            stack.append(op(x, stack[-1], stack[-2]))
            stack.pop(-2)
            stack.pop(-2)
        else:
            stack.append(x)
        i -= 1
    except IndexError:
        print("%.6f\n"%stack[-1])
        break
```

24591: 中序表达式转后序表达式

<http://cs101.openjudge.cn/practice/24591/>

思路：这道题想了挺久的，最初的代码是通过另一个用于标识括号层数的stack实现的，原理上也没问题但是最后结果是同个括号里计算顺序会变倒序。原理上和波兰表达式类似，只是因为几乎是反方向进行，所以需要考虑的边界情况比较多，多考虑一些边界情况思路就会清晰一些。

代码

```

1 operatorSet = {'+', '-', '*', '/', '(', ')'}
2 operatorWeight = {'+': 0, '-': 0, '*': 1, '/': 1, '(': -1, ')': -1}
3 def isop(t):
4     global operatorSet
5     return t in operatorSet
6 def op(op, i, j):
7     if op == '+':
8         return i + j
9     elif op == '-':
10        return i - j
11    elif op == '*':
12        return i * j
13    else:
14        return i / j
15 def useable(string):
16     val = []
17     number = ""
18     global operatorSet
19     for x in string:
20         if x in operatorSet:
21             if number:
22                 val.append(number)
23                 val.append(x)
24                 number = ""
25             else:
26                 number += x
27         if number:
28             val.append(number)
29     return val
30
31 for _ in range(int(input())):
32     ans = []
33     stack = []
34     n = 0
35     l = ["("] + useable(input()) + [")"]
36     while 1:
37         try:
38             x = l[n]
39             if isop(x):
40                 if x == '(':
41                     stack.append(x)
42                 elif x == ')':
43                     while 1:
44                         y = stack[-1]
45                         if y != '(':
46                             ans.append(y)
47                             stack.pop()
48                         else:
49                             stack.pop()
50                             break
51                 else:
52
53                     while operatorWeight[stack[-1]] >= operatorWeight[x]:
54                         ans.append(stack[-1])
55                         stack.pop()

```

```
56         stack.append(x)
57     else:
58         ans.append(x)
59     n += 1
60 except IndexError:
61     stack.reverse()
62     print(' '.join(ans + stack))
63     break
```

代码运行截图

状态: Accepted

源代码

```
operatorSet = {'+', '-', '*', '/', '(', ')'}
operatorWeight = {'+': 0, '-': 0, '*': 1, '/': 1, '(': -1, ')': -1}
def isOp(t):
    global operatorSet
    return t in operatorSet
def op(op, i, j):
    if op == '+':
        return i + j
    elif op == '-':
        return i - j
    elif op == '*':
        return i * j
    else:
        return i / j
def useable(string):
    val = []
    number = ""
    global operatorSet
    for x in string:
        if x in operatorSet:
            if number:
                val.append(number)
                val.append(x)
                number = ""
            else:
                number += x
        if number:
            val.append(number)
    return val

for _ in range(int(input())):
    ans = []
    stack = []
    n = 0
    l = ["("] + useable(input()) + [")"]
    while 1:
        try:
            x = l[n]
            if isOp(x):
                if x == '(':
                    stack.append(x)
                elif x == ')':
                    while 1:
                        y = stack[-1]
                        if y != '(':
                            ans.append(y)
                            stack.pop()
                        else:
                            stack.pop()
                            break
            else:
                while operatorWeight[stack[-1]] >= operatorWeight[x]:
                    ans.append(stack.pop())
                stack.append(x)
            n += 1
        except:
            break
    print("".join(ans))
```



```

        while operatorweight[stack[-1]] >= operatorweight[x]:
            ans.append(stack[-1])
            stack.pop()
            stack.append(x)
        else:
            ans.append(x)
            n += 1
    except IndexError:
        stack.reverse()
    print(' '.join(ans + stack))
    break

```

22068: 合法出栈序列

<http://cs101.openjudge.cn/practice/22068/>

思路：思路其实很直接，倒过来模拟stack的push()和pop()操作，观察最终是否能够清空stack，做的时候感觉最麻烦的一点是最终判断递归是否结束，调试了好久。

代码

```

1  def check(i = -1, j = -1, length = -1):
2      if i > min:
3          if stack and stack[-1] == standard[i]:
4              stack.pop()
5              i -= 1
6          else:
7              try:
8                  stack.append(test[j])
9                  j -= 1
10             except IndexError:
11                 pass
12         else:
13             return "YES"
14         if len(stack) == length:
15             if length == 0:
16                 return "YES"
17             else:
18                 return "NO"
19         return check(i, j, len(stack))
20
21 standard = input()
22 while 1:
23     try:
24         test = input()
25         if len(test) != len(standard) or set(test) != set(standard): #I hate
this...
26             print("NO")

```

```

27         else:
28             min = -len(standard)
29             stack = []
30             i = -1 #standard
31             j = -1 #text
32             print(check())
33     except EOFError:
34         break

```

代码运行截图

状态: Accepted

源代码

```

def check(i = -1, j = -1, length = -1):
    if i > min:
        if stack and stack[-1] == standard[i]:
            stack.pop()
            i -= 1
        else:
            try:
                stack.append(test[j])
                j -= 1
            except IndexError:
                pass
    else:
        return "YES"
    if len(stack) == length:
        if length == 0:
            return "YES"
        else:
            return "NO"
    return check(i, j, len(stack))

standard = input()
while 1:
    try:
        test = input()
        if len(test) != len(standard) or set(test) != set(standard): #I
            print("NO")
        else:
            min = -len(standard)
            stack = []
            i = -1 #standard
            j = -1 #text
            print(check())
    except EOFError:
        break

```

06646: 二叉树的深度

<http://cs101.openjudge.cn/practice/06646/>

思路：定义树节点（包含属性：nodeID与两个子节点的nodeID）与树（有一个用于存所有节点，以nodeID为键的dict()），并通过递归得到树的高度。

代码

```
1 class treeNode(object):
2     leftSubNodeID:int
3     rightSubNodeID:int
4     nodeID:int
5
6     def __init__(self, id, left, right):
7         self.leftSubNodeID = left
8         self.rightSubNodeID = right
9         self.nodeID = id
10
11     def getLeftSubNodeID(self):
12         return self.leftSubNodeID
13
14     def getRightSubNodeID(self):
15         return self.rightSubNodeID
16
17 class biTree(object):
18     nodeDic:dict
19
20     def __init__(self):
21         self.nodeDic = dict()
22
23     def add(self, key, node):
24         self.nodeDic[key] = node
25
26     def get(self, key):
27         if key == -1:
28             return False
29         else:
30             return self.nodeDic[key]
31
32     def getTreeDep(self, nodeID=1):
33         currentNode = self.get(nodeID)
34         if currentNode:
35             return(1 + max(self.getTreeDep(currentNode.getLeftSubNodeID()),
36 self.getTreeDep(currentNode.getRightSubNodeID())))
37         else:
38             return 0
39
40 n = int(input())
41 myBiTree = biTree()
42 for i in range(n):
43     l, r = map(int, input().split())
44     myBiTree.add(i + 1, treeNode(i + 1, l, r))
45 print(myBiTree.getTreeDep())
```

代码运行截图

状态: Accepted

源代码

```
class treeNode(object):
    leftSubNodeID:int
    rightSubNodeID:int
    nodeID:int

    def __init__(self, id, left, right):
        self.leftSubNodeID = left
        self.rightSubNodeID = right
        self.nodeID = id
    def getLeftSubNodeID(self):
        return self.leftSubNodeID
    def getRightSubNodeID(self):
        return self.rightSubNodeID

class biTree(object):
    nodeDic:dict

    def __init__(self):
        self.nodeDic = dict()
    def add(self, key, node):
        self.nodeDic[key] = node
    def get(self, key):
        if key == -1:
            return False
        else:
            return self.nodeDic[key]
    def getTreeDep(self, nodeID=1):
        currentNode = self.get(nodeID)
        if currentNode:
            return 1 + max(self.getTreeDep(currentNode.getLeftSubNodeID), self.getTreeDep(currentNode.getRightSubNodeID))
        else:
            return 0

n = int(input())
myBiTree = biTree()
for i in range(n):
    l, r = map(int, input().split())
    myBiTree.add(i + 1, treeNode(i + 1, l, r))
print(myBiTree.getTreeDep())
```

02299: Ultra-QuickSort

<http://cs101.openjudge.cn/practice/02299/>

思路：使用归并排序兼求逆序数。

代码

```
1 count = 0
2 def merge(la, lb):
3     global count
4     i = j = 0; lc = []
5     while i < len(la) and j < len(lb):
6         if lb[j] < la[i]:
7             lc.append(lb[j])
8             count += len(la) - i
9             j += 1
10        else:
11            lc.append(la[i])
12            i += 1
13        lc += la[i:] + lb[j:]
14    return lc
15 def ultraQuickSort(l, lIndex, rIndex):
16     if rIndex - lIndex <= 1:
17         return
18     mIndex = (lIndex + rIndex) // 2
19     ultraQuickSort(l, lIndex, mIndex)
20     ultraQuickSort(l, mIndex, rIndex)
21     l[lIndex:rIndex] = merge(l[lIndex:mIndex], l[mIndex:rIndex])
22
23 while 1:
24     x = int(input())
25     if x == 0: break
26     count = 0
27     l = [int(input()) for _ in range(x)]
28     ultraQuickSort(l, 0, x)
29     print(count)
```

代码运行截图

状态: Accepted

源代码

```
count = 0
def merge(la, lb):
    global count
    i = j = 0; lc = []
    while i < len(la) and j < len(lb):
        if lb[j] < la[i]:
            lc.append(lb[j])
            count += len(la) - i
            j += 1
        else:
            lc.append(la[i])
            i += 1
    lc += la[i:] + lb[j:]
    return lc
def ultraQuickSort(l, lIndex, rIndex):
    if rIndex - lIndex <= 1:
        return
    mIndex = (lIndex + rIndex) // 2
    ultraQuickSort(l, lIndex, mIndex)
    ultraQuickSort(l, mIndex, rIndex)
    l[lIndex:rIndex] = merge(l[lIndex:mIndex], l[mIndex:rIndex])

while 1:
    x = int(input())
    if x == 0: break
    count = 0
    l = [int(input()) for _ in range(x)]
    ultraQuickSort(l, 0, x)
    print(count)
```

2. 学习总结和收获

这周题目确实比较难，花了很多时间学习相关概念，下周应该找一些题练习一下。主要是栈和排序，感觉和计概内容确实有很大不同。