

$$\boxed{y^5 + 4y^2 + y + 2x^3 = 0} \quad (A)$$

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$$\boxed{G(x, y) = 0} \quad (B)$$

$$D_x [y^5 + 4y^2 + y + 2x^3] = D_x [0];$$

$$D_x [y]^5 + 4 \cdot D_x [y]^2 + D_x [y] + 2 D_x [x^3] = D_x [0];$$

$$5y^4 \cdot y' + 4 \cdot 2 \cdot y \cdot y' + 1 \cdot y^{1-1} \cdot y' + 2 \cdot 3 \cdot x^2 = 0;$$

$$y' [5y^4 + 8y + 1] = -6x^2;$$

$$y' = \frac{-6x^2}{5y^4 + 8y + 1} \quad \text{ou} \quad \boxed{\frac{dy}{dx} = \frac{-6x^2}{5y^4 + 8y + 1}} \quad (C)$$

PARA $x^2 + y^2 - 4 = 0 \Rightarrow \begin{cases} y = +\sqrt{4-x^2} \\ y = -\sqrt{4-x^2} \end{cases}$

DERIVANDO:

$$y = (4 - x^2)^{\frac{1}{2}} \Rightarrow \frac{dy}{dx} = \frac{1}{2} (4 - x^2)^{-\frac{1}{2}} (-2x) = \frac{-x}{(4 - x^2)^{\frac{1}{2}}};$$

$$\frac{dy}{dx} = \frac{-x}{\sqrt{4-x^2}};$$

$$\boxed{\frac{dy}{dx} = \frac{-x}{y}}$$