

12ª Lista de Exercícios Métodos Matemáticos

(Eq. da Onda)

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Resolva:

$$\begin{aligned} 1) \quad & 4y_{xx} = y_{tt}, \quad 0 < x < \pi, \quad t > 0; \\ & y(0, t) = y(\pi, t) = 0, \quad y(x, 0) = \frac{1}{10} \text{Sen}(2x), \\ & y_t(x, 0) = 0. \end{aligned}$$

$$\text{Resp: } y(x, t) = \frac{1}{10} \text{Sen}(2x) \text{Cos}(4t)$$

$$\begin{aligned} 2) \quad & y_{xx} = y_{tt}, \quad 0 < x < 1, \quad t > 0; \\ & y(0, t) = y(1, t) = 0, \quad y(x, 0) = \frac{1}{10} \text{Sen}(\pi x) - \frac{1}{20} \text{Sen}(3\pi x), \\ & y_t(x, 0) = 0. \end{aligned}$$

$$\text{Resp: } y(x, t) = \frac{1}{10} \text{Sen}(\pi x) \text{Cos}(\pi t) - \frac{1}{20} \text{Sen}(3\pi x) \text{Cos}(3\pi t)$$

$$\begin{aligned} 3) \quad & 4y_{tt} = y_{xx}, \quad 0 < x < 2, \quad t > 0; \\ & y(0, t) = y(2, t) = 0, \quad y(x, 0) = \frac{1}{5} \text{Sen}(\pi x) \cdot \text{Cos}(\pi x), \\ & y_t(x, 0) = 0. \end{aligned}$$

$$\text{Resp: } y(x, t) = \frac{1}{10} \text{Sen}(2\pi x) \text{Cos}(\pi t)$$

