

31. (a) Direção reversa (b) Número de bobinas duplas

33.  $3x - y + 3z = 3$  35.  $\frac{\sqrt{3}}{2}x - \frac{1}{2}y + z = \frac{\pi}{3}$

37.  $-x + 2z = 1$  39.  $3\sqrt{14}$  41.  $\sqrt{14}\pi$

43.  $\frac{4}{15}(3^{5/2} - 2^{7/2} + 1)$  45.  $(2\pi/3)(2\sqrt{2} - 1)$

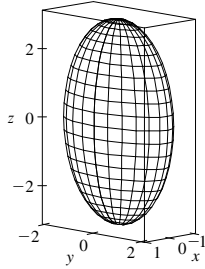
47.  $\frac{1}{2}\sqrt{21} + \frac{17}{4}[\ln(2 + \sqrt{21}) - \ln \sqrt{17}]$  49. 4

51.  $A(S) \leq \sqrt{3}\pi R^2$  53. 13,9783

55. (a) 24,2055 (b) 24,2476

57.  $\frac{45}{8}\sqrt{14} + \frac{15}{16}\ln[(11\sqrt{5} + 3\sqrt{70})/(3\sqrt{5} + \sqrt{70})]$

59. (b)



(c)  $\int_0^{2\pi} \int_0^\pi \sqrt{36 \sin^4 u \cos^2 v + 9 \sin^4 u \sin^2 v + 4 \cos^2 u \sin^2 u} du dv$

61.  $4\pi$  63.  $2a^2(\pi - 2)$

## EXERCÍCIOS 16.7

1. 49,09 3.  $900\pi$  5.  $11\sqrt{14}$  7.  $\frac{2}{3}(2\sqrt{2} - 1)$

9.  $171\sqrt{14}$  11.  $\sqrt{21}/3$  13.  $364\sqrt{2}\pi/3$

15.  $(\pi/60)(391\sqrt{17} + 1)$  17.  $16\pi$  19. 12 21. 4

23.  $\frac{713}{180}$  25.  $-\frac{4}{3}\pi$  27. 0 29. 48 31.  $2\pi + \frac{8}{3}$

33. 4,5822 35. 3,4895

37.  $\iint_S \mathbf{F} \cdot d\mathbf{S} = \iint_D [P(\partial h/\partial x) - Q + R(\partial h/\partial z)] dA$ , onde

 $D$  = projeção de  $S$  no plano  $xy$ 

39.  $(0, 0, a/2)$

41. (a)  $I_z = \iint_S (x^2 + y^2)\rho(x, y, z) dS$  (b)  $4329\sqrt{2}\pi/5$

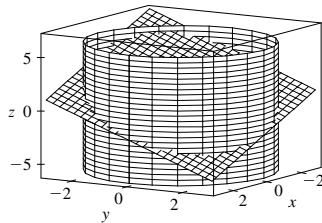
43. 0 kg/s 45.  $\frac{8}{3}\pi a^3 \epsilon_0$  47.  $1248\pi$

## EXERCÍCIOS 16.8

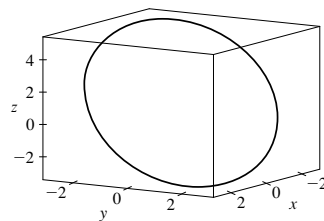
3. 0 5. 0 7. -1 9.  $80\pi$

11. (a)  $81\pi/2$

(b)



(c)  $x = 3 \cos t, y = 3 \sin t,$   
 $z = 1 - 3(\cos t + \sin t),$   
 $0 \leq t \leq 2\pi$



17. 3

## EXERCÍCIOS 16.9

5.  $\frac{9}{2}$  7.  $9\pi/2$  9. 0 11.  $32\pi/3$  13.  $2\pi$

15.  $341\sqrt{2}/60 + \frac{81}{20} \arcsin(\sqrt{3}/3)$

17.  $13\pi/20$  19. Negativa em  $P_1$ , positiva em  $P_2$

21.  $\text{div } \mathbf{F} > 0$  em quadrantes I, II;  $\text{div } \mathbf{F} < 0$  em quadrantes III, IV

## CAPÍTULO 16 REVISÃO

## Teste Verdadeiro-Falso

1. Falso 3. Verdadeiro 5. Falso

7. Falso 9. Verdadeiro 11. Verdadeiro

## Exercícios

1. (a) Negativa (b) Positiva 3.  $6\sqrt{10}$  5.  $\frac{1}{15}$

7.  $\frac{110}{3}$  9.  $\frac{11}{12} - 4/e$  11.  $f(x, y) = e^y + xe^{xy}$  13. 0

17.  $-8\pi$  25.  $\frac{1}{6}(27 - 5\sqrt{5})$  27.  $(\pi/60)(391\sqrt{17} + 1)$

29.  $-64\pi/3$  33.  $-\frac{1}{2}$  37. -4 39. 21

## CAPÍTULO 17

## EXERCÍCIOS 17.1

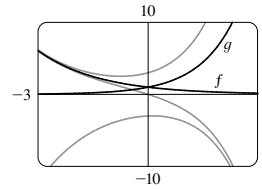
1.  $y = c_1 e^{3x} + c_2 e^{-2x}$  3.  $y = c_1 \cos 4x + c_2 \sin 4x$

5.  $y = c_1 e^{2x/3} + c_2 x e^{2x/3}$  7.  $y = c_1 + c_2 e^{x/2}$

9.  $y = e^{2x}(c_1 \cos 3x + c_2 \sin 3x)$

11.  $y = c_1 e^{(\sqrt{3}-1)x/2} + c_2 e^{-(\sqrt{3}+1)x/2}$

13.  $P = e^{-t}[c_1 \cos(\frac{1}{10}t) + c_2 \sin(\frac{1}{10}t)]$

15. Todas as soluções de tendem a 0 ou  $\pm\infty$  à medida que  $x \rightarrow \pm\infty$ .

17.  $y = 2e^{-3x/2} + e^{-x}$  19.  $y = e^{-2x/3} + \frac{2}{3}xe^{-2x/3}$

21.  $y = e^{3x}(2 \cos x - 3 \sin x)$

23.  $y = \frac{1}{7}e^{4x-4} - \frac{1}{7}e^{3-3x}$  25.  $y = 5 \cos 2x + 3 \sin 2x$

27.  $y = 2e^{-2x} - 2xe^{-2x}$  29.  $y = \frac{e-2}{e-1} + \frac{e^x}{e-1}$

31. Sem solução

33. (b)  $\lambda = n^2\pi^2/L^2$ ,  $n$  um inteiro positivo;  $y = C \sin(n\pi x/L)$

35. (a)  $b - a \neq n\pi$ ,  $n$  qualquer inteiro

(b)  $b - a = n\pi$  e  $\frac{c}{d} \neq e^{a-b} \frac{\cos a}{\cos b}$  a menos que  $\cos b = 0$ , então

$$\frac{c}{d} \neq e^{a-b} \frac{\sin a}{\sin b}$$

(c)  $b - a = n\pi$  e  $\frac{c}{d} = e^{a-b} \frac{\cos a}{\cos b}$  a menos que  $\cos b = 0$ , então

$$\frac{c}{d} = e^{a-b} \frac{\sin a}{\sin b}$$

## EXERCÍCIOS 17.2

1.  $y = c_1 e^{3x} + c_2 e^{-x} - \frac{7}{65} \cos 2x - \frac{4}{65} \sin 2x$

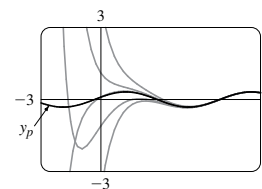
3.  $y = c_1 \cos 3x + c_2 \sin 3x + \frac{1}{13}e^{-2x}$

5.  $y = e^{2x}(c_1 \cos x + c_2 \sin x) + \frac{1}{10}e^{-x}$

7.  $y = \frac{3}{2} \cos x + \frac{11}{2} \sin x + \frac{1}{2}e^x + x^3 - 6x$

9.  $y = e^x(\frac{1}{2}x^2 - x + 2)$

11.

As soluções são assintóticas a  $y_p = \frac{1}{10} \cos x + \frac{3}{10} \sin x$  quando  $x \rightarrow \infty$ . Exceto por  $y_p$ , todas as soluções aproximam-se de  $\infty$  ou  $-\infty$  quando  $x \rightarrow -\infty$ .

13.  $y_p = Ae^{2x} + (Bx^2 + Cx + D) \cos x + (Ex^2 + Fx + G) \sin x$

15.  $y_p = Axe^x + B \cos x + C \sin x$

17.  $y_p = xe^{-x}[(Ax^2 + Bx + C) \cos 3x + (Dx^2 + Ex + F) \sin 3x]$

19.  $y = c_1 \cos(\frac{1}{2}x) + c_2 \sin(\frac{1}{2}x) - \frac{1}{3} \cos x$