## Inverse Transforms and Transforms of Derivatives

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• Some known values for inverse Laplace transforms,  $\mathcal{L}^{-1}\{f(t)\}$ , are shown:

$$1 = \mathcal{L}^{-1} \left\{ \frac{1}{s} \right\}$$

$$t^{n} = \mathcal{L}^{-1} \left\{ \frac{n!}{s^{n+1}} \right\} \quad e^{at} = \mathcal{L}^{-1} \left\{ \frac{1}{s-a} \right\}$$

$$\sin kt = \mathcal{L}^{-1} \left\{ \frac{k}{s^{2} + k^{2}} \right\} \quad \cos kt = \mathcal{L}^{-1} \left\{ \frac{s}{s^{2} + k^{2}} \right\}$$

$$\sinh kt = \mathcal{L}^{-1} \left\{ \frac{k}{s^{2} - k^{2}} \right\} \quad \cosh kt = \mathcal{L}^{-1} \left\{ \frac{s}{s^{2} - k^{2}} \right\}$$

$$(1)$$

• If  $f, f', \ldots, f^{n-1}$  are continuous on  $[0, \infty)$ , and are of exponential order and if  $f^{(n)}(t)$  is piecewise continuous on  $[0, \infty)$ , then (2) where  $F(s) = \mathcal{L}\{f(t)\}$ 

$$\mathcal{L}\{f^{(n)}(t)\} = s^n F(s) - s^{n-1} f(0) - s^{n-2} f'(0) - \dots - f^{(n-1)}(0)$$
(2)