

Rotational Motion & Angular Momentum Lab

AP PHYSICS — 1

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1 Pre-Lab Questions

1. A .15[kg] block is held 1[m] above the floor. Calculate the time it will take for the object to strike the ground.

free fall problem

By using the equation:

$$\Delta x = v_{oy}t + \frac{1}{2}a_yt^2$$

We get:

$$-1 = \frac{1}{2}gt^2$$

Once t is solved for, we find:

$$t = .451[\text{s}]$$

2. Consider the same block hanging vertically and attached by a cord and pulley to a .1[g] frictionless cart sitting on a table. Calculate the time it takes for the object to strike the ground once it is released.

atwood machine problem

By using the equation:

$$g(m_2 - m_1) = (m_1 + m_2)a$$

We get:

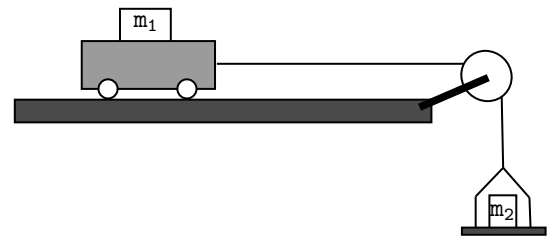
$$g(.15 - .0001) = (.15 + .0001)a$$

Then, a is found to be:

$$a = 9.8001$$

This can then be used to find t :

$$t = \sqrt{\frac{2}{a}} = .4518[\text{s}]$$



3. Consider the same block hanging vertically and, this time, attached by a cord and pulley to a wheel having uniform mass of $.1[kg]$ and a radius of $.1[m]$. Calculate the time it will take for the object to strike the ground once it is released. Hint: Keep the Moment of Inertia as the variable I throughout the calculations for simplicity.

(moment of inertia for disk = $\frac{1}{2}m_d r^2$)

First, set up force equations

Bucket: $F_g - F_T = m_b a$

Disk: $\Sigma \tau = I \alpha$

Then, simplify the Disk formula:

$$r F_T = \frac{1}{2} m_d r^2 \frac{a}{r}$$

When substituted:

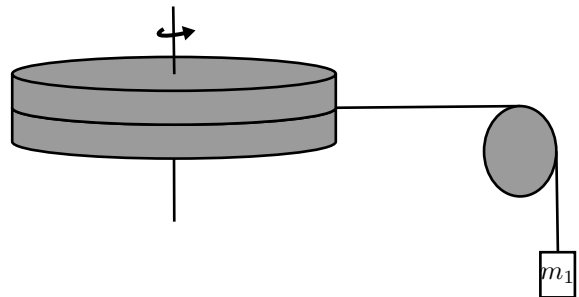
$$m_b g - \frac{1}{2} m_d a = m_b a$$

When solved, a is found to be:

$$a = 7.355 \left[\frac{m}{s^2} \right]$$

This a can then be used to find t :

$$t = \sqrt{\frac{2}{a}} = .5215[s]$$



2 Collected Data & Formulas

Wheel #	Time Trial 1	Time Trial 2	Time Trial 3	Average Time
Wheel 1	4.61[s]	4.615[s]	4.31[s]	4.572[s]
Wheel 2	2.79[s]	2.735[s]	2.535[s]	2.687[s]
Wheel 3	1.45[s]	1.565[s]	1.565[s]	1.527[s]
Wheel 4	.84[s]	.98[s]	.805[s]	.875[s]

Value	Equation
Acceleration of Free Falling Mass	g
Angular Acceleration of the Wheel	$\alpha = \frac{a}{r}$
Final Angular Velocity of the Wheel	$\omega_f = \omega_o + \alpha t$
Moment of Inertia of the Wheel	$I = \frac{\Sigma \tau}{\alpha}$
Angular Momentum of the Wheel	$L = I\omega$

3 Calculations*

3.1 Acceleration of Falling Mass

$$v = \frac{\Delta d}{t} \rightarrow \frac{1[\text{m}]}{1.527[\text{s}]} \rightarrow .6549 \left[\frac{\text{m}}{\text{s}} \right]$$

$$a = \frac{\Delta v}{t} \rightarrow \frac{.6549 \left[\frac{\text{m}}{\text{s}} \right]}{1.527[\text{s}]} = .4289 \left[\frac{\text{m}}{\text{s}^2} \right]$$

3.2 Angular Acceleration of the Wheel

$$a = r\alpha \rightarrow \frac{a}{r} = \alpha$$

$$r = .0333[\text{m}] \rightarrow \frac{.4289 \left[\frac{\text{m}}{\text{s}^2} \right]}{.0333[\text{m}]}$$

$$\therefore \alpha = 12.88 \left[\frac{\text{rad}}{\text{s}^2} \right]$$

3.3 Final Angular Velocity of the Wheel

$$\omega_f = \omega_o + \alpha t \rightarrow \omega_o = 0 \rightarrow \omega_f = \alpha t$$

$$\omega_f = 12.88 \left[\frac{\text{rad}}{\text{s}^2} \right] * 1.527[\text{s}] \rightarrow 19.668 \left[\frac{\text{rad}}{\text{s}} \right]$$

*Calculations performed with Wheel 3 Data

3.4 Moment of Inertia of the Wheel

$$I = \frac{\Sigma \tau}{\alpha} \rightarrow I = \frac{r F_T \sin(\theta)}{\alpha}$$

$$\frac{r F_T \sin(\theta)}{\alpha} \rightarrow \frac{.0333[\text{m}] * F_T}{12.88[\frac{\text{rad}}{\text{s}^2}]}$$

$$F_g - F_T = ma \rightarrow F_T = mg - ma \rightarrow F_T = .05601[\text{N}]$$

$$\frac{.0333[\text{m}] * .05601[\text{N}]}{12.88[\frac{\text{rad}}{\text{s}^2}]} \rightarrow .000145[\text{kg} \cdot \text{m}^2]$$

3.5 Angular Momentum of the Wheel

$$L = I\omega \rightarrow L = .000145[\text{kg} \cdot \text{m}^2] * 19.668 \left[\frac{\text{rad}}{\text{s}} \right]$$

$$\therefore L = .002848 \left[\frac{\text{kg} \cdot \text{m}^2}{\text{s}} \right]$$

4 Analysis

4.1 Data Table

Wheel	Radius [m]	Avg. Time [s]	Accel. of Mass [$\frac{\text{m}}{\text{s}^2}$]	Angul. Accel. [$\frac{\text{rad}}{\text{s}^2}$]	Angul. Vel. [$\frac{\text{rad}}{\text{s}}$]	Moment of Inertia [$\text{kg} \cdot \text{m}^2$]	Angul. Momen. [$\frac{\text{kg} \cdot \text{m}^2}{\text{s}}$]
1	.0175	4.572	.04789	2.733	12.4984	$3.59 \cdot 10^{-4}$	$4.482 \cdot 10^{-3}$
2	.0250	2.687	.1385	5.5401	14.887	$2.53 \cdot 10^{-4}$	$3.763 \cdot 10^{-3}$
3	.0333	1.527	.4289	12.88	19.668	$1.45 \cdot 10^{-4}$	$2.848 \cdot 10^{-3}$
4	.0521	.875	1.3061	25.0695	21.9358	$1.16 \cdot 10^{-4}$	$2.553 \cdot 10^{-3}$

4.2 Analysis Questions

1. Explain the relationship between the radius and free fall time using words.

Free fall time is directly proportional to the square of radius. In other words, radius is inversely proportional to the square root of free fall time.

2. What would you expect to observe if your changing variable was the hanging mass instead of the radius of the wheel? Explain your answer using words and equations.

If the changing variable was the hanging mass, the result of increasing the mass would most likely be a decrease in time and moment of inertia, but an increase in all other factors, such as acceleration, angular velocity, and angular momentum. This is clear because the time it would take to fall would decrease, and acceleration would increase because:

$$v = \frac{\Delta x}{t} \rightarrow a = \frac{\Delta v}{t}$$

Acceleration is inversely proportional to time, and, as such, acceleration will increase because time decreases. Furthermore, angular acceleration will increase because:

$$\frac{a}{r} = \alpha$$

Because angular acceleration will increase, the moment of inertia will decrease because it is inversely proportional to angular acceleration:

$$I = \frac{\Sigma\tau}{\alpha}$$

Hence, it is clear that time and moment of inertia will decrease, whereas all other factors will increase.

3. What would you expect to observe if your changing variable was the mass of the rotating platform instead of the radius of the wheel? Explain your answer using words and equations.

If the mass of the rotating platform were to be increased, moment of inertia and time would increase. All other factors would decrease. This is because the force of tension is not dependent upon the mass of the platform, and is therefore constant. The formula for the moment of inertia is, with proportionality constant, k :

$$I = k * mr^2$$

With an increase in mass, the moment of inertia will be greater. Angular acceleration, and therefore all other factors, aside from time, would be less to keep proportionality:

$$\Sigma\tau = I\alpha$$

Overall, a change in platform mass would result in greater time and moment of inertia, but a decrease in all other factors.