

Linear Algebra 3.1 Homework

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3. $2(4) - 1(3) = 5$

5. $5(3) + 12 = 27$

11. $(\lambda - 3)(\lambda - 1) - 4(2) = \lambda^2 - 4\lambda - 5$

13. (a) $M_{11} = 4$

(a) $C_{11} = 4$

(b) $M_{12} = 3$

(b) $C_{12} = -3$

(c) $M_{21} = 2$

(c) $C_{21} = -2$

(d) $M_{22} = 1$

(d) $C_{22} = 1$

15. (a) $M_{11} = 23$

(a) $C_{11} = 23$

(b) $M_{12} = -8$

(b) $C_{12} = 8$

(c) $M_{13} = -22$

(c) $C_{13} = -22$

(d) $M_{21} = 5$

(d) $C_{21} = -5$

(e) $M_{22} = -5$

(e) $C_{22} = -5$

(f) $M_{23} = 5$

(f) $C_{23} = -5$

(g) $M_{31} = 7$

(g) $C_{31} = 7$

(h) $M_{32} = -22$

(h) $C_{32} = 22$

(i) $M_{33} = -23$

(i) $C_{33} = -23$

17. (a) $4(-5) + 5(-5) + 6(-5) = -75$

(b) $2(8) + 5(-5) - 3(22) = -75$

19. About Row 2: $3[-1(3(4) - 4(-2))] + 2(1) = -58$

25. About Row 2: $3[-1(y + 1)] + 2(x + 1) = -3y + 2x - 1$

27. About Column 1: $5[6(2) + 12(-1)] + 4[3(2) + 6(-1)] = 0$

29. About Row 1:

$$\begin{aligned}
 & \text{(a) } w\{-15[32(17)] - 24[-840 - 396] + 30[32(46)]\} \\
 & \text{(b) } -x\{21[32(17)] - 24[350 + 40(18)] + 30[-32(50)]\} \\
 & \text{(c) } y\{21[-840 - 396] + 15[350 + 40(18)] + 30[-220 + 40(24)]\} \\
 & \text{(d) } -z\{21[32(46)] + 15[-32(50)] + 24[-220 + 24(40)]\} \\
 & \qquad \qquad \qquad = 65,664w + 62,256x + 12,294 - 24,672z
 \end{aligned}$$

41. About Column 1: $5[0(-2) - 6(0(2) + 0(1)) + 0(2)] = 0$

43. (a) False:

$$\begin{vmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{vmatrix} = a_{11}a_{22} - a_{12}a_{21}$$

(b) True. In such a case, the only possible way to find a determinant is if it equals the first (and only) entry.

(c) False. That is the definition of a minor. A cofactor could either be equal to the statement, or the negative version of the statement.

44. (a) False. One needs to form the product of the diagonal entries, not the sum.

(b) True. Generally, it is better to expand on a row or column with the most zeros, but any row or column would work.

(c) True. Because the formula involves multiplying by the entry at the ij th point, multiplying by zero would result in zero, so this is true.

45. $(x + 3)(x + 2) - 2 = 0 \rightarrow x^2 + 5x + 4 = 0 \rightarrow (x + 1)(x + 4) = 0 \rightarrow x = -1, -4$

51. $(\lambda)((\lambda^2 + \lambda) - 2) = 0 \rightarrow \lambda(\lambda^2 + \lambda - 2) = 0 \rightarrow \lambda(\lambda - 1)(\lambda + 2) = 0 \rightarrow \lambda = 0, 1, -2$

63. $wz - xy = -(xy - wz)$ True

64. $cwz - cxy = c(wz - xy)$ True

65. $wz - xy = w(z + cy) - y(x + cw) \rightarrow wz + \cancel{cyw} - xy - \cancel{cxy} = wz - xy$ True

67. About Column 1: $(yz^2 - y^2z) - (xz^2 - x^2z) + (xy^2 - x^2y)$

$$\begin{aligned}
 x^2z + x^2y + xy^2 - y^2z - xz^2 + yz^2 &= (y - x)(z - x)(z - y) \\
 &\text{True}
 \end{aligned}$$