Linear Algebra 4.1 Homework

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7.
$$\langle 1, 3 \rangle + \langle 2, -2 \rangle = \langle 3, 1 \rangle$$

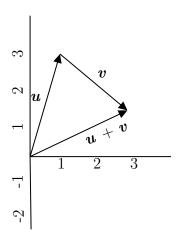


Figure 1: Problem 7 Figure

11.
$$\overrightarrow{\mathbf{v}} = \frac{3}{2}\overrightarrow{\mathbf{u}} \Rightarrow \frac{3}{2}\langle -2, 3 \rangle = \langle -3, \frac{9}{2} \rangle$$

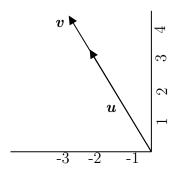


Figure 2: Problem 11 Figure

19. (a)
$$\overrightarrow{\mathbf{u}} - \overrightarrow{\mathbf{v}} = \langle 1, 2, 3 \rangle - \langle 2, 2, -1 \rangle = \langle -1, 0, 4 \rangle$$

(b)
$$\overrightarrow{\mathbf{v}} - \overrightarrow{\mathbf{u}} = \langle 2, 2, -1 \rangle - \langle 1, 2, 3 \rangle = \langle 1, 0, -4 \rangle$$

21.
$$2\overrightarrow{\mathbf{u}} + 4\overrightarrow{\mathbf{v}} - \overrightarrow{\mathbf{w}} = 2\langle 1, 2, 3 \rangle + 4\langle 2, 2, -1 \rangle - \langle 4, 0, -4 \rangle = \langle 6, 12, 6 \rangle$$

24.
$$\overrightarrow{\mathbf{z}} = -\frac{2\overrightarrow{\mathbf{u}} + \overrightarrow{\mathbf{v}} - \overrightarrow{\mathbf{w}}}{3} \Rightarrow -\frac{1}{3} \left(2\langle 1, 2, 3 \rangle + \langle 2, 2, -1 \rangle - \langle 4, 0, -4 \rangle \right) = \langle 0, -2, -3 \rangle$$

29. (a)
$$\overrightarrow{\mathbf{u}} - \overrightarrow{\mathbf{v}} = \langle 4, 0, -3, 5 \rangle - \langle 0, 2, 5, 4 \rangle = \langle 4, -2, -8, 1 \rangle$$

(b)
$$2\overrightarrow{\mathbf{u}} + 6\overrightarrow{\mathbf{v}} = 2\langle 4, 0, -3, 5 \rangle + 6\langle 0, 2, 5, 4 \rangle = \langle 8, 12, 24, 34 \rangle$$

(c)
$$2\overrightarrow{\mathbf{v}} - \overrightarrow{\mathbf{u}} = 2\langle 0, 2, 5, 4 \rangle - \langle 4, 0, -3, 5 \rangle = \langle -4, 4, 13, 3 \rangle$$

35.
$$\overrightarrow{\mathbf{w}} = \frac{1}{3}(\overrightarrow{\mathbf{u}} - 2\overrightarrow{\mathbf{v}}) = \frac{1}{3}(\langle 1, -1, 0, 1 \rangle - 2\langle 0, 2, 3, -1) = \langle \frac{1}{3}, -\frac{5}{3}, -2, 1 \rangle$$

41.
$$\overrightarrow{\mathbf{v}} = \overrightarrow{\mathbf{u}} + \overrightarrow{\mathbf{w}}$$

- 49. $c_1\langle 1, 1, 2, 2 \rangle + c_2\langle 2, 3, 5, 6 \rangle + c_3\langle -3, 1, -4, 2 \rangle = \langle 0, 5, 3, 0 \rangle$. Such a combination is not possible.
- 55. Such a combination is not possible (although number 56 is)