

Properties of Determinants

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- If \mathbf{A} and \mathbf{B} are square matrices of order n , then $\det(\mathbf{AB}) = \det(\mathbf{A})\det(\mathbf{B})$
- All row operations are extended to columns
- Let $\det(\mathbf{A}) = n$ and c be a scalar, then $\det(c\mathbf{A}) = c^n \det(\mathbf{A})$
- \mathbf{A} is invertible iff the determinant of $\mathbf{A} \neq 0$
- Fundamental Theorem (version II)
 1. If \mathbf{A} is an $n \times n$ matrix, then the following conditions are equivalent:
 - (a) \mathbf{A} is invertible
 - (b) $\mathbf{A}x = \mathbf{B}$ has a unique solution for any $n \times 1$ column matrix \mathbf{B}
 - (c) $\mathbf{A}x = 0$ has only trivial solution $x = 0$
 - (d) $\mathbf{A} = \tilde{R}\mathbf{I}_n$
 - (e) \mathbf{A} can be written as a product of elementary matrices
 - (f) $\det(\mathbf{A}) \neq 0$