Properties of Matrix Operations

Michael Brodskiy

Professor: Lynn Knight

February 3, 2021

• Let A, B, and C be matrices and c and d be constants

$$1. \mathbf{A} + \mathbf{B} = \mathbf{B} + \mathbf{A}$$

2.
$$A + (B + C) = (A + B) + C$$

3.
$$(cd)\mathbf{A} = c(d\mathbf{A})$$

4.
$$1A = A$$

5.
$$(c+d)\mathbf{A} = c\mathbf{A} + d\mathbf{A}$$

6.
$$c(\mathbf{A} + \mathbf{B}) = c\mathbf{A} + c\mathbf{B}$$

• Let **A** be a matrix, c be a constant, and \mathbf{O}_{mn} be a zero matrix

$$1. \mathbf{A} + \mathbf{O}_{mn} = \mathbf{A}$$

$$2. \mathbf{A} + (-\mathbf{A}) = \mathbf{O}_{mn}$$

3. If
$$c\mathbf{A} = \mathbf{O}_{mn}$$
, then $c = 0$ or $\mathbf{A} = \mathbf{O}_{mn}$

 \bullet Let **A**, **B**, and **C** be matrices, and c be a constant

1.
$$A(BC) = (AB)C$$

$$2. \mathbf{A}(\mathbf{B} + \mathbf{C}) = \mathbf{A}\mathbf{B} + \mathbf{A}\mathbf{C}$$

3.
$$(\mathbf{A} + \mathbf{B})\mathbf{C} = \mathbf{A}\mathbf{C} + \mathbf{B}\mathbf{C}$$

4.
$$c(\mathbf{AB}) = (c\mathbf{A})\mathbf{B} = \mathbf{A}(c\mathbf{B})$$