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```
clear all;  
close all % Clean the workspace
```

PROBLEM 1

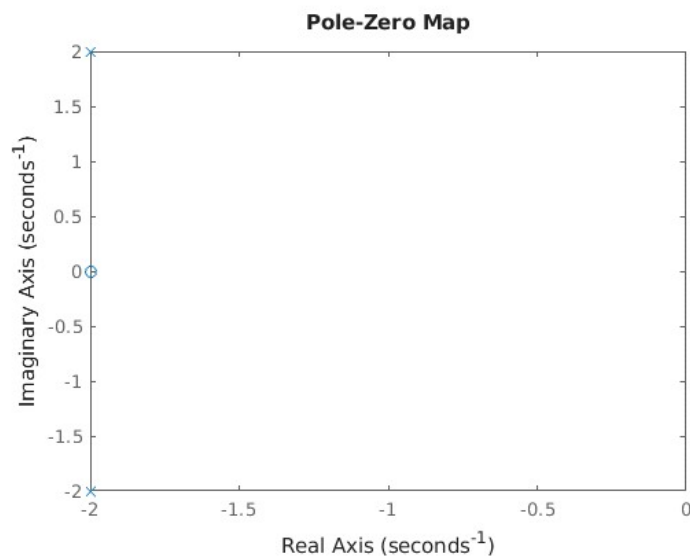
PART A

```
numerator = [1 2];  
denominator = [1 4 8];  
H = tf(numerator, denominator); % Define the transfer function
```

PART B

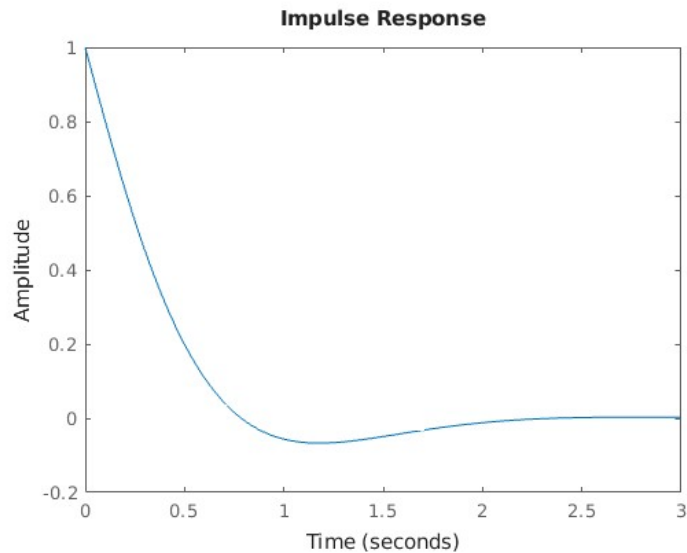
```
zeros = zero(H); % Find the zeros of the transfer function  
poles = pole(H); % Find the poles of the transfer function  
pzplot(H); % Plot the plot-zero plot
```

```
pause;
```



PART C

```
impz(H); % Impulse response plot  
  
pause;
```



PART D

```
t = [0:.01:1]; % Create time array  
x = exp(-2 * t); % Create impulse  
y = lsim(H, x, t); % Find the response to input  
plot(y, t);  
xlabel('Response to Given Signal');  
ylabel('Magnitude');  
  
clear all;  
close all; % Clean the workspace
```

PROBLEM 2

```
m = 1; % Mass is one kilogram, as given in the problem  
k = 1; % k (spring constant) is derived from the requested frequency (1 rad/s)  
omega = sqrt(m/k); % Define the requested frequency  
v = [2 (1/sqrt(2)) 1/3]; % Define the requested viscosity values  
chi = v ./ (2 * sqrt(m*k)); % Define the damping factor  
  
H1 = tf([omega^2], [1 (2 * chi(1) * omega) (omega^2)]);
```

```
H2 = tf([omega^2], [1 (2 * chi(2) * omega) (omega^2)]);
H3 = tf([omega^2], [1 (2 * chi(3) * omega) (omega^2)]); % Define the transfer functions
```

SIMULATION TASK 1

```
hold on; % Plot figures on one plot
pzplot(H1, H2, H3); % Plot the different cases
legend('Case 1', 'Case 2', 'Case 3');

pause;

hold off; % Clear the current figure

t = [0:.1:30]; % Create a 30-second time vector

S1 = step(H1, t);
S2 = step(H2, t);
S3 = step(H3, t); % Compute the three step responses

plot(t, S1, t, S2, t, S3); % Plot the three step responses
xlabel('Frequency');
ylabel('Magnitude');
legend('Case 1', 'Case 2', 'Case 3');

S1_info = stepinfo(H1);
S2_info = stepinfo(H2);
S3_info = stepinfo(H3); % Get the step response info for each system

display('S1 Rise Time, Settling Time, and Overshoot:')
display(S1_info.RiseTime);
display(S1_info.SettlingTime);
display(S1_info.Overshoot);

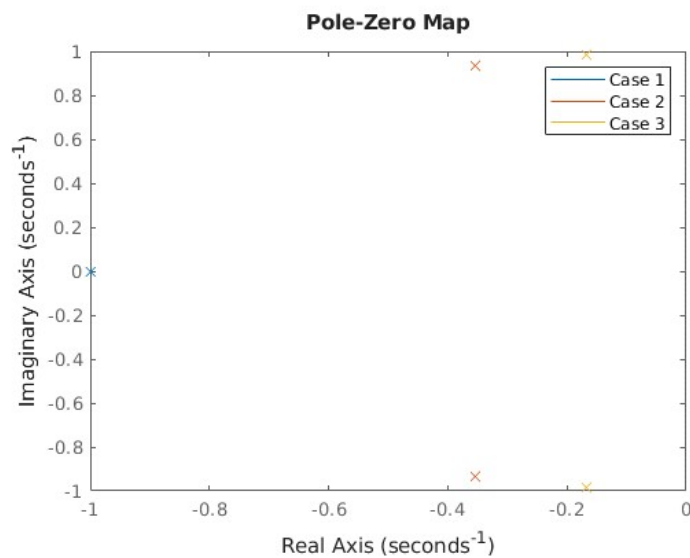
display('S2 Rise Time, Settling Time, and Overshoot:')
display(S2_info.RiseTime);
display(S2_info.SettlingTime);
display(S2_info.Overshoot);

display('S3 Rise Time, Settling Time, and Overshoot:')
display(S3_info.RiseTime);
display(S3_info.SettlingTime);
display(S3_info.Overshoot);

% We may see that, for larger values of the damping factor, the poles
% become close to zero on the imaginary axis and around -1 on the real axis.
```

% We may observe that a larger rise time corresponds to a larger dampening factor. Furthermore, there is more oscillating with smaller dampening factor values, which are indicated by the overshoot (with no overshoot when $\chi = 2$). We may see that a larger value of the dampening factor corresponds to less settling time. The bandwidth is larger with larger χ values.

% We may see that a greater dampening leads to lesser magnitude % fluctuation. Once ω gets to a larger value, χ affects it less.



S1 Rise Time, Settling Time, and Overshoot:
3.3579

5.8339

0

S2 Rise Time, Settling Time, and Overshoot:
1.3983

10.9489

30.4890

S3 Rise Time, Settling Time, and Overshoot:
1.1865

22.9277

58.3143

