

# Many-Electron Atoms

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# 1 The Pauli Exclusion Principle

- An important rule proposed by Wolfgang Pauli (1925):
  - No two electrons in a single atom can have the same set of quantum numbers  $(n, l, m_l, m_s)$
  - It applies to all “spin 1/2” particles (fermions)
- Examples:
  - Hydrogen:  $1e^-$  in ground state:  $(1, 0, 0, \pm\frac{1}{2})$
  - Helium:  $2e^-$ :  $(1, 0, 0, -\frac{1}{2})$  and  $(1, 0, 0, \frac{1}{2})$
  - Lithium:  $(1, 0, 0, -\frac{1}{2})$ ,  $(1, 0, 0, \frac{1}{2})$ , and  $(2, l, m_l, m_s)$ 
    - \* If the electron has spin 1, this may be different:
    - \* Lithium:  $(1, 0, 0, 1)$ ,  $(1, 0, 0, \pm 1/0)$ , and  $(1, 0, 0, \pm 1/0)$
- Electron states in many-electron atoms
  - “Filling rule”:  $e^-$ ’s occupy the lowest levels first
  - Orbitals with the same  $n$  lie at about the same distance from the nucleus  $\implies r_n = n^2 a_o$  (an atomic shell)

$n$	1	2	3	4	5
Shell	$K$	$L$	$M$	$N$	$O$

- According to the Pauli Exclusion Principle, the maximum amount of electrons in each subshell is  $2(2l + 1)$
- Equivalent levels of  $d$  are much higher in energy levels because of the “electron screening effect”

# 2 Outer Electrons: Screening and Optical Transitions

- Screening Effect of Electron Levels
  - Lithium ( $1s^2 2s^1$ )
    - \* The ionization energy of Li is only 5.39[eV]
    - \* For the electron in the  $2s$  shell, its ionization energy is 3.4[eV]
    - \* This is due to interactions between different shells
  - To an outer electron, the charge of the nucleus can be screened or shielded by the electrons in the inner shells — this is the screening effect

- The less penetrating the wave function, the more accurate the screening model is
- The parity of wave functions:

$$\begin{array}{ll} \text{Even:} & \psi(x) = \psi(-x) \\ \text{Odd:} & \psi(-x) = -\psi(x) \end{array}$$

#### The Selection Rule

- $\Delta l = l_2 - l_1 = \pm 1$
- This means, by optical transition, it is forbidden for an electron to make a transition to a different-numbered, but same-lettered subshell
  - \* For example,  $np$  to  $ns$  or vice versa is permitted for any values  $n$