

# Lecture VI Notes

Michael Brodskiy

Professor: V. Cherkassky

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## 1 Arc Length and Curvature of Three Dimensional Functions – 13.3

As the arc length of a two dimensional function is defined by:  $\int_a^b \sqrt{f'(t)^2 + g'(t)^2} dt$ , the arc length of a three dimensional function is defined by:  $\int_a^b \sqrt{f'(t)^2 + g'(t)^2 + h'(t)^2} dt$ , or more simply:  $\int_a^b |\vec{r}'(t)| dt$

The curvature,  $\kappa$ , of a vector function may be found using the formula:  $\kappa(t) = \frac{|\vec{r}'(t) \times \vec{r}''(t)|}{|\vec{r}'(t)|^3}$