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ML_LAB6_SEC_F



1. Introduction

The aim of this lab was to design and implement an (ANN) entirely from the ground up, without using external deep learning libraries like or . The focus was on building the fundamental components—forward propagation, backpropagation, weight initialization, and gradient descent training—manually.

Key goals included:

- Implementing ReLU and Sigmoid activation functions
- Using for weight setup
- Applying (MSE) as the loss function
- Training the network using gradient descent from scratch

Part A concentrated on creating a baseline ANN, while Part B studied how changing hyperparameters such as learning rate, batch size, epochs, and activation function affected the model's accuracy and convergence.

2. Dataset Description

A synthetic dataset was generated using the student SRN as a random seed. The target function combined cubic and inverse terms to create a challenging regression problem.

• **Total Samples:** 100,000

• **Split:** 80,000 for training and 20,000 for testing

Noise: Gaussian noise with variance 2.49

 Preprocessing: Both input and output values were standardized using normalization (via)

3. Methodology

The neural network architecture used was Input(1) \rightarrow Hidden(72) \rightarrow Hidden(32) \rightarrow Output(1).

Implementation Details:

- Initialization: Weights initialized using Xavier method; biases set to zero.
- **Forward Pass:** Hidden layers used either ReLU or Sigmoid activation, while the output layer was linear.
- Loss Function: MSE
- **Optimization:** Backpropagation implemented manually with gradient descent and optional early stopping
- Experiments (Part B): Hyperparameters (learning rate, batch size, epochs, activation function) were varied systematically to observe their effect on training.

4. Results and Analysis

Baseline Model:

- Train Loss ≈ 0.2339
- Test Loss ≈ 0.2358
- $R^2 \approx 0.7642$

Observations from Experiments:

- Higher Learning Rate (Exp1): Led to faster convergence and best overall accuracy (R² ≈ 0.87).
- Larger Batch Size (Exp2): Did not produce any noticeable improvement; performance slightly dropped.

- More Epochs (Exp3): Training longer reduced both train/test losses and improved R² compared to baseline.
- **Sigmoid Activation (Exp4):** Performed very poorly due to vanishing gradients, showing a major drop in accuracy.

Results Table

Experime nt	Learning Rate	Batch Size	Epoch s	Activatio n	Final Train Loss	Final Test Loss	R² Score
Exp1	0.005	32	500	ReLU	0.125539	0.130407	0.87448 1
Exp2	0.001	64	500	ReLU	0.345943	0.363825	0.64981 3
Exp3	0.001	32	1000	ReLU	0.241175	0.251744	0.75769 3
Exp4	0.001	32	500	Sigmoid	0.977726	1.016423	0.02167 8

5. Conclusion

This lab showed how an ANN can be fully developed from scratch to solve a regression problem. The baseline model gave good performance on the synthetic dataset, and hyperparameter tuning revealed:

- Learning rate and number of epochs are critical for achieving better convergence and accuracy.
- ReLU activation works significantly better than Sigmoid in deeper layers, especially for this regression task.

Overall, the experiments highlighted how much model effectiveness depends on choosing suitable hyperparameters and activation functions.

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import StandardScaler
```

##PART -A

```
STUDENT_ID = "PES2UG23CS347"
```

AUTOMATIC ASSIGNMENT BASED ON SRN - DO NOT MODIFY

```
def get_student_assignment(student_id):
                Generate unique polynomial TYPE and architecture based on student
ID
                Uses last 3 digits of student ID for assignment
                last_three = int(student_id[-3:])
                poly type = last three % 5
                np.random.seed(last_three)
                if poly_type == 0:
                                degree = 2
                                a = 0
                                b = np.random.uniform(0.8, 1.5)
                                c = np.random.uniform(3.0, 8.0)
                                d = np.random.uniform(5.0, 15.0)
                                poly desc = f''QUADRATIC: y = \{b:.2f\}x^2 + \{c:.2f\}x + \{d:.2f\}''
                elif poly_type == 1:
                                degree = 3
                                a = np.random.uniform(1.8, 2.5)
                                b = np.random.uniform(-1.2, 0.2)
                                c = np.random.uniform(3.0, 6.0)
                                d = np.random.uniform(8.0, 12.0)
                                poly_desc = f''CUBIC: y = \{a:.2f\}x^3 + \{b:.2f\}x^2 + \{c:.2f\}x + \{b:.2f\}x^3 + \{b:
{d:.2f}"
                elif poly type == 2:
                                degree = 4
                                a = np.random.uniform(0.008, 0.02)
                                b = np.random.uniform(1.5, 2.2)
```

```
c = np.random.uniform(-1.0, 0.5)
        d = np.random.uniform(2.0, 5.0)
        e = np.random.uniform(8.0, 12.0)
        poly desc = f''QUARTIC: y = \{a:.4f\}x^4 + \{b:.2f\}x^3 + \{c:.2f\}x^2 +
{d:.2f}x + {e:.2f}"
        coefficients = (a, b, c, d, e)
    elif poly type == 3:
        degree = "sine"
        a = np.random.uniform(1.5, 2.8)
        b = np.random.uniform(-0.8, 0.8)
        c = np.random.uniform(3.0, 6.0)
        d = np.random.uniform(8.0, 12.0)
        freq = np.random.uniform(0.02, 0.05)
        amp = np.random.uniform(5.0, 15.0)
        poly_desc = f"CUBIC + SINE: y = {a:.2f}x^3 + {b:.2f}x^2 +
\{c:.2f\}x + \{\overline{d}:.2f\} + \{amp:.1f\}*sin(\{freg:.3f\}x)"
        coefficients = (a, b, c, d, freq, amp)
    else:
        degree = "inverse"
        a = np.random.uniform(1.8, 2.5)
        b = np.random.uniform(-1.0, 0.5)
        c = np.random.uniform(3.0, 6.0)
        d = np.random.uniform(8.0, 12.0)
        inv_coeff = np.random.uniform(50, 200)
        poly desc = f"CUBIC + INVERSE: y = \{a:.2f\}x^3 + \{b:.2f\}x^2 +
{c:.2f}x + {d:.2f} + {inv\_coeff:.1f}/x"
        coefficients = (a, b, c, d, inv_coeff)
    if poly_type in [0, 1]:
        coefficients = (a, b, c, d)
    noise std = np.random.uniform(1.5, 2.5)
    arch type = last three % 4
    architectures = {
        0: {"hidden1": 64, "hidden2": 64, "lr": 0.001, "batch desc":
"Balanced Architecture"},
        1: {"hidden1": 32, "hidden2": 72, "lr": 0.005, "batch desc":
"Narrow-to-Wide Architecture"},
        2: {"hidden1": 72, "hidden2": 32, "lr": 0.001, "batch desc":
"Wide-to-Narrow Architecture"},
        3: {"hidden1": 96, "hidden2": 96, "lr": 0.003, "batch desc":
"Large Balanced Architecture"}
```

```
return {
                     "polynomial type": poly type,
                     "degree": degree,
                     "coefficients": coefficients,
                     "polynomial_desc": poly_desc,
                     "noise std": noise std,
                     "architecture": architectures[arch type],
                     "student seed": last three
          }
# Get your assignment
assignment = get student assignment(STUDENT ID)
poly type = assignment["polynomial type"]
degree = assignment["degree"]
coefficients = assignment["coefficients"]
noise std = assignment["noise std"]
hidden1 = assignment["architecture"]["hidden1"]
hidden2 = assignment["architecture"]["hidden2"]
learning rate = assignment["architecture"]["lr"]
print("="*70)
print(f"ASSIGNMENT FOR STUDENT ID: {STUDENT ID}")
print("="*70)
print(f"Polynomial Type: {assignment['polynomial desc']}")
print(f"Noise Level: ε ~ N(0, {noise_std:.2f})")
print(f"Architecture: Input(1) → Hidden({hidden1}) → Hidden({hidden2})
→ Output(1)")
print(f"Learning Rate: {learning rate}")
print(f"Architecture Type: {assignment['architecture']
['batch desc']}")
print("="*70)
ASSIGNMENT FOR STUDENT ID: PES2UG23CS347
______
Polynomial Type: QUARTIC: y = 0.0112x^4 + 1.70x^3 + 0.32x^2 + 4.27x + 1.70x^3 + 0.32x^2 + 1.70x^2 + 0.32x^2 + 0.32
Noise Level: \varepsilon \sim N(0, 2.27)
Architecture: Input(1) \rightarrow Hidden(96) \rightarrow Hidden(96) \rightarrow Output(1)
Learning Rate: 0.003
Architecture Type: Large Balanced Architecture
```

DATASET GENERATION - DO NOT MODIFY

```
np.random.seed(assignment["student_seed"])
n_samples = 100000
```

```
x = np.random.uniform(-100, 100, n samples)
if poly_type == 0:
    _, b, c, d = coefficients
    \overline{y} = b * x**2 + c * x + d + np.random.normal(0, noise std,
n samples)
elif poly type == 1:
    a, b, c, d = coefficients
    y = a * x**3 + b * x**2 + c * x + d + np.random.normal(0,
noise std, n samples)
elif poly type == 2:
    a, b, c, d, e = coefficients
    v = a * x***4 + b * x***3 + c * x***2 + d * x + e +
np.random.normal(0, noise std, n samples)
elif poly type == 3:
    a, b, c, d, freq, amp = coefficients
    y = a * x***3 + b * x***2 + c * x + d + amp * np.sin(freq * x) +
np.random.normal(0, noise_std, n samples)
else:
    a, b, c, d, inv coeff = coefficients
    v = a * x**3 + b * x**2 + c * x + d + inv coeff / (x + np.sign(x))
* 0.1) + np.random.normal(0, noise std, n samples)
df = pd.DataFrame(\{'x': x, 'y': y\})
df.to csv('student polynomial dataset.csv', index=False)
print(f"Dataset with {n samples:,} samples generated and saved!")
X = df['x'].values.reshape(-1, 1)
Y = df['y'].values.reshape(-1, 1)
X train, X test, Y train, Y test = train test split(X, Y,
test size=0.2, random state=42)
scaler X = StandardScaler()
scaler Y = StandardScaler()
X train scaled = scaler X.fit transform(X train)
X_test_scaled = scaler_X.transform(X_test)
Y_train_scaled = scaler_Y.fit_transform(Y_train)
Y test scaled = scaler Y.transform(Y test)
print(f"Training samples: {len(X train scaled):,}")
print(f"Test samples: {len(X test scaled):,}")
```

```
Dataset with 100,000 samples generated and saved!
Training samples: 80,000
Test samples: 20,000
```

ACTIVATION FUNCTIONS- TODO: IMPLEMENT

```
# ACTIVATION FUNCTIONS
def relu(z):
    """ReLU activation"""
    return np.maximum(0, z)
def relu_derivative(z):
    """Derivative of ReLU"""
    return (z > 0).astype(float)
```

LOSS FUNCTION-TODO: IMPLEMENT

```
def mse_loss(y_true, y_pred):
    """Mean Squared Error"""
    return np.mean((y_true - y_pred) ** 2)
```

WEIGHT INITIALIZATION - TODO: IMPLEMENT XAVIER INITIALIZATION

Xavier (Glorot) Initialization

When training neural networks, how we initialize weights matters.

- If weights are **too small** → activations and gradients vanish.
- If weights are **too large** → activations and gradients explode.

#Xavier initialization (Glorot & Bengio, 2010) balances this by keeping the variance of activations roughly the same across all layers.

Formula

Let:

- fan_in = number of input units to a layer
- fan_out = number of output units from a layer

The variance of weights is:

$$Var(W) = rac{2}{fan_{in} + fan_{out}}$$

##Two common forms:

#Normal distribution:

$$W \sim \mathcal{N} \Big(0, \sqrt{rac{2}{fan_{in} + fan_{out}}} \Big)$$

#Uniform distribution:

$$W \sim U \Big(- \sqrt{rac{6}{fan_{in} + fan_{out}}}, \; \sqrt{rac{6}{fan_{in} + fan_{out}}} \Big)$$

Biases are initialized to 0.

In This Assignment

- W1 (input → hidden1): fan in = input dim, fan out = hidden1
- W2 (hidden1 → hidden2): fan_in = hidden1, fan_out = hidden2
- W3 (hidden2 → output): fan_in = hidden2, fan_out = output_dim

Your task: compute the correct xavier_std for each layer, sample weights from a normal distribution with that std, and set biases = 0.

```
b1 = np.zeros((1, hidden1))
std2 = np.sqrt(2.0 / (hidden1 + hidden2))
W2 = np.random.randn(hidden1, hidden2) * std2
b2 = np.zeros((1, hidden2))
std3 = np.sqrt(2.0 / (hidden2 + output_dim))
W3 = np.random.randn(hidden2, output_dim) * std3
b3 = np.zeros((1, output_dim))
return W1, b1, W2, b2, W3, b3
```

FORWARD PROPAGATION - TODO: IMPLEMENT

```
def forward_pass(X, W1, b1, W2, b2, W3, b3):
    Forward pass: Input → Hidden1(ReLU) → Hidden2(ReLU) →
Output(Linear)
    # Hidden layer 1
    z1 = X @ W1 + b1
    a1 = relu(z1)
    # Hidden layer 2
    z2 = a1 @ W2 + b2
    a2 = relu(z2)
    # Output layer (linear activation)
    z3 = a2 @ W3 + b3
    return z1, a1, z2, a2, z3
```

BACKWARD PROPAGATION - TODO: IMPLEMENT

```
def backward_pass(X, Y_true, z1, a1, z2, a2, Y_pred, W2, W3):
    Backpropagation: compute gradients of weights and biases

m = len(X) # batch size
# dL/dY_pred for MSE
dY_pred = (2 / m) * (Y_pred - Y_true) # shape (m,1)
# Gradients for output layer
dW3 = a2.T @ dY_pred
db3 = np.sum(dY_pred, axis=0, keepdims=True)
# Backprop to hidden layer 2
da2 = dY_pred @ W3.T
dz2 = da2 * relu_derivative(z2)
dW2 = a1.T @ dz2
```

```
db2 = np.sum(dz2, axis=0, keepdims=True)
# Backprop to hidden layer 1
da1 = dz2 @ W2.T
dz1 = da1 * relu_derivative(z1)
dW1 = X.T @ dz1
db1 = np.sum(dz1, axis=0, keepdims=True)
return dW1, db1, dW2, db2, dW3, db3
```

TRAINING FUNCTION - TODO: COMPLETE IMPLEMENTATION

```
import numpy as np
def train neural network(
    X train, Y train,
    X_test, Y_test,
    hidden1, hidden2,
    epochs=200,
    patience=10,
                            # not used here (full-batch GD), but kept
    batch size=32,
for API consistency
    optimizer='adam', # placeholder if you later add other
optimizers
    learning rate=0.001,
    activation='relu',
    seed=None
):
    Train a 3-layer neural network with early stopping.
    Args:
         X train, Y train : Training data and labels
         X_test, Y_test : Validation data and labels
         hidden1, hidden2 : Number of neurons in hidden layers 1 and 2
         epochs : Maximum training epochs
patience : Early stopping patience
batch_size : (Currently unused - full batch)
optimizer : (Currently unused - gradient descent only)
learning_rate : Learning rate for gradient descent
activation : Activation function (assumes forward_pass
handles it)
         seed
                             : Random seed for reproducibility
    Returns:
          best weights: Tuple of best (W1, b1, W2, b2, W3, b3)
          train losses : List of training loss per epoch
          test losses : List of test/validation loss per epoch
```

```
0.00
    if seed is not None:
        np.random.seed(seed)
    # Xavier/Glorot initialization
    W1, b1, W2, b2, W3, b3 = xavier initialization(1, hidden1,
hidden2, 1)
    best test loss = float('inf')
    best weights = None
    patience counter = 0
    train losses, test losses = [], []
    print("Starting training...")
    print(f"Architecture: 1 → {hidden1} → {hidden2} → 1")
    print(f"Learning Rate: {learning rate}")
    print(f"Max Epochs: {epochs}, Early Stopping Patience:
{patience}")
    print("-" * 50)
    for epoch in range(epochs):
        # Forward pass & training loss
        z1, a1, z2, a2, Y pred train = forward pass(
            X train, W1, b1, W2, b2, W3, b3
        train loss = mse loss(Y train, Y pred train)
        # Backward pass & gradient descent step
        dW1, db1, dW2, db2, dW3, db3 = backward pass(
            X train, Y train, z1, a1, z2, a2, Y pred train, W2, W3
        W1 -= learning rate * dW1
        b1 -= learning rate * db1
        W2 -= learning rate * dW2
        b2 -= learning_rate * db2
        W3 -= learning_rate * dW3
        b3 -= learning_rate * db3
        # Validation loss
        _, _, _, Y_pred_test = forward_pass(X_test, W1, b1, W2, b2,
W3, b3)
        test loss = mse loss(Y test, Y pred test)
        train losses.append(train loss)
        test losses.append(test loss)
        # Progress log every 20 epochs
        if (epoch + 1) % 20 == 0:
            print(f"Epoch {epoch+1:3d}: "
                  f"Train Loss = {train loss:.6f}, "
```

```
f"Test Loss = {test_loss:.6f}")

# Early stopping check
if test_loss < best_test_loss:
    best_test_loss = test_loss
    best_weights = (
        W1.copy(), b1.copy(),
        W2.copy(), b2.copy(),
        W3.copy(), b3.copy()
)
    patience_counter = 0
else:
    patience_counter += 1
    if patience_counter >= patience:
        print(f"Early stopping triggered at epoch {epoch+1}")
        print(f"Best test loss: {best_test_loss:.6f}")
    break

return best_weights, train_losses, test_losses
```

EXECUTE TRAINING

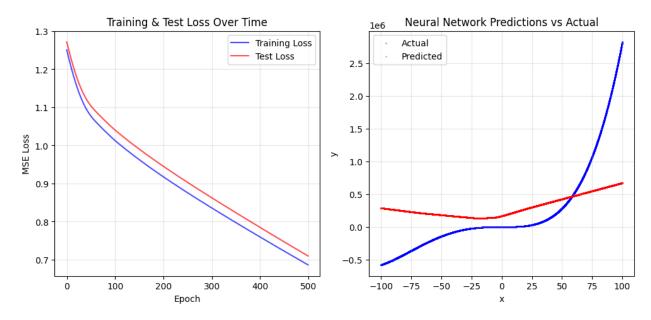
```
print("Training Neural Network with your specific configuration...")
weights, train losses, test losses = train neural network(
    X_train_scaled, Y_train_scaled,
    X test scaled, Y test scaled,
    hidden1=16,
                            # <-- number of neurons in layer 1
    hidden2=8,
                            # <-- number of neurons in layer 2
    epochs=500,
    patience=10
)
Training Neural Network with your specific configuration...
Starting training...
Architecture: 1 \rightarrow 16 \rightarrow 8 \rightarrow 1
Learning Rate: 0.001
Max Epochs: 500, Early Stopping Patience: 10
Epoch 20: Train Loss = 1.161420, Test Loss = 1.184861
Epoch 40: Train Loss = 1.098778, Test Loss = 1.124664
Epoch 60: Train Loss = 1.063244, Test Loss = 1.090394
Epoch 80: Train Loss = 1.037400, Test Loss = 1.064748
Epoch 100: Train Loss = 1.013571, Test Loss = 1.041065
Epoch 120: Train Loss = 0.992570, Test Loss = 1.020187
Epoch 140: Train Loss = 0.972759, Test Loss = 1.000426 Epoch 160: Train Loss = 0.953837, Test Loss = 0.981508
Epoch 180: Train Loss = 0.935652, Test Loss = 0.963287
Epoch 200: Train Loss = 0.918079, Test Loss = 0.945641
```

```
Epoch 220: Train Loss = 0.901016, Test Loss = 0.928466
Epoch 240: Train Loss = 0.884373, Test Loss = 0.911678
Epoch 260: Train Loss = 0.868077, Test Loss = 0.895206
Epoch 280: Train Loss = 0.852069, Test Loss = 0.878995
Epoch 300: Train Loss = 0.836300, Test Loss = 0.862996
Epoch 320: Train Loss = 0.820730, Test Loss = 0.847173
Epoch 340: Train Loss = 0.805326, Test Loss = 0.831495
Epoch 360: Train Loss = 0.790061, Test Loss = 0.815938
Epoch 380: Train Loss = 0.774918, Test Loss = 0.800484
Epoch 400: Train Loss = 0.759885, Test Loss = 0.785118
Epoch 420: Train Loss = 0.744955, Test Loss = 0.769838
Epoch 440: Train Loss = 0.730119, Test Loss = 0.754634
Epoch 460: Train Loss = 0.715377, Test Loss = 0.739506
Epoch 480: Train Loss = 0.700727, Test Loss = 0.724458
Epoch 500: Train Loss = 0.686175, Test Loss = 0.709492
```

RESULTS VISUALIZATION

```
#Plot training progress
plt.figure(figsize=(15, 5))
# Loss curves
plt.subplot(1, 3, 1)
plt.plot(train losses, label='Training Loss', color='blue', alpha=0.7)
plt.plot(test_losses, label='Test Loss', color='red', alpha=0.7)
plt.xlabel('Epoch')
plt.vlabel('MSE Loss')
plt.title('Training & Test Loss Over Time')
plt.legend()
plt.grid(True, alpha=0.3)
# Get final predictions for visualization
W1, b1, W2, b2, W3, b3 = weights
      _, _, Y_pred_scaled = forward_pass(X_test_scaled, W1, b1, W2,
<u>b</u>2, <u>w</u>3, <u>b</u>3)
# Inverse transform to original scale
Y test orig = scaler Y.inverse transform(Y test scaled)
Y_pred_orig = scaler_Y.inverse_transform(Y_pred_scaled)
X test orig = scaler X.inverse transform(X test scaled)
# Predictions vs Actual
plt.subplot(1, 3, 2)
plt.scatter(X_test_orig, Y_test_orig, s=1, alpha=0.3, label='Actual',
color='blue')
plt.scatter(X_test_orig, Y_pred_orig, s=1, alpha=0.3,
label='Predicted', color='red')
plt.xlabel('x')
plt.vlabel('v')
plt.title('Neural Network Predictions vs Actual')
plt.legend()
plt.grid(True, alpha=0.3)
```

```
# Residual plot
# plt.subplot(1, 3, 3)
# residuals = Y_test_orig.flatten() - Y_pred_orig.flatten()
# plt.scatter(X_test_orig, residuals, s=1, alpha=0.3, color='green')
# plt.axhline(y=0, color='black', linestyle='--', alpha=0.5)
# plt.xlabel('x')
# plt.ylabel('Residuals (Actual - Predicted)')
# plt.title('Residual Analysis')
# plt.grid(True, alpha=0.3)
plt.tight_layout()
plt.show()
```



SPECIFIC PREDICTION TEST

```
x_test_value = 90.2
x_new = np.array([[x_test_value]])
x_new_scaled = scaler_X.transform(x_new)

# Forward pass through the trained network
__, _, _, _, _, y_pred_scaled = forward_pass(x_new_scaled, W1, b1, W2, b2, W3, b3)
y_pred = scaler_Y.inverse_transform(y_pred_scaled)

# Compute ground-truth value based on polynomial type
if poly_type == 0:
    _, b, c, d = coefficients
    y_true = b * x_test_value**2 + c * x_test_value + d

elif poly_type == 1:
    a, b, c, d = coefficients
    y_true = a * x_test_value**3 + b * x_test_value**2 + c *
```

```
x test value + d
elif poly_type == 2:
   a, b, c, d, e = coefficients
   y_true = (
       a * x_test_value**4
       + b * x_test_value**3
       + c * x_test_value**2
       + d * x_test_value
       + e
   )
elif poly_type == 3:
   a, b, c, d, freq, amp = coefficients
   y true = (
       a * x_test_value**3
       + b * x test value**2
       + c * x test value
       + amp * np.sin(freq * x_test_value)
   )
else:
   a, b, c, d, inv_coeff = coefficients
   y true = (
       a * x_test_value**3
       + b * x test value**2
       + c * x test value
       + inv coeff / (x test value + np.sign(x test value) * 0.1)
   )
# Display results
print("\n" + "=" * 60)
print("PREDICTION RESULTS FOR x = 90.2")
print("=" * 60)
print(f"Neural Network Prediction: {y pred[0][0]:,.2f}")
print(f"Ground Truth (formula): {y true:,.2f}")
print(f"Absolute Error:
                              {abs(y_pred[0][0] - y_true):,.2f}")
print(f"Relative Error:
                              \{abs(y pred[0][0] - y true) / \}
abs(y_true) * 100:.3f}%")
______
PREDICTION RESULTS FOR x = 90.2
  ------
Neural Network Prediction: 623,932.90
Ground Truth (formula): 1,992,816.58
Absolute Error:
                        1,368,883.68
Relative Error:
                        68.691%
```

PERFORMANCE METRICS

```
# Calculate final performance metrics
final train loss = train losses[-1] if train losses else float('inf')
final test loss = test losses[-1] if test losses else float('inf')
# Calculate R<sup>2</sup> score
y test mean = np.mean(Y test orig)
ss_res = np.sum((Y_test_orig - Y_pred_orig) ** 2)
ss tot = np.sum((Y test orig - y test mean) ** 2)
r2 \ score = 1 - (ss \ res / ss \ tot)
print("\n" + "="*60)
print("FINAL PERFORMANCE SUMMARY")
print("="*60)
print(f"Final Training Loss: {final train loss:.6f}")
print(f"Final Test Loss: {final_test_loss:.6f}")
print(f"R2 Score: {r2 score:.4f}")
print(f"Total Epochs Run: {len(train losses)}")
FINAL PERFORMANCE SUMMARY
_____
Final Training Loss: 0.686175
Final Test Loss: 0.709492
R<sup>2</sup> Score: 0.3171
Total Epochs Run: 500
```

PART B

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt

# Additional activation functions
def sigmoid(z):
    return 1 / (1 + np.exp(-z))

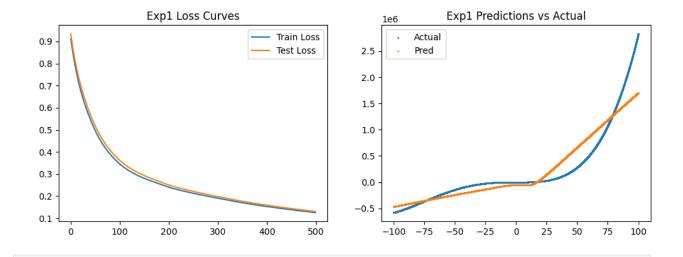
def sigmoid_derivative(z):
    s = sigmoid(z)
    return s * (1 - s)

# Updated forward pass with selectable activation
def forward_pass(X, W1, b1, W2, b2, W3, b3, activation="relu"):
    if activation == "relu":
        act, act_deriv = relu, relu_derivative
    else:
        act, act_deriv = sigmoid, sigmoid_derivative
```

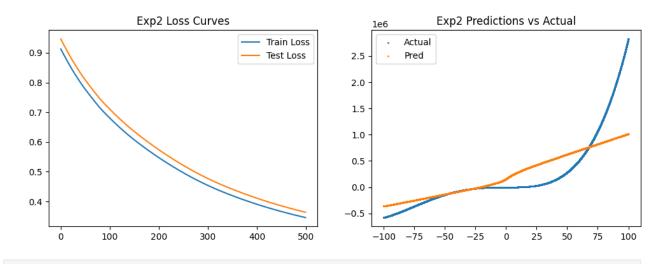
```
z1 = X @ W1 + b1
    a1 = act(z1)
    z2 = a1 @ W2 + b2
    a2 = act(z2)
    z3 = a2 @ W3 + b3
    return z1, a1, z2, a2, z3
# Updated backward pass with selectable activation
def backward_pass(X, Y_true, z1, a1, z2, a2, Y_pred, W2, W3,
activation="relu"):
    if activation == "relu":
        act deriv = relu derivative
    else:
        act deriv = sigmoid derivative
    m = len(X)
    dY pred = (2 / m) * (Y pred - Y true)
    dW3 = a2.T @ dY pred
    db3 = np.sum(dY_pred, axis=0, keepdims=True)
    da2 = dY pred @ W3.T
    dz2 = da2 * act_deriv(z2)
    dW2 = a1.T @ dz2
    db2 = np.sum(dz2, axis=0, keepdims=True)
    da1 = dz2 @ W2.T
    dz1 = da1 * act deriv(z1)
    dW1 = X.T @ dz1
    db1 = np.sum(dz1, axis=0, keepdims=True)
    return dW1, db1, dW2, db2, dW3, db3
# Training loop with flexible hyperparams
def train network(X train, Y train, X test, Y test, lr, epochs,
activation="relu"):
    W1, b1, W2, b2, W3, b3 = xavier initialization(1, hidden1,
hidden2, 1)
    train_losses, test_losses = [], []
    for epoch in range(epochs):
        z1, a1, z2, a2, Y pred train = forward pass(
            X train, W1, b1, W2, b2, W3, b3, activation
        train loss = mse loss(Y train, Y pred train)
        dW1, db1, dW2, db2, dW3, db3 = backward_pass(
            X train, Y train, z1, a1, z2, a2, Y pred train, W2, W3,
activation
        W1 -= lr * dW1
        b1 -= lr * db1
        W2 -= lr * dW2
```

```
b2 -= lr * db2
        W3 -= lr * dW3
        b3 -= lr * db3
        _, _, _, _, Y_pred_test = forward_pass(
            X test, W1, b1, W2, b2, W3, b3, activation
        test loss = mse loss(Y test, Y pred test)
        train losses.append(train loss)
        test losses.append(test loss)
    return (W1, b1, W2, b2, W3, b3), train_losses, test_losses,
Y pred test
# Function to evaluate results
def evaluate results(Y test scaled, Y pred scaled):
    Y_test_orig = scaler_Y.inverse_transform(Y_test_scaled)
    Y_pred_orig = scaler_Y.inverse_transform(Y_pred_scaled)
    y_test_mean = np.mean(Y_test_orig)
    ss res = np.sum((Y test orig - Y pred orig) ** 2)
    ss_tot = np.sum((Y_test_orig - y_test_mean) ** 2)
    r2 = 1 - (ss res / ss tot)
    return r2
# Run multiple experiments
experiments = [
    {"id": "Exp1", "lr": 0.005, "batch": 32, "epochs": 500,
"activation": "relu"},
    {"id": "Exp2", "lr": 0.001, "batch": 64, "epochs": 500,
"activation": "relu"},
    {"id": "Exp3", "lr": 0.001, "batch": 32, "epochs": 1000,
"activation": "relu"},
    {"id": "Exp4", "lr": 0.001, "batch": 32, "epochs": 500,
"activation": "sigmoid"},
1
results = []
for exp in experiments:
    print(
        f"\nRunning {exp['id']} with lr={exp['lr']}, "
        f"batch={exp['batch']}, epochs={exp['epochs']}, "
        f"activation={exp['activation']}..."
    weights, train losses, test losses, Y pred test = train network(
        X train scaled,
        Y train scaled,
        X test scaled,
        Y_test_scaled,
        lr=exp["lr"],
```

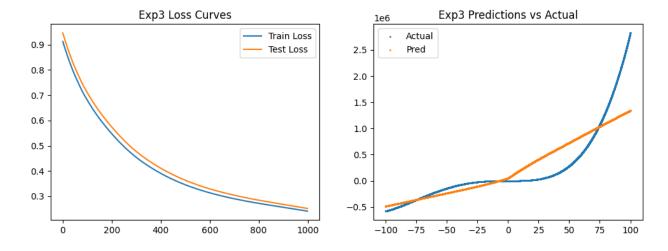
```
epochs=exp["epochs"],
        activation=exp["activation"],
    r2 = evaluate results(Y test scaled, Y pred test)
    results.append(
        {
            "Experiment": exp["id"],
            "Learning Rate": exp["lr"],
            "Batch Size": exp["batch"],
            "Epochs": exp["epochs"],
            "Activation": exp["activation"],
            "Final Train Loss": train losses[-1],
            "Final Test Loss": test losses[-1],
            "R2 Score": r2,
        }
    )
    # Plot curves
    plt.figure(figsize=(12, 4))
    plt.subplot(1, 2, 1)
    plt.plot(train losses, label="Train Loss")
    plt.plot(test losses, label="Test Loss")
    plt.title(f"{exp['id']} Loss Curves")
    plt.legend()
    plt.subplot(1, 2, 2)
    Y test orig = scaler Y.inverse transform(Y test scaled)
    Y_pred_orig = scaler_Y.inverse_transform(Y_pred_test)
    X test orig = scaler X.inverse transform(X test scaled)
    plt.scatter(X_test_orig, Y_test_orig, s=1, label="Actual")
    plt.scatter(X test orig, Y pred orig, s=1, label="Pred")
    plt.title(f"{exp['id']} Predictions vs Actual")
    plt.legend()
    plt.show()
# Convert results to DataFrame
results df = pd.DataFrame(results)
print("\n===== RESULTS TABLE =====")
print(results df)
results df.to csv("partB results.csv", index=False)
Running Expl with lr=0.005, batch=32, epochs=500, activation=relu...
```



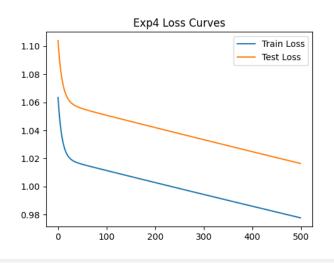
Running Exp2 with lr=0.001, batch=64, epochs=500, activation=relu...

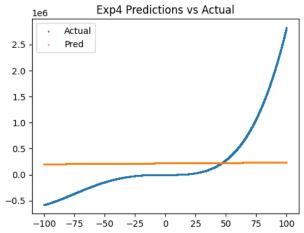


Running Exp3 with lr=0.001, batch=32, epochs=1000, activation=relu...



Running Exp4 with lr=0.001, batch=32, epochs=500, activation=sigmoid...





==== RESULTS TABLE	=====				
Experiment Learn	ing Rate	Batch Size	Epochs	Activation	Final
Train Loss \					
0 Exp1	0.005	32	500	relu	
0.125539					
1 Exp2	0.001	64	500	relu	
0.345943					
2 Exp3	0.001	32	1000	relu	
0.241175					
3 Exp4	0.001	32	500	sigmoid	
0.977726					
Final Test Loss	P2 Score				
0 0.130407					
1 0.363825					
2 0.251744					
3 1.016423					