

# Algorithmes fondamentaux



# Opération *Scan*



## Définition d'une opération *scan*

- un tableau en entrée
- un opérateur binaire et associatif
- un élément neutre  $[ \text{e} \text{ op } a = a ]$

## *Scan* inclusif ou exclusif

```
int acc = élément_neutre;

for (i=0 ; i<n; i++) {
    acc = acc op in[i];
    out[i] = acc;
}
```

scan **inclusif**

```
int acc = élément_neutre;

for (i=0 ; i<n; i++) {
    out[i] = acc;
    acc = acc op in[i];
}
```

scan **exclusif**

# Opération *Scan*



## Exemple

- entrée : [ 1 2 3 4 5 6 7 8 ]
- opérateur : +
- élément neutre : 0

- sortie du *scan inclusif* :  
[ 1 3 6 10 15 21 28 36 ]

- sortie du *scan exclusif* :  
[ 0 1 3 6 10 15 21 28 ]

```
int acc = élément_neutre;

for (i=0 ; i<n; i++) {
    acc = acc op in[i];
    out[i] = acc;
}
```

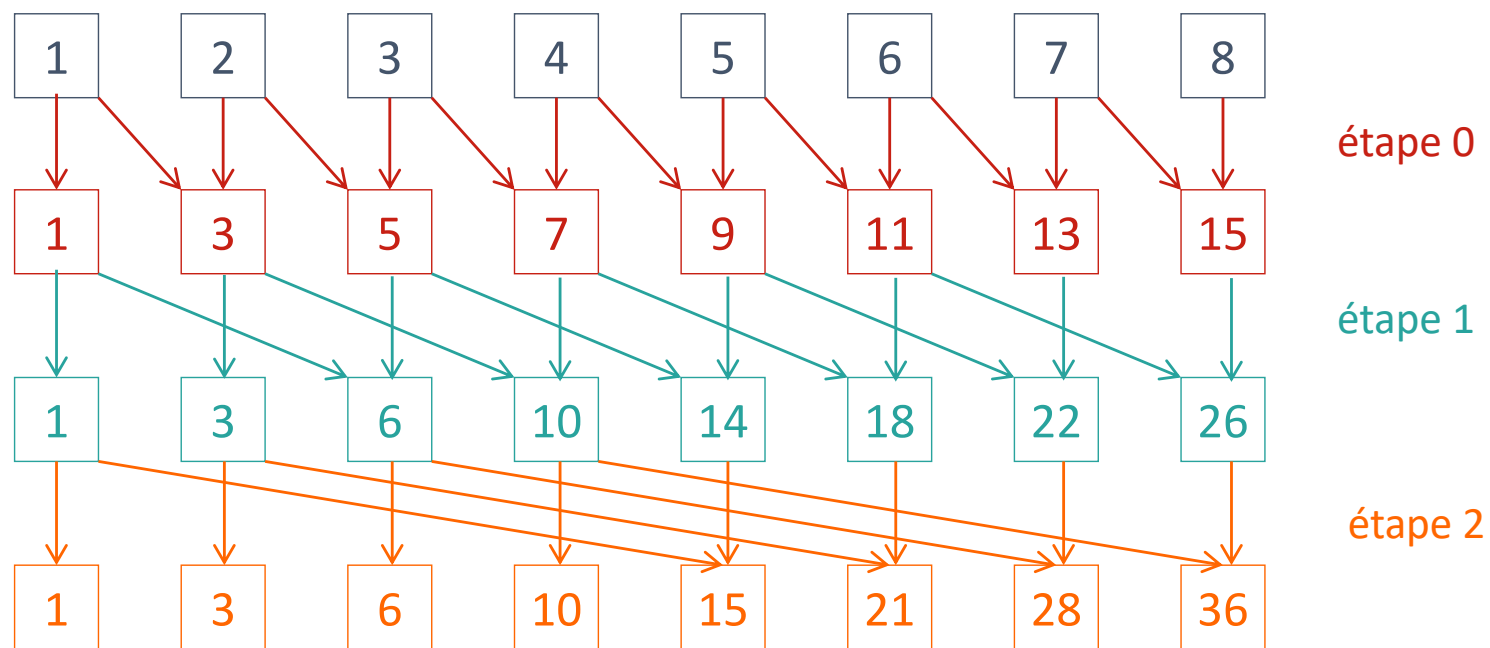
```
int acc = élément_neutre;

for (i=0 ; i<n; i++) {
    out[i] = acc;
    acc = acc op in[i];
}
```

# Opération *Scan inclusif*



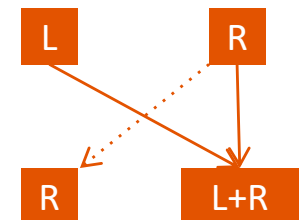
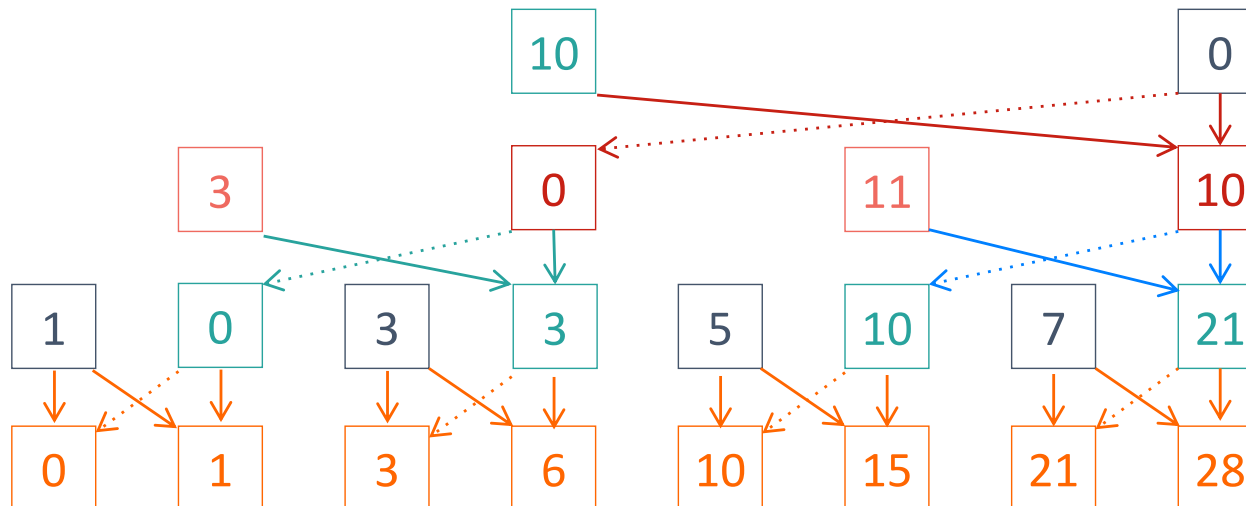
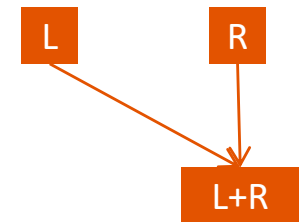
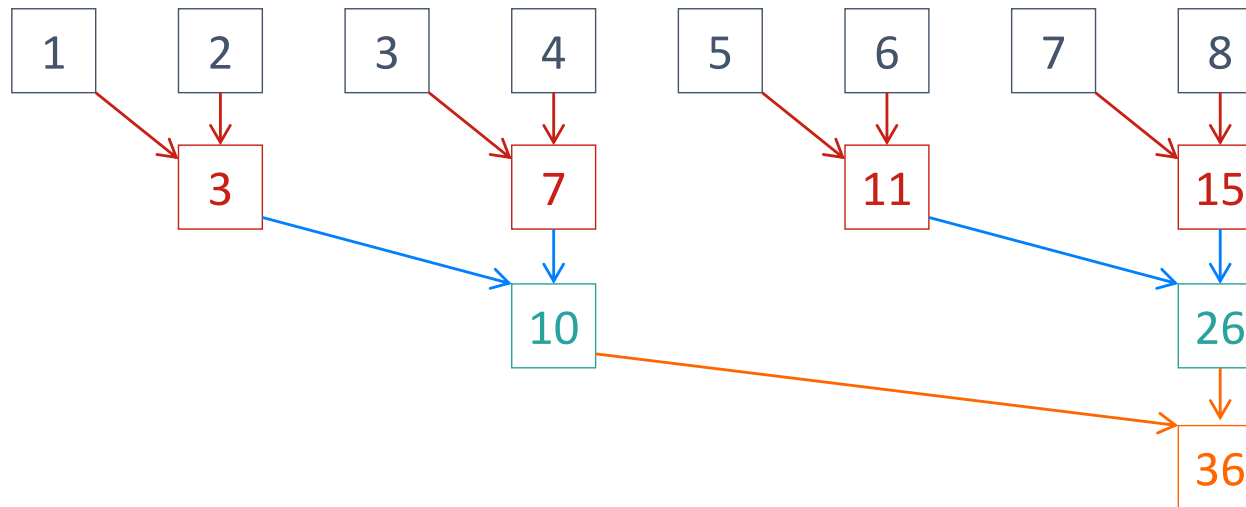
## Algorithme de Hillis/Steele



Etape  $i$  : chaque thread de numéro  $> 2^i$  ajoute à sa somme locale celle de son voisin qui se trouve  $2^i$  positions à gauche

# Opération *Scan exclusif*

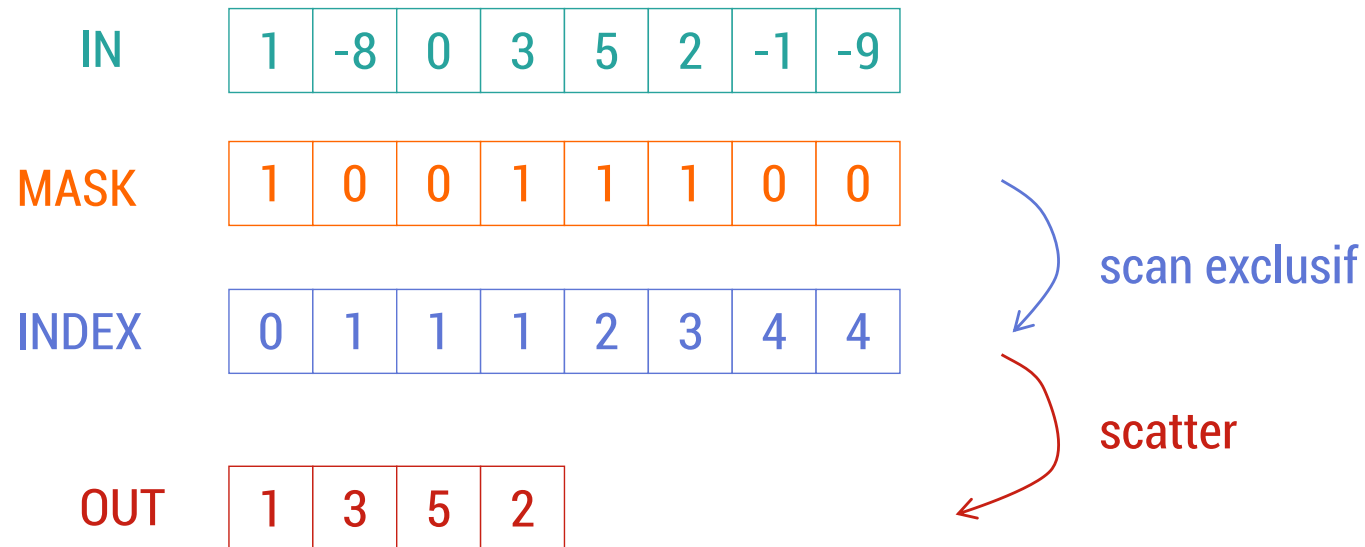
## Algorithme de Blelloch



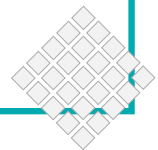
# Exercice : réduction de flot



A partir d'un tableau *IN* de  $n$  éléments, générer un tableau *OUT* qui contient tous les éléments de *IN* strictement supérieurs à 0, dans le même ordre.



```
__global__ void stream_compaction(int *d_out, int *d_in, int n){
    extern __shared__ int mask[] ;
    int tid = threadIdx.x ;
    int offset ;
    int my_mask;
    int a, b, tmp, my_data;
    my_data = d_in[tid];
    // création du masque
    if (tid < n){
        if (my_data > 0)
            my_mask = 1 ;
        else
            my_mask = 0 ;
        mask[tid] = my_mask ;
    }
    // scan du masque selon l'algorithme de Blelloch
```

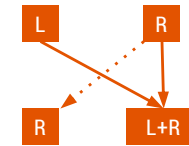
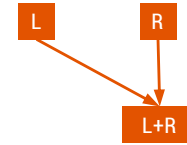
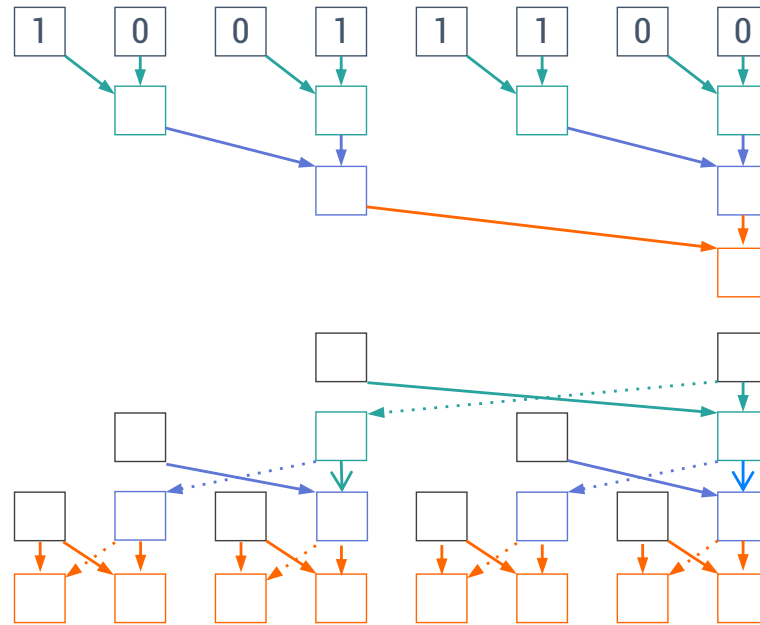


## Scan du masque

IN

1	-8	0	3	5	2	-1	-9
---	----	---	---	---	---	----	----

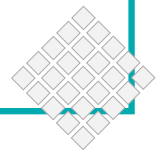
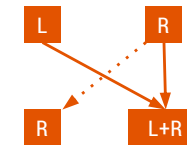
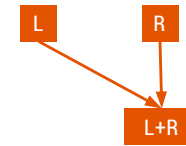
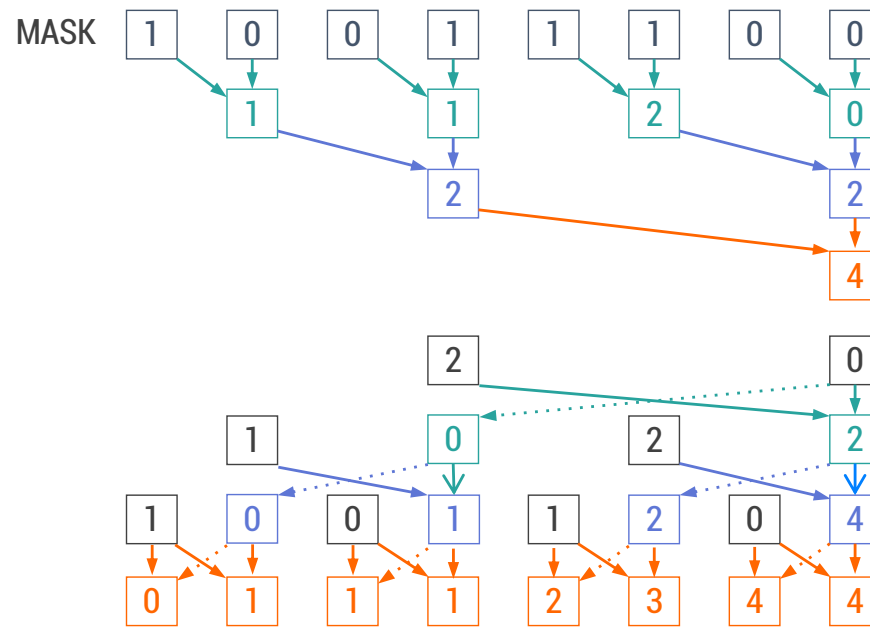
MASK





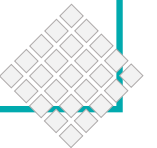
# Scan du masque

IN 1 -8 0 3 5 2 -1 -9

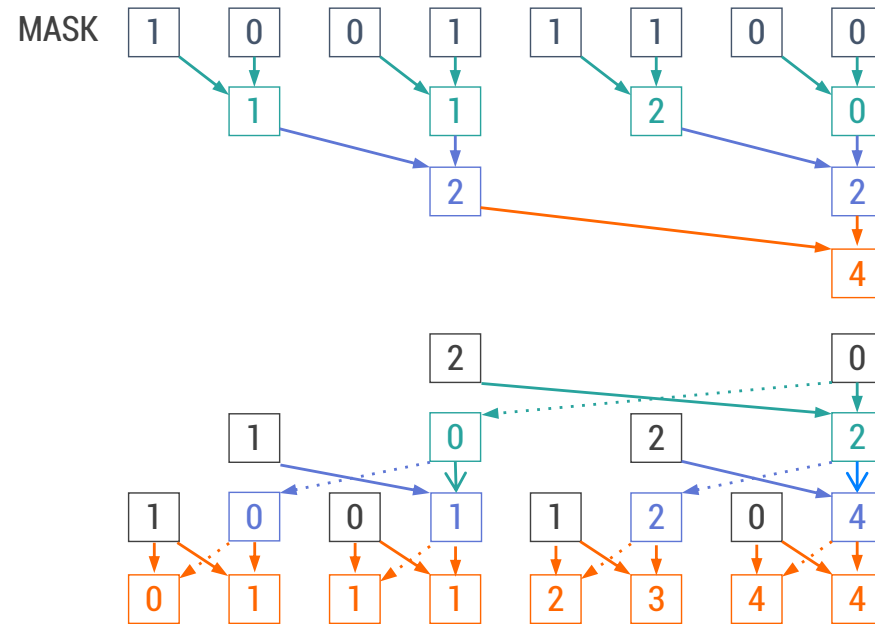


## Scan du masque

	offset = 1	offset = 2	offset = 4
th0	mask[1] += mask[0]	mask[3] += mask[1]	mask[7] += mask[3]
th1	mask[3] += mask[2]	mask[7] += mask[5]	
th2	mask[5] += mask[4]		
th3	mask[7] += mask[6]	mask[ f1(offset, tid) ] += mask[ f2(offset, tid) ]	



## Scan du masque



offset = 1

th0 mask[1] += mask[0]  
 th1 mask[3] += mask[2]  
 th2 mask[5] += mask[4]  
 th3 mask[7] += mask[6]

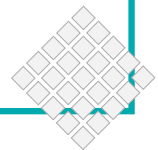
offset = 2

mask[3] += mask[1]  
 mask[7] += mask[5]

offset = 4

mask[7] += mask[3]

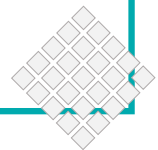
mask[ offset \* (2\*tid+2) - 1 ] += mask[ offset \* (2\*tid+1) - 1 ]



```

__global__ void stream_compaction(int *d_out, int *d_in, int n){
    extern __shared__ int mask[] ;
    int tid = threadIdx.x ;
    int offset ;
    int my_mask;
    int a, b, tmp, my_data;
    my_data = d_in[tid];
    // création du masque
    ...
    // scan du masque selon l'algorithme de Blelloch - 1ère partie
    offset = 1 ;
    for (int d=n>>1 ; d>0 ; d>>=1) {
        __syncthreads() ;
        if (tid < d) {
            a = offset * (2*tid+1) - 1 ;
            b = offset * (2*tid+2) - 1 ;
            if (b<n) mask[b] += mask[a] ;
        }
        offset *= 2 ;
    }
    __syncthreads() ;
    // scan du masque selon l'algorithme de Blelloch - 2ème partie
    ...

```



## Scan du masque

offset = 4

th0  
tmp = mask[7]  
mask[7] += mask[3]  
mask[3] = tmp

th1

th2

th3

```
tmp = mask[ g1(offset, tid) ]  
mask[ g1(offset, tid) ] += mask[ g2(offset, tid) ]  
mask[ g2(offset, tid) ] = tmp
```

offset = 2

tmp = mask[7]  
mask[7] += mask[5]  
mask[5] = tmp

tmp = mask[3]  
mask[3] += mask[1]  
mask[1] = tmp

offset = 4

tmp = mask[7]  
mask[7] += mask[6]  
mask[6] = tmp

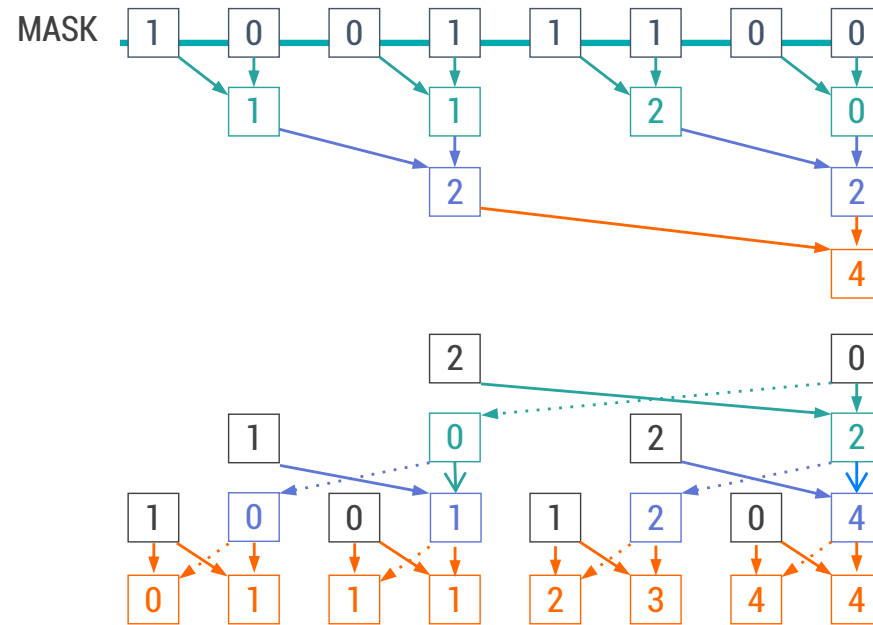
tmp = mask[5]  
mask[5] += mask[4]  
mask[4] = tmp

tmp = mask[3]  
mask[3] += mask[2]  
mask[2] = tmp

tmp = mask[1]  
mask[1] += mask[0]  
mask[0] = tmp



## Scan du masque



offset = 4

th0

```
tmp = mask[7]
mask[7] += mask[3]
mask[3] = tmp
```

th1

offset = 2

```
tmp = mask[7]
mask[7] += mask[5]
mask[5] = tmp

tmp = mask[3]
mask[3] += mask[1]
mask[1] = tmp
```

th2

offset = 4

```
tmp = mask[7]
mask[7] += mask[6]
mask[6] = tmp

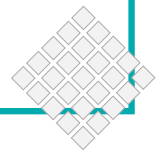
tmp = mask[5]
mask[5] += mask[4]
mask[4] = tmp

tmp = mask[3]
mask[3] += mask[2]
mask[2] = tmp

tmp = mask[1]
mask[1] += mask[0]
mask[0] = tmp
```

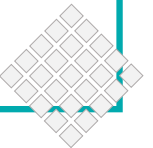
th3

```
tmp = mask[ offset * (2*tid +2) - 1 ]
mask[ offset * (2*tid +2) - 1 ] += mask[ offset * (2*tid +1) - 1 ]
mask[ offset * (2*tid +1) - 1 ] = tmp
```



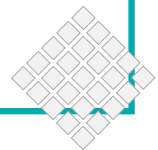
```
// scan du masque selon l'algorithme de Blelloch - 2ème partie
if (tid == 0)
    mask[n-1] = 0 ;
for (int d=1 ; d<n ; d *= 2){
    offset >>=1 ;
    __syncthreads() ;
    if (tid < d) {
        a = offset * (2*tid+1) - 1 ;
        b = offset * (2*tid+2) - 1 ;
        tmp = mask[b] ;
        mask[b] += mask[a] ;
        mask[a] = tmp ;
    }
}
__syncthreads() ;

// scatter
...
```



```
// scan du masque selon l'algorithme de Blelloch - 2ème partie
if (tid == 0)
    mask[n-1] = 0 ;
for (int d=1 ; d<n ; d *= 2){
    offset >>=1 ;
    __syncthreads() ;
    if (tid < d) {
        a = offset * (2*tid+1) - 1 ;
        b = offset * (2*tid+2) - 1 ;
        tmp = mask[b] ;
        mask[b] += mask[a] ;
        mask[a] = tmp ;
    }
}
__syncthreads() ;

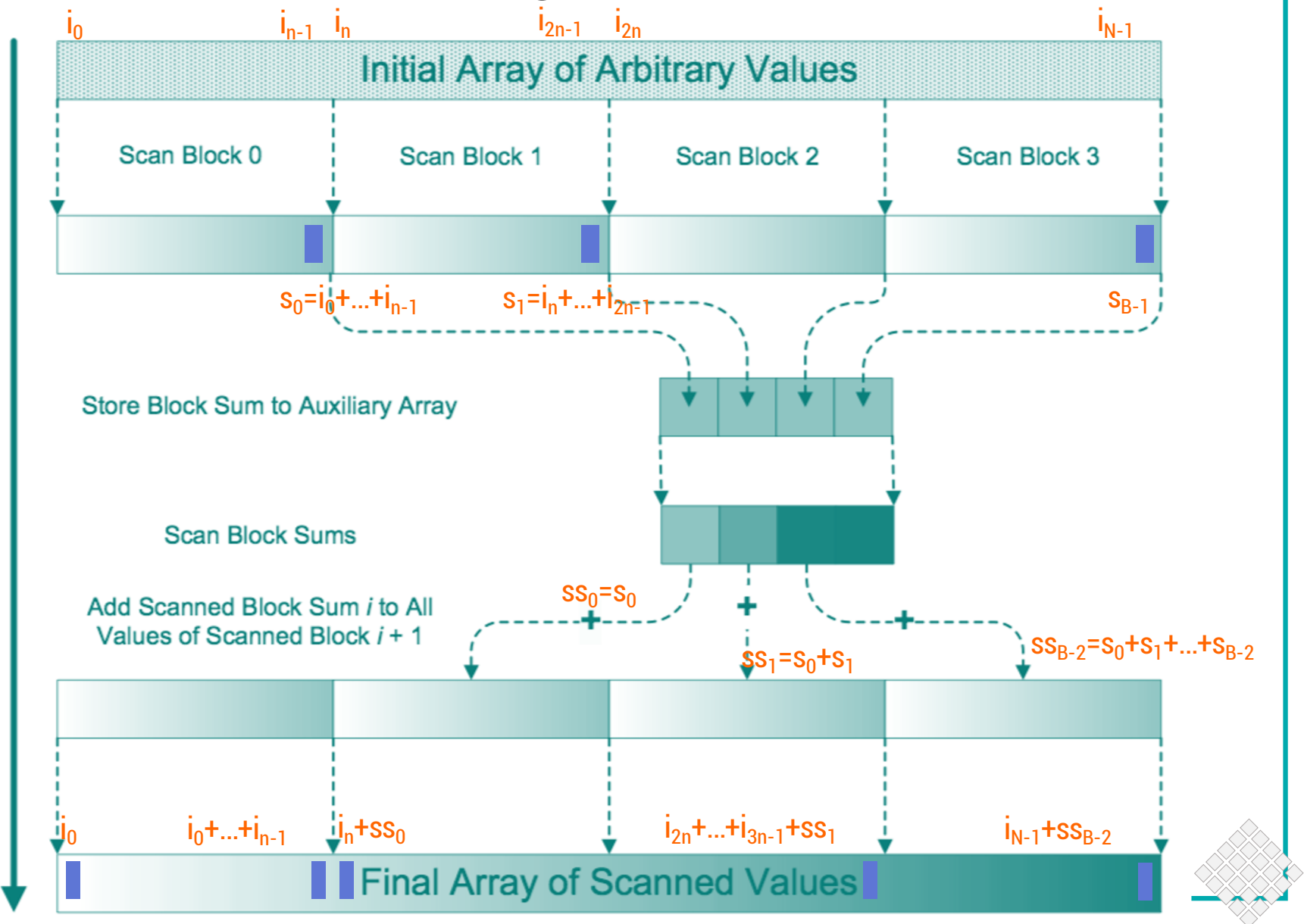
// scatter
if (my_mask == 1){
    d_out[mask[tid]] = my_data ;
}
```





## EXERCICE

### Scan pour des entrées de longueur quelconque

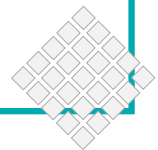


```

__device__ void scanBlock(int *d_out, int *d_in, int n){
    // scan sur un bloc (n <= BLOCK_SIZE) [algo de Blelloch => scan exclusif]
    int tid = threadIdx.x ;
    int offset, a, b, tmp;
    offset = 1 ;
    d_out[tid] = d_in[tid];
    __syncthreads();
    for (int d=n>>1 ; d>0 ; d>>=1) {
        __syncthreads() ;
        if (tid < d) {
            a = offset * (2*tid+1) - 1 ;
            b = offset * (2*tid+2) - 1 ;
            if (b<n) d_out[b] += d_out[a] ;
        }
        offset *= 2 ;
    }
    __syncthreads() ;
    if (tid == 0)
        d_out[n-1] = 0 ;
    for (int d=1 ; d<n ; d *= 2){
        offset >>=1 ;
        __syncthreads() ;
        if (tid < d) {
            a = offset * (2*tid+1) - 1 ;
            b = offset * (2*tid+2) - 1 ;
            tmp = d_out[b] ;
            d_out[b] += d_out[a] ;
            d_out[a] = tmp ;
        }
    }
    __syncthreads();
    d_out[tid] += d_in[tid]; // pour que le scan soit inclusif
}

```

Cette **fonction**, appellable depuis un kernel, calcule la contribution d'un thread au calcul du ***scan inclusif*** (+) sur un tableau.



```

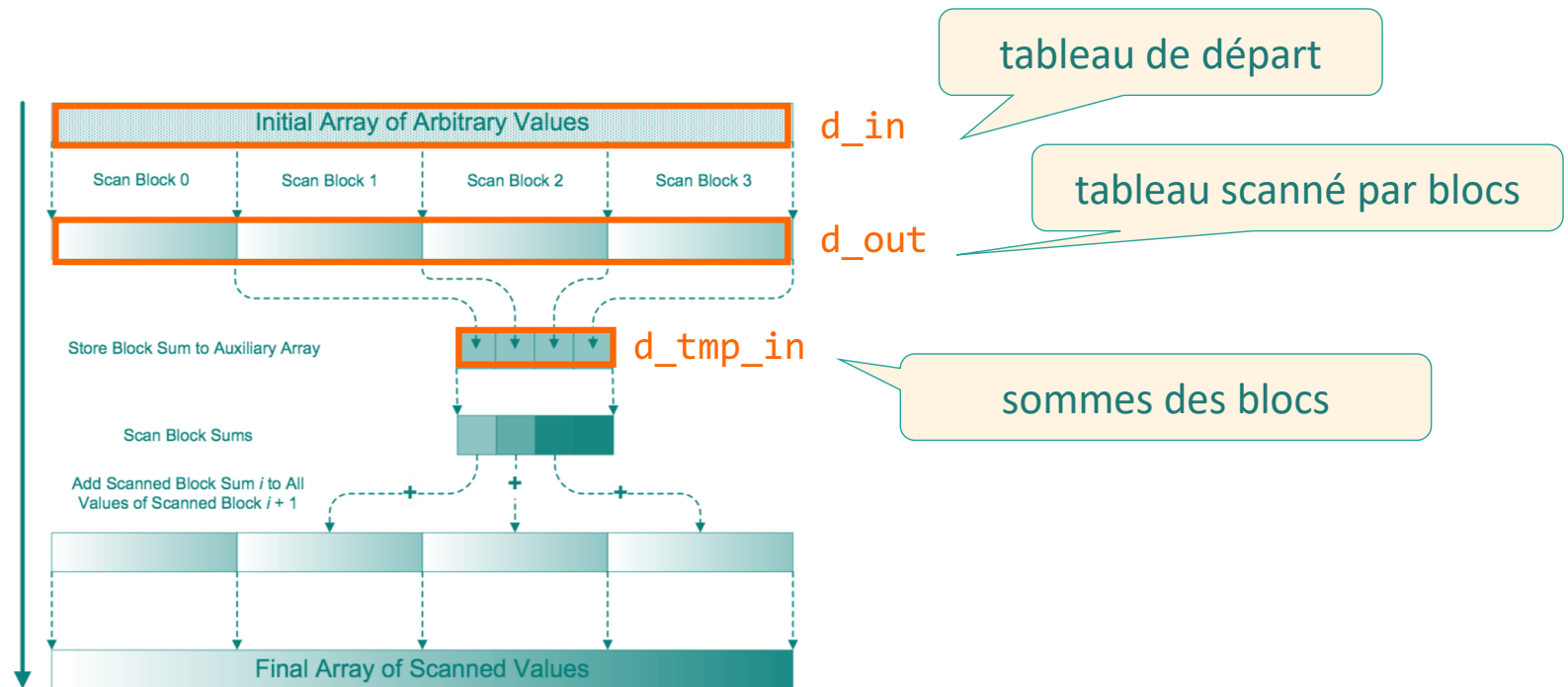
__device__ void scanBlock(int *d_out, int *d_in, int n){
    ... // scan sur un bloc (n <= BLOCK_SIZE)
}

```

```

__global__ void scanKernel_1(int *d_out, int *d_in, int *d_tmp, int size){
}

```



```
__device__ void scanBlock(int *d_out, int *d_in, int n){
    ... // scan sur un bloc (n <= BLOCK_SIZE)
}
```

```
__global__ void scanKernel_1(int *d_out, int *d_in, int *d_tmp, int size){
}
```

```
__global__ void scanKernel_2(int *d_out, int *d_in, int size){
}
```

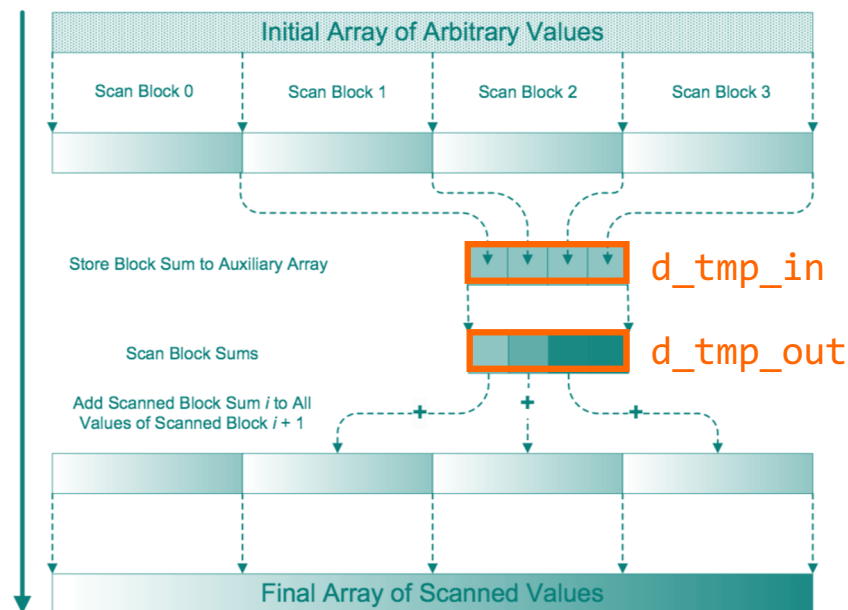


tableau de départ

tableau scanné

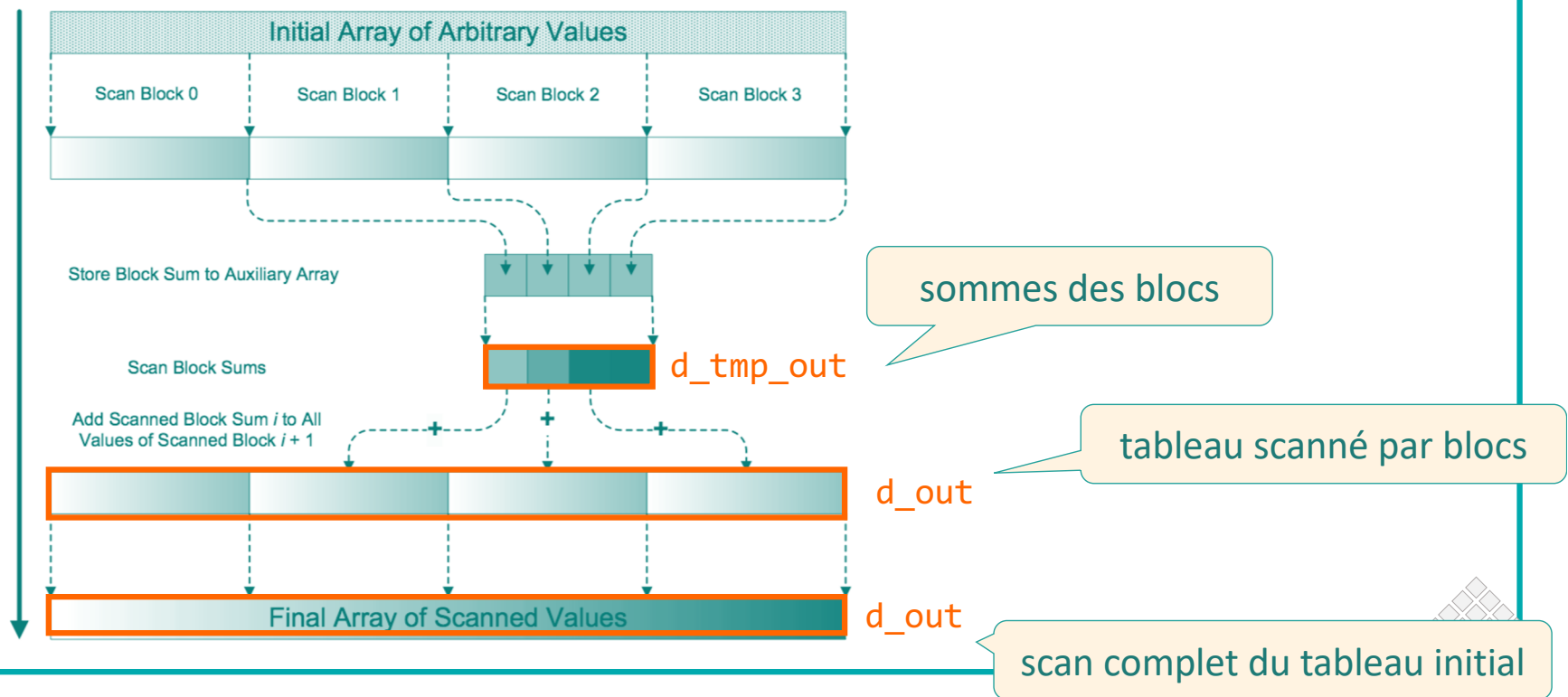


```
__device__ void scanBlock(int *d_out, int *d_in, int n){
    ... // scan sur un bloc (n <= BLOCK_SIZE)
}
```

```
__global__ void scanKernel_1(int *d_out, int *d_in, int *d_tmp, int size){
}
```

```
__global__ void scanKernel_2(int *d_out, int *d_in, int size){
}
```

```
__global__ void scanKernel_3(int *d_out, int *d_tmp, int size){
}
```



```
#define BLOCK_SIZE 1024
```

```
void scan(int *out, int *in, int size){  
    int *d_in, *d_out, *d_tmp_in, *d_tmp_out;  
    int *tmp;  
    int num_blocks = size / BLOCK_SIZE;  
    if (size % BLOCK_SIZE)  
        num_blocks++;
```

```
    cudaMalloc((void **)&d_in, size*sizeof(int));  
    cudaMalloc((void **)&d_out, size*sizeof(int));  
    cudaMalloc((void **)&d_tmp_in, num_blocks*sizeof(int));  
    cudaMalloc((void **)&d_tmp_out, num_blocks*sizeof(int));
```

```
    cudaMemcpy(d_in, in, size*sizeof(int), cudaMemcpyHostToDevice);
```

```
    scanKernel_1<<<num_blocks, BLOCK_SIZE>>>(d_out, d_in, d_tmp_in, size);
```

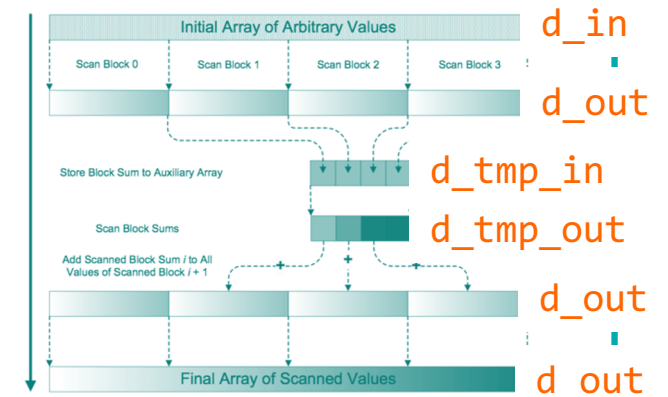
```
    scanKernel_2<<<1, num_blocks>>>(d_tmp_out, d_tmp_in, num_blocks);
```

```
    scanKernel_3<<<num_blocks-1, BLOCK_SIZE>>>(d_out, d_tmp_out, size);
```

```
    cudaMemcpy(out, d_out, size*sizeof(int), cudaMemcpyDeviceToHost);
```

```
    cudaFree(d_in); cudaFree(d_out); cudaFree(d_tmp_in); cudaFree(d_tmp_out);
```

```
}
```



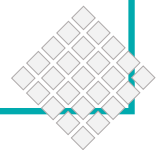
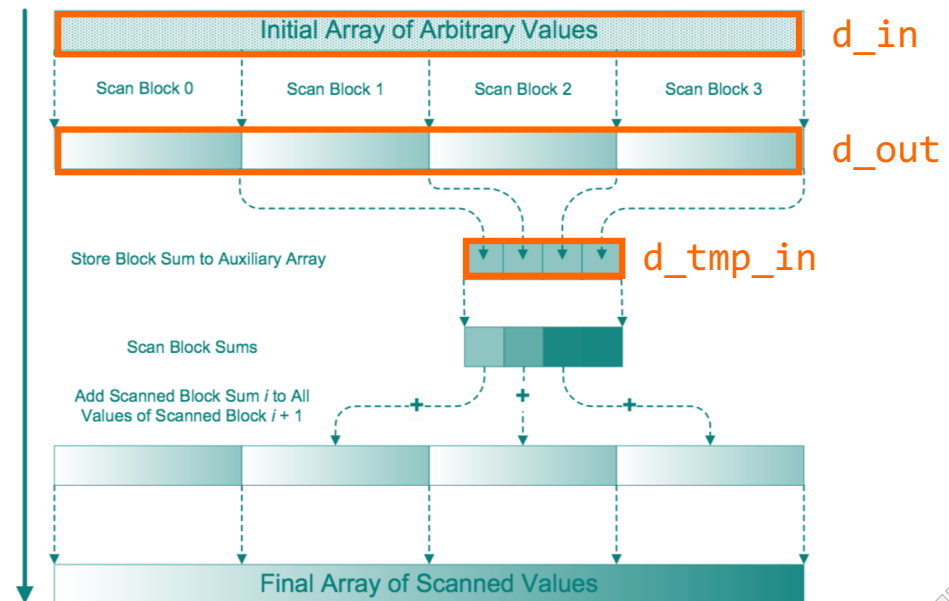
```

__device__ void scanBlock(int *d_out, int *d_in, int n){
    ... // scan sur un bloc (n <= BLOCK_SIZE)
}

__global__ void scanKernel_1(int *d_out, int *d_in, int *d_tmp, int size){

}

```



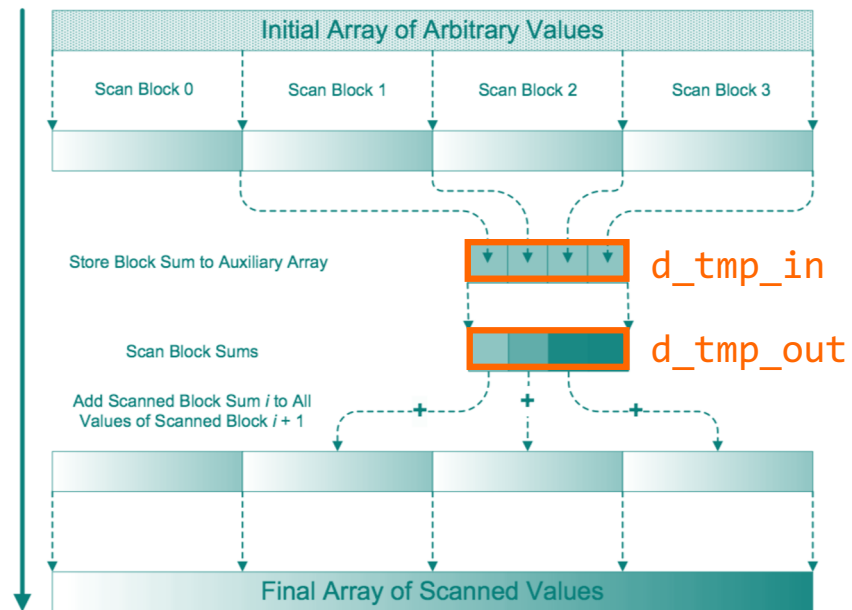
```

__device__ void scanBlock(int *d_out, int *d_in, int n){
    ... // scan sur un bloc (n <= BLOCK_SIZE)
}

__global__ void scanKernel_2(int *d_out, int *d_in, int size){

}

```





```

__device__ void scanBlock(int *d_out, int *d_in, int n){
    ... // scan sur un bloc (n <= BLOCK_SIZE)
}

__global__ void scanKernel_3(int *d_out, int *d_tmp, int size){

}

```

