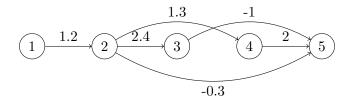
CSCI 3104-Spring 2016: Assignment #8.

Assigned date: Wednesday, 4/6/2016, Due date: Tuesday, 4/12/2016, before class

Maximum Points: 40 points (includes 5 points for legibility).

Note: This assignment must be turned in on paper, before class. Please do not email: it is very hard for us to keep track of email submissions. Further instructions are on the moodle page.

P1 (20 points) Let G be a directed acyclic graph with n vertices and m edges. We will find how to compute single source shortest paths for G running in time $\Theta(m + n \log(n))$. Let us take the example below.



- (A) Find a topological ordering of the graph G. How much time does it take for n nodes and m edges. Write down a topological ordering for the graph G above?
- (B) Design an algorithm that uses the topological ordering of G to find shortest paths from a single source. Illustrate the working of your algorithm to compute shortest path distances and the resulting tree starting from node 2.
- (C) What is the running time of the overall algorithm for finding shortest paths in DAGs.

P2 (20 points) A dictionary cipher substitutes each word in the dictionary by a string according to a codebook. Example codebook can be like below.

Word	Code
hello	juuyakjel
world	kjaue
how	ajsuei
are	lloppyy
you	jkjauieu

We have a part of the codebook that allows us to translate some words but are missing the other part. A long cipher-text with n letters is provided.

"jkjkuieuijuuyakjelkjkiekjaueajuseilloppyyaskjirrjkjauieukjkaiejjuyyajjuuyakjel"

Our goal is to split the cipher text to highlight known words and parts that cannot be decoded. For instance, the messge above may be split as follows:

"jkjkuieui + <u>juuyakjel</u> + kjkie + <u>kjaue</u> + <u>ajusei</u> + <u>lloppyy</u> + askjirr + <u>jkjauieu</u> + kjkaiejjuyyaj + <u>juuyakjel</u>"

This split yields 6 known codewords (underlined) from the codebook and 34 characters that are

ciphered, i.e., not part of a known codeword. The cost of such a split is taken to be 6 + 2 * 34 = 74.

Formally, we are given a codebook with codewords and a long cipher-text string with n characters. Our goal is to find a minimum cost split that splits the given cipher text into a set of known

codewords and ciphered characters so that the cost (defined as number of code words + 2 * number of ciphered characters) is minimized.

- (A) Show how a given string can be converted in to a graph whose vertices are the positions in the string and edges encode cost. Show how you can add edges to the graph corresponding to codewords and ciphered characters.
- (B) Show how the shortest cost path from the first position to the last yields an optimal way to split the string.