## Data Structures

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Realdolmen

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## Who am I?

- ► Master of Engineering: Computer Science (KUL)
  - Computational informatics
- ► Realdolmen: acADDemICT in 09/2015
- Current project: Planning infrastructure @ Infrabel

## Outline

1 Introductory Data Structures

Array Linked List Hash Table Tree Heap Binary Search Tree Red-Black Tree

- Java Collection API & Map API Java Collection API Java Map API
- Advanced Data Structures
  Skip list
  Bloom Filter
  van Emde Boas Tree

## Outline

Introductory Data Structures Array

Linked List Hash Table Tree

- 2 Java Collection API & Map API Java Collection API Java Map API
- 3 Advanced Data Structures
  Skip list
  Bloom Filter
  van Emde Boas Tree



### What are Data Structures?

#### Data Structure<sup>1</sup>

A way in which data are stored for efficient search and retrieval. Different data structures are suited for different problems.

- ▶ Data type ≠ data structure
- ▶ java.util.HashSet vs. hash table
- array vs. array

<sup>&</sup>lt;sup>1</sup>Encyclopædia Britannica

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> Linked List Hash Table Tree

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#### Definition

- ► An indexed set of related elements.<sup>2</sup>
- ► An assemblage of items that are randomly accessible by integers, the index.<sup>3</sup>
- ► Example: linear array



 $<sup>^2\</sup>mathrm{Oxford}$  Dictionary

<sup>&</sup>lt;sup>3</sup>National Institute of Standards & Technology

- ▶ get
- ▶ set
- ▶ indexOf



## Operations

- ▶ get
- ▶ set
- ▶ indexOf



get(1)

## Operations

- ▶ get
- ▶ set
- ▶ indexOf



get(1)

## Operations

- ▶ get *O*(1)
- ▶ set
- ▶ indexOf



get(1)

## Operations

- ▶ get *O*(1)
- ▶ set
- ▶ indexOf



set(2)

## Operations

- ▶ get *O*(1)
- ▶ set
- ▶ indexOf



set(2)

### Operations

- ightharpoonup get O(1)
- ▶ set O(1)
- ▶ indexOf



set(2)

#### **Operations**

- ightharpoonup get O(1)
- ▶ set O(1)
- ▶ indexOf



#### **Operations**

- ightharpoonup get O(1)
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- ightharpoonup get O(1)
- ▶ set O(1)
- ▶ indexOf



- ightharpoonup get O(1)
- ▶ set O(1)
- ▶ indexOf O(n)



## Outline

1 Introductory Data Structures

Linked List Hash Table Tree

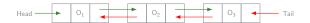
- 2 Java Collection API & Map API Java Collection API Java Map API
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#### Definition

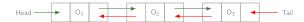
A linked list is a data structure in which the objects are arranged in a linear order. Unlike arrays in which the linear order is determined by indices, the order is determined by a pointer in each object.<sup>4</sup>

- ▶ Different types: singly, doubly, multiply, circular, . . .
- Example: doubly linked list



Introduction to Algorithms By Cormen, Leierson, Rivest & Stein

- ▶ add/remove first/last
- ▶ get/insertAt
- ▶ indexOf





### Operations

- ▶ add/remove first/last
- ▶ get/insertAt
- ▶ indexOf



 $addFirst(O_4)$ 

- ▶ add/remove first/last
- ▶ get/insertAt
- ▶ indexOf



 $addFirst(O_4)$ 

- ▶ add/remove first/last
- ▶ get/insertAt
- ▶ indexOf



 $addFirst(O_4)$ 

- ▶ add/remove first/last O(1)
- ▶ get/insertAt
- ▶ indexOf



 $addFirst(O_4)$ 

### Operations

- ▶ add/remove first/last O(1)
- ▶ get/insertAt
- ▶ indexOf



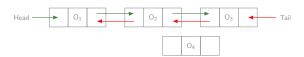
insertAt(2)

O(1)

### Linked List

### Operations

- ▶ add/remove first/last
- ▶ get/insertAt
- ▶ indexOf

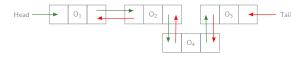


insertAt(2)

O(1)

### Linked List

- ▶ add/remove first/last
  - . /:
- ▶ get/insertAt
- ▶ indexOf



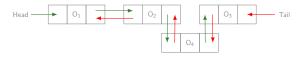
insertAt(2)

### **Operations**

- ▶ add/remove first/last
- O(n)

O(1)

- ▶ get/insertAt
- ▶ indexOf



insertAt(2)

### **Operations**

- ▶ add/remove first/last
- O(1) O(n)

- ▶ get/insertAt
- ▶ indexOf



### **Operations**

- ► add/remove first/last
- O(1) O(n)

▶ get/insertAt

O(n

▶ indexOf



### Operations

- ▶ add/remove first/last
- O(1)

▶ get/insertAt

O(n)

▶ indexOf



### Operations

- ▶ add/remove first/last O(1)
- ▶ get/insertAt O(n)
- ▶ indexOf O(n)



#### Linked List

- ▶ add/remove first/last O(1)
- ▶ get/insertAt O(n)
- ▶ indexOf O(n)





## Outline

Introductory Data Structures

Array Linked List Hash Table Tree

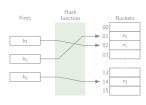
- 2 Java Collection API & Map API Java Collection API Java Map API
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#### Definition

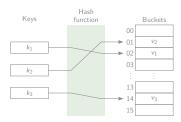
A dictionary in which keys are mapped to array positions by hash functions.<sup>5</sup>

- ► Hash functions: determinism, uniformity, defined range, data normalisation, non-invertible, perfect, . . .
- ▶ Collisions resolution: chaining, open addressing, . . .
- Example:



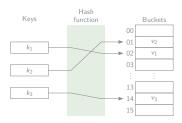
<sup>&</sup>lt;sup>5</sup>National Institute of Standards & Technology

- ▶ put
- remove
- ▶ get



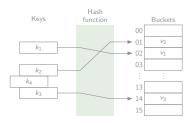


- ▶ put
- remove
- ▶ get



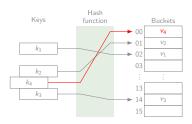
 $put(0_4)$ 

- ▶ put
- remove
- ▶ get



 $put(0_4)$ 

- ▶ put
- remove
- ▶ get

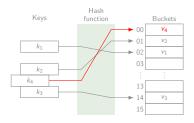


 $put(0_4)$ 

### Operations

▶ put

- O(1) / O(n)
- remove
- ▶ get

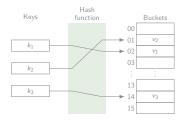


 $put(0_4)$ 

### Operations

▶ put

- O(1) / O(n)
- ► remove
- ▶ get

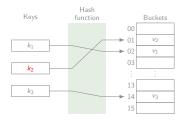


 $\texttt{remove}(\mathbb{O}_2)$ 

### Operations

▶ put

- O(1) / O(n)
- remove
- ▶ get

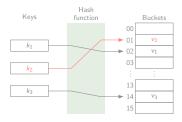


 $remove(O_2)$ 

### Operations

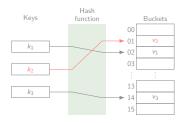
▶ put

- O(1) / O(n)
- ► remove
- ▶ get



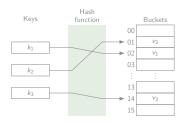
 $remove(O_2)$ 

- ▶ put O(1) / O(n)
- ▶ remove O(1) / O(n)
- ▶ get



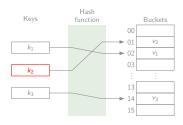
 $remove(O_2)$ 

- ▶ put O(1) / O(n)
- ▶ remove O(1) / O(n)
- ▶ get



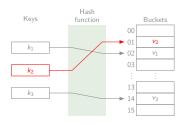
 $get(O_2)$ 

- ▶ put O(1) / O(n)
- ▶ remove O(1) / O(n)
- ▶ get



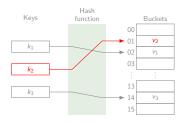
 $get(O_2)$ 

- ▶ put O(1) / O(n)
- remove O(1) / O(n)
- ▶ get



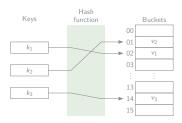
 $get(O_2)$ 

- ▶ put O(1) / O(n)
- ▶ remove O(1) / O(n)
- ▶ get O(1) / O(n)



 $get(O_2)$ 

- ▶ put O(1) / O(n)
- remove O(1) / O(n)
- ▶ get O(1) / O(n)



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Array Linked List

Tree

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  Skip list
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#### Tree

#### Definition

A data structure made up of nodes or vertices and edges without having any cycle. A tree that is not empty consists of a root node and potentially many levels of additional nodes that form a hierarchy.

- Depth, binary, (nearly) complete, . . .
- Example:





#### Tree

#### Definition

A data structure made up of nodes or vertices and edges without having any cycle. A tree that is not empty consists of a root node and potentially many levels of additional nodes that form a hierarchy.

- ▶ Depth, binary, (nearly) complete, ...
- Example:





## Binary Heap

#### Definition (Heap)

A complete tree where every node has a key more extreme (greater or less) than or equal to the key of its parent.<sup>6</sup>

#### Definition (Binary Heap)

A binary heap data structure is an array object that we can view as a nearly complete binary tree that satisfies the min-heap or max-heap property.<sup>7</sup>

<sup>&</sup>lt;sup>6</sup>National Institute of Standards & Technology

Introduction to Algorithms By Cormen, Leierson, Rivest & Stein

- ▶ Parent(n)  $\lfloor \frac{n-1}{2} \rfloor$
- Left(n) 2n+1
- ▶ Right(n) 2(n+1)











ıdd (8)













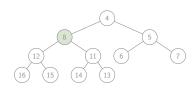


















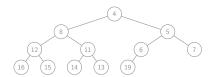


add (19)









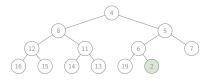




add 2







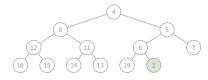




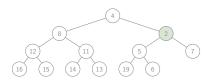
















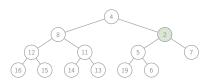


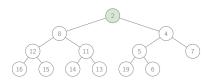




















poll

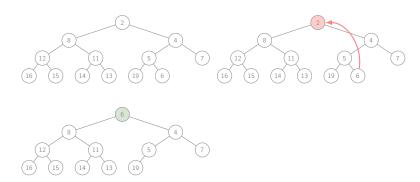




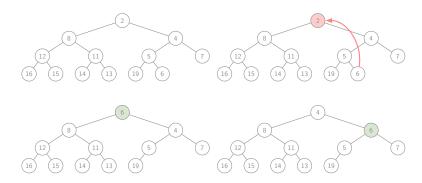




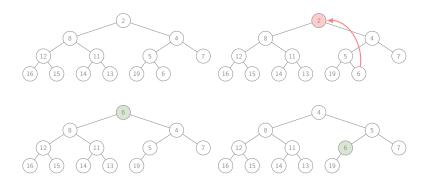














- ▶ insert
- ► removeAt
- peek
- ▶ poll



- ▶ insert  $O(\log n)$
- removeAt  $O(\log n)$
- ightharpoonup peek O(1)
- ▶ poll  $O(\log n)$



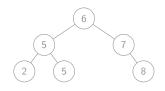
- ▶ insert  $O(\log n)$
- ▶ removeAt  $O(\log n)$
- ▶ peek O(1)
- ▶ poll  $O(\log n)$
- Heapsort
- Frequently used in Priority Queues

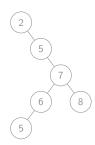


## Binary Search Tree

#### Definition

A binary tree in which the left child  $\leq$  the parent and the right child  $\geq$  the parent.







## Binary Search Tree

- ▶ insert  $O(\log n) / O(n)$
- delete  $O(\log n) / O(n)$
- search  $O(\log n) / O(n)$



- ▶ Binary search tree
- Approximately balanced
- ► NIL leaves
- Red-black properties

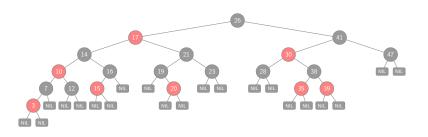


- ▶ Binary search tree
- Approximately balanced
- NIL leaves
- Red-black properties
  - Every node is either red or black
  - ▶ Root is black
  - ► Every leaf is black
  - ▶ If a node is red, its children are black
  - For each node, all paths to its descendant leaves contain the same number of black nodes

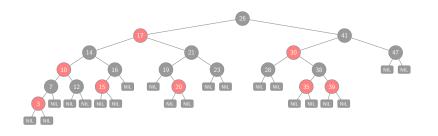


- ► Node is either red or black
- ► Root is black

- Every leaf is black
- ► If red, children are black
- ▶ ∀ node: all paths to its leaves have the same number of black nodes



- ▶ insert
- ► delete
- ▶ search



- ▶ insert  $O(\log n)$
- delete  $O(\log n)$
- $\triangleright$  search  $O(\log n)$



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   Linked List
   Hash Table
   Tree
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#### Outline

Java Collection API & Map API Java Collection API

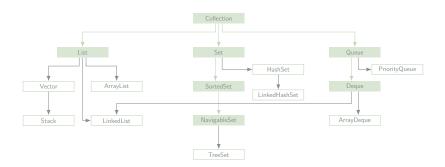


#### Java Collection API





#### Java Collection API



	Impl	add	remove	contains	get
LinkedList	linked list				
ArrayList	array				
Vector	array				
Stack	array				



	Impl	add	remove	contains	get
LinkedList	linked list	O(1)			
ArrayList	array				
Vector	array				
Stack	array				



	Impl	add	remove	contains	get
LinkedList	linked list	O(1)	O(1)		
ArrayList	array				
Vector	array				
Stack	array				



	Impl	add	remove	contains	get
LinkedList	linked list	O(1)	O(1)	O(n)	
ArrayList	array				
Vector	array				
Stack	array				



#### Impl add remove contains get LinkedList linked list O(1)O(1)O(n)O(n)ArrayList array Vector array Stack array

	Impl	add	remove	contains	get
LinkedList	linked list	O(1)	O(1)	O(n)	<i>O</i> ( <i>n</i> )
ArrayList	array	O(1)			
Vector	array				
Stack	array				



	Impl	add	remove	contains	get
LinkedList	linked list	O(1)	O(1)	O(n)	O(n)
ArrayList	array	O(1)	O(n)		
Vector	array				
Stack	array				



#### Impl add remove contains get LinkedList linked list O(1)O(1)O(n)O(n)ArrayList O(1)O(n)O(n)array Vector array Stack array



	Impl	add	remove	contains	get
LinkedList	linked list	O(1)	O(1)	O(n)	<i>O</i> ( <i>n</i> )
ArrayList	array	O(1)	O(n)	O(n)	O(1)
Vector	array				
Stack	array				



	Impl	add	remove	contains	get
LinkedList	linked list	O(1)	O(1)	O(n)	O(n)
ArrayList	array	O(1)	O(n)	O(n)	O(1)
Vector	array	O(1)	O(n)	O(n)	O(1)
Stack	array	O(1)	O(n)	O(n)	O(1)



## Set Interface

	Impl	add	contains	next
HashSet	hash table			
LinkedHashSet	hash table linked list			
TreeSet	red-black tree			



#### Set Interface

	Impl	add	contains	next
HashSet	hash table	O(1)		
LinkedHashSet	hash table linked list			
TreeSet	red-black tree			



#### Set Interface

	Impl	add	contains	next
HashSet	hash table	O(1)	O(1)	
LinkedHashSet	hash table linked list			
TreeSet	red-black tree			



	Impl	add	contains	next
HashSet	hash table	O(1)	O(1)	O(h/n)
LinkedHashSet	hash table linked list			
TreeSet	red-black tree			



	Impl	add	contains	next
HashSet	hash table	O(1)	O(1)	O(h/n)
LinkedHashSet	hash table linked list	O(1)		
TreeSet	red-black tree			



	Impl	add	contains	next
HashSet	hash table	O(1)	O(1)	O(h/n)
LinkedHashSet	hash table linked list	O(1)	O(1)	
TreeSet	red-black tree			



	Impl	add	contains	next
HashSet	hash table	O(1)	O(1)	O(h/n)
LinkedHashSet	hash table linked list	O(1)	O(1)	O(1)
TreeSet	red-black tree			



	Impl	add	contains	next
HashSet	hash table	O(1)	O(1)	O(h/n)
LinkedHashSet	hash table linked list	O(1)	O(1)	O(1)
TreeSet	red-black tree	$O(\log n)$		



	Impl	add	contains	next
HashSet	hash table	O(1)	O(1)	O(h/n)
LinkedHashSet	hash table linked list	O(1)	O(1)	O(1)
TreeSet	red-black tree	$O(\log n)$	$O(\log n)$	



	Impl	add	contains	next
HashSet	hash table	O(1)	O(1)	O(h/n)
LinkedHashSet	hash table linked list	O(1)	O(1)	O(1)
TreeSet	red-black tree	$O(\log n)$	$O(\log n)$	$O(\log n)$



	Impl	offer	peak	poll
PriorityQueue	binary heap			
ArrayDeque	array			
LinkedList	linked list			



	Impl	offer	peak	poll
PriorityQueue	binary heap	$O(\log n)$		
ArrayDeque	array			
LinkedList	linked list			



	Impl	offer	peak	poll
PriorityQueue	binary heap	$O(\log n)$	O(1)	
ArrayDeque	array			
LinkedList	linked list			



	Impl	offer	peak	poll
PriorityQueue	binary heap	$O(\log n)$	O(1)	$O(\log n)$
ArrayDeque	array			
LinkedList	linked list			



	Impl	offer	peak	poll
PriorityQueue	binary heap	$O(\log n)$	O(1)	$O(\log n)$
ArrayDeque	array	O(1)		
LinkedList	linked list			



	Impl	offer	peak	poll
PriorityQueue	binary heap	$O(\log n)$	O(1)	$O(\log n)$
ArrayDeque	array	O(1)	O(1)	
LinkedList	linked list			



	Impl	offer	peak	poll
PriorityQueue	binary heap	$O(\log n)$	O(1)	$O(\log n)$
ArrayDeque	array	O(1)	O(1)	O(1)
LinkedList	linked list			



#### Impl offer peak poll PriorityQueue $O(\log n)$ $O(\log n)$ binary heap O(1)ArrayDeque O(1)O(1)O(1)array LinkedList linked list O(1)O(1)O(1)



#### Outline

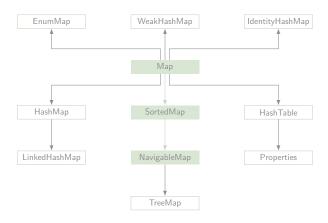
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## Java Map API



## Java Map API



	Impl	get	containsKey	next
HashTable	hash table			
Properties	hash table			
HashMap	hash table			
LinkedHashMap	hash table linked list			
TreeMap	red-black tree			
IdendityHashMap	array			
WeekHashMap	hash table			
EnumMap	array			



	Impl	get	containsKey	next
HashTable	hash table	O(1)		
Properties	hash table	O(1)		
HashMap	hash table	O(1)		
LinkedHashMap	hash table linked list			
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IdendityHashMap	array			
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EnumMap	array			



	Impl	get	containsKey	next
HashTable	hash table	O(1)	O(1)	
Properties	hash table	O(1)	O(1)	
HashMap	hash table	O(1)	O(1)	
LinkedHashMap	hash table linked list			
TreeMap	red-black tree			
Idendity Hash Map	array			
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	Impl	get	containsKey	next
HashTable	hash table	O(1)	O(1)	O(h/n)
Properties	hash table	O(1)	O(1)	O(h/n)
HashMap	hash table	O(1)	O(1)	O(h/n)
LinkedHashMap	hash table linked list			
TreeMap	red-black tree			
Idendity Hash Map	array			
WeekHashMap	hash table			
EnumMap	array			

	Impl	get	containsKey	next
HashTable	hash table	O(1)	O(1)	O(h/n)
Properties	hash table	O(1)	O(1)	O(h/n)
HashMap	hash table	O(1)	O(1)	O(h/n)
LinkedHashMap	hash table linked list	O(1)		
TreeMap	red-black tree			
IdendityHashMap	array			
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	Impl	get	containsKey	next
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HashMap	hash table	O(1)	O(1)	O(h/n)
LinkedHashMap	hash table linked list	O(1)	O(1)	
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LinkedHashMap	hash table linked list	O(1)	O(1)	O(1)
TreeMap	red-black tree	$O(\log n)$		
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HashTable	hash table	O(1)	O(1)	O(h/n)
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TreeMap	red-black tree	$O(\log n)$	$O(\log n)$	$O(\log n)$
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#### Outline

- 1 Introductory Data Structures
  Array
  Linked List
  Hash Table
- 2 Java Collection API & Map API Java Collection API Java Map API
- 3 Advanced Data Structures
  Skip list
  Bloom Filter
  van Emde Boas Tree



#### Outline

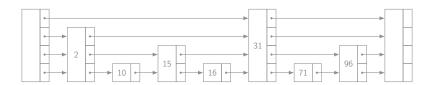
- Introductory Data Structures
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Bloom Filter van Emde Boas Tree

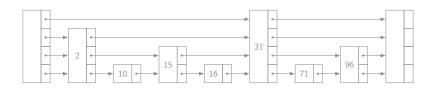


- ► Balanced binary tree alternative
  - ▶ insert, delete & search in  $O(\log n)$
- ▶ Probabilistic balancing rather than strictly enforced balancing
- ▶ Insertion and deletion  $\rightarrow$  simpler and faster
- Linked hierarchy of subsequences, with each successive subsequence skipping over fewer elements than the previous one
  - ▶ Hierarchy has  $\approx \log n$  levels

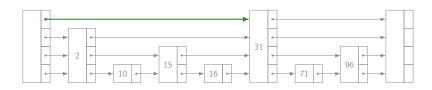




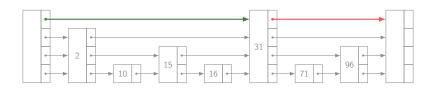




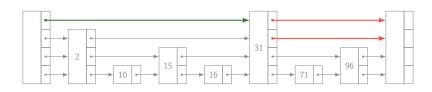
find 71



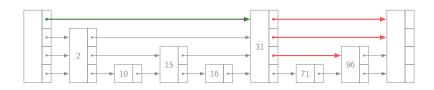
find 71



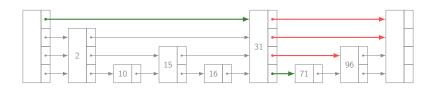
find 71



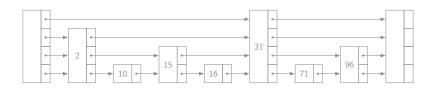
find 71



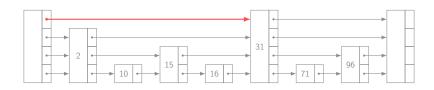
find 71



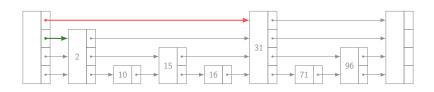
find 71



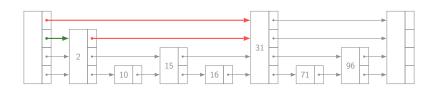
find 12



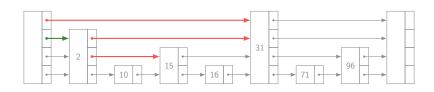
find 12



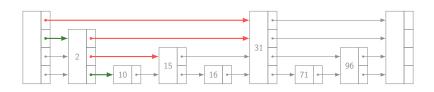
find 12



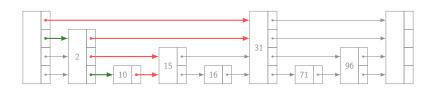
find 12



find 12

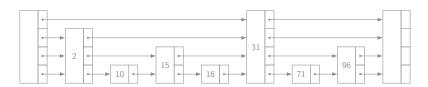


find 12

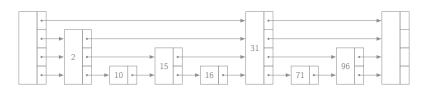


find 12

- ▶ insert at level=1
- ▶ while (coinflip() == HEADS)
   insert at ++level

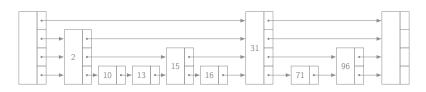


- ▶ insert at level=1
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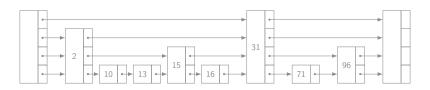
insert 13

- ▶ insert at level=1
- while (coinflip() == HEADS)
  insert at ++level



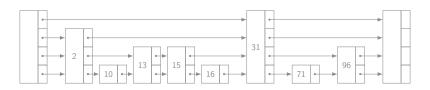
insert 13

- ▶ insert at level=1
- while (coinflip() == HEADS)
  insert at ++level



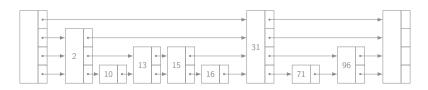
insert 13 — Coinflips: H

- ▶ insert at level=1
- while (coinflip() == HEADS)
  insert at ++level



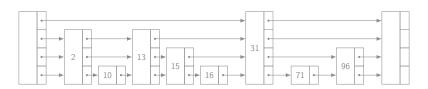
insert 13 — Coinflips: H

- ▶ insert at level=1
- while (coinflip() == HEADS)
  insert at ++level



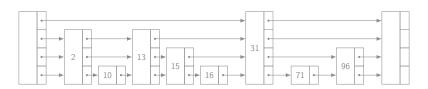
insert 13 — Coinflips: HH

- ▶ insert at level=1
- ▶ while (coinflip() == HEADS)
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insert 13 — Coinflips: HH

- ▶ insert at level=1
- ▶ while (coinflip() == HEADS)
   insert at ++level



insert 13 — Coinflips: HHT

### Operations

- ▶ insert
- ► delete
- ▶ search

#### **Operations**

- ▶ insert  $O(\log n) / O(n)$
- ▶ delete  $O(\log n) / O(n)$
- ▶ search  $O(\log n) / O(n)$



## Outline

- Introductory Data Structures
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- Java Collection API & Map API Java Collection API Java Map API
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  Skip list
  Bloom Filter



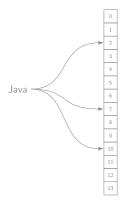
- ▶ Data structure to indicate if an element is contained in a set
- ▶ Bit array → space efficient
- Probabilistic
  - ► False positives possible
  - ► False negatives impossible
- ▶ Elements can be added to the set, but not removed

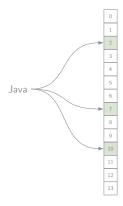


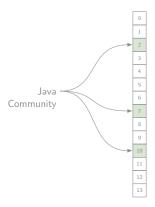


Java

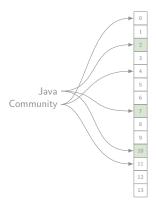




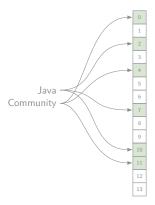




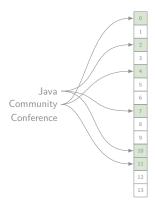


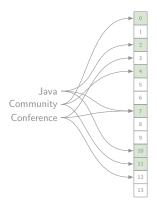


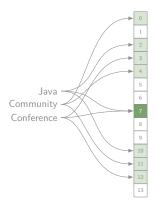




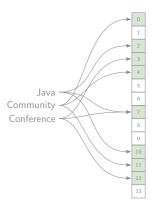




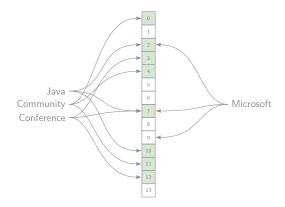




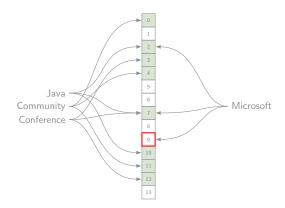


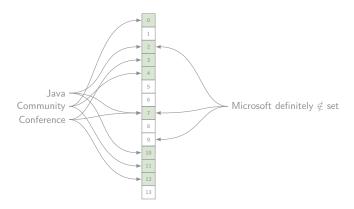


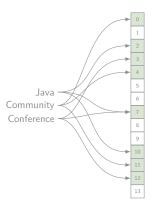
Microsoft





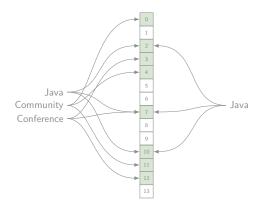




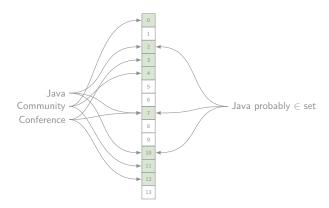


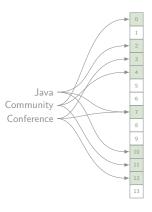
Java



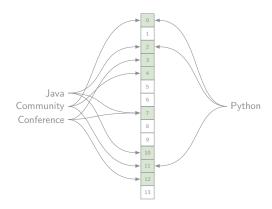


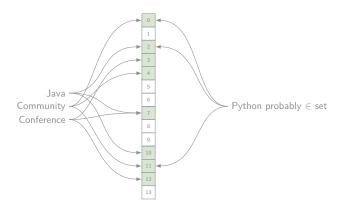






Python





#### Math

- ▶ m: array length
- ► k: # hash functions

- ▶ *n*: # of inserted elements
- p: false positive probability
- $\# \text{ bits needed: } m = \frac{-n \ln p}{(\ln 2)^2}$
- ▶ Optimal # of hash functions:  $k = \frac{m}{n} \ln(2)$

#### Math

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- $\# \text{ bits needed: } m = \frac{-n \ln p}{(\ln 2)^2}$
- ▶ Optimal # of hash functions:  $k = \frac{m}{n} \ln(2)$
- Supports unions and intersections
- ► Fits arbitrarily # of elements (false positive rate increases)
- Common application: caching

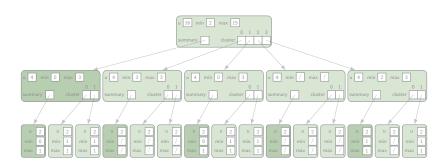
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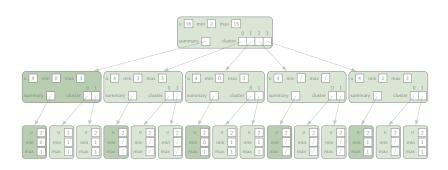


- Dynamic ordered set/map
  - ▶ insert, delete, contains, minimum, maximum, successor, predecessor operations in  $O(\log \log U)$
- ► Integer keys
  - ► No duplicates
- ightharpoonup O(U) space ightharpoonup only for large collections

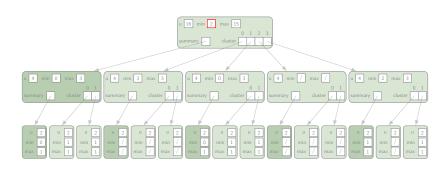




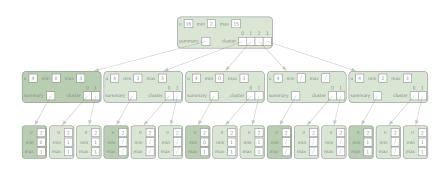




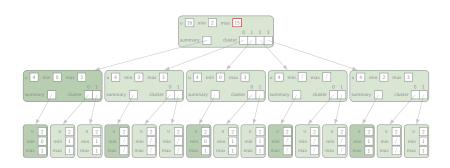




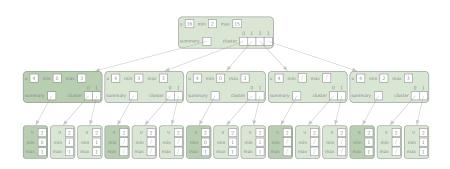




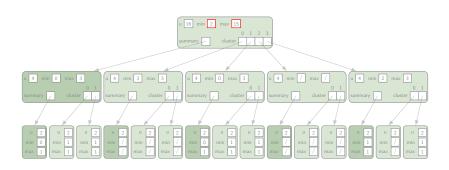




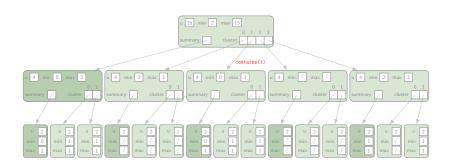




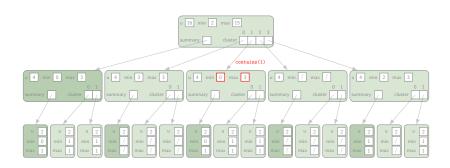




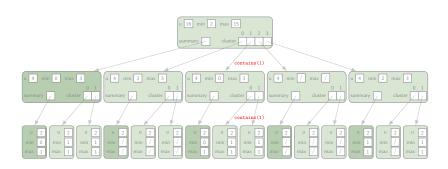




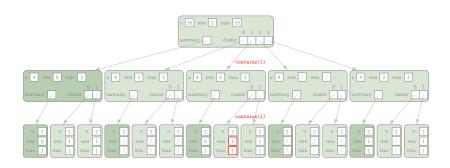




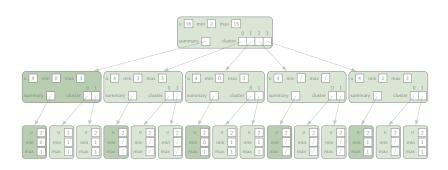




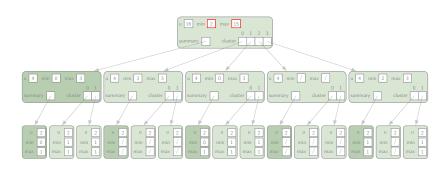




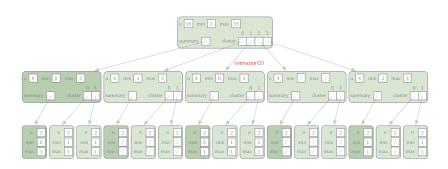




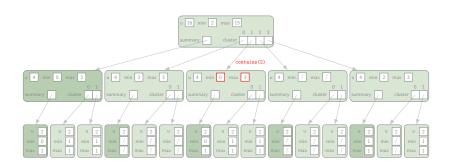




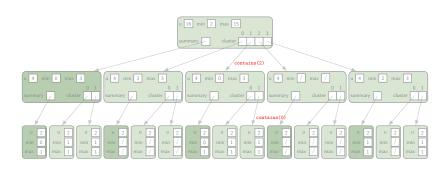




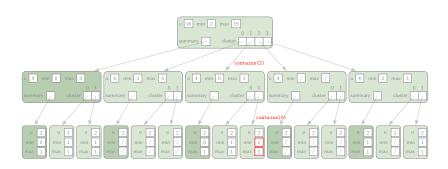




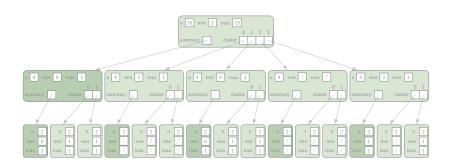




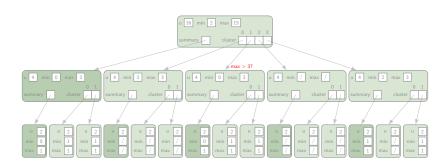




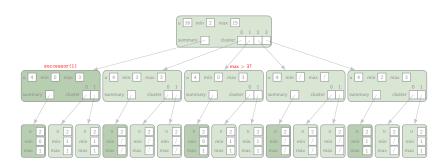




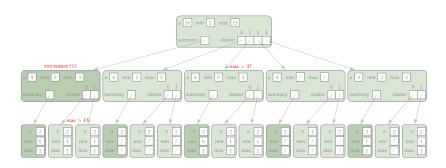




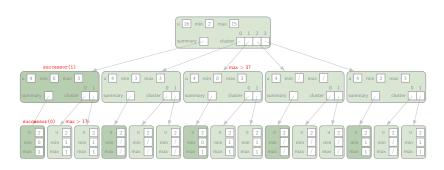




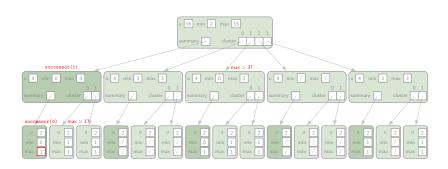




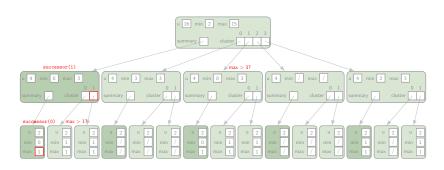








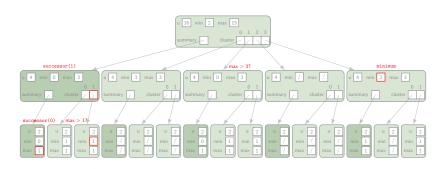




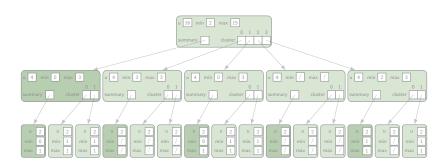




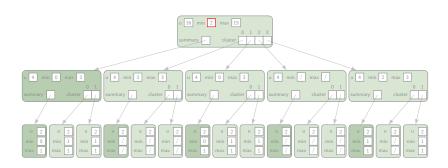




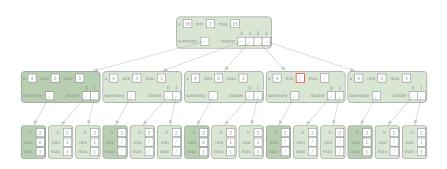




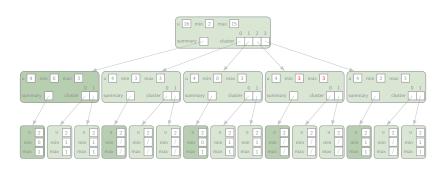




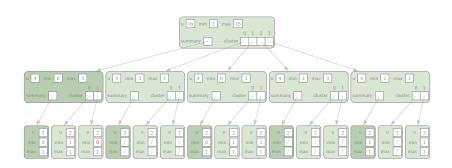














## Operations

▶ min, max, isEmpty

O(1)

 $\triangleright$  insert, delete, contains, succ, pred  $O(\log \log U)$ 

► O(U) space

► X-fast trie:  $O(n \log U)$  space

 $\triangleright$  Y-fast trie: O(n) space

 $V = 2^k, k \in \mathbb{N}$ 

# Thank you for your attention!

Slides:

https://github.com/MDhondt/Data-Structures-presentation