Data Structures

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Realdolmen

June 23, 2017

Who am I?

- Master of Engineering: Computer Science (KUL)
  - Computational informatics
- RealdolMen: acADDemICT in 09/2015
- Current project: Planning infrastructure @ Infrabel

Outline

1. Introductory Data Structures
   - Array
   - Linked List
   - Hash Table
   - Tree
2. Java Collection API & Map API
   - Java Collection API
   - Java Map API
3. Advanced Data Structures
   - Stuff...

Outline

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What are Data Structures?

Data Structure[1]

A way in which data are stored for efficient search and retrieval. Different data structures are suited for different problems.

- Data type $\neq$ data structure
- `java.util.HashSet` vs. hash table
- `array` vs. array

[1] Encyclopædia Britannica

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Array

Definition

- An indexed set of related elements.[2]
- An assemblage of items that are randomly accessible by integers, the index.[3]

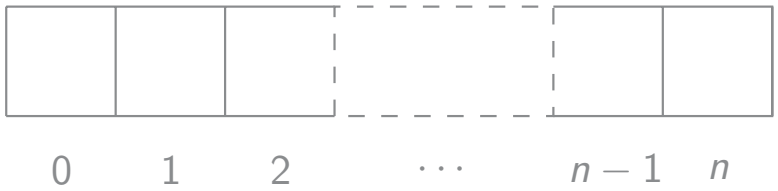
- Example: linear array

[2] Oxford Dictionary
[3] National Institute of Standards & Technology

Array

Operations

- `get`
- `set`
- `indexOf`



Array

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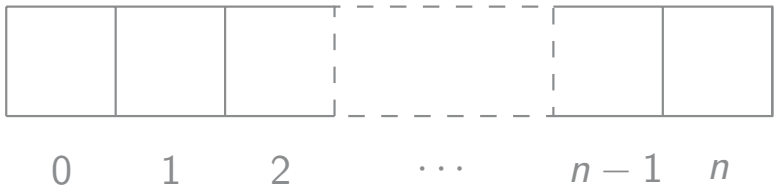

`get(1)`

Array

Operations

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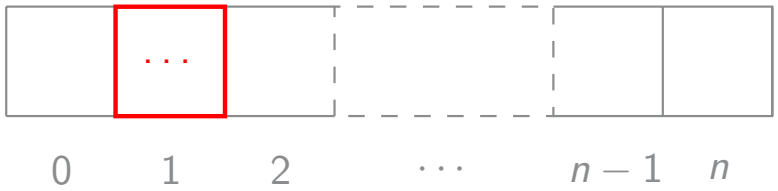
- `set`
- `indexOf`

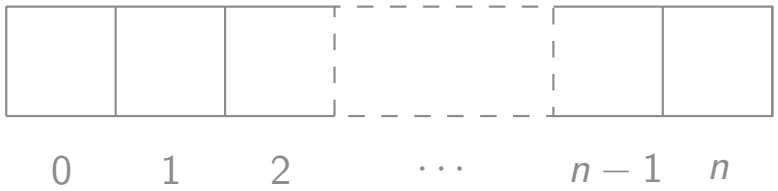


`get(1)`

Array

Operations

- `get` $O(1)$
- `set`
- `indexOf`



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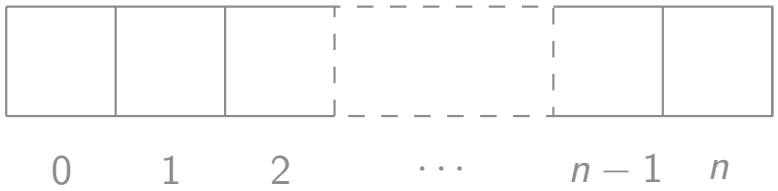

`set(2)`

Array

Operations

- `get` $O(1)$
- `set`
- `indexOf`

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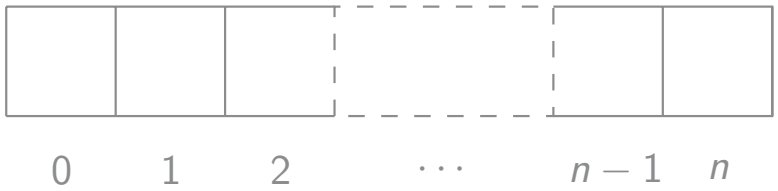

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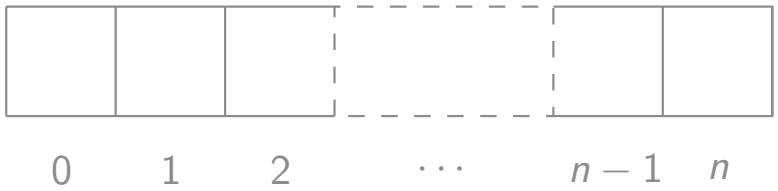
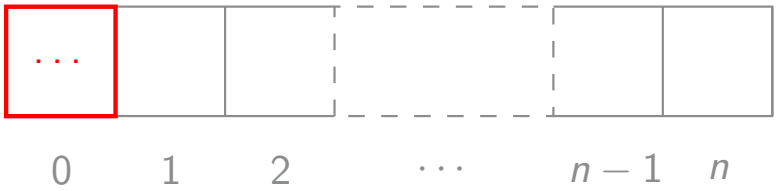


`indexOf(object)`

Array

Operations

- `get` $O(1)$
- `set` $O(1)$
- `indexOf`



`indexOf(object)`

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Operations

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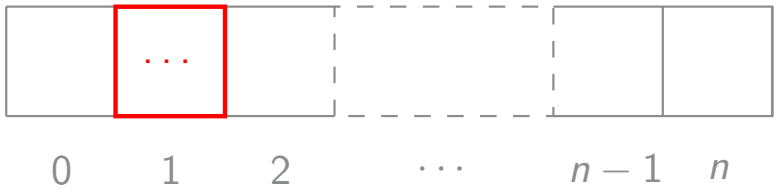

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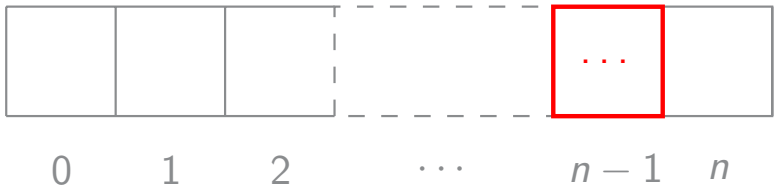

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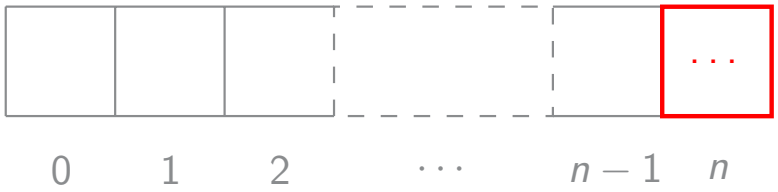

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Operations

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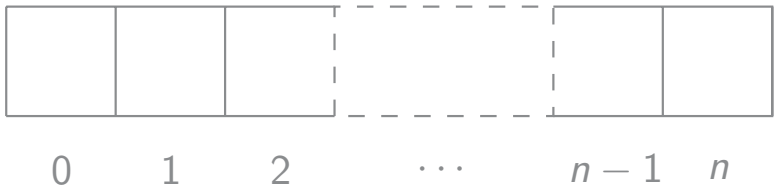
- `indexOf` $O(n)$



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Linked List

Definition

A linked list is a data structure in which the objects are arranged in a linear order. Unlike arrays in which the linear order is determined by indices, the order is determined by a pointer in each object.[4]

- Different types: singly, doubly, multiply, circular, ...
- Example: doubly linked list

[4] Introduction to Algorithms By Cormen, Leierson, Rivest & Stein

Linked List

Operations

- `add/remove first/last`
- `get/insertAt`
- `indexOf`

Linked List

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- `add/remove first/last`
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`addFirst(`O_4`)`

Linked List

Operations

- `add/remove first/last`
- `get/insertAt`
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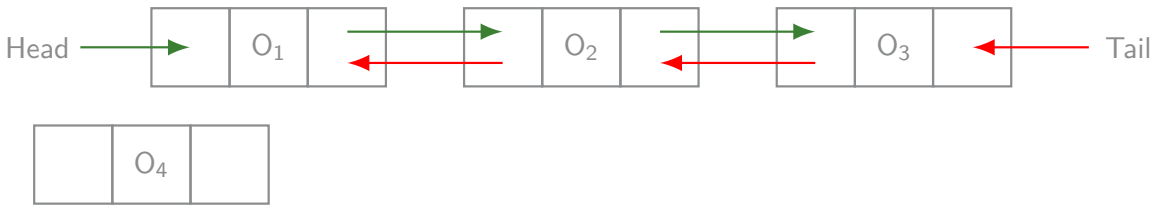

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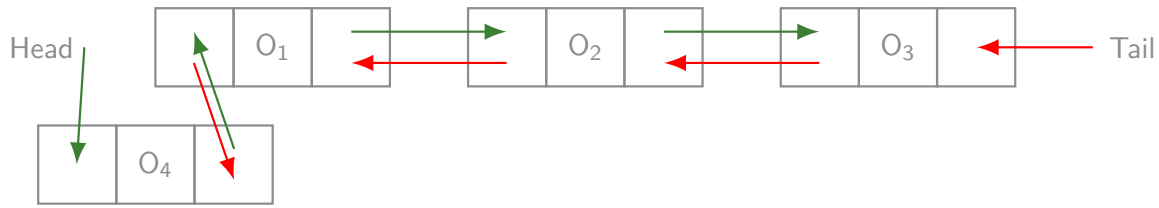

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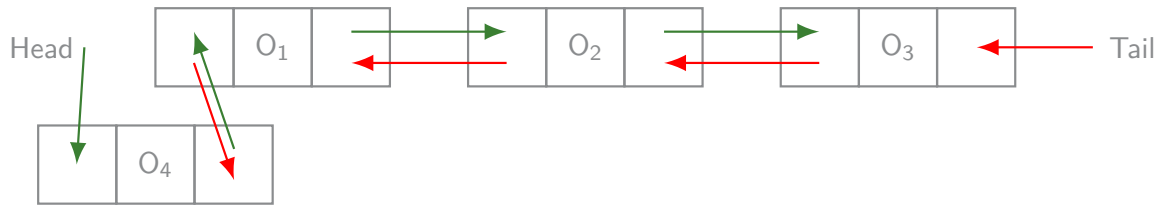

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Linked List

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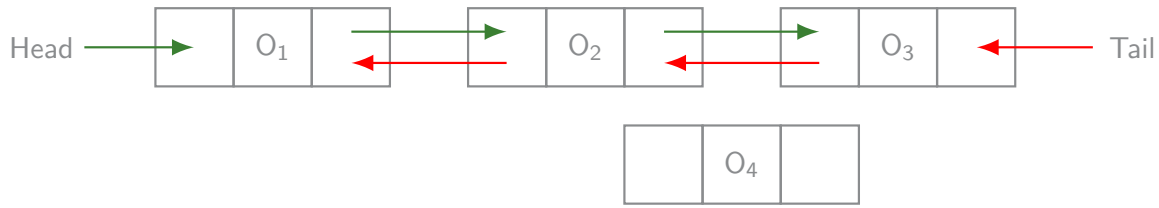
`insertAt(2)`

Linked List

Operations

- `add/remove first/last` $O(1)$
- `get/insertAt`
- `indexOf`



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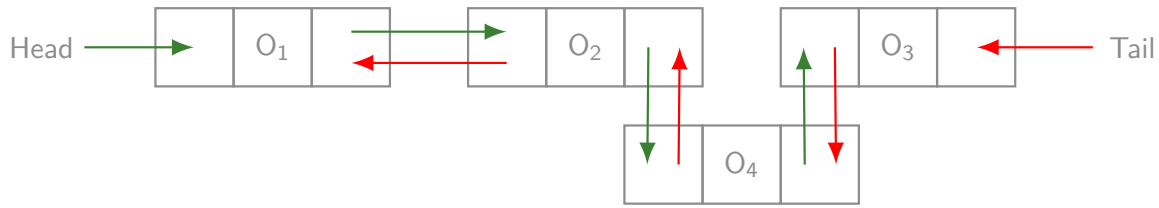

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Linked List

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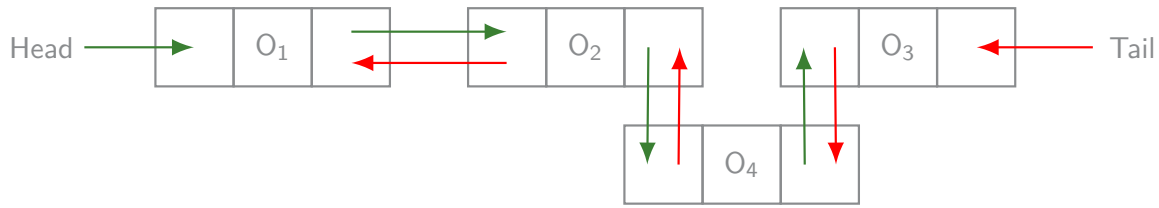

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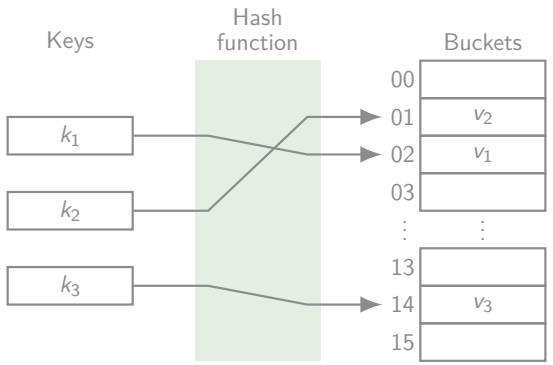
Hash Table

Definition

A dictionary in which keys are mapped to array positions by hash functions.[5]

- Hash functions: determinism, uniformity, defined range, data normalisation, non-invertible, perfect, ...
- Collisions resolution: chaining, open addressing, ...
- Example:

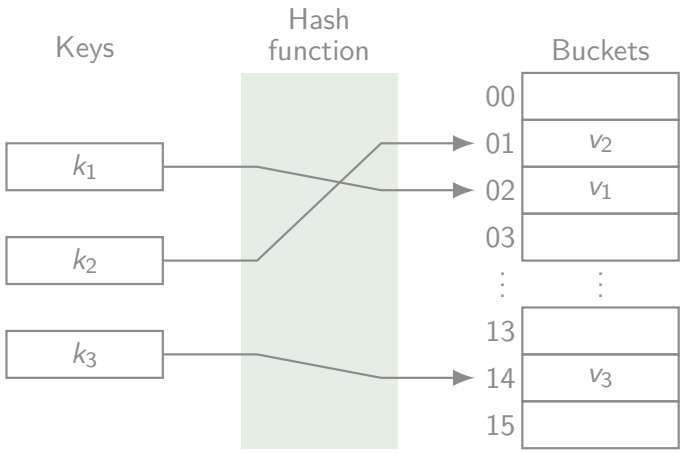


[5] National Institute of Standards & Technology

Hash Table

Operations

- `put`
- `remove`
- `get`



Hash Table

Operations

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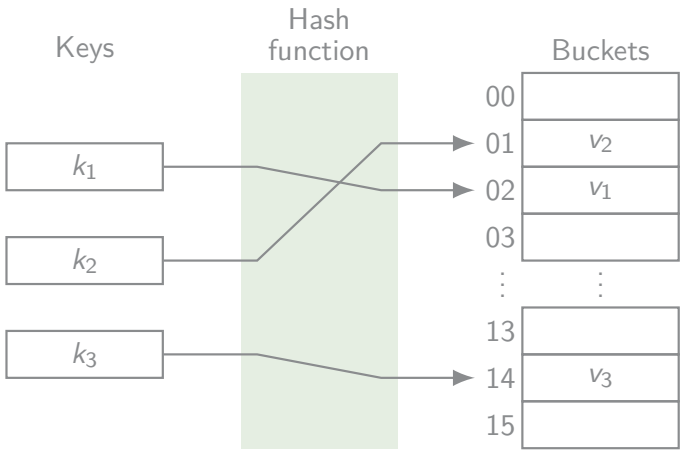
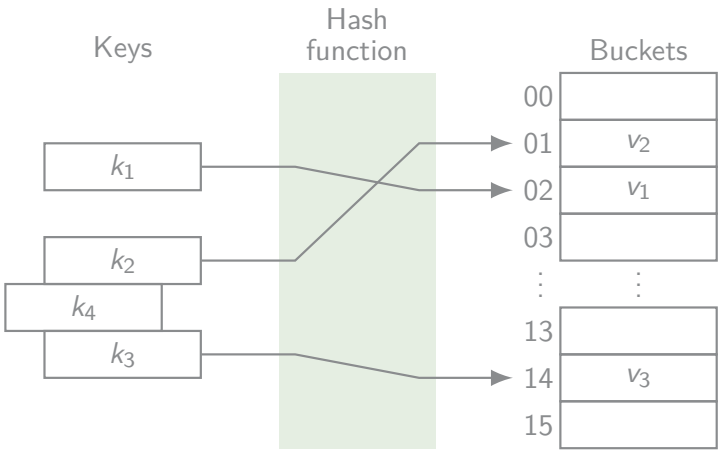


`put(`O_4`)`

Hash Table

Operations

- `put`
- `remove`
- `get`



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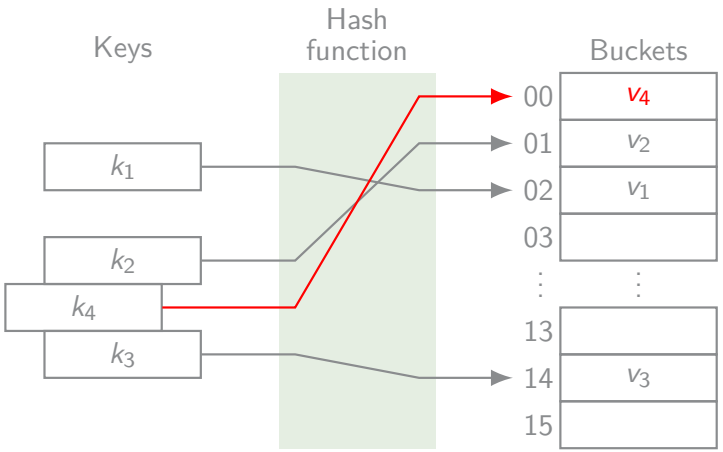
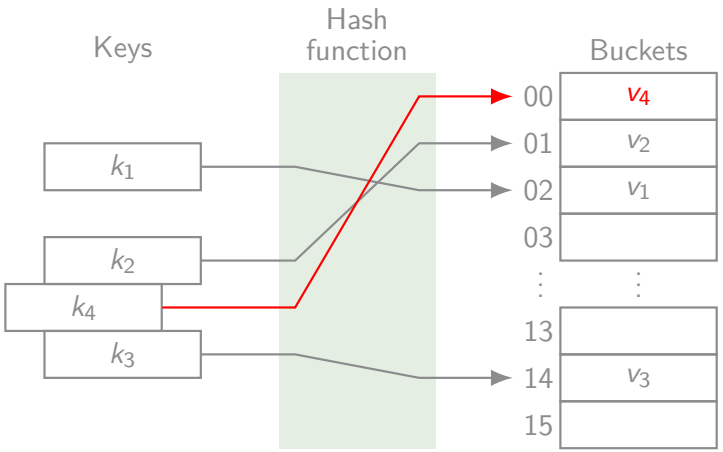


`put(O4)`

Hash Table

Operations

- `put` $O(1)$ / $O(n)$
- `remove`
- `get`



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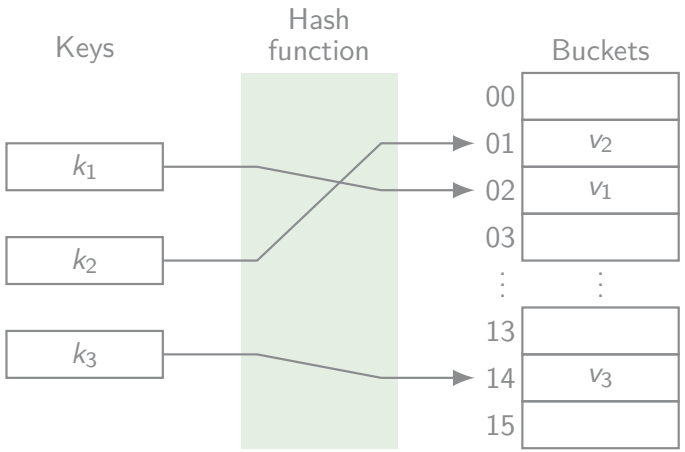
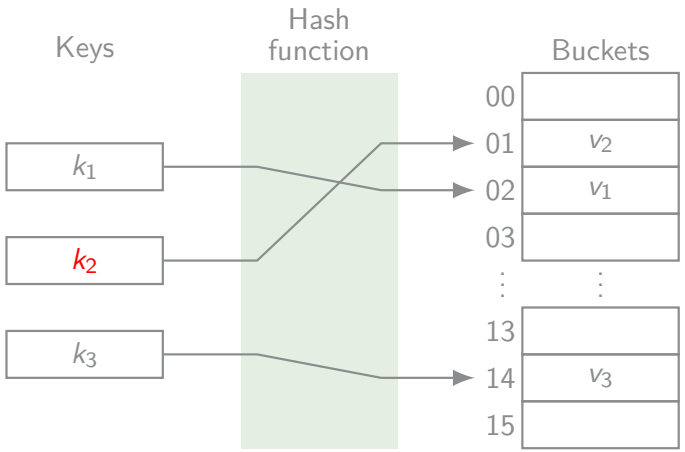


`remove(`O_2`)`

Hash Table

Operations

- `put` $O(1)$ / $O(n)$
- `remove`
- `get`



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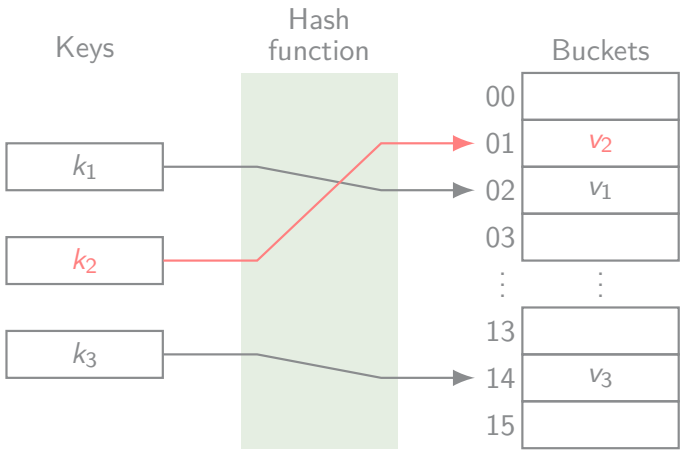

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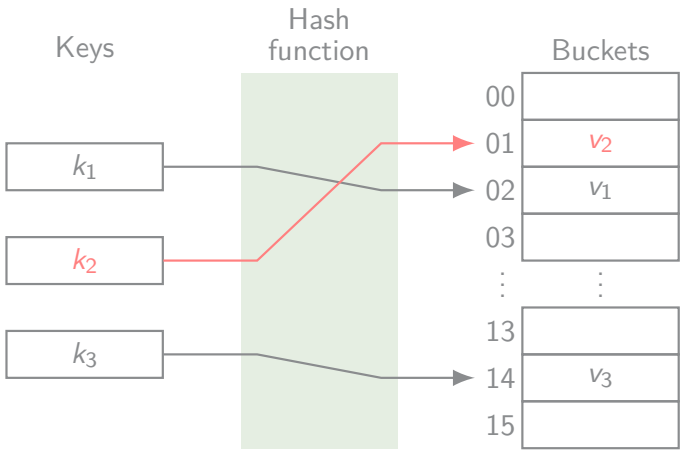

`remove(`0_2`)`

Hash Table

Operations

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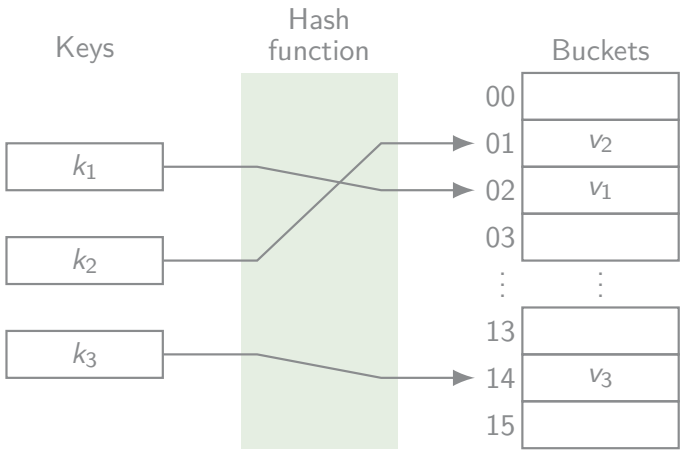
- `get`



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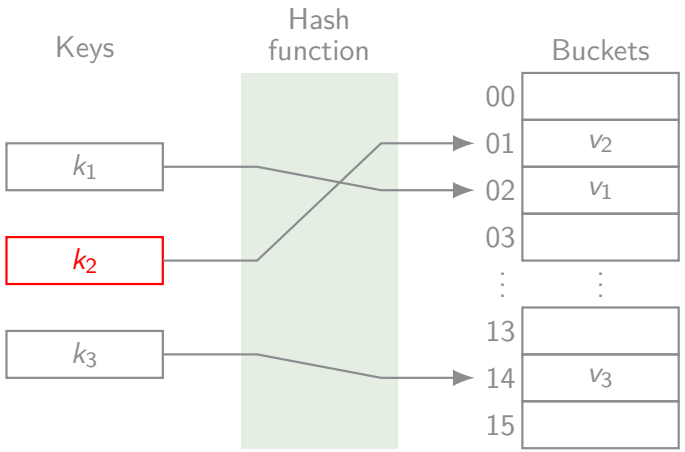

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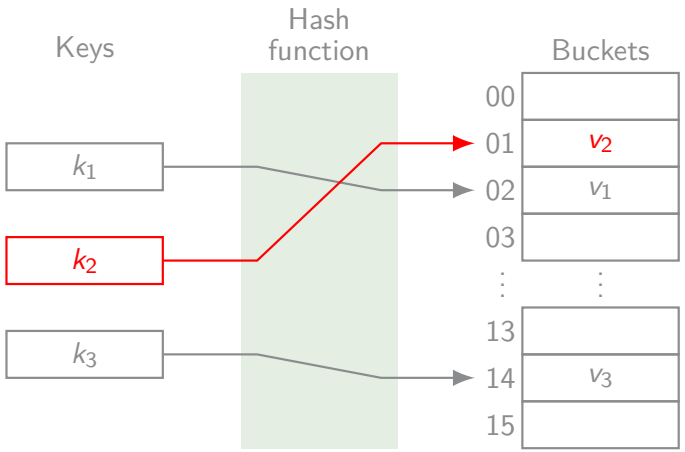

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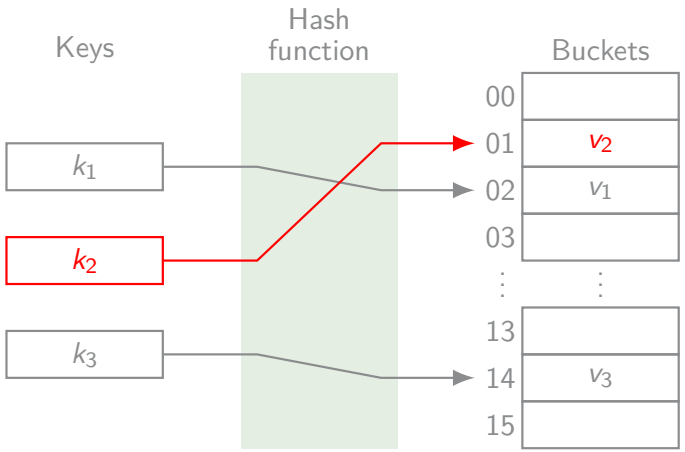

`get`(O_2)

Hash Table

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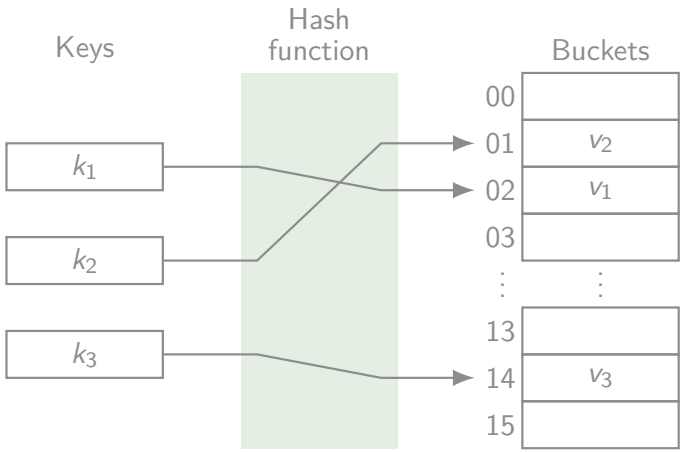
- `get` $O(1)$ / $O(n)$



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   - Tree
     - Heap
     - Red-Black Tree
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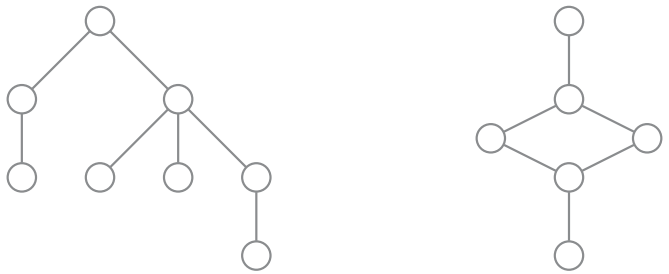
Tree

Definition

A data structure made up of nodes or vertices and edges without having any cycle. A tree that is not empty consists of a root node and potentially many levels of additional nodes that form a hierarchy.

- Depth, binary, (nearly) complete, ...
- Example:



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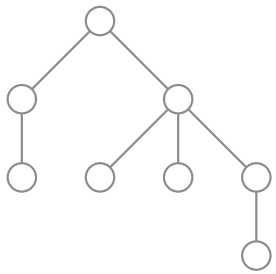
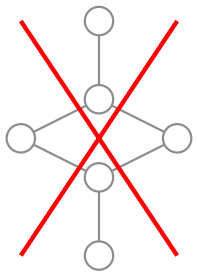




Binary Heap

Definition (Heap)

A complete tree where every node has a key more extreme (greater or less) than or equal to the key of its parent.[6]

Definition (Binary Heap)

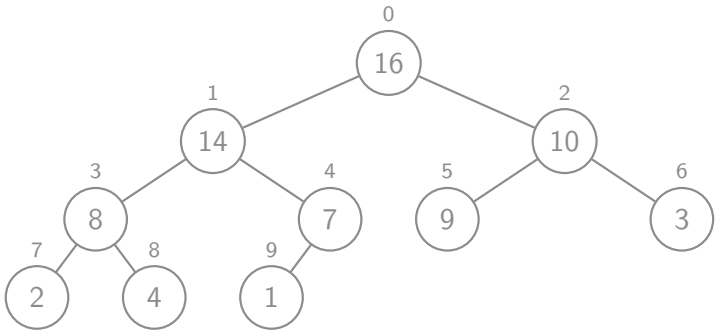
A binary heap data structure is an array object that we can view as a nearly complete binary tree that satisfies the min-heap or max-heap property.[7]

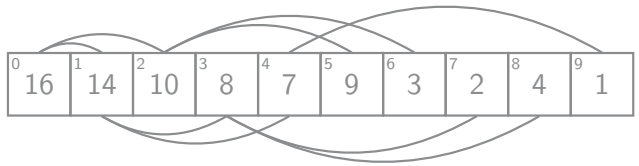
[6] National Institute of Standards & Technology

[7] Introduction to Algorithms By Cormen, Leierson, Rivest & Stein

Binary Max-Heap

- `Parent(n)` $\lfloor \frac{n-1}{2} \rfloor$
- `Left(n)` $2n+1$
- `Right(n)` $2(n+1)$





Red-Black Tree

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Red-Black Tree

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Outline

1. Introductory Data Structures
   - Array
   - Linked List
   - Hash Table
   - Tree
2. Java Collection API & Map API
   - Java Collection API
   - Java Map API
3. Advanced Data Structures
   - Stuff...

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Java Collection API

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Java Map API

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