

Assignment 3

$$\boxed{1)} \quad h_1 = w_x x_1 + w_h h_0 = 0.1 \times 10 + 1 \times 1 \\ = 2$$

$$h_2 = w_h h_1 + w_x x_2 = 1 \times 2 + 0.1 \times 10 \\ = 3$$

$$\hat{y}_2 = w_y h_2 = 2 \times 3 = 6 \neq$$

2)  $L_t \Rightarrow$  For 2 outputs

$$\hat{y}_2 = 6$$

$$\hat{y}_1 = w_h h_1 = 2$$

$$L_t = \sum_{i=1}^2 (\hat{y}_i - y_i) = 1 + 9 = 10$$

$$3) \quad \frac{\partial L_t}{\partial h_1} = \frac{\partial L_1}{\partial h_1} + \frac{\partial L_2}{\partial h_1}$$

$$* \quad \frac{\partial L_1}{\partial h_1} = \frac{\partial L_1}{\partial y_1} * \frac{\partial y_1}{\partial h_1}$$

$$= 2(\hat{y}_1 - y_1) * w_y$$

$$= -6 * 2 = -12$$

$$* \quad \frac{\partial L_2}{\partial h_1} = \frac{\partial L_2}{\partial y_2} * \frac{\partial y_2}{\partial h_2} * \frac{\partial h_2}{\partial h_1}$$

$$= 2(\hat{y}_2 - y_2) * w_y * w_h$$

$$= 2 * 2 * 1 = 4$$

$$\therefore \frac{\partial L_t}{\partial h_1} = -8$$

$$4) \quad \frac{\partial L_t}{\partial w_h} = \frac{\partial L_1}{\partial w_h} + \frac{\partial L_2}{\partial w_h}$$

$$\times \frac{\partial L_1}{\partial w_h} = \frac{\partial L_1}{\partial y_1} \times \frac{\partial y_1}{\partial h_1} \times \frac{\partial h_1}{\partial w_h}$$

$$= 2(\hat{y}_1 - y_1) \times w_y \times h_0$$

$$= -6 \times 2 \times 1 = -12$$

$$\times \frac{\partial L_2}{\partial w_h} = \sum_{i=2}^0 \frac{\partial L_2}{\partial y_2} \times \frac{\partial y_2}{\partial h_2} \times \frac{\partial h_2}{\partial h_i} \times \frac{\partial h_i}{\partial w_h}$$

$$= 2(\hat{y}_2 - y_2) \times w_y \left[ \frac{\partial h_2}{\partial w_h} + \frac{\partial h_2}{\partial h_1} \times \frac{\partial h_1}{w_h} + \frac{\partial h_2}{\partial h_0} \right]$$

$$= 2(\hat{y}_2 - y_2) \times w_y [h_1 + w_h \times h_0]$$

$$= 2 \times 2 \times [2 + 1] = 8$$



$$\therefore \frac{\partial L_t}{\partial w_n} = -4$$

[2] \* to observe this, we must check the impact of the first input on the last output

$$\frac{\partial J_n}{\partial w} = \sum_{i=0}^n \frac{\partial J_n}{\partial y_n} * \frac{\partial y_n}{\partial h_n} * \left( \frac{\partial h_n}{\partial h_i} * \frac{\partial h_i}{\partial w} \right)$$

@  $i=0$  }  $\rightarrow$  First input

$$\frac{\partial h_n}{\partial h_0} = \frac{\partial h_n}{\partial h_{n-1}} * \frac{\partial h_{n-1}}{\partial h_{n-2}} * \dots * \frac{\partial h_1}{\partial h_0}$$

$$\text{and } \frac{\partial h_n}{\partial h_{n-1}} = w_{hh} * \tanh'(w_{hh} h_{n-1}, w_{xh} x_n)$$

\* where  $w_{hh}$  is probably sampled from unit

gaussian ( $< 1$ ), and derivative of  $\tanh \leq 1$

, so we keep multiplying small numbers

, so  $\frac{\partial h_n}{\partial h_0}$  becomes very small no., hence

$h_0$  has no impact on  $y_n$  (Vanishing gradients)  
(short memory)

[3] For long sequences, where vanishing gradients must be avoided, so we can keep track of long term info.

[4] Adv: using a training algorithm which is applied to sequence data, where RNN is used (since weights are shared for each time step, then errors are calculated and accumulated for each time step to update single



weight)

\* Disadv: high Computational Cost For  
Single parameter update

5) a) FeedForward NN will assume that  
prediction of each letter depends only  
on that letter, which isn't the case, since  
we have to learn from the whole sequence  
before predicting one letter

b) word embedding where each letter is  
encoded to hot vector

c) many to many (encoder-decoder) since  
we need to watch the whole sequence before  
output the first letter

e) \* choose similar length texts to be in the same patch

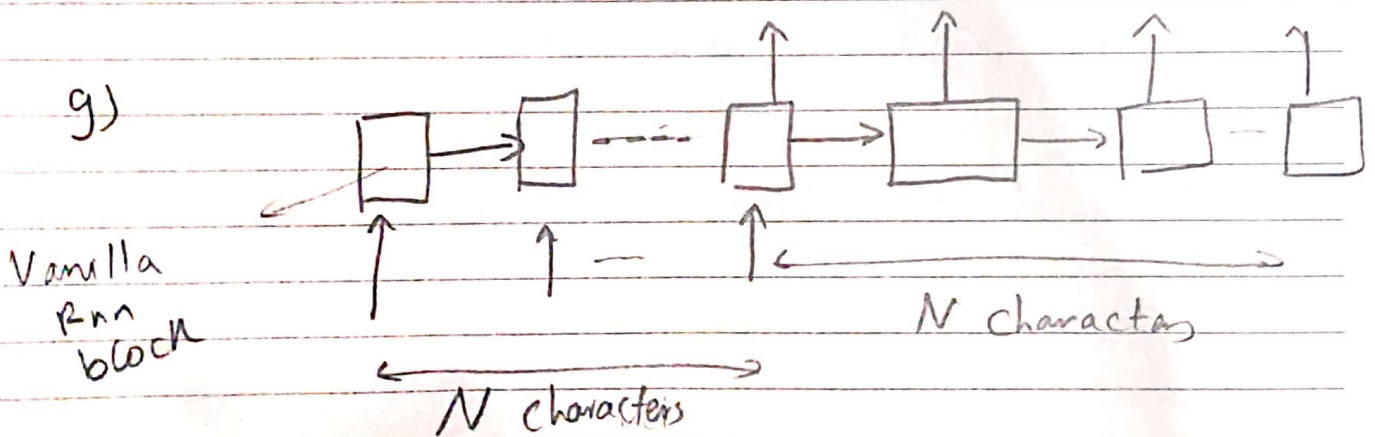
\* use padding

\* or choose patch size of 1

f) Convert each character into hot vector

\* divide training data into patches, same text lengths per patch

g)



\* encoder decoder arch

h. ~~to~~ decode the hot vector into characters  
the concatenate them