Introduction to Digital Systems Part III (Sequential Components) 2024/2025

Sequential Logic Fundamentals and Basic Circuits

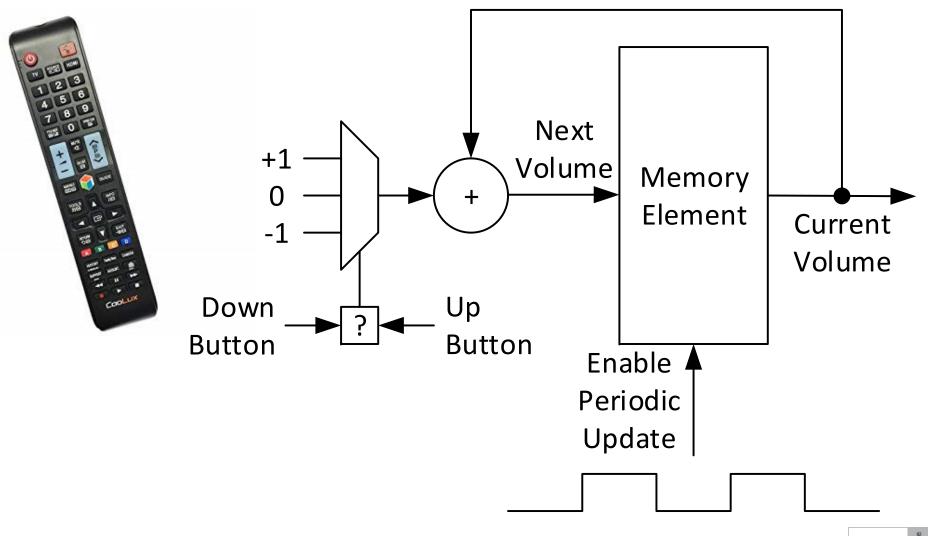


Lecture Contents

- Sequential logic circuits fundamentals
 - Motivation and concepts
- Sequential logic basic circuits (memory elements built with ordinary gates and feedback loops)
 - S-R Latch
 - D Latch
 - D Flip-flop

Figures and most content extracted from: John F. Wakerly, "Digital Design – Principles and Practices", 4 ed., Pearson – Prentice Hall, 2006 (chapter 7). Reading chapter 7 (4th ed.) or chapter 10 (5th ed.) is highly recommended.

Sequential Circuit Example

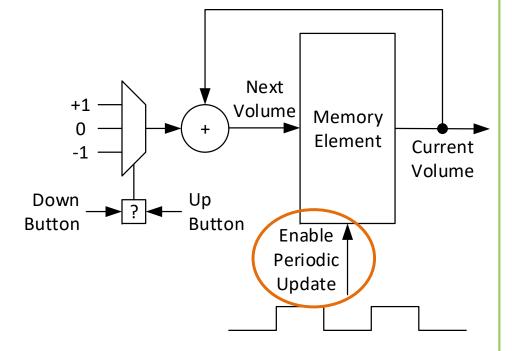


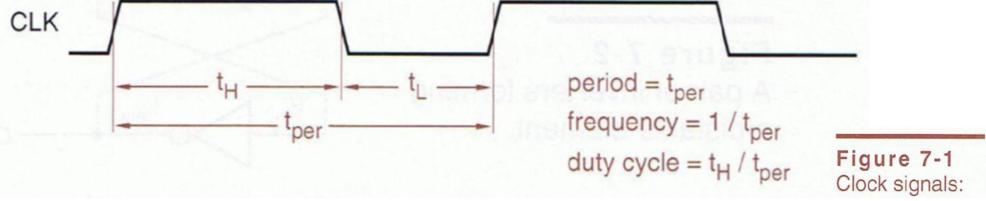
Introduction

- **Combinational** logic circuit
 - Is one whose outputs depend only on its current inputs
- Sequential logic circuit
 - Is one whose outputs depend <u>not</u> only on its current inputs, but also on the past sequence of inputs, possibly far back in time
- State of a sequential circuit
 - Is a collection of state variables whose values at any one time contain all the information about the past, necessary to account for the circuit's future behavior
- N-bit state variable: 2^N maximum number of states

Clock Signals

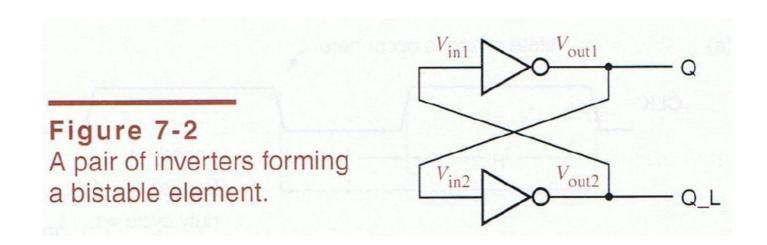
- State changes of most sequential circuits occur at times specified by a free-running clock signal
- Active high / active low clock signals





Bistable Element (Basic Structure)

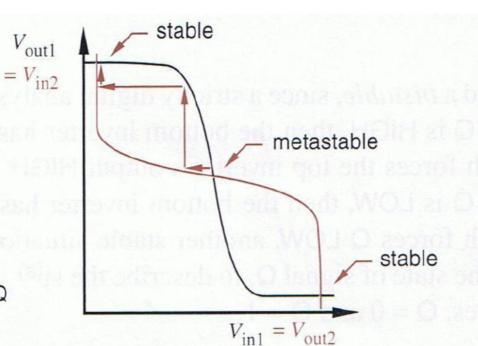
- No inputs and therefore no way of controlling or changing its state (random set at power up)
- Only illustrative but serves the basis for more complex and useful memory elements

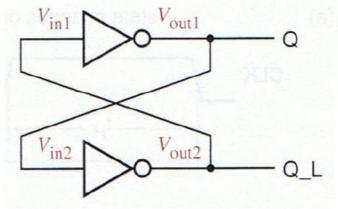


Bistable Element (Analog Analysis)

Figure 7-3

Transfer functions for inverters in a bistable feedback loop.





$$V_{\text{in1}} = V_{\text{out2}}$$

$$= T(V_{\text{in2}})$$

$$= T(V_{\text{out1}})$$

$$= T(T(V_{\text{in1}}))$$

Transfer function:

 $V_{\text{outl}} = T(V_{\text{inl}})$

 $V_{\text{out2}} = T(V_{\text{in2}})$

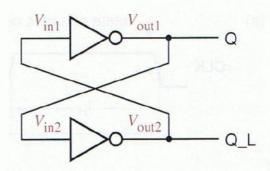
3 equilibrium points: 2 stable and 1 metastable

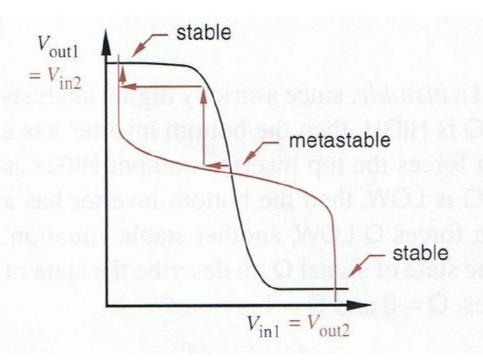


Metastability

Figure 7-3

Transfer functions for inverters in a bistable feedback loop.





Transfer function:

$$V_{\text{outl}} = T(V_{\text{in1}})$$

$$V_{\text{out2}} = T(V_{\text{in2}})$$

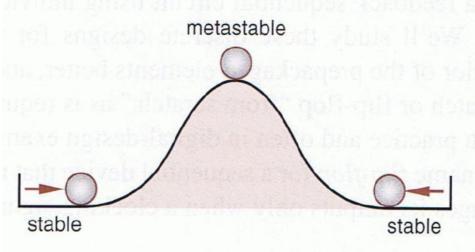


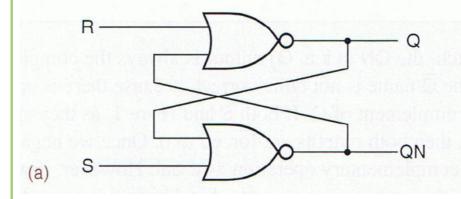
Figure 7-4

Ball and hill analogy for metastable behavior.

Effects of noise and circuit impairments on metastability



S-R Latch (Structure and Function Table)



S	R	Q	QN
0	0	last Q	last QN
0	1	0	1
1	0	1	0
1	1	0	0

Figure 7-5
S-R latch: (a) circuit design using NOR gates; (b) function table.

S-R Latch (Operation/Timing Diagrams)

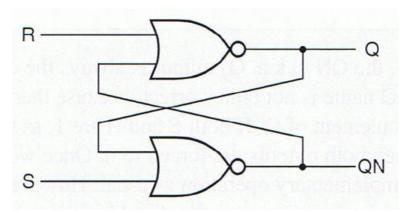
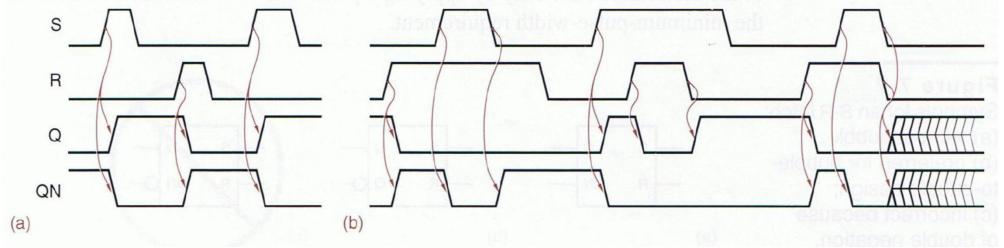
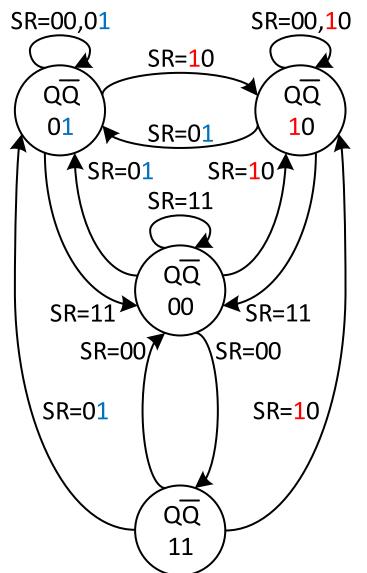


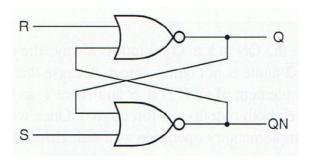
Figure 7-6 Typical operation of an S-R latch: (a) "normal" inputs; (b) S and R asserted simultaneously.



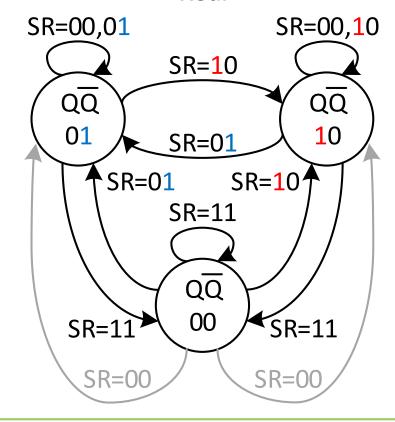
S-R Latch (State Diagram)

Theoretical



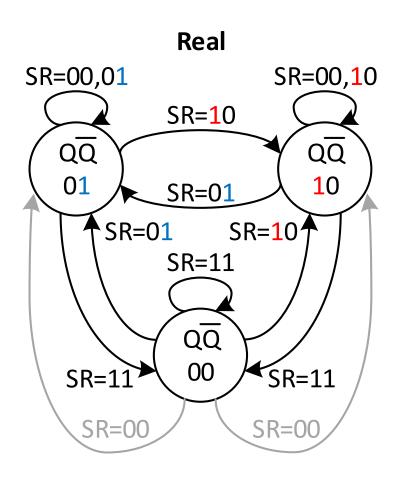


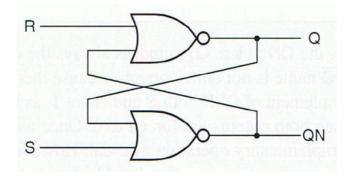
Real

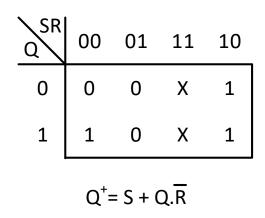




S-R Latch (Characteristic Equation)



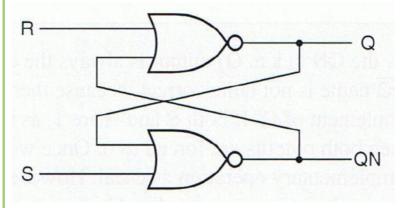




S-R Latch (Symbol)

Figure 7-7 Symbols for an S-R latch: (a) without bubble; (b) preferred for bubble-to-bubble design; (c) incorrect because of double negation. (a) (b) (c) (c) (d) (e) (e) (f) (f) (f) (f) (g) (g) (h) (h)

S-R Latch (Timing Parameters)



- t_{pLH} propagation time LOW-to-HIGH
- t_{pHL} propagation time HIGH-to-LOW
- T_{pw(min)} minimum pulse width

Non-determinism/metastability due to violation of $T_{pw(min)}$

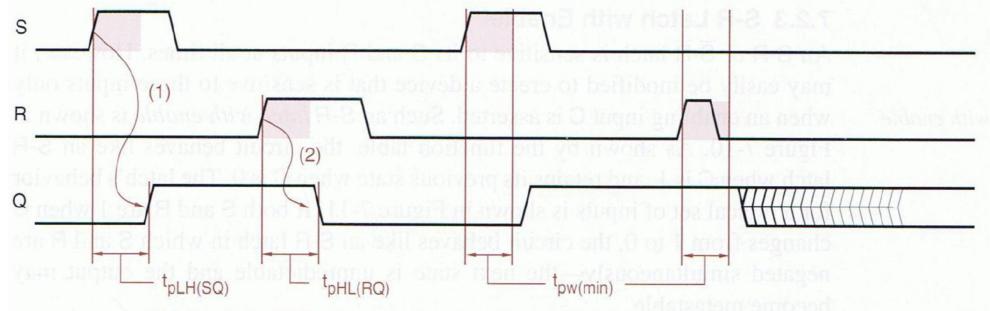
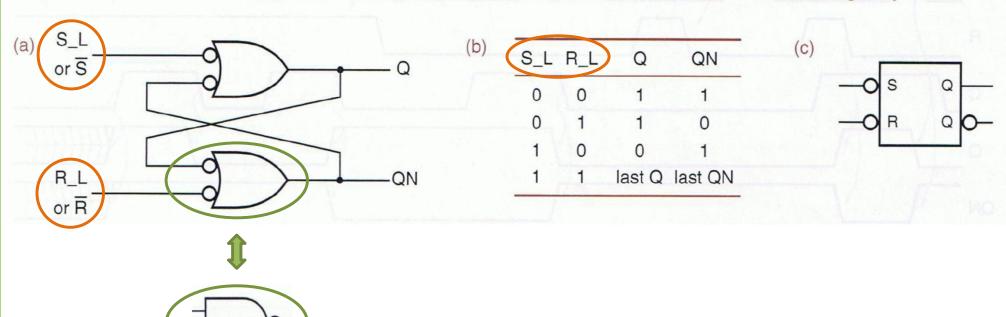


Figure 7-8 Timing parameters for an S-R latch.

S-R Latch (with NAND Gates)

Figure 7-9 S-R latch: (a) circuit design using NAND gates; (b) function table; (c) logic symbol.



S-R Latch with Enable (C)

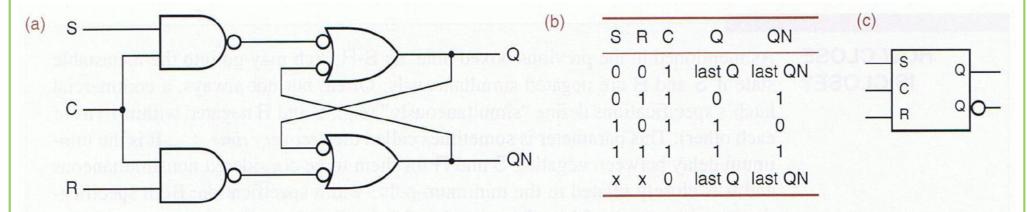


Figure 7-10 S-R latch with enable: (a) circuit using NAND gates; (b) function table; (c) logic symbol.

S-R Latch with Enable (Operation)

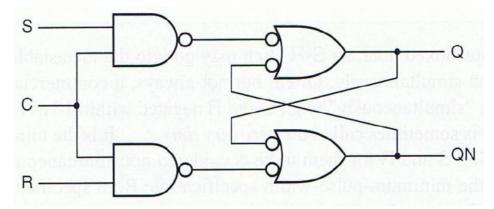
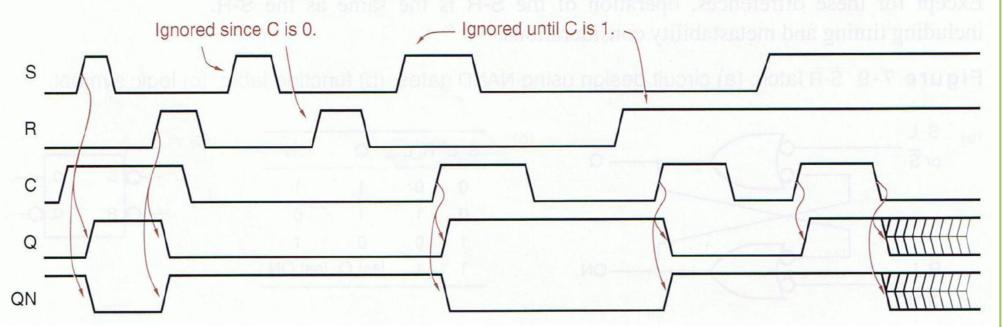


Figure 7-11 Typical operation of an S-R latch with enable.



D Latch (Structure and Operation)

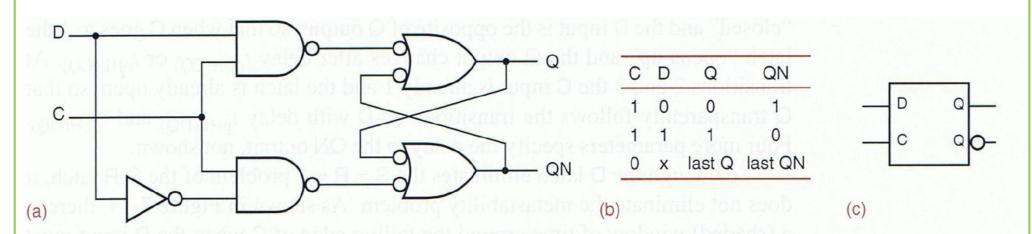


Figure 7-12 D latch: (a) circuit design using NAND gates; (b) function table; (c) logic symbol.

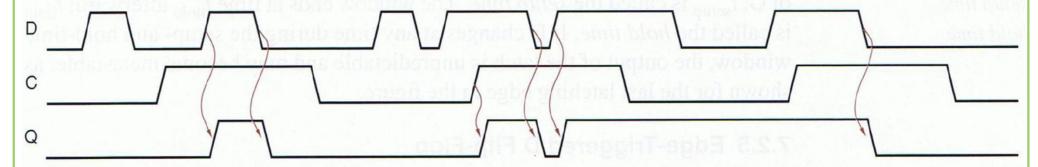
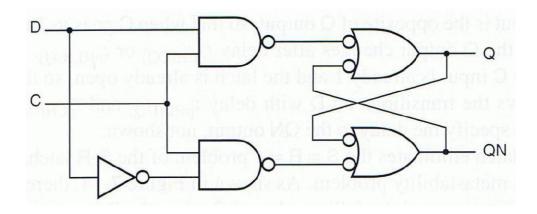
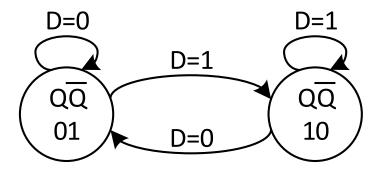


Figure 7-13 Functional behavior of a D latch for various inputs.

D Latch

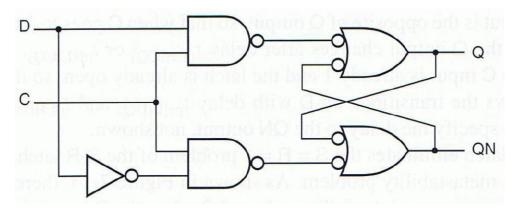
(State Diagram and Characteristic Equation)





Q	0	1			
0	0	1			
1	0	1			
$Q^{\dagger} = D$					

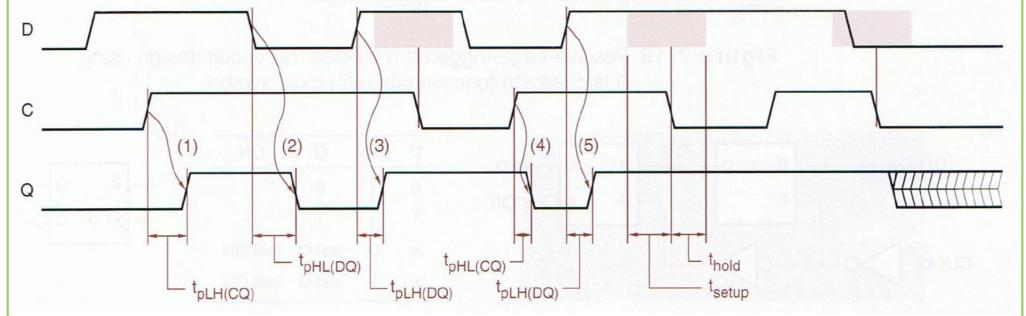
D Latch (Timing Parameters)



- t_{DLH} propagation time LOW-to-HIGH
- t_{pHL} propagation time HIGH-to-LOW
- t_{setup} setup time
- t_{hold} hold time

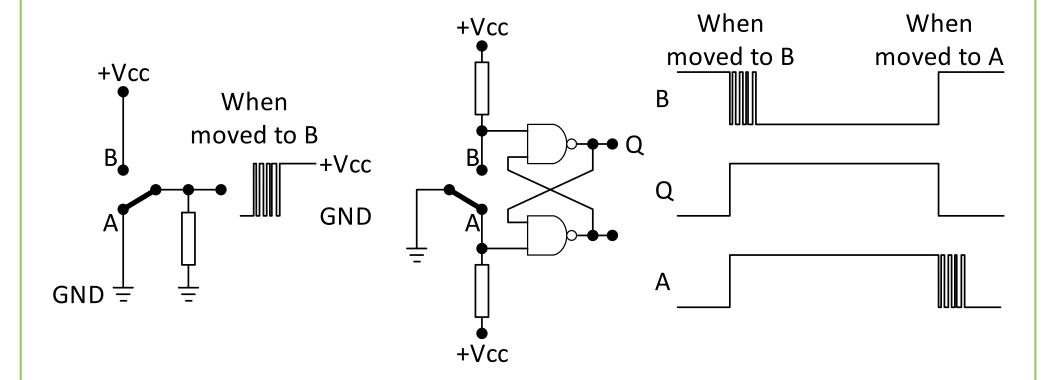
Non-determinism/metastability due to violation of t_{setup} and/or t_{hold}

Figure 7-14 Timing parameters for a D latch.

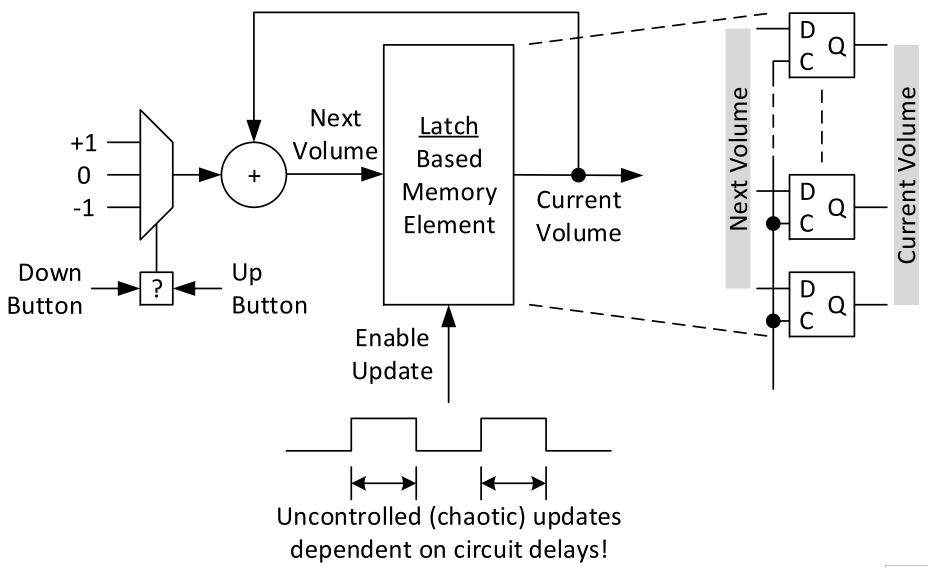


Application Example of an S-R Latch

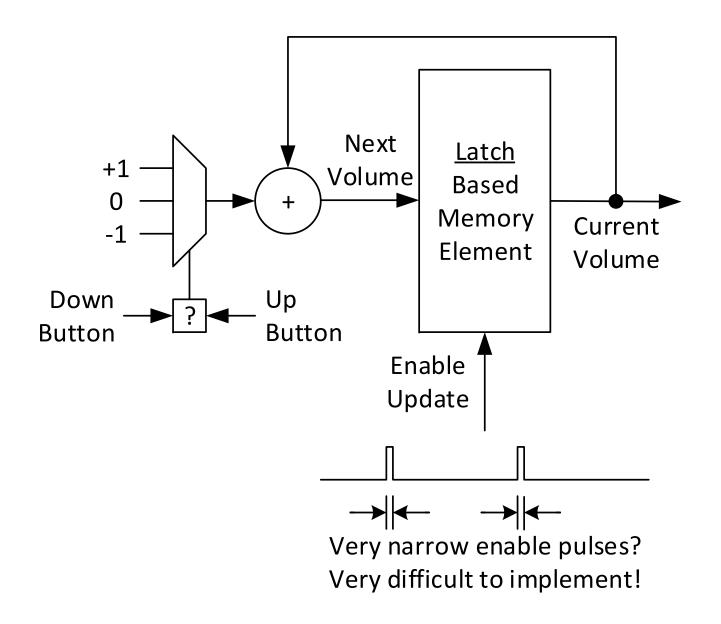
Debounce mechanical switches



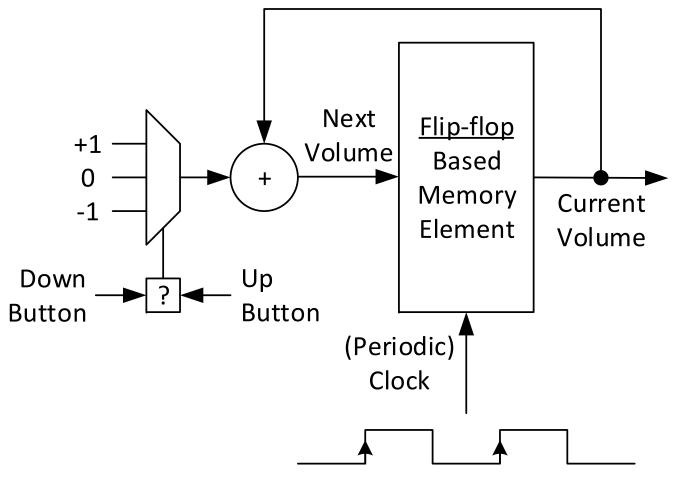
Latch Limitations/Issues



Possible Solution? Unfeasible!



A Feasible Solution

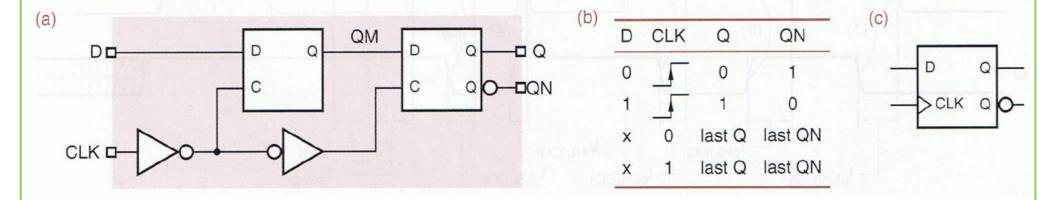


Periodic updates triggered by one of the edges (rising or falling) of a clock signal

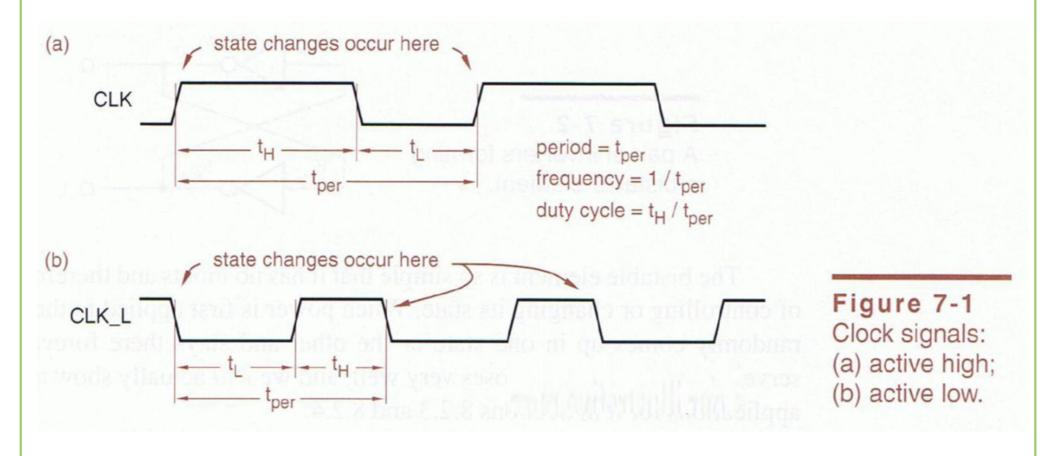
Positive-edge-triggered D Flip-flop

Latches are not used frequently but are a building block for flip-flops

Figure 7-15 Positive-edge-triggered D flip-flop: (a) circuit design using D latches; (b) function table; (c) logic symbol.



Clock Signals (revisited)



Positive-edge-triggered D Flip-flop (Functional Behavior / Operation)

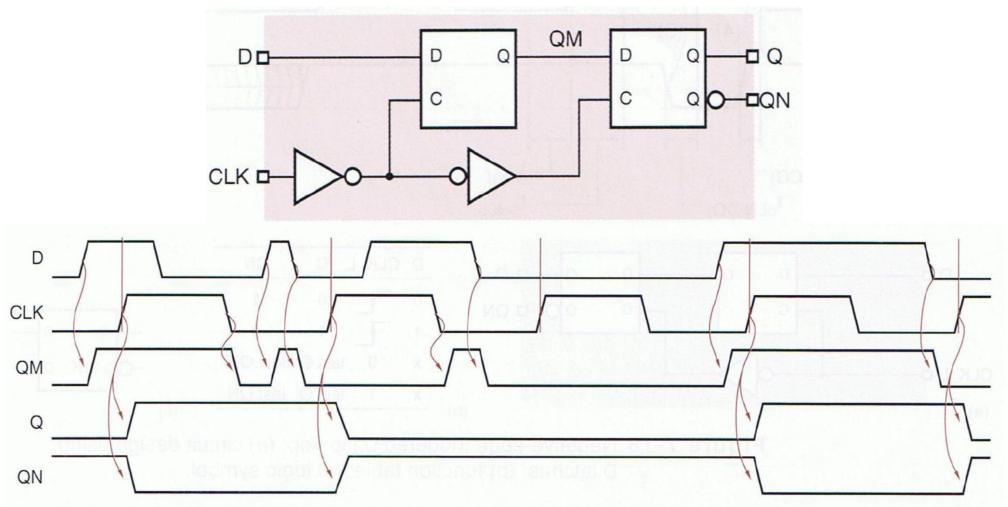
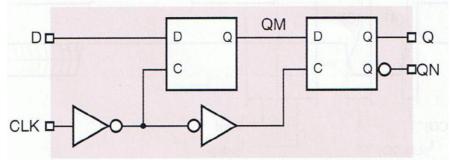


Figure 7-16 Functional behavior of a positive-edge-triggered D flip-flop.

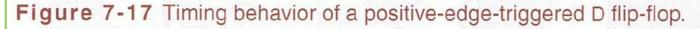


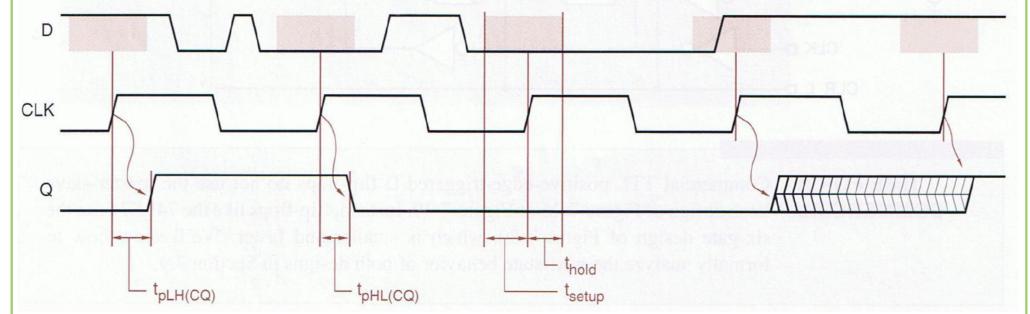
Positive-edge-triggered D Flip-flop (Timing Behavior)



- $\bullet \qquad t_{\text{pLH}} \text{propagation time LOW-to-HIGH} \\$
- t_{pHL} propagation time HIGH-to-LOW
- t_{setup} setup time
- t_{hold} hold time

Non-determinism/metastability due to violation of t_{setup} and/or t_{hold}





Negative-edge-triggered D Flip-flop

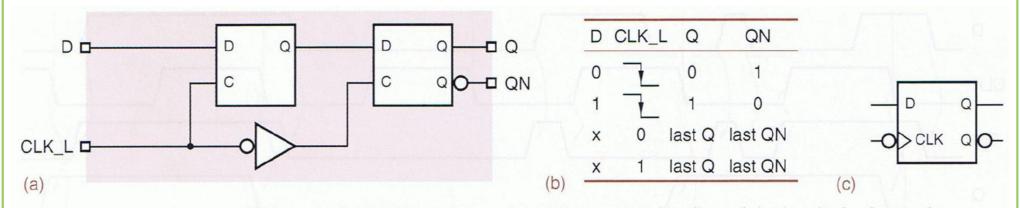
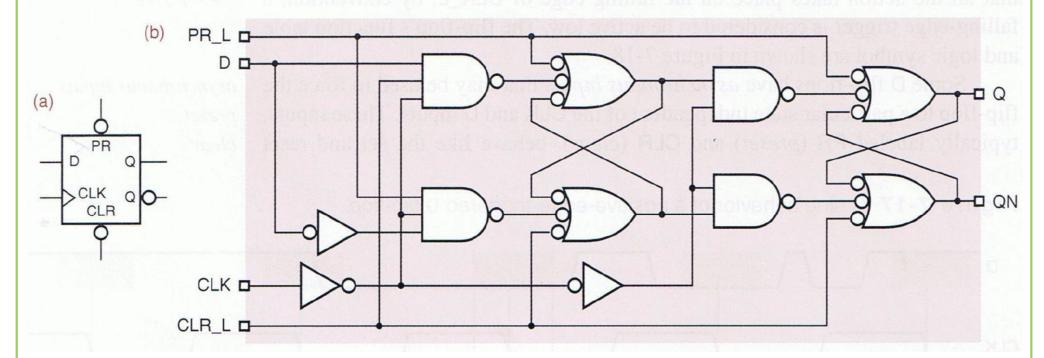


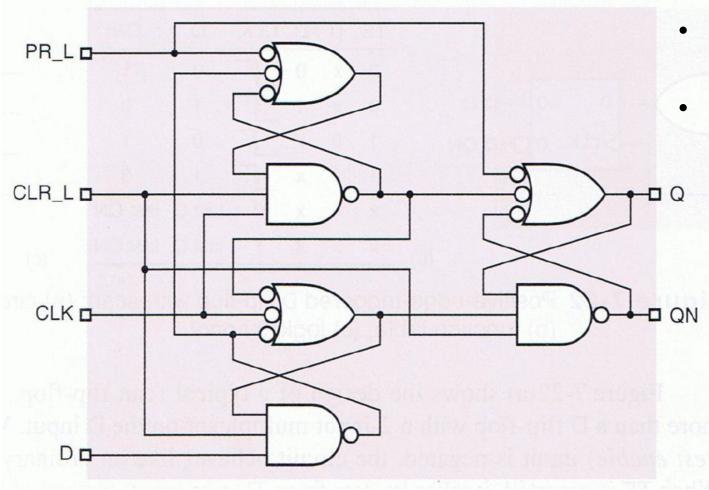
Figure 7-18 Negative-edge triggered D flip-flop: (a) circuit design using D latches; (b) function table; (c) logic symbol.

Positive-edge-triggered D Flip-flop with Preset and Clear

Figure 7-19 Positive-edge-triggered D flip-flop with preset and clear: (a) logic symbol; (b) circuit design using NAND gates.



Positive-edge-triggered D Flip-flop (7474 Commercial Integrated Circuit)

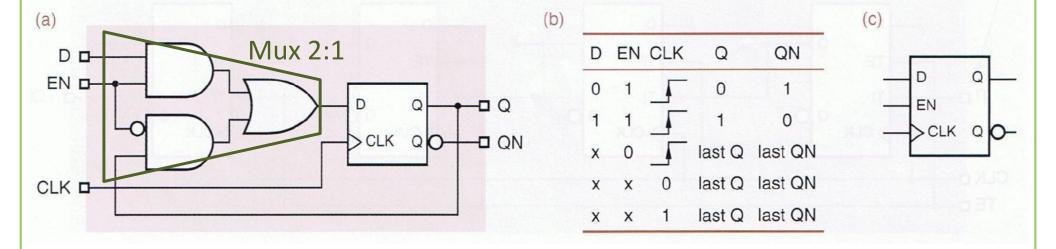


- 6 gates instead of 8 gates + inverters
- To be analyzed later...

Figure 7-20 Commercial circuit for a positive-edgetriggered D flip-flop such as 74LS74.

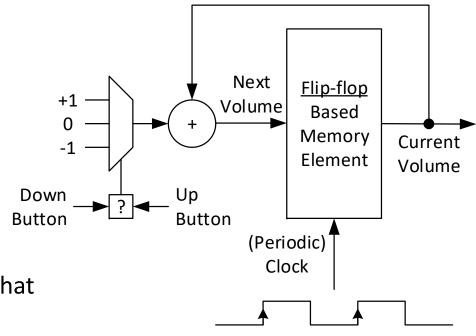
Positive-edge-triggered D Flip-flop with Enable

Figure 7-21 Positive-edge-triggered D flip-flop with enable: (a) circuit design; (b) function table; (c) logic symbol.



Exercise

- Design the complete logic diagram of the volume control system based on positive-edge-triggered D Flipflops with enable (assume 16 levels of volume).
- Component budget
 - Flip-flops
 - Adder
 - Mux 2:1
 - Logic gates
- From the usability point of view, what could be the clock frequency?
- How to force a predefined volume level (e.g. half scale) at power up?



Periodic updates triggered by one of the edges (rising or falling) of a clock signal

Conclusion

- At the end of this lecture and corresponding lab, it is fundamental to know and understand the structure, operation and timing behavior of basic sequential logic circuits (latches and flip-flops)
- Plan for the next lectures
 - Analysis of sequential circuits (Finite State Machines) and timing aspects
 - Synthesis of sequential circuits (Finite State Machines)
 - Standard sequential circuits
 - Registers and shift registers
 - Counters
 - Iterative vs. sequential circuits

Reading chapter 7 (4th ed.) or chapter 10 (5th ed.) of John F. Wakerly, "Digital Design – Principles and Practices", Pearson – Prentice Hall, is highly recommended.