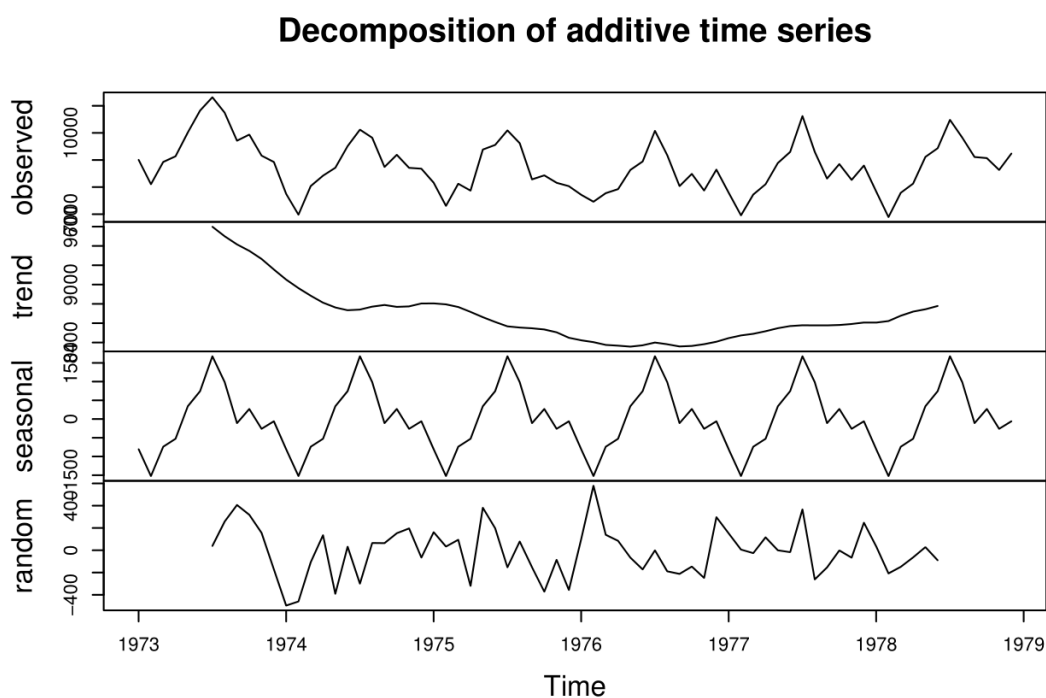


时间序列第一次作业

翁武泰 222018314210008

对 B6 的数据创建时间序列 `death_ts`，使用 `decompose` 函数对 `death_ts` 分解，得到如下图较为精准的结果，可与后面方法得到的结果做对比。

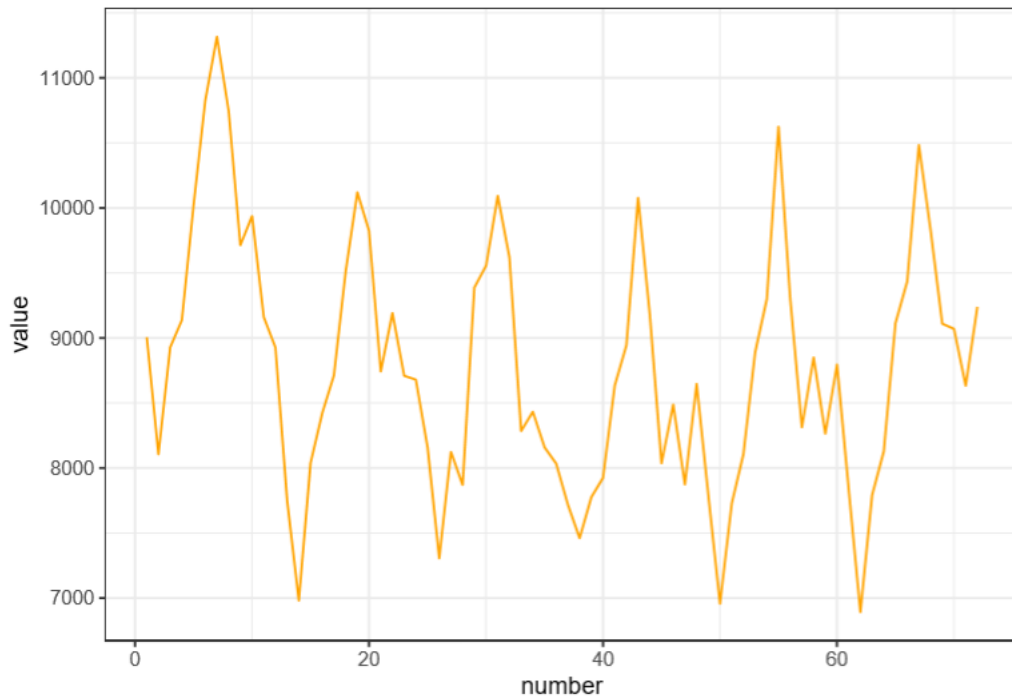
```
death_ts <- ts(death_data, frequency = 12, start = c(1973,1))
death_decomposition <- decompose(death_ts)
plot(death_decomposition)
```



转化数据格式，通过 `ggplot` 作图得到 1973 年至 1978 年美国在意外事故中的死亡人数数据图。通过观察发现周期 $T = 12$ ，即一年为一周期。

```
death_tibble <- as_tibble(death_data)
death_tibble <- death_tibble %>% mutate(number = c(1:72))
death_date_frame <- as.data.frame(death_tibble)
```

```
ggplot(death_tibble) +
  geom_line(aes(x = number, y = value), color = 'orange') +
  theme_bw()
```

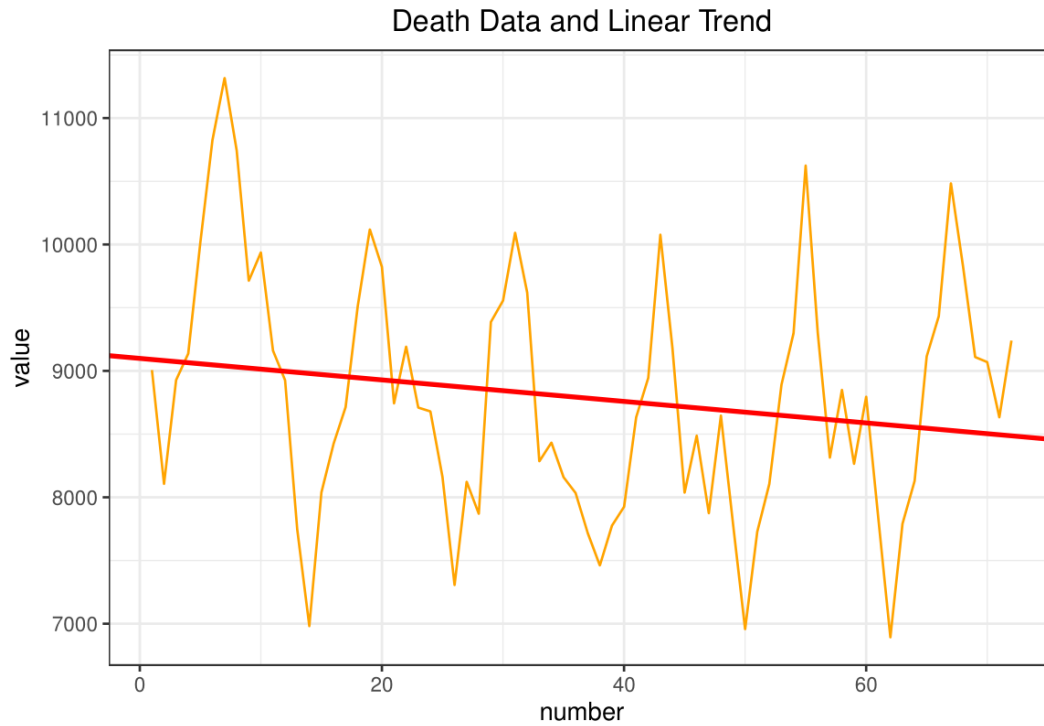


通过回归模型，对数据进行线性回归和二次回归，得到直线趋势项和二次趋势项如下图所示。其中橙线为数据，红线为趋势项。

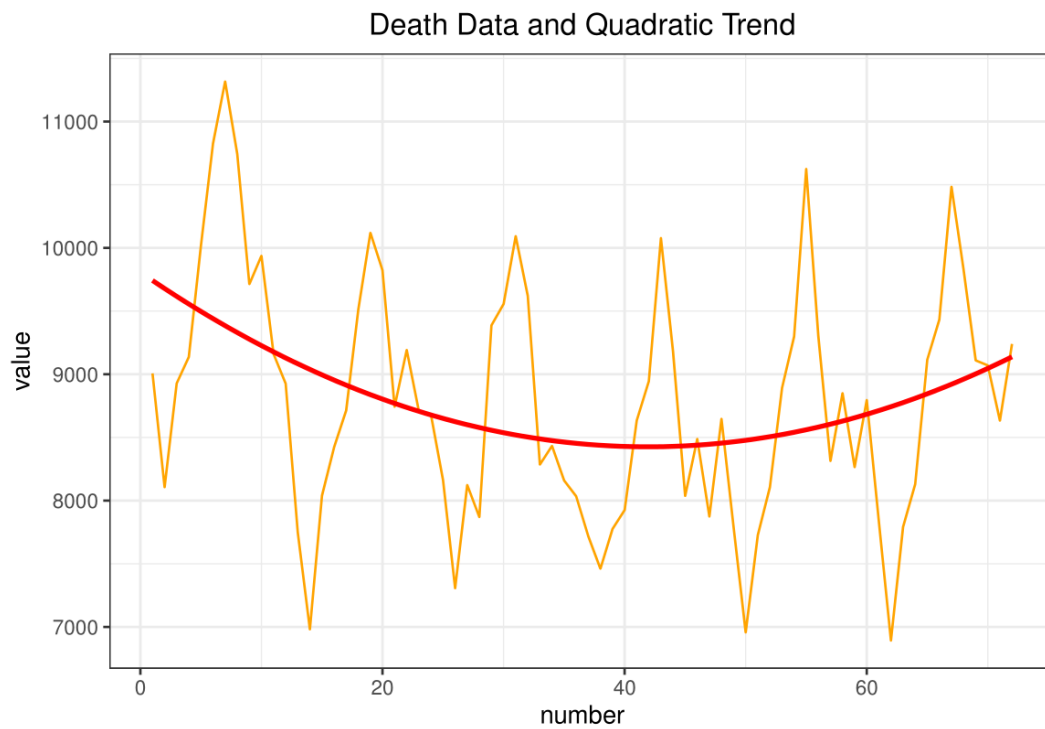
```
# linear function regression
model_linear <- lm(formula = value ~ number, data = death_date_frame)
coefficient_linear <- coefficients(model_linear)
coefficient_linear

# quadratic function regression
model_quadratic <- lm(formula = value ~ poly(number,2), data = death_date_frame)
coefficient_quadratic <- coefficients(model_quadratic)
coefficient_quadratic

ggplot(death_tibble) +
  geom_line(aes(x = number, y = value), color = 'orange') +
  geom_abline(slope = coefficient_linear[2],
              intercept = coefficient_linear[1],
              color = 'red', size = 1) +
  labs(title = 'Death Data and Linear Trend') +
  theme_bw() +
  theme(plot.title = element_text(hjust = 0.5))
```



```
# quadratic function plot
ggplot(death_tibble, aes(x = number, y = value)) +
  geom_line(color = 'orange') +
  geom_smooth(method = "lm", formula = y ~ poly(x, 2),
             color='red', size = 1, se = FALSE) +
  labs(title = 'Death Data and Quadratic Trend') +
  theme_bw() +
  theme(plot.title = element_text(hjust = 0.5))
```



用原始数据减去趋势项的估计，以第 k 月的平均值作为季节项 $S(k)$ 的估计，根据课本公式 (1.7) 计算出 \hat{S} ，再用原始数据减去趋势项数据的估计和季节项的估计得随机项的估计。其中 S_1, S_2 表示线性回归和二次回归后得到的季节项， T_1, T_2 和 R_1, R_2 同理。

| people | number | S1 | T1 | R1 | S2 | T2 | R2 |
|--------|--------|-------------|----------|------------|----------|------------|-------------|
| 9007 | 1 | -791.42567 | 9090.702 | 707.723616 | -3513748 | 9865.552 | 3512889.107 |
| 8106 | 2 | -1543.08312 | 9082.193 | 566.890282 | -3675389 | 16097.470 | 3667397.975 |
| 8928 | 3 | -754.40724 | 9073.684 | 608.723616 | -3840646 | 27484.377 | 3822089.510 |
| 9137 | 4 | -545.06470 | 9065.174 | 616.890282 | -4011637 | 44026.274 | 3976747.379 |
| 10017 | 5 | 324.77785 | 9056.665 | 635.556949 | -4187122 | 65723.162 | 4131415.747 |
| 10826 | 6 | 802.45373 | 9048.156 | 975.390282 | -4368154 | 92575.039 | 4286405.282 |
| 11317 | 7 | 1668.46294 | 9039.647 | 608.890282 | -4553953 | 124581.907 | 4440688.484 |
| 10744 | 8 | 973.30549 | 9031.138 | 739.556949 | -4746469 | 161743.765 | 4595468.852 |
| 9713 | 9 | -67.01863 | 9022.628 | 757.390282 | -4944484 | 204060.612 | 4750136.387 |
| 9938 | 10 | 236.32391 | 9014.119 | 687.556949 | -5146311 | 251532.450 | 4904716.256 |
| 9161 | 11 | -283.16688 | 9005.610 | 438.556949 | -5354115 | 304159.278 | 5059116.958 |
| 8927 | 12 | -21.15766 | 8997.101 | -48.943051 | -5566293 | 361941.096 | 5213279.159 |

```
for (i in 1 : 72) {
  death_tibble[i,3] <- death_tibble[i,1] -
    (coefficient_linear[2] * death_tibble[i,2]
     + coefficient_linear[1])
}

death_tibble <- rename(death_tibble, 'S_and_T' = 'value')

for (i in 0 : 11) {
  sum <- 0
  for (j in 1 : 72) {
    if (j %% 12 == i)
      sum <- sum + death_tibble[j,3]
  }
  sum <- sum / 6
  for (j in 1 : 72) {
    if (j %% 12 == i)
      death_tibble[j,4] <- sum
  }
}
```

```

death_tibble <- rename(death_tibble, 'S' = 'value')
death_tibble <- rename(death_tibble, 'qwe' = 'S_and_T')
death_tibble <- rename(death_tibble, 'S_and_T1' = 'S')
death_tibble <- rename(death_tibble, 'S1' = 'value')
death_tibble <- rename(death_tibble, 'people' = 'qwe')

for (i in 1 : 72) {
  death_tibble[i,5] <- coefficient_linear[2] * death_tibble[i,2]
  + coefficient_linear[1]
}

death_tibble <- rename(death_tibble, 'qwe' = 'number')
death_tibble <- rename(death_tibble, 'T1' = 'number')
death_tibble <- rename(death_tibble, 'number' = 'qwe')

for (i in 1 : 72) {
  death_tibble[i,6] <- death_tibble[i,1] - death_tibble[i,4]
  - death_tibble[i,5]
}

death_tibble <- rename(death_tibble, 'qwe' = 'people')
death_tibble <- rename(death_tibble, 'R1' = 'people')
death_tibble <- rename(death_tibble, 'people' = 'qwe')

death_tibble <- death_tibble[-3]

for (i in 1 : 72) {
  death_tibble[i,6] <- death_tibble[i,1]
  - (coefficient_quadratic[3] * death_tibble[i,2]^2
  + coefficient_quadratic[2] * death_tibble[i,2]
  + coefficient_quadratic[1])
}

death_tibble <- rename(death_tibble, 'qwe' = 'people')
death_tibble <- rename(death_tibble, 'S_and_T2' = 'people')
death_tibble <- rename(death_tibble, 'people' = 'qwe')

for (i in 0 : 11) {
  sum <- 0
  for (j in 1 :72) {
    if (j %% 12 == i)
      sum <- sum + death_tibble[j,6]
  }
  sum <- sum / 6
  for (j in 1 :72) {
    if (j %% 12 == i)
      death_tibble[j,7] <- sum
  }
}

```

```

death_tibble <- rename(death_tibble, 'qwe' = 'S_and_T2')
death_tibble <- rename(death_tibble, 'S2' = 'S_and_T2')
death_tibble <- rename(death_tibble, 'S_and_T2' = 'qwe')

for (i in 1 : 72) {
  death_tibble[i,8] <- coefficient_quadratic[3] *
    death_tibble[i,2]^2
  + coefficient_quadratic[2] * death_tibble[i,2]
  + coefficient_quadratic[1]
}

death_tibble <- rename(death_tibble, 'qwe' = 'number')
death_tibble <- rename(death_tibble, 'T2' = 'number')
death_tibble <- rename(death_tibble, 'number' = 'qwe')

for (i in 1 : 72) {
  death_tibble[i,9] <- death_tibble[i,1] - death_tibble[i,7]
  - death_tibble[i,8]
}

death_tibble <- rename(death_tibble, 'qwe' = 'people')
death_tibble <- rename(death_tibble, 'R2' = 'people')
death_tibble <- rename(death_tibble, 'people' = 'qwe')

death_tibble <- death_tibble[-6]

death_tibble

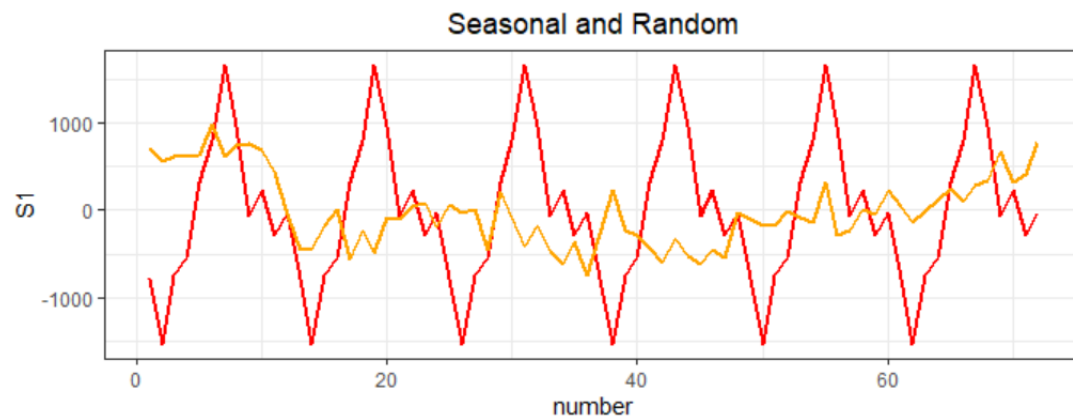
```

绘制季节项和随机项如下图所示。其中红色为季节项，橙色为随机项。

```

ggplot(death_tibble) +
  geom_line(aes(x = number, y = S1), color = 'red', size = 1) +
  geom_line(aes(x = number, y = R1), color = 'orange', size = 1) +
  labs(title = 'Seasonal and Random') +
  theme_bw() +
  theme(plot.title = element_text(hjust = 0.5))

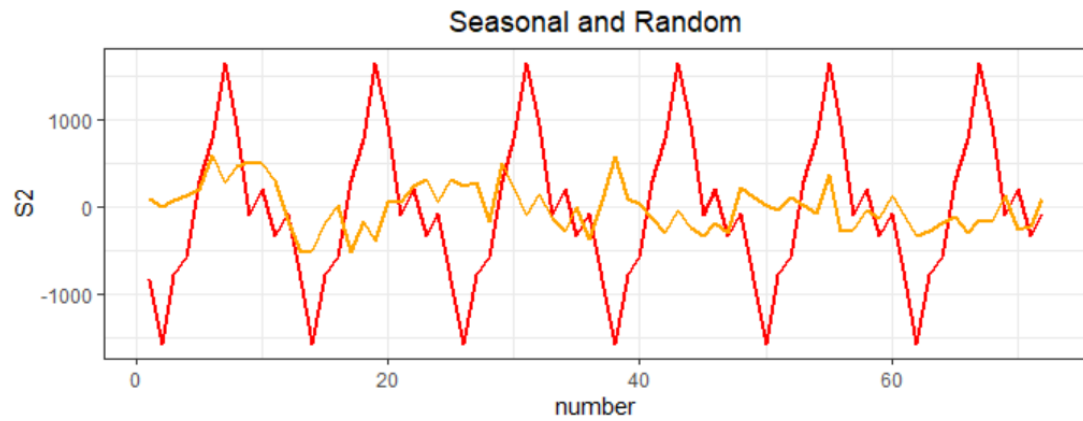
```



```

ggplot(death_tibble) +
  geom_line(aes(x = number, y = S2), color = 'red', size = 1) +
  geom_line(aes(x = number, y = R2), color = 'orange', size = 1) +
  labs(title = 'Seasonal and Random') +
  theme_bw() +
  theme(plot.title = element_text(hjust = 0.5))

```



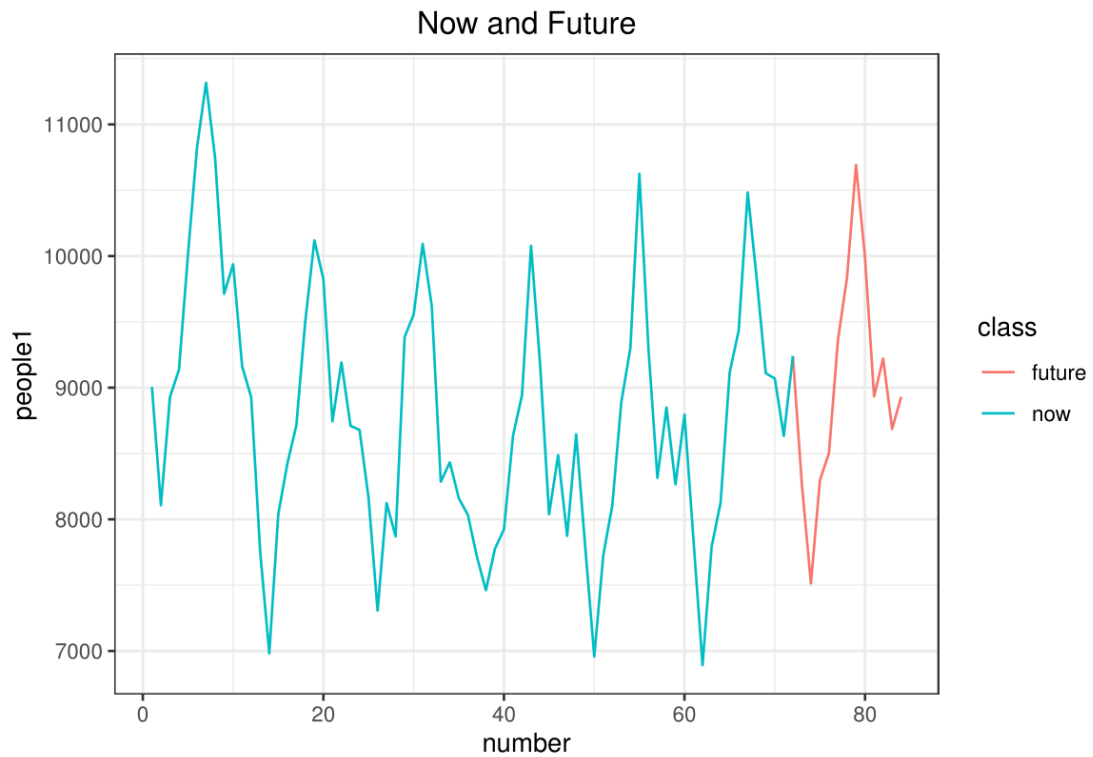
根据公式（1.9）预测，得到结果并绘制图片如下所示。

```
for (i in 1 : 12) {
  f_tibble[i,2] <- death_tibble[i,6]
  + coefficient_linear[2] * death_tibble[i,2]
  + coefficient_linear[1]
  f_tibble[i,3] <- death_tibble[i,3]
  + coefficient_quadratic[3] * f_tibble[i,1]^2
  + coefficient_quadratic[2] * f_tibble[i,1]
  + coefficient_quadratic[1]
}

f_tibble <- rename(f_tibble, 'F1' = 'S2')
f_tibble <- rename(f_tibble, 'F2' = 'S1')
```

| month | 1979 | 1979 |
|-------|----------|----------|
| 1 | 8265.502 | 8468.374 |
| 2 | 7512.326 | 7768.417 |
| 3 | 8297.884 | 8610.393 |
| 4 | 8502.508 | 8874.635 |
| 5 | 9366.032 | 9800.978 |
| 6 | 9835.789 | 10336.75 |
| 7 | 10692.28 | 11262.46 |
| 8 | 9986.004 | 10628.61 |
| 9 | 8932.962 | 9651.181 |
| 10 | 9221.986 | 10019.02 |
| 11 | 8686.577 | 9565.633 |
| 12 | 8931.067 | 9895.342 |

```
ggplot(f) +
  geom_line(aes(x = number, y = people1, color = type1)) +
  labs(
    title = 'Now and Future',
    color = 'class'
  ) +
  theme_bw() +
  theme(plot.title = element_text(hjust = 0.5))
```



```
ggplot(f) +
  geom_line(aes(x = number, y = people2, color = type2)) +
  labs(
    title = 'Now and Future',
    color = 'class'
  ) +
  theme_bw() +
  theme(plot.title = element_text(hjust = 0.5))
```

