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Final Answers MATH103 April 2011

December 6, 2014

How to use this resource

- When you feel reasonably confident, simulate a full exam and grade your solutions. For your grading you can get the full solutions here.
- If you're not quite ready to simulate a full exam, we suggest you thoroughly and slowly work through each problem. Use this document with the final answers only to check if your answer is correct, without spoiling the full solution.
- Should you need more help, check out the hints and video lecture on the Math Educational Resources.

Tips for Using Previous Exams to Study: Work through problems

Resist the temptation to read any of the final answers below before completing each question by yourself first! We recommend you follow the guide below.

- 1. How to use the final answer: The final answer is not a substitution for the full solution! The final answer alone will not give you full marks. The final answer is provided so that you can check the correctness of your work without spoiling the full solution.
 - To answer each question, only use what you could also use in the exam. Download the raw exam here.
 - If you found an answer, how could you verify that it is correct from your work only? E.g. check if the units make sense, etc. Only then compare with our result.
 - If your answer is correct: good job! Move on to the next question.
 - Otherwise, go back to your work and check it for improvements. Is there another approach you could try? If you still can't get to the right answer, you can check the full solution on the Math Educational Resources.
- 2. **Reflect on your work:** Generally, reflect on how you solved the problem. Don't just focus on the final answer, but whether your mental process was correct. If you were stuck at any point, what helped you to go forward? What made you confident that your answer was correct? What can you take away from this so that, next time, you can complete a similar question without any help?
- 3. **Plan further studying:** Once you feel confident enough with a particular topic, move on to topics that need more work. Focus on questions that you find challenging, not on those that are easy for you. Once you are ready to tackle a full exam, follow the advice for the full exam (click here).

Please note that all final answers were extracted automatically from the full solution. It is possible that the final answer shown here is not complete, or it may be missing entirely. In such a case, please notify mer-wiki@math.ubc.ca. Your feedback helps us improve.

This pdf was created for your convenience when you study Math and prepare for your final exams. All the content here, and much more, is freely available on the Math Educational Resources.

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Question 1 (a) Easiness: 77/100

Final answer. Then, we know that $\sum_{n=2}^{\infty} \frac{n}{1-n^3} = \sum_{n=2}^{\infty} \frac{n}{1-n^3}$ is absolutely convergent and hence convergent.

Question 1 (b) Easiness: 46/100

Final answer. $y = \frac{2}{b-a}$.

Question 1 (c) Easiness: 50/100

Final answer. $\overline{N} = 3.5$.

Question 2 (a) Easiness: 81/100

Final answer. $I_1 = -\frac{1}{2\pi}$.

Question 2 (b) Easiness: 79/100

Final Answer. $I_2 = \frac{1}{5}\cos^5 x - \frac{1}{3}\cos^3 x + C$

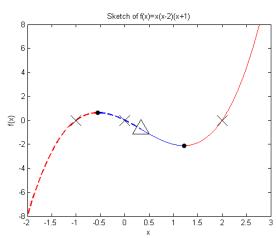
Question 2 (c) Easiness: 9/100

Final answer. y(0) = 1 and dy/dx = 1 = y-x.

Question 2 (d) Easiness: 4/100

Final answer. $C(n,k) = \frac{n!}{k!(n-k)!}$. (This is the number of ways to choose k objects among n total objects.)

Question 3 (a) Easiness: 51/100



FINAL ANSWER. The picture to the right

shows a

sketch of the graph. We have labelled intervals of increasing with red and decreasing with blue. Concave up is a thin solid line while concave down is a thick dashed line. We have placed x's to mark the roots, filled in

circles to mark the local maximum and minimum, and triangles to indicate the point of inflection.

Question 3 (b)

Easiness: 64/100

Final answer. $f(x) = x^3 - x^2 - 2x$.

Question 4 (a)

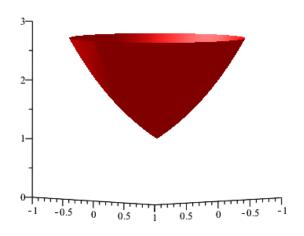
Easiness: 62/100

Final answer.
$$V_1 = \pi \left(\frac{e^2}{2} - 2e + \frac{5}{2} \right)$$

Question 4 (b)

Easiness: 13/100

Final answer. Reality check: Note that we obtain the same value for V_2 with both methods. To visualize



the full bowl we can look at the 3D figure

Question 5 (a)

Easiness: 65/100

FINAL ANSWER. $p_A(t) = e^{-t}$.

Question 5 (b)

Easiness: 59/100

FINAL ANSWER. Therefore, C=2.

Question 5 (c)

Easiness: 8/100

Final answer. $e^{-t}e^{-2t} = e^{-3t}$.

Question 5 (d)

Easiness: 14/100

Final answer. Hence, lightbulb A has the longer expected lifetime.

Question 6 (a) Easiness: 62/100

Final answer. For this equation to be true, we require that $y = \pm 1$ or x = 0. Since x = 0 does not fit the definition of a steady state solution, we are left with the steady solutions $y = \pm 1$.

Question 6 (b) Easiness: 27/100

FINAL ANSWER. Note that this solution does satisfy -1 < y(x) < 1 for all x.Remember: It is important (and usually easy) to check that your solution actually satisfies the differential equation.

Question 7 (a) Easiness: 64/100

FINAL ANSWER. For any $n \ge 1$, we can show that $f^{(n)}(x) = \frac{(-1)^{n-1}(n-1)!}{(1+x)^n}$. Hence, $f^{(n)}(0) = (-1)^{n-1}(n-1)!$ and therefore, $f(x) = \sum_{n=1}^{\infty} \frac{(-1)^{n-1}}{n} x^n$.)

Question 7 (b) Easiness: 61/100

Final answer. (Note that this is a pretty good approximation. $\frac{1703}{1800} \approx 0.946111$, while WolframAlpha approximates the full integral $\int_0^1 \frac{\sin x}{x} dx$ with 0.946083.)

Question 7 (c) Easiness: 56/100

Final answer. $x \cos(x) = \sum_{k=0}^{\infty} (-1)^k \frac{x^{2k+1}}{(2k)!}$

Question 8 Easiness: 32/100

Final answer. $A(t) = ((\sqrt{2} - 1)t + 1)^2$.