

## 1. (30 分)

$$w = \frac{\sum_{i=1}^m y_i (x_i - \bar{x})}{\sum_{i=1}^m x_i^2 - \bar{x} \sum_{i=1}^m x_i} = \frac{\sum_{i=1}^m (y_i x_i - y_i \bar{x})}{\sum_{i=1}^m (x_i^2 - x_i \bar{x})}$$

又因为  $\bar{y} \sum_{i=1}^m x_i = \bar{x} \sum_{i=1}^m y_i = \sum_{i=1}^m \bar{y} x_i = \sum_{i=1}^m \bar{x} y_i = m \bar{x} \bar{y} = \sum_{i=1}^m \bar{x} \bar{y}$ ,  $\sum_{i=1}^m x_i \bar{x} = \bar{x} \sum_{i=1}^m x_i = \bar{x} \cdot m \cdot \frac{1}{m} \cdot \sum_{i=1}^m x_i = m \bar{x}^2 = \sum_{i=1}^m \bar{x}^2$ , 则上式可化为:

$$w = \frac{\sum_{i=1}^m (y_i x_i - y_i \bar{x} - x_i \bar{y} + \bar{x} \bar{y})}{\sum_{i=1}^m (x_i^2 - x_i \bar{x} - x_i \bar{x} + \bar{x}^2)} = \frac{\sum_{i=1}^m (x_i - \bar{x})(y_i - \bar{y})}{\sum_{i=1}^m (x_i - \bar{x})^2}$$

## 2. (40 分)

(1)使用最小二乘法, 可得优化目标如下

$$L_1(w) = \sum_{i=1}^3 (y_i - wx_i)^2 = (0.9 - w)^2 + (0.1 - 0)^2 + (2.2 - 2w)^2$$

通过将导数设置为0, 得到

$$\frac{\partial L_1(w)}{\partial w} = -2 * (0.9 - w) - 4 * (2.2 - 2w) = 0$$
$$w = 1.06$$

(2) 使用最小二乘法, 可得优化目标如下:

$$L_2(w) = \sum_{i=1}^3 (y_i - wx_i^2)^2 = (0.9 - w)^2 + (0.1 - 0)^2 + (2.2 - 4w)^2$$

对 w 求导后为 0, 得到

$$\frac{\partial L_2(w)}{\partial w} = -2 * (0.9 - w) - 8 * (2.2 - 4w) = 0$$

解得

$$w = \frac{19.4}{34} \approx 0.57$$

## 3. (30 分)

$$y = -17.0594 + 0.0982x_1 - 0.0881x_2 - 0.0583x_3 - 0.6069x_4 + 0.1093x_5 + 0.8926x_6 - 0.3389x_7 + 0.3755x_8 + 0.0180x_9 + 0.2913x_{10} + 0.0951x_{11} + 0.5189x_{12} - 1.7791$$

均方误差:

$$E(f; D) = \frac{1}{m} \sum_{i=1}^m (f(x_i) - y_i)^2 = 28.5206$$

错误率.