

**Q1: Show, using the definition of the big-Oh, that the function  $f(n) = 0.5n + 255$  is  $O(n)$**

**Big- $O(n)$**

**$n$  is valid for all value so,**

$$g(n) = 225/0.5 = 510$$

$$g(n) = n. \text{ For all } n > 510$$

$$g(n) > f(n) \text{ Therefore, } f(n) = O(n).$$

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**Q2: Using the big-Oh notation, the worst-case running time of the following algorithm:**

Big- $O$ :

The worst case of the algorithm  $n^3$  because the three nested loop are working.

$n$  (belong to outer loop) \*  $n$  (belong to inner loop) +  $n$  (belong to mood condition)

**$O(n^2+n)$  so  $O(n^2)$ .**

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**Q3: Describe the worst case running time of the following (a, b and c) codes in “big-Oh” notation in terms of the variable  $n$ .**

A) The worst case is  $O(n^4) \Rightarrow (n * n * n * n) \Rightarrow n^4$  because of the nested loop.

B) The worst case is  $O(n) \Rightarrow$  (B and the function  $f3$  are returning the values so the time complexity of returning the function is  **$O(n+n)$**  which is equal to  **$O(2n)$** , so that removing constant so the  **$O(n)$**  )

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**Q4 Suppose you have a queue  $Q$ , which contains two elements in the following order: 5 4.**

A)

**Q.insert(3);**

**Q.insert(8);**

**Q.remove();**

**Q.remove();**

**Q.remove();**

**Q.insert(9);**

|   |   |   |   |
|---|---|---|---|
| 5 | 4 |   |   |
| 5 | 4 | 3 |   |
| 5 | 4 | 3 | 8 |
| 4 | 3 | 8 |   |
| 3 | 8 |   |   |
| 8 |   |   |   |
| 8 | 9 |   |   |

B)

|   |   |   |   |   |
|---|---|---|---|---|
| 5 | 4 | 3 |   |   |
| 5 | 4 | 3 | 2 |   |
| 5 | 4 | 3 | 2 | 1 |

now print/pop the element and the output is reverse 1,2,3,4,5

C) Code file is attached

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**Q5: What will be output of the following programs?**

The outer will run  $< 3$  and the inner loop will run  $< 1$ ,

**Stack output will be**

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|   |
|---|
| A |
| B |
| A |
| C |
| A |
| B |

Queue Output will be

|   |   |   |   |   |   |
|---|---|---|---|---|---|
| b | a | c | a | b | a |
|---|---|---|---|---|---|

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Q6 Design and analyze an algorithm that for a given positive integer n counts the number of different ways to write n as a sum of 1, 2, 3, and 4. For examples, if n = 4, the output should be 8, as Code:

```
class Counter {  
    public int count(int key){  
        int count = 0;  
        for(int i = 1; i <= key; i++){  
            for(int j = 1; j <= key; j++){  
                for(int k = 1; k <= key; k++){  
                    for(int m = 1; m <= key; m++){  
                        if(i + j + k + m == key)  
                            count++;  
  
                        if(i + j + k == key)  
                            count++;  
                    }  
                    if(i+j == key)  
                        count++;  
                }  
                if(i == key)  
                    count++;  
            }  
        }  
        return count;  
    }  
    public static void main(String[] args) {  
        System.out.print((new counter()).count(4));  
    }  
}
```

output:

8

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Q7: Write the code to satisfy the requirement, output should be as depicted in figure (attach screenshots of the program output in word file and submit code as separate file)

Output:

```
Input: SORTINGEXAMPLE
Pivot: E  SORTINGEXAMPLE
Recurse Left: AERTINGEXSMPLO
Recurse right: AEEGILMNOPRSTX
Sorted: AEEGILMNOPRSTX
```

Code:

```
public class Quicksort {
    static boolean print = true;
    static int pivot;
    public static void main(String[] args) {
        String temp = "SORTINGEXAMPLE";

        int[] arr = ConvertIntemp(temp);
        int low = 0;
        int high = arr.length-1;

        System.out.println("----- Quick Sort -----");
        System.out.println("Input: "+ temp);

        sort(arr,low,high);

        System.out.println("Sorted: "+ConvertInString(arr));
    }

    static int[] ConvertIntemp(String temp){
        int[] arr = new int[temp.length()];

        for (int i = 0; i < temp.length(); i++) {
            arr[i] = Integer.parseInt(String.valueOf((int) temp.charAt(i)));
        }

        return arr;
    }
    static String ConvertInString(int[] temp){
        String arr = "";

        for (int i = 0; i < temp.length; i++) {
            arr += String.valueOf((char) temp[i]);
        }

        return arr;
    }

    static void sort(int arr[], int low, int high){
        if (low < high){
```

```

    int pi = partition(arr, low, high);
    if(true){
        if(arr.length/2 <= low){
            System.out.print("Recurse right: ");
        } else {
            System.out.print("Recurse Left: ");
        }
        System.out.print(ConvertInString(arr)+"\n");
    }

    sort(arr, low, pi-1);
    sort(arr, pi+1, high);
}

static int partition(int arr[], int low, int high){
    pivot = arr[high];
    int i = (low-1); // index of smaller element

    if(print){
        print = false;
        System.out.println("Pivot: "+((char) pivot)+" "+ConvertInString(arr));
    }

    for (int j=low; j<high; j++)
        if (arr[j] < pivot)
            i += swap(arr,i+1,j);

    return (i+swap(arr,i+1,high));
}

public static int swap(int arr[], int i, int j) {
    int temp = arr[i];
    arr[i] = arr[j];
    arr[j] = temp;

    return 1;
}
}

```

**Q8. Evaluate and write the result for the following given expression, take values for the operands (show detailed work/dry run)**

**i)  $abc^*+de*f+g^*+$**

| Input             | Postfix          | Infix |
|-------------------|------------------|-------|
| $abc^*+de*f+g^*+$ | $bc^*+de*f+g^*+$ | A     |
| $abc^*+de*f+g^*+$ | $c^*+de*f+g^*+$  | Ab    |

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| Input         | Postfix    | Infix                     |
|---------------|------------|---------------------------|
| abc*+de*f+g*+ | *+de*f+g*+ | Abc                       |
| abc*+de*f+g*+ | +de*f+g*+  | a(b*c)                    |
| abc*+de*f+g*+ | de*f+g*+   | (a+(b*c))                 |
| abc*+de*f+g*+ | e*f+g*+    | (a+(b*c))d                |
| abc*+de*f+g*+ | *f+g*+     | (a+(b*c))de               |
| abc*+de*f+g*+ | f+g*+      | (a+(b*c))(d*e)            |
| abc*+de*f+g*+ | +g*+       | (a+(b*c))(d*e)f           |
| abc*+de*f+g*+ | g*+        | (a+(b*c))((d*e)+f)        |
| abc*+de*f+g*+ | *+         | (a+(b*c))((d*e)+f)g       |
| abc*+de*f+g*+ | +          | (a+(b*c))(((d*e)+f)*g)    |
| abc*+de*f+g*+ |            | ((a+(b*c))+(((d*e)+f)*g)) |
|               |            |                           |

**((a+(b\*c))+(((d\*e)+f)\*g))** [Now put the value a=1,b=2,c=3,d=4,e=5,f=6,g=7

(1+(2\*3))+(((4\*5)+6)\*7))

(1+6)+(20+6\*7)

7+182

**189**

**-+a\*/bc^d**

| Input String | Prefix Expression | Stack (Infix)  |
|--------------|-------------------|----------------|
| -+a*/bc*def  | -+a*/bc*de        | f              |
| -+a*/bc*def  | -+a*/bc*d         | fe             |
| -+a*/bc*def  | -+a*/bc*          | fed            |
| -+a*/bc*def  | -+a*/bc           | f(d*e)         |
| -+a*/bc*def  | -+a*/b            | f(d*e)c        |
| -+a*/bc*def  | -+a*/             | f(d*e)cb       |
| -+a*/bc*def  | -+a*              | f(d*e)(b/c)    |
| -+a*/bc*def  | -+a               | f((b/c)*(d*e)) |

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| Input String | Prefix Expression | Stack (Infix)         |
|--------------|-------------------|-----------------------|
| --a*/bc*def  | --+               | f((b/c)8(d^e))a       |
| --a*/bc*def  | -                 | f(a+((b/c)8(d^e)))    |
| --a*/bc*def  |                   | ((a+((b/c)*(d^e)))-f) |

((a+((b/c)\*(d^e)))-f) [Now put the value a=1,b=2,c=3,d=4,e=5,f=6]

((1+((2/3)\*(4^5)))-6)  
(1+((0.67)\*(1024)))-6  
(1+682.6)-6  
683.6-6

**Output: 677.6**

**C) (((A + B) \* C) - ((D + E) / F))**

Postfix: ab + c \* de + f /-

Prefix: -\*+abc/+def

---

**Q9: Here is an array of ten integers:**

**5 3 8 9 1 7 0 2 6 4**

a) Write the output of this array after the FIRST iteration of the selection sort.

```
import java.util.Arrays;
public class Main {
    public static void main(String[] args) {
        int array[] = {};

        Sorting ob = new Sorting();
        ob.SelectionSorting(array);
    }
}
class Sorting{

    void SelectionSorting(int arr[]){
        int length = arr.length,
            swap,
            countloop = 0;
        System.out.println("----- Selection Sorting -----");
        System.out.println(Arrays.toString(arr));

        for (int i = 0; i < (length-1); i++) {
            int minIndex = i;
```

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```
        for (int j = i+1; j < length; j++) {
            System.out.println("j = "+j+",minIndex = "+minIndex+",minValue = "+arr[minIndex]+",Check("+arr[j]+"<" +arr[minIndex]+") => "+(arr[j] < arr[minIndex]));
            if (arr[j] < arr[minIndex]) {
                minIndex = j;
            }
            countloop++;
        }
        swap = arr[minIndex];
        arr[minIndex] = arr[i];
        arr[i] = swap;
        System.out.println("----- i = "+i+" Complete -----");
    };

    System.out.println(Arrays.toString(arr));

}

System.out.println("Number of time value inner loop works: "+countloop);
}
```

### Output:

```
----- Selection Sorting -----
[5, 3, 8, 9, 1, 7, 0, 2, 6, 4]
j = 1,minIndex = 0,minValue = 5,Check(3<5) => true
j = 2,minIndex = 1,minValue = 3,Check(8<3) => false
j = 3,minIndex = 1,minValue = 3,Check(9<3) => false
j = 4,minIndex = 1,minValue = 3,Check(1<3) => true
j = 5,minIndex = 4,minValue = 1,Check(7<1) => false
j = 6,minIndex = 4,minValue = 1,Check(0<1) => true
j = 7,minIndex = 6,minValue = 0,Check(2<0) => false
j = 8,minIndex = 6,minValue = 0,Check(6<0) => false
j = 9,minIndex = 6,minValue = 0,Check(4<0) => false
----- i = 0 Complete -----
[0, 3, 8, 9, 1, 7, 5, 2, 6, 4]
j = 2,minIndex = 1,minValue = 3,Check(8<3) => false
j = 3,minIndex = 1,minValue = 3,Check(9<3) => false
j = 4,minIndex = 1,minValue = 3,Check(1<3) => true
j = 5,minIndex = 4,minValue = 1,Check(7<1) => false
j = 6,minIndex = 4,minValue = 1,Check(5<1) => false
j = 7,minIndex = 4,minValue = 1,Check(2<1) => false
j = 8,minIndex = 4,minValue = 1,Check(6<1) => false
j = 9,minIndex = 4,minValue = 1,Check(4<1) => false
----- i = 1 Complete -----
```

b) Then, write the output of this array after FIRST iteration of the loop in an insertion sort.

```
class Sorting{

    void InsertionSorting(int arr[]) {
        int length = arr.length,
            countloop = 0;
        System.out.println("----- Insertion Sorting ----- ");
    }
}
```

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```
System.out.println(Arrays.toString(arr));

for (int i = 1; i < (length); ++i) {
    int key = arr[i];
    int j = i - 1;
    while (j >= 0 && arr[j] > key) {
        System.out.println("j = "+j+",key = "+key+",Check("+arr[j]+"<"+key+" )=> "+(j >= 0 && arr[j] > key));
        arr[j + 1] = arr[j];
        j = j - 1;
        countloop++;
    }
    arr[j + 1] = key;
    System.out.println(Arrays.toString(arr));
    System.out.println("----- i = " + i + " Complete -----");
}

System.out.println("Number of time value inner loop works: "+countloop);
}
```

output:

```
----- Insertion Sorting -----
[5, 3, 8, 9, 1, 7, 0, 2, 6, 4]
j = 0,key = 3,Check(5<3) => true
[3, 5, 8, 9, 1, 7, 0, 2, 6, 4]
----- i = 1 Complete -----
[3, 5, 8, 9, 1, 7, 0, 2, 6, 4]
```

c) Finally, sort the array using bubble sort.

```
package com.company;

import java.util.Arrays;
import java.util.Scanner;

public class BubbleSorting1 {
    public static void main(String[] args) {
        System.out.println("1) Implement Bubble Sort.\n");

        // int length;
        // Scanner scan = new Scanner(System.in);

        // System.out.print("Enter the Length of the array: ");
        //

        int arr[] = new int[]{5,3,8,9,1,7,0,2,6,4};
        int length = arr.length;
        // for (int i = 0; i < length; i++) {
        //     System.out.print("Enter the Value of index: "+i+" : ");
        //     arr[i] = scan.nextInt();
        // }

        System.out.println("\nArray before bubble sorting: "+ Arrays.toString(arr));
    }
}
```



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```
int swap;
for (int i = 0; i < length-1; i++) {
    for (int j = 0; j < (length-i)-1; j++) {
        if (arr[j] > arr[j+1]) {
            swap = arr[j];
            arr[j] = arr[j+1];
            arr[j+1] = swap;
        }
    }
}

System.out.println("\nArray After bubble sorting: " + Arrays.toString(arr));
}
}
```

Output:

```
Array before bubble sorting: [5, 3, 8, 9, 1, 7, 0, 2, 6, 4]

Array After bubble sorting: [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
```

**Q10: Do as directed (Choose sorting algorithm wisely)**

**A)**

0 1 2 3 4 5 6 7 8 42 24 6 17 30 13 90 47 2 {l=1}  
0 1 2 3 4 5 6 7 8 42 24 6 17 30 13 90 47 2 {l=2}  
0 1 2 3 4 5 6 7 8 42 24 6 17 30 13 90 47 2 {l=3}  
0 1 2 3 4 5 6 7 8 42 24 6 17 30 13 90 47 2 {l=4}  
0 1 2 3 4 5 6 7 8 42 24 6 17 30 13 90 47 2 {l=5}  
0 1 2 3 4 5 6 7 8 42 24 6 17 30 13 90 47 2 {l=6}  
0 1 2 3 4 5 6 7 8 42 24 6 17 30 13 90 47 2 {l=7}

It can be sort by insertion sort.

**B)** Selection sorting Methods

**C)** In this case, we use queue

**D)** Insertion Sort