

Q1: Show, using the definition of the big-Oh, that the function $f(n) = 0.5n + 255$ is $O(n)$

Big- $O(n)$

n is valid for all value so,

$$g(n) = 225/0.5 = 510$$

$$g(n) = n. \text{ For all } n > 510$$

$$g(n) > f(n) \text{ Therefore, } f(n) = O(n).$$

Q2: Using the big-Oh notation, the worst-case running time of the following algorithm:

Big- O :

The worst case of the algorithm n^3 because the three nested loop are working.

n (belong to outer loop) * n (belong to inner loop) * n (belong to mood condition)

$$O(n^3).$$

Q3: Describe the worst case running time of the following (a, b and c) codes in “big-Oh” notation in terms of the variable n .

- A) The worst case is $O(n^4) \Rightarrow (n * n * n * n) \Rightarrow n^4$ because of the nested loop.
- B) The worst case is $O(n) \Rightarrow$ (B and the function $f3$ are returning the values so the time complexity of returning the function is $O(n+n)$ which is equal to $O(2n)$, so that removing constant so the $O(n)$)

Q4 Suppose you have a queue Q , which contains two elements in the following order: 5 4.

A)

$Q.insert(3);$

$Q.insert(8);$

$Q.remove();$

$Q.remove();$

$Q.remove();$

$Q.insert(9);$

5	4		
5	4	3	
5	4	3	8
4	3	8	
3	8		
8			
8	9		

B)

5	4	3		
5	4	3	8	
4	3	8		
3	8			
8				
1				
1	2			
1	2	3		
1	2	3	4	
1	2	3	4	5

C) Code file is attached

Q5: What will be output of the following programs?

The outer will run < 3 and the inner loop will run < 1,
Stack output will be

B
A
C
A
B
A

Queue Output will be

a	b	a	c	a	b
---	---	---	---	---	---

Q6 Design and analyze an algorithm that for a given positive integer n counts the number of different ways to write n as a sum of 1, 2, 3, and 4. For examples, if n = 4, the output should be 8, as Code:

```
class GFG {
    public static int count(int key){
        int count = 0;
        for(int i = 1; i <= 4; i++){
            if(i == key)
                count++;

            for(int j = 1; j <= 4; j++){
                if(i+j == key)
                    count++;

                for(int k = 1; k <= 4; k++){
                    if(i + j + k == key)
                        count++;

                    for(int m = 1; m <= 4; m++){
                        if(i + j + k + m == key)
                            count++;
                    }
                }
            }
        }
        return count;
    }
    public static void main(String[] args) {
        System.out.print(count(4));
    }
}
```

Muhammad Fahad

FA19-BSSE-0014

Am

```
}  
}
```

output:

8

Q7: Write the code to satisfy the requirement, output should be as depicted in figure (attach screenshots of the program output in word file and submit code as separate file)

Output:

```
Input: SORTINGEXAMPLE  
Pivot: E  SORTINGEXAMPLE  
Recurse Left: AERTINGEXSMPLO  
Recurse right: AEEGILMNOPRSTX  
Sorted: AEEGILMNOPRSTX
```

Code:

```
public class Quicksort {  
    static boolean print = true;  
    static int pivot;  
    public static void main(String[] args) {  
        String temp = "SORTINGEXAMPLE";  
  
        int[] arr = ConvertIntemp(temp);  
        int low = 0;  
        int high = arr.length-1;  
  
        System.out.println("----- Quick Sort -----");  
        System.out.println("Input: "+ temp);  
  
        sort(arr,low,high);  
  
        System.out.println("Sorted: "+ConvertInString(arr));  
    }  
  
    static int[] ConvertIntemp(String temp){  
        int[] arr = new int[temp.length()];  
  
        for (int i = 0; i < temp.length(); i++) {  
            arr[i] = Integer.parseInt(String.valueOf((int) temp.charAt(i)));  
        }  
  
        return arr;  
    }  
    static String ConvertInString(int[] temp){  
        String arr = "";  
  
        for (int i = 0; i < temp.length; i++) {  
            arr += String.valueOf((char) temp[i]);  
        }  
    }  
}
```

```
    return arr;
}

static void sort(int arr[], int low, int high){
    if (low < high){
        int pi = partition(arr, low, high);
        if(true){
            if(arr.length/2 <= low){
                System.out.print("Recurse right: ");
            }else {
                System.out.print("Recurse Left: ");
            }
            System.out.print(ConvertInString(arr)+"\n");
        }

        sort(arr, low, pi-1);
        sort(arr, pi+1, high);
    }
}

static int partition(int arr[], int low, int high){
    pivot = arr[high];
    int i = (low-1); // index of smaller element

    if(print){
        print = false;
        System.out.println("Pivot: "+((char) pivot)+" "+ConvertInString(arr));
    }

    for (int j=low; j<high; j++)
        if (arr[j] < pivot)
            i += swap(arr,i+1,j);

    return (i+swap(arr,i+1,high));
}

public static int swap(int arr[], int i, int j) {
    int temp = arr[i];
    arr[i] = arr[j];
    arr[j] = temp;

    return 1;
}
}
```

Q8. Evaluate and write the result for the following given expression, take values for the operands (show detailed work/dry run)

i) $abc^*+de*f+g^*+$

Input	Postfix	Infix
$abc^*+de*f+g^*+$	$bc^*+de*f+g^*+$	A
$abc^*+de*f+g^*+$	$c^*+de*f+g^*+$	Ab
$abc^*+de*f+g^*+$	$*+de*f+g^*+$	Abc
$abc^*+de*f+g^*+$	$+de*f+g^*+$	$a(b*c)$
$abc^*+de*f+g^*+$	$de*f+g^*+$	$(a+(b*c))$
$abc^*+de*f+g^*+$	$e*f+g^*+$	$(a+(b*c))d$
$abc^*+de*f+g^*+$	$*f+g^*+$	$(a+(b*c))de$
$abc^*+de*f+g^*+$	$f+g^*+$	$(a+(b*c))(d*e)$
$abc^*+de*f+g^*+$	$+g^*+$	$(a+(b*c))(d*e)f$
$abc^*+de*f+g^*+$	g^*+	$(a+(b*c))((d*e)+f)$
$abc^*+de*f+g^*+$	$*+$	$(a+(b*c))((d*e)+f)g$
$abc^*+de*f+g^*+$	$+$	$(a+(b*c))(((d*e)+f)*g)$
$abc^*+de*f+g^*+$		$((a+(b*c))+(((d*e)+f)*g))$

$((a+(b*c))+(((d*e)+f)*g))$ [Now put the value $a=1, b=2, c=3, d=4, e=5, f=6, g=7$

$(1+(2*3))+(((4*5)+6)*7))$

$(1+6)+(20+6*7)$

$7+182$

189

 $-+a^*/bc^d$

Input String	Prefix Expression	Stack (Infix)
$-+a^*/bc^d$	$-+a^*/bc^d$	f
$-+a^*/bc^d$	$-+a^*/bc^d$	fe
$-+a^*/bc^d$	$-+a^*/bc^*$	fed
$-+a^*/bc^d$	$-+a^*/bc$	$f(d*e)$
$-+a^*/bc^d$	$-+a^*/b$	$f(d*e)c$
$-+a^*/bc^d$	$-+a^*/$	$f(d*e)cb$

Muhammad Fahad
FA19-BSSE-0014
Am

Input String	Prefix Expression	Stack (Infix)
--a*/bc*def	--a*	f(d*e)(b/c)
--a*/bc*def	--a	f((b/c)*(d*e))
--a*/bc*def	--+	f((b/c)8(d^e))a
--a*/bc*def	-	f(a+((b/c)8(d^e)))
--a*/bc*def		((a+((b/c)*(d^e)))-f)

((a+((b/c)*(d^e)))-f) [Now put the value a=1,b=2,c=3,d=4,e=5,f=6]

((1+((2/3)*(4^5)))-6)
(1+((0.67)*(1024)))-6
(1+682.6)-6
683.6-6

Output: 677.6

C) (((A + B) * C) - ((D + E) / F))

Postfix: ab + c * de + f / -

Prefix: -*+abc/+def

Q9: Here is an array of ten integers:

5 3 8 9 1 7 0 2 6 4

a) Write the output of this array after the FIRST iteration of the selection sort.

```
import java.util.Arrays;
public class Main {
    public static void main(String[] args) {
        int array[] = { };

        Sorting ob = new Sorting();
        ob.SelectionSorting(array);
    }
}
class Sorting{

    void SelectionSorting(int arr[]){
        int length = arr.length,
        swap,
        countloop = 0;
```

Muhammad Fahad

FA19-BSSE-0014

Am

```
System.out.println("----- Selection Sorting ----- ");
System.out.println(Arrays.toString(arr));

for (int i = 0; i < (length-1); i++) {
    int minIndex = i;
    for (int j = i+1; j < length; j++) {
        System.out.println("j = "+j+",minIndex = "+minIndex+",minValue = 
"+arr[minIndex]+",Check("+arr[j]+"<"+arr[minIndex]+") => "+(arr[j] < arr[minIndex]));
        if (arr[j] < arr[minIndex]) {
            minIndex = j;
        }
        countloop++;
    }
    swap = arr[minIndex];
    arr[minIndex] = arr[i];
    arr[i] = swap;
    System.out.println("----- i = "+i+" Complete ----- 
");
    System.out.println(Arrays.toString(arr));
}

System.out.println("Number of time value inner loop works: "+countloop);
}
```

Output:

```
----- Selection Sorting -----
[5, 3, 8, 9, 1, 7, 0, 2, 6, 4]
j = 1,minIndex = 0,minValue = 5,Check(3<5) => true
j = 2,minIndex = 1,minValue = 3,Check(8<3) => false
j = 3,minIndex = 1,minValue = 3,Check(9<3) => false
j = 4,minIndex = 1,minValue = 3,Check(1<3) => true
j = 5,minIndex = 4,minValue = 1,Check(7<1) => false
j = 6,minIndex = 4,minValue = 1,Check(0<1) => true
j = 7,minIndex = 6,minValue = 0,Check(2<0) => false
j = 8,minIndex = 6,minValue = 0,Check(6<0) => false
j = 9,minIndex = 6,minValue = 0,Check(4<0) => false
----- i = 0 Complete -----
[0, 3, 8, 9, 1, 7, 5, 2, 6, 4]
j = 2,minIndex = 1,minValue = 3,Check(8<3) => false
j = 3,minIndex = 1,minValue = 3,Check(9<3) => false
j = 4,minIndex = 1,minValue = 3,Check(1<3) => true
j = 5,minIndex = 4,minValue = 1,Check(7<1) => false
j = 6,minIndex = 4,minValue = 1,Check(5<1) => false
j = 7,minIndex = 4,minValue = 1,Check(2<1) => false
j = 8,minIndex = 4,minValue = 1,Check(6<1) => false
j = 9,minIndex = 4,minValue = 1,Check(4<1) => false
----- i = 1 Complete -----
```

b) Then, write the output of this array after FIRST iteration of the loop in an insertion sort.

Muhammad Fahad

FA19-BSSE-0014

Am

```
class Sorting{

    void InsertionSorting(int arr[]) {
        int length = arr.length,
            countloop = 0;
        System.out.println("----- Insertion Sorting ----- ");
        System.out.println(Arrays.toString(arr));

        for (int i = 1; i < (length); ++i) {
            int key = arr[i];
            int j = i - 1;
            while (j >= 0 && arr[j] > key) {
                System.out.println("j = "+j+",key = "+key+",Check("+arr[j]+"<"+key+" ) => "+(j >= 0 && arr[j] > key));
                arr[j + 1] = arr[j];
                j = j - 1;
                countloop++;
            }
            arr[j + 1] = key;
            System.out.println(Arrays.toString(arr));
            System.out.println("----- i = " + i + " Complete ----- ");
        }
        System.out.println("Number of time value inner loop works: "+countloop);
    }
}
```

output:

```
----- Insertion Sorting -----
[5, 3, 8, 9, 1, 7, 0, 2, 6, 4]
j = 0,key = 3,Check(5<3) => true
[3, 5, 8, 9, 1, 7, 0, 2, 6, 4]
----- i = 1 Complete -----
[3, 5, 8, 9, 1, 7, 0, 2, 6, 4]
```

c) Finally, sort the array using bubble sort.

```
package com.company;

import java.util.Arrays;
import java.util.Scanner;

public class BubbleSorting1 {
    public static void main(String[] args) {
        System.out.println("1) Implement Bubble Sort.\n");

        // int length;
        // Scanner scan = new Scanner(System.in);

        // System.out.print("Enter the Length of the array: ");
        //

        int arr[] = new int[]{5,3,8,9,1,7,0,2,6,4};
        int length = arr.length;
        // for (int i = 0; i < length; i++) {
```


Muhammad Fahad

FA19-BSSE-0014

Am

```
//      System.out.print("Enter the Value of index: "+i+" : ");
//      arr[i] = scan.nextInt();
//      }

System.out.println("\nArray before bubble sorting: "+ Arrays.toString(arr));

int swap;
for (int i = 0; i < length-1; i++) {
    for (int j = 0; j < (length-i)-1; j++) {
        if (arr[j] > arr[j+1]) {
            swap = arr[j];
            arr[j] = arr[j+1];
            arr[j+1] = swap;
        }
    }
}

System.out.println("\nArray After bubble sorting: "+ Arrays.toString(arr));
}
```

Output:

```
Array before bubble sorting: [5, 3, 8, 9, 1, 7, 0, 2, 6, 4]

Array After bubble sorting: [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
```

Q10: Do as directed (Choose sorting algorithm wisely)

A)

0 1 2 3 4 5 6 7 8 42 24 6 17 30 13 90 47 2 {l=1}
0 1 2 3 4 5 6 7 8 42 24 6 17 30 13 90 47 2 {l=2}
0 1 2 3 4 5 6 7 8 42 24 6 17 30 13 90 47 2 {l=3}
0 1 2 3 4 5 6 7 8 42 24 6 17 30 13 90 47 2 {l=4}
0 1 2 3 4 5 6 7 8 42 24 6 17 30 13 90 47 2 {l=5}
0 1 2 3 4 5 6 7 8 42 24 6 17 30 13 90 47 2 {l=6}
0 1 2 3 4 5 6 7 8 42 24 6 17 30 13 90 47 2 {l=7}

It can be sort by insertion sort.

B) Selection sorting Methods

C) In this case, we use queue

D) Insertion Sort