

ECP 8506 Simulation Sciences

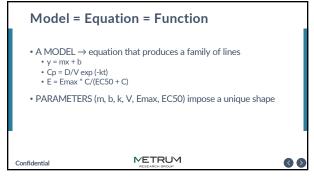
- Introduce basic concepts and nomenclature of nlme modeling
- The reason why is mrgsolve relies on many of the same concepts, and uses many of the same terms
- Simulations often take off where the model estimation process ends
- With modeling, we start with data and fit a model to the data

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With simulation, we start with the model and generate predictions for model qualification or for what-if scenarios

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To start... ...we'll make it simple

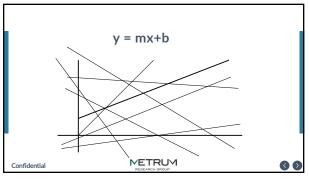
• Consider the model for a straight line

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How Does This All Work?

- We start with data
- From an EXPERIMENT
- Then we need a model that plausibly goes through the data Up to the modeling scientist, guided by EXPERIENCE

 - (and there a lot of models to choose from)
- Then we need parameters for that model to specify a particular shape to best fit the model predictions to observed data
 - We most often turn parameter estimation over to ELECTRONS in a computer program
- (and there are a lot of them to choose from)

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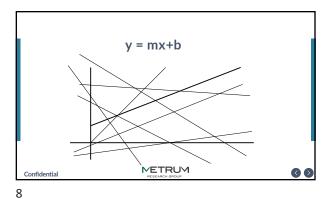
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We start with data

Then we propose a MODEL that might reasonably predict the data

Then we need to think about which parameters to choose to match the data

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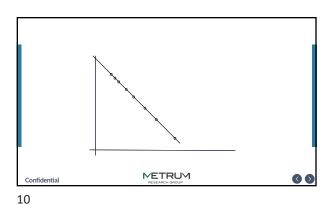
Getting Parameters

• Model

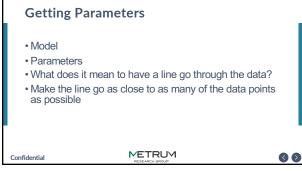
• Parameters

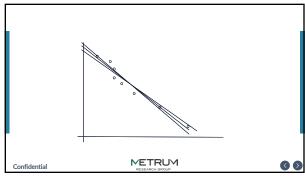
• What does it mean to have a line go through the data?

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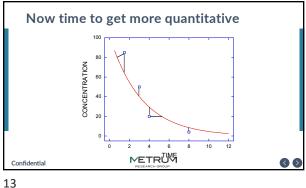


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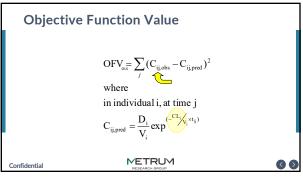
What you need Observed data Model Cp=D/V exp(-Kt) RESIDUALS · Model parameters Different set of V=48L RESIDUALS K=0.412 hr-1 Predicted data V=42L K=0.356 hr-1 **METRUM** 00

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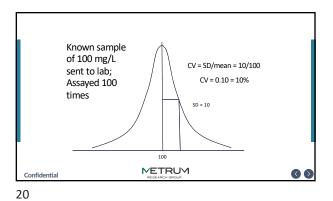
Nonlinear Regression Time to get more mathematical (Cobs –Cpred) \sum (Cobs –Cpred) \sum (Cobs –Cpred) 2 $SSQ = \sum (Cobs - Cpred) 2$ Cobs are the data Cpred = D/V * exp^(-kt) D is dose t is time k is a first-order rate constant
V is volume of distribution TIME **Nonlinear Regression Algorithm** 1. You must give initial starting values for each parameter in your model Computer calculates the SSQ Search for another parameter set (i.e., new pair of CL, V) Compute new SSQ 5. If new SSQ is lower; loop back to 3, or 6. Stop when a lower SSQ cannot be found METRUM

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Terms from estimation you need for **Simulation** • Model Parameters • Predicted data (i.e., simulated under the model) Residuals METRUM **3** Confidential



Analytical Variability • With most analytical systems, the noise of the response increases in proportion to the signal • Constant S/N ratio • Constant Coefficient of Variation (CV) CV = SD/mean • Analytical variability is usually 5-10%; acceptable up to 20% (FDA)



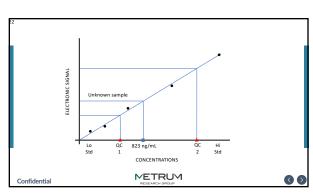
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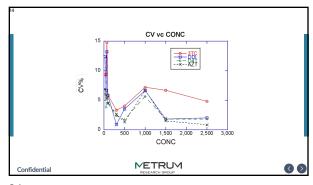
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CV = 10% SD = 10 SD = 0.1 SD = 1.0 METRUM **O D**



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	Q	Cs		
Sample	75	300	1500	
1	75.3	306	1567	
2	78.2	299	1553	
3	72.6	305	1532	
4	69.1	302	1525	
5	69.4	287	1510	
mean	72.9	300	1537	
SD	3.89	7.66	22.66	
CV%	5.30%	2.60%	1.50%	
		•		



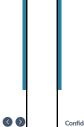
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So why is all this important?

• An assumption of nonlinear regression is that the variance at all observations is equal

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- · Homoschedasticity
- Clearly not what we have in PK systems



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Objective Function Value (WLS) Residuals (RES) are now Weighted Residuals (WRES) in individual i, at time j

 $W_{ij} = weight = variance = SD^2 = (CV \times Cp)^2$ METRUM

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Terms from estimation you need for **Simulation** Model

Heteroscedasticity C V=SD/mean SD = CV x mean

> SD = 0.1 x 1 = 0.1 Residual = 10

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SD = 0.1 x 100 = 10

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- Parameters
- Observed data
- Predicted data (i.e., simulated under the model)
- Residuals

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Weighted residuals (WRES)

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NLME Population Pharmacokinetics

- Experimental unit is the population, not the individual
- The PK parameters of interest are POPULATION means and variances, not those in any individual subject
- Pool ALL data from ALL subjects and analyze them simultaneously

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- PopPK Modeling four models
- PK model
- Covariate model
- Between subject variability (BSV) Interindividual variability
- Residual unexplained variability (RUV) Intraindividual variability

ALL FOUR MODELS ALSO APPLY TO SIMULATION

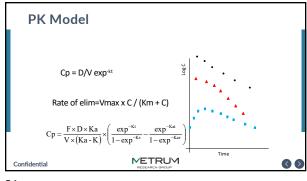
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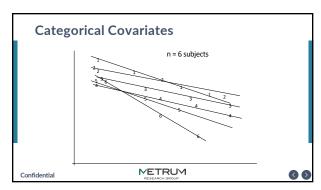
Covariate Model

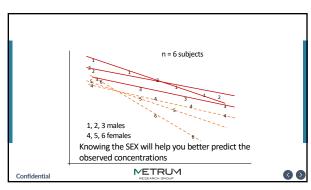
Covariates help us understand what patient-specific characteristics are important determinants of PK parameters

The covariate model specifies a mathematical relationship between a PK parameter and the covariate (fixed effects)

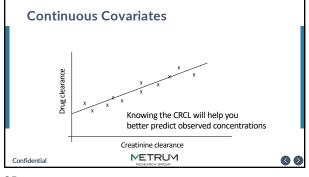
usually requires the addition of another parameter in the model

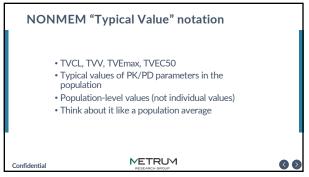
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Regression Parameters • THETAs are the labels used for the regression parameters • y = mx + b y = THETA(1) * x + THETA(2) • USING NONMEM TV notation TVslope = THETA(1) TVintercept = THETA(2) y = TVslope * x + TVintercept

NONMEM Typical Value notation

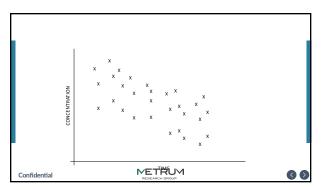
• PK parameters vs. Regression parameters
• PK/PD models can get complex, and each "PK parameter" might have multiple regression parameters

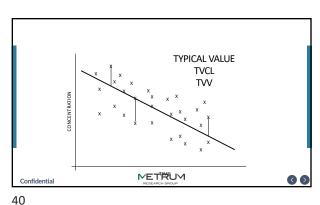
TVCL = THETA(1) + THETA(2)*CLCR

TVV = THETA(3) if male, or

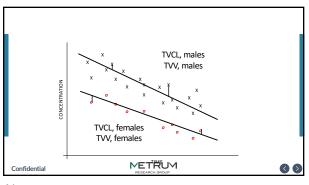
TVV = THETA(4) if female

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Categorical Covariates

• Often modeled as a fractional multiplier

TVCL = THETA(1)

IF (SEX.EQ.0) TVCL = TVCL * THETA(2)

• THETA(1) is the TVCL for males

• THETA(2) is the fraction by which the male TVCL is multiplied to get the female TVCL

• THETA(1)=4.0; THETA(2)=0.75

• TVCLmale = 4.0; TVCLfemale = 4.0 x 0.75 = 3.0

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Continuous Covariates • TVCL = THETA(1)*(WT/70)**THETA(2) Allows a bend in the relationship Usually a more stable parameterization THETA(1) is the TVCL for a standard 70kg subject • THETA(2) ~ 0 → no relationship with WT • THETA(2) ~ 1 → CL proportional with WT • You might choose the denominator as a reference value • Often chosen as the median, or the mean of the covariate **METRUM** 90 Confidential

Terms from estimation you need for **Simulation**

- Model
- Parameters
- Observed data
- Predicted data (i.e., simulated under the model)
- Residuals
- · Weighted residuals
- Typical Value notation (TVCL, TVV, etc.)
- Fixed effects
- Covariate models

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Limitation to Fixed-effects • Not all 32 yo, 6'4", 84 kg, *1*3 males with a CRCL of 93 mL/min will have the same actual CL that is being predicted by the regression equation • PopPK is interested in means and variances • How can we formalize the notion that not everyone is at the mean? **RANDOM EFFECTS**

More NONMEMese • ETA (η) • The difference between an individual's true parameter (e.g., CLi) and that $\underline{\textbf{predicted}}$ by the regression equation (TVCLi) e.g., TVCLi = THETA(1)*WTi CLi = TVCLi + ETAi

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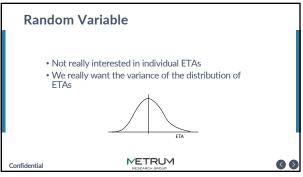
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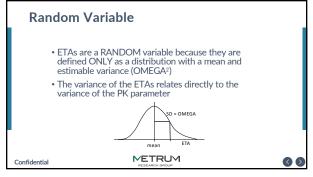
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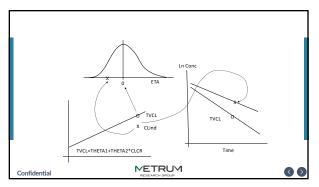
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Between Subject Variability (BSV) Model • TVCL = THETA(1) + THETA(2)*WT + ... CL = TVCL + ETA(1) • An individual may have a CL different from the TV, even AFTER that TVCL has been adjusted for WT, SEX, RACE, AGE, etc. • Similar for V, etc. V = TVV + ETA(2)METRUM 00 Confidential 47







BSV: Additive Model
CL = TVCL + ETA(1)

• In this additive model, the SD of the ETAs
(OMEGA) is the SD of the parameter in the
population
• OMEGA(1)² = 16
SD of CL is 4.0

However, biological parameters are often right (positively) skewed because they are bounded by zero at the low end
 Better approximated using a log normal distribution
 Normal distribution in the log world

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BSV: Exponential Model
CL = TVCL * EXP(ETA(1))

log CL = log TVCL + ETA(1)

• In this exponential model, OMEGA is the variability expressed as the CV in the population

• If OMEGA(1)² = 0.09
CV of CL is 30% (SQRT 0.09 = 0.30)

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Terms from estimation you need for **Simulation** • Random effects Model Parameters • BSV/IIV Observed data • ETA • Predicted data Omega • Residuals · Weighted residuals • Typical Value notation Fixed effects Covariate models METRUM 00 Confidential

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Residual Unexplained Variability (RUV) Model • Even after you get the right PK model • and even after you take into account all the covariates that are predictive, • and even after you allow BSV to account for differences in PK parameters

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• You still cannot perfectly predict most

concentrations

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Analytical errors Model misspecification Errors in recording time of dose Errors in recording time of blood draws Compliance issues Content uniformity of dosage forms

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More NONMEMese

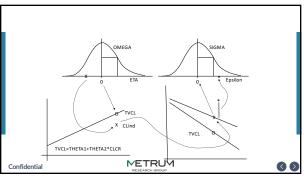
• Epsilon (ε)
• The difference between the observed concentration and the concentration predicted by the model
• Cobs = Cpred + ε

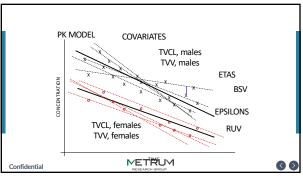
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We don't have an interest in any particular difference, only the collection of them
 Epsilon is another RANDOM variable
 Defined by a mean and a variance (SIGMA²)
 The estimated variance of the Epsilons is an estimate of how much variability remains in the system after you take into account the PK, covariate, and BSV models

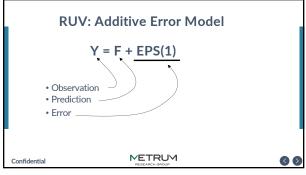
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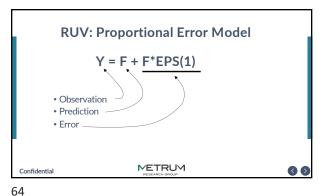


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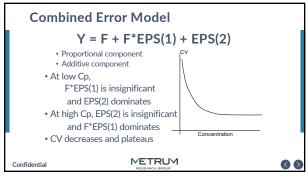
RUV: Additive Error Model Y = F + EPS(1)• Constant SD across all concentrations \bullet SD of the epsilons (SIGMA) is the SD of the residual unexplained errors • SIGMA² = 5.29 • SD RUV = +/- 2.3 mg/L • May be appropriate with concentrations over a limited range, such as TDM data METRUM 00

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RUV: Proportional Error Model Y = F + F*EPS(1)• Constant CV model • The SD of the epsilons (SIGMA) is the CV of the RUV • SIGMA² = 0.0234 • CV% RUV = 15.3% • Absolute error is usually smaller at lower concentrations, increases with observation METRUM Confidential

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Terms from estimation you need for Simulation • Model • Random effects Parameters • BSV/IIV Observed data • ETA Predicted data • Omega • Residuals • RUV · Weighted residuals Epsilon • Typical Value notation Sigma Fixed effects Covariate models METRUM 00 Confidential

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PRED vs. IPRED

• PRED is the prediction based on the population-based (TV) regression equations

TVCL = THETA(1)+THETA(2)*WT+.....

• All the ETAs are set to zero

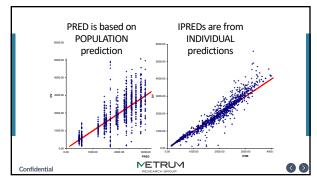
Cpred = D/TVV * exp[-(TVCL/TVV)*t]

• IPRED is the prediction based on CL₁, not TVCL₁, with individual ETAs calculated

CL₁ = TVCL₁ + ETA(1) V₁ = TVV₁ + ETA(2)

Cpred = D/V₁ * exp[-(CL₁/V₁)*t]

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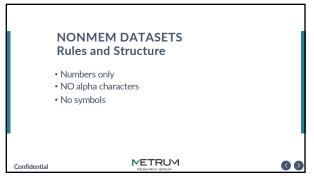
WRES vs CWRES

• WRES are calculated using the PRED, and then weighted
• It's a historical definition
• CWRES are calculated with the RES based on IPREDs, and then weighted
• You will usually see CWRES in plots rather than WRES

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: 1. Based on: 001
:: 2. Description: 1-comp iv, linear elim
:: 3. Lauk:
:: 3.

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NONMEM DATASETS Rules and Structure

- EVENT RECORD: Each row of the data set
- Only one type of event can occur per record
 - AMT event (dose)
 - DV (observation) event
 - OTHER type occasionally used (e.g., covariate changes)
- Each AMT and DV (drug conc, metabolite conc, or PD effect) must EACH be on different rows
- EVEN IF AT THE SAME TIME!!!

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NONMEM DATASETS
Rules and Structure

• All records from an individual MUST be contiguous

• Within each individual, all records must be in time order

• But there is a way to reset the system back to TIME=0

• Handy for multiple doses

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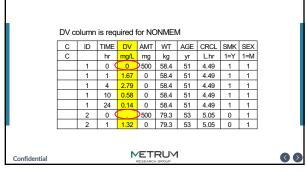
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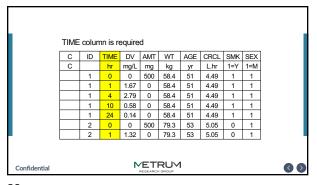
С	ID	TIME	DV	AMT	WT	AGE	CRCL	SMK	SEX
	1	0	0	500	58.4	51	4.49	1	1
	1	1	1.67	0	58.4	51	4.49	1	1
	1	4	2.79	0	58.4	51	4.49	1	1
	1	10	0.58	0	58.4	51	4.49	1	1
	1	24	0.14	0	58.4	51	4.49	1	1
	2	0	0	500	79.3	53	5.05	0	1
	2	1	1.32	0	79.3	53	5.05	0	1

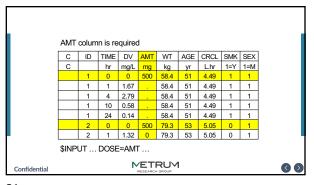
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An ID	colur	nn is r	equire	d for	NONN	IEM				
С	ID	TIME	DV	AMT	WT	AGE	CRCL	SMK	SEX	
С		hr	mg/L	mg	kg	yr	L.hr	1=Y	1=M	
	1	0	0	500	58.4	51	4.49	1	1	
	1	1	1.67	0	58.4	51	4.49	1	1	
	1	4	2.79	0	58.4	51	4.49	1	1	
	1	10	0.58	0	58.4	51	4.49	1	1	
	1	24	0.14	0	58.4	51	4.49	1	1	
	2	0	0	500	79.3	53	5.05	0	1	
	2	1	1.32	0	79.3	53	5.05	0	1	



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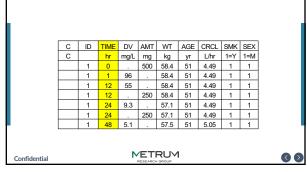


	MUS	T be s	equen	iced in	TIME	E order					
	С	ID	TIME	DV	AMT	WT	AGE	CRCL	SMK	SEX	
	С		hr	mg/L	mg	kg	yr	L.hr	1=Y	1=M	
		1	0	0	500	58.4	51	4.49	1	1	
		1	1	1.67	0	58.4	51	4.49	1	1	
		1	4	2.79	0	58.4	51	4.49	1	1	
		1	10	0.58	0	58.4	51	4.49	1	1	
		1	24	0.14	0	58.4	51	4.49	1	1	
		2	0	0	500	79.3	53	5.05	0	1	
		2	1	1.32	0	79.3	53	5.05	0	1	
	NMTF not B	RAM is	going ositive	to ch	eck to	make	sure	DV and	AMT	are	
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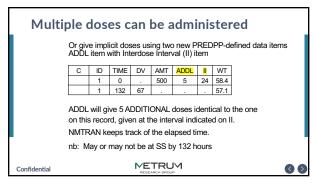
	No co	ovaria	tes are	requi	red to	r NON	IMEM				
	С	ID	TIME	DV	AMT	WT	AGE	CRCL	SMK	SEX	
	С		hr	mg/L	mg	kg	yr	L.hr	1=Y	1=M	
		1	0	0	500	58.4	51	4.49	1	1	
		1	1	1.67	0	58.4	51	4.49	1	1	
		1	4	2.79	0	58.4	51	4.49	1	1	
		1	10	0.58	0	58.4	51	4.49	1	1	
		1	24	0.14	0	58.4	51	4.49	1	1	
		2	0	0	500	79.3	53	5.05	0	1	
		2	1	1.32	0	79.3	53	5.05	0	1	
	As su	ıch, N	O rule	to use	WT,	WGT,	SIZE,	TBW, I	BW e	tc.	
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	ID	TIME	DV	AMT	RATE	AGE	CRCL	SMK	SEX	
C	ID	hr	mg/J	mg	mg/hr		L.hr	1=Y	1=M	
	1	0	"	500	500	31	4.49	1	1	
	1	1	1.67	0		51	4.49	1	1	
	1	4	2.79	0		51	4.49	1	1	
	1	10	0.58	0		51	4.49	1	1	
	1	24	0.14	0	<u> </u>	51	4.49	1	1	
	2	0	ď	500	1000	33	5.05	0	1	
	2	1	1.32	0		53	5.05	0	1	



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ID TIME DV AMT WT AGE hr mg/L kg yr 0 51 1 2 96 58.4 51 1 12 55 58.4 51 57.1 51 0 2 0 34 57.1 51 2 2 143 57.1 51 2 12 2 26 12 57.1 51 57.1 51 500mg has been given every 24h for a gazillion dose BUT... 500mg at time=0 is the last dose given (without additional dosing recs)

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MDV

 Missing Dependent Variable
 1 = DV missing (i.e., usually a dose event)
 0 = DV not missing (i.e., an Observation record)
 Required by NONMEM
 NMTRAN will append this column in FDATA if you don't provide it

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• Event ID

0 = observation event

1 = dosing record

2 = other record

3 = resets time and zeroes out compartments

4 = resets time and compartments, AND gives another dose, using the same event record

• Required by PREDPP

• NMTRAN will append it to FDATA

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EVID=4 zeroes out ALL compartments; resets TIME; AND... ID TIME DV AMT SS II EVID MDV hr mg/L mg 0 77 500 77 12 55 77 24 24 89 1 1000 AND gives the DOSE specified on the record METRUM 00 Confidential

This last dose could be months later ID TIME DV AMT SS С hr mg/L mg 0 500 77 1 96 0 0 77 0 0 77 1 12 55 1 0 500 24 1 81 0 81 24 34 EVID=4 zeroes out ALL compartments; resets TIME=0 or TIME=24 (or whatever); AND with SS=1, puts the system at a NEW steady state

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