



**UTM**  
UNIVERSITI TEKNOLOGI MALAYSIA

**INSPIRING CREATIVE AND INNOVATIVE MINDS**

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# **Chapter 2**

**(Part 2)**

# **Functions**



## Exercise 1

Determine which of the relations  $f$  are functions from the set  $X$  to the set  $Y$ .

a)  $X = \{-2, -1, 0, 1, 2\}$ ,  $Y = \{-3, 4, 5\}$  and

$$f = \{(-2, -3), (-1, -3), (0, 4), (1, 5), (2, -3)\}$$

b)  $X = \{-2, -1, 0, 1, 2\}$ ,  $Y = \{-3, 4, 5\}$  and

$$f = \{(-2, -3), (1, 4), (2, 5)\}$$

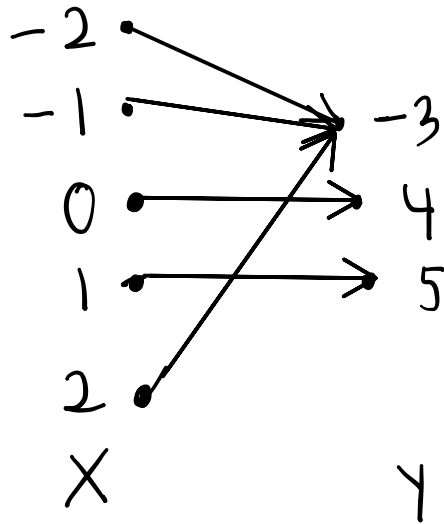
c)  $X = Y = \{-3, -1, 0, 2\}$  and

$$f = \{(-3, -1), (-3, 0), (-1, 2), (0, 2), (2, -1)\}$$

In case any of these relations are functions, determine if they are one-to-one, onto  $Y$ , and/or bijection.

Determine which of the relations  $f$  are functions from the set  $X$  to the set  $Y$ .

a)  $X = \{-2, -1, 0, 1, 2\}$ ,  $Y = \{-3, 4, 5\}$  and  
 $f = \{(-2, -3), (-1, -3), (0, 4), (1, 5), (2, -3)\}$



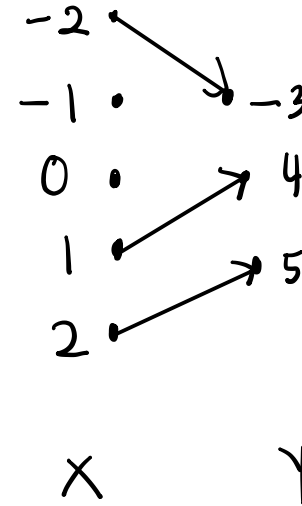
This is function. This function is not one-to-one because  $f(-2) = f(-1) = f(2) = -3$ .

It is onto  $Y$ .

Since the function is onto  $Y$  but not one-to-one,

$\therefore$  It is not bijection

b)  $X = \{-2, -1, 0, 1, 2\}$ ,  $Y = \{-3, 4, 5\}$  and  
 $f = \{(-2, -3), (1, 4), (2, 5)\}$

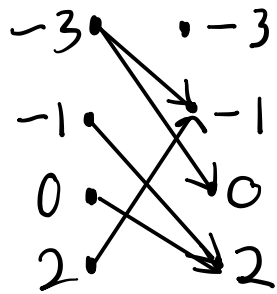


This is not function.

This is because  $-1$  and  $0$  don't have image.

c)  $X = Y = \{-3, -1, 0, 2\}$  and

$$f = \{(-3, -1), (-3, 0), (-1, 2), (0, 2), (2, -1)\}$$



This is function.

The function is not one-to-one because  $f(-3) = f(2) = -1$

The function is not onto  $Y$  because  $-3$  don't have object.

Therefore this is not bijection because the function is not one-to-one and onto  $Y$ .



## Exercise 2

■ Find each inverse function.

a)  $f(x) = 4x + 2, x \in R$

b)  $f(x) = 3 + (1/x), x \in R$



■ Find each inverse function.

a)  $f(x) = 4x + 2, x \in \mathbb{R}$

$$f(x) = y$$

$$\text{let } f^{-1}(y) = x$$

$$y = 4x + 2$$

$$y - 2 = 4x$$

$$x = \frac{y-2}{4}$$

$$f^{-1}(y) = \frac{y-2}{4}$$

$$f^{-1}(x) = \frac{x-2}{4}$$

b)  $f(x) = 3 + (1/x), x \in \mathbb{R}$

$$f(x) = y$$

$$\text{let } f^{-1}(y) = x$$

$$y = 3 + \frac{1}{x}$$

$$y - 3 = \frac{1}{x}$$

$$x = \frac{1}{y-3}$$

$$f^{-1}(y) = \frac{1}{y-3}$$

$$f^{-1}(x) = \frac{1}{x-3}$$



## Exercise 3

- Let  $f$  dan  $g$  be functions from the positive integers to the positive integers defined by the equations,

$$f(n) = n^2, \quad g(n) = 2^n$$

- Find the compositions

a)  $f \circ f$

b)  $g \circ g$

c)  $f \circ g$

d)  $g \circ f$

- Let  $f$  and  $g$  be functions from the positive integers to the positive integers defined by the equations,

$$f(n) = n^2, \quad g(n) = 2^n$$

a)  $f \circ f$

$$\begin{aligned} f(f(x)) &= f(n^2) \\ &= (n^2)^2 \\ &= n^4 \end{aligned}$$

b)  $g \circ g$

$$\begin{aligned} g(g(x)) &= g(2^n) \\ &= 2^{(2^n)} \\ &= (2^2)^n \\ &= 4^n \end{aligned}$$

c)  $f \circ g$

$$\begin{aligned} f(g(x)) &= f(2^n) \\ &= (2^n)^2 \\ &= 4^n \end{aligned}$$

d)  $g \circ f$

$$\begin{aligned} g(f(x)) &= g(n^2) \\ &= 2^{n^2} \end{aligned}$$