Computerized Simulation Exercise No. 3

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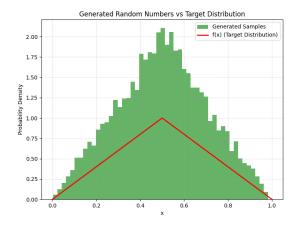
Date: 1403.10.03

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Write a program using the **accept-reject method** to generate random numbers following a custom probability distribution defined by the piecewise function as follows:

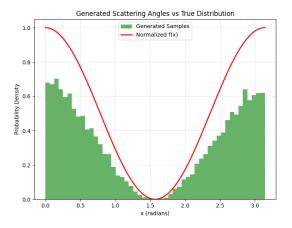
$$f(x) = \begin{cases} 2x & 0 \le x \le 0.5\\ 2(1-x) & 0.5 < x \le 1. \end{cases}$$

```
import numpy as np
import numpy as numpy as
```



Simulate the distribution of angles at which particles scatter when the probability distribution of scattering angles is proportional to $\cos^2(x)$. Use the **accept-reject method** to generate the angles.

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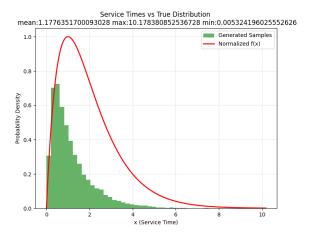
Simulate service times for customers in a queue. Assume service times follow a specific distribution (e.g., $f(x) = xe^{-x}$), and use the **accept-reject method** to generate the times. Analyze the average waiting time.

```
import numpy as np
import numpy as np
import nampfoit(b,py)not as plt

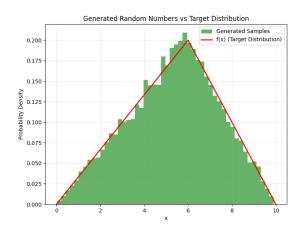
def service_time_distribution(s):
    return x * np.exp(x) if x > 0 clse 0

def accept_reject_sampling(target_func, proposal_func, domain, n_samples, max_val):
    samples = []
    while len(samples) < n_samples:
        x = np.random.exponential())
    if y = target_func(x) / (max_val * proposal_func(x)):
        samples_samples)
    return np.array(samples)

def plot_results(amples, target_func, bins=50):
    x_als = nm.linspace(0, max(samples), 1000)
    f_vals = np.array(larget_func(x) / for x in x_vals])
    plt.figuret_func(x) / for x_in x_vals])
    plt.figuret_func(x) / for x_in x_vals])
    plt.figuret_func(x) / for x_in x_vals
    plt.figuret_func(x)
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Generate random numbers for a triangular distribution defined on $\left[a,b\right]$ with mode c.

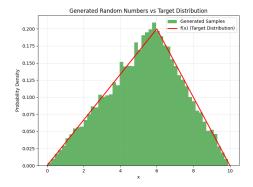


Implement a random number generator for the Rayleigh distribution with variance σ^2 .

The Rayleigh distribution is a continuous probability distribution commonly used in signal processing, radar systems, and various statistical applications.

$$PDF: f(x;\sigma) = \frac{x}{\sigma^2}e^{-\frac{x^2}{2\sigma^2}}, \quad x \ge 0,$$

$$CDF : F(x; \sigma) = 1 - e^{-\frac{x^2}{2\sigma^2}}, \quad x \ge 0.$$



Simulate a bank with multiple counters where:

- Customer arrival times follow an exponential distribution.
- Service times at counters also follow an exponential distribution.

```
import many as np
def sample specential(cfs);
return sp.gradus.exponential(cfs);
return sp.gradus.exponential(cfs);
return sp.gradus.exponential(cfs);

def similar band for acconters, prival_rate, service_rate, similation_time);

def similar band for acconters, prival_rate;
counters_free_at = [0] * mm.counters

varial_counters_free_at = [0] * mm.counters

varial_counters_gradus = [1] total_system.time = [1]

total_system.time = similation_time;

while current_time = similation_time;

pot_spiniture = xount_time in counters_free_at if t > current_time], default=float('tef'))

if next_prival < mext_prival

corrent_time = next_prival

free_counters = [1 for i, t in enumerate(counters_free_at) if t <= current_time)

if free_counters = [1 for i, t in enumerate(counters_free_at) if rec_counters_free_at)

counters_free_atlassinged_counter > current_time > service_time

counters_free_atlassinged_counter > current_time > service_time

total_system_time_support(corrent_time)

else

varial_counter_ince_atlassinged_counter > current_time > service_time

counter_strival < counter_time_support(corrent_time)

else

varial_time_ince_atlassinged_counter_ince_seponential(arrival_rate)

elf next_departure = float('utf):

corrent_time = next_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_counter_ince_atlassinger_
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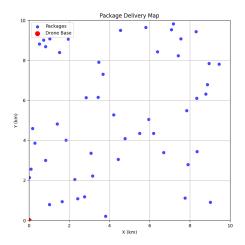
The simulation was conducted using the following input parameters:

- Number of Counters: 3
- Arrival Rate (λ_a) : 2 customers per unit time
- Service Rate (λ_s) : 3 customers per unit time
- Simulation Time: 5000 time units

Based on the input parameters, the simulation produced the following results:

- Average Waiting Time: 0.14 time units.
- Counter Usage: 40.03%, 19.41%, 6.67%
- Average Time in System: 0.34 time units.

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toport many as no manda manda no
toport manda
to
```



- Average Delivery Time: 11.06 hours
- \bullet Total Distance Traveled by All Drones: 41.04 km