



# Faculty of Engineering - Cairo University Electronics and Electrical Communications Department IC - Assignment 3

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## 1. The transfer function that satisfies the specifications:

In a bandpass filter (BPF),  $[\omega_o^2 =$  $\omega_1\omega_2=\omega_3\omega_4$ ], the symmetry is preserved by shifting the 5 MHz frequency to  $\frac{20}{3}$ MHz. This adjustment still meets the original specifications.

## **Designing using Chebyshev**

## **Polynomial:**

$$f_{o_{BPF}} = \sqrt{20 * 10} = 14.14 \, MHz$$
 $BW = 20 - 10 = 10 \, MHz$ 
 $A_p = 20 \log(1 + \epsilon^2) \le 2 \, dB$ 
 $A_p = 1.4 \, dB$ 
 $\epsilon = 0.617$ 

$$s_{1.2} = -0.216 \pm i0.945$$

 $\beta = \frac{1}{n} \sinh^{-1} \left( \frac{1}{n} \right) = 0.42$ 

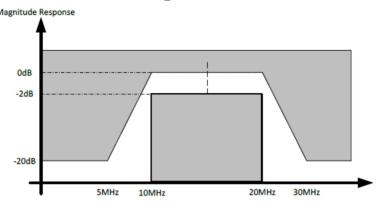


Figure 1: BPF specification

$$\begin{aligned} \omega_{o_{BPF}} &= 2 * \pi * f_{o_{BPF}} = 88.85 \, Mrad/sec \\ Q &= 14.14/10 = 1.414 \\ \Omega_{s} &= \frac{\omega_{4} - \omega_{3}}{BW} = \frac{7}{3} \\ A_{s} &= 20 \log(\epsilon) + 6(n-1) + 20 n \log(\Omega_{s}) = 20 \, dB \\ n &= 2.26 = 3 \\ s_{k} &= \sinh(\beta) \sin\left(\frac{2k-1}{2n}\pi\right) + \mathrm{i} \cosh(\beta) \cos\left(\frac{2k-1}{2n}\pi\right) \\ s_{3} &= -0.4324 \end{aligned}$$

## The Normalized LPF:

$$H_{LPF} = \frac{0.4063}{(s + 0.4324)(s^2 + 0.432s + 0.93968)}$$

## The Denormalization to BPF & of poles and zeros:

$$s_{BPF} = \frac{\omega_0}{BW} \left( \frac{s}{\omega_0} + \frac{\omega_0}{s} \right) = \frac{1.59 * 10^{-8} s^2 + 1.256 * 10^8}{s}$$

By substituting of each (s) in  $H_{LPF}$  by (s<sub>BPF</sub>):

$$\mathsf{H}_{\mathsf{BPF}} = \frac{1*10^{23}*s^3}{\left(s^6 + 5.435*10^{7*}s^5 + 2.812*10^{16}*s^4 + 9.589*10^{23}*s^3 + \right)}\\ \frac{2.22*10^{32}*s^2 + 3.388*10^{39}*s + 4.9223*10^{47}}{(s^6 + 5.435*10^{7*}s^5 + 2.812*10^{16}*s^4 + 9.589*10^{23}*s^3 + 1)}$$

#### By using MATLAB, the poles and zeros:

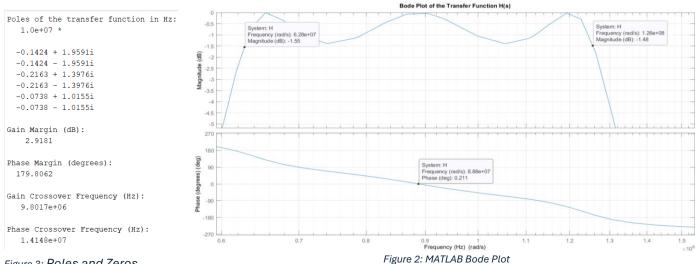


Figure 3: Poles and Zeros.

## 2. Circuit Design (Biquad filter topology):

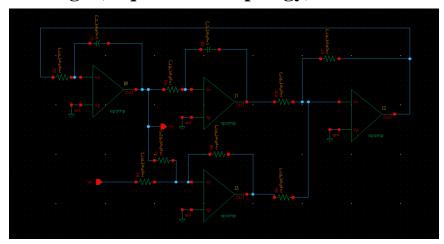


Figure 4: One Stage Biquad filter

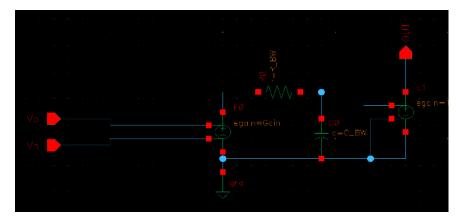


Figure 5 : Opamp model

#### The cascaded TF from $H_{BPF}$ :

```
Gain = nthroot((D/E^3),3);
p = [S6 S5 S4 S3 S2 S1 S0];
r = roots(p)

numerator = [Gain 0];

denominator1 = [1,-1*(r(1)+r(2)),r(1)*r(2)];
H1 = tf(numerator, denominator1)

denominator2 = [1,-1*(r(3)+r(4)),r(3)*r(4)];
H2 = tf(numerator, denominator2)

denominator3 = [1,-1*(r(6)+r(5)),r(5)*r(6)];
H3 = tf(numerator, denominator3)
```

Figure 6: the cascaded TF

The Biquad BPF TF topology:

$$H_{BPF} = \frac{-H_o * S \frac{1}{R1C}}{S^2 + S \frac{1}{QR1C} + \frac{1}{(R1C)^2}}$$

Design steps for  $H_o=1$ , equal R, C topology and comparing H1, H2, H3 with the Biquad TF :

R1 = 1 (K
$$\Omega$$
), R2 =  $Q * R1$ 

TF	H1	H2	H3
R2 (KΩ)	6.8950	3.2694	6.8950
C (pF)	8.1025	11.254	15.631

#### **Circuit Schematic:**

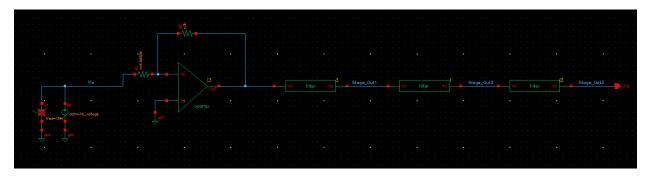


Figure 7: Circuit schematic

To normalize the filter, an op-amp was added initially to provide a gain of  $\frac{1}{K1*K2*K2}$  to achieve overall gain  $(4.65*10^7)^3$ . Given the transfer function  $TF = -\frac{RF}{R0}$ , RF is set to 1k $\Omega$  and R0 is set to 6.97k $\Omega$  to achieve the required gain.

## 3. Simulation results:

## **AC Analysis:**

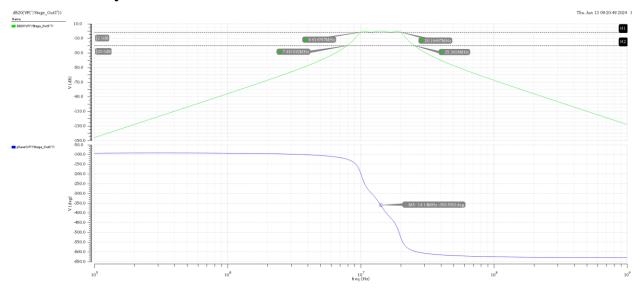


Figure 8 : Gain and Phase response (AC Analysis)

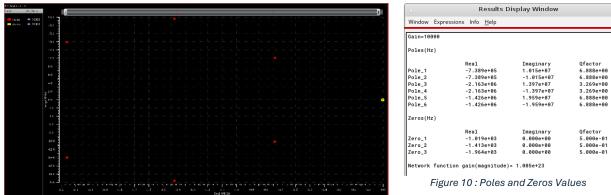


Figure 9 : Poles and Zeros analysis

- As shown Magnitude response meets our expectations.
- Poles: Same as in hand analysis Values match our calculations.
- **Zeros**: we noticed that all zeros aren't exactly at zero but it has very small values compared to poles, so their effect on our response is negligible.

Because that the used op-amps aren't ideal and some mismatches.

1- Center frequency=14.14MHZ 2-phase at fc=-359.5921deg

3-BW=11MHZ

## **Output referred noise Analysis:**

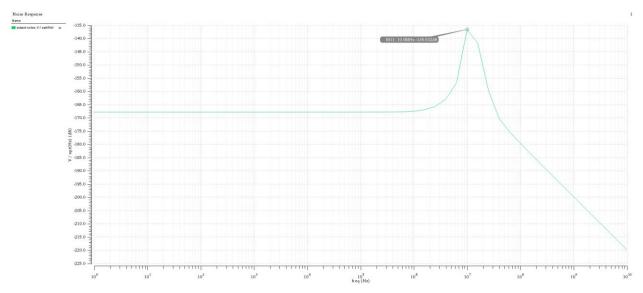


Figure 11: Output referred noise in dB

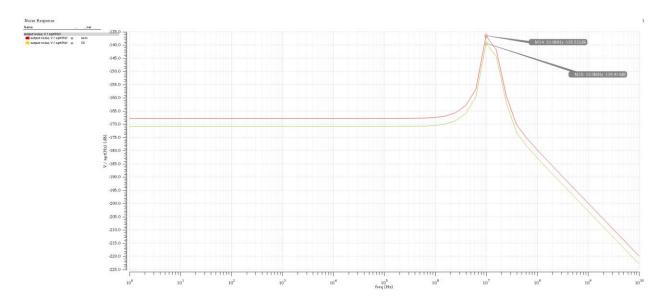


Figure 12 : Output referred noise after reducing R TO 0.5R

- 1Maximum output-referred noise is =149.065 nV/sqrt(HZ) at frequency =10MHZ
- After reducing the value of resistance by 50% of its primary value we noticed that:
- Output-referred noise decreased by almost  $1/\sqrt{2}$  compared to the primary value and Maximum output-referred noise is =106.978 nV/sqrt(HZ) at frequency =10MHZ.
- There is a trade-off between the noise and power consumption as when we reduce the resistance the noise will decrease and power consumption will increase.

## Transient response analysis:

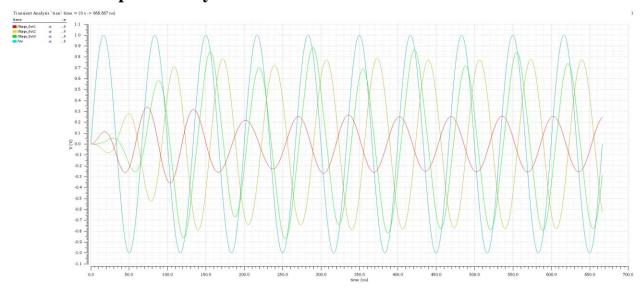


Figure 13 : Transient response

## **DFT:**

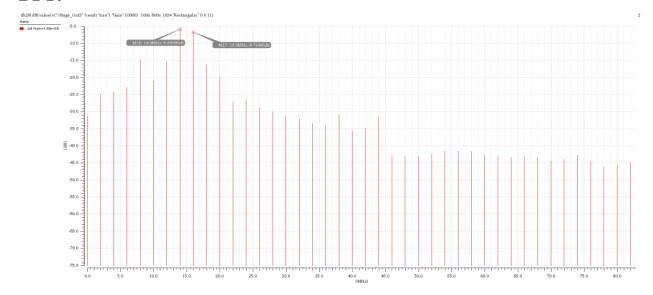


Figure 14 : DFT

DFT Varying all capacitors by ±15%

Comment: Cap (-15% change):

The transfer function has been changed due to the changing in caps values, this means that TF has shifted to high frequency because each stage will shift  $\omega_0^2 = \frac{1}{R_1^2 C^2}$  but quality factor will remain the same  $Q = \frac{R_2}{R_1}$ .

Cap (+15% change):

The transfer function has been changed due to the changing in caps values, this means that TF has shifted to lower frequency because each stage will shift  $\omega_0^2 = \frac{1}{R_1^2 C^2}$  but quality factor will remain the same  $Q = \frac{R_2}{R_1}$ .

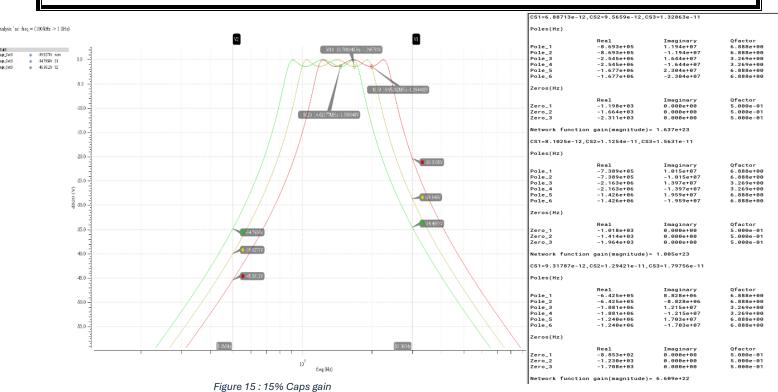


Figure 16 : Values

#### Varying capacitors in 1st section by ±2%

#### Comment:

Transfer function had been slightly changed due to the small change in caps in first sec values, which leads to small shift in the frequency response of the filter, and small change in the locations of poles and zeros.

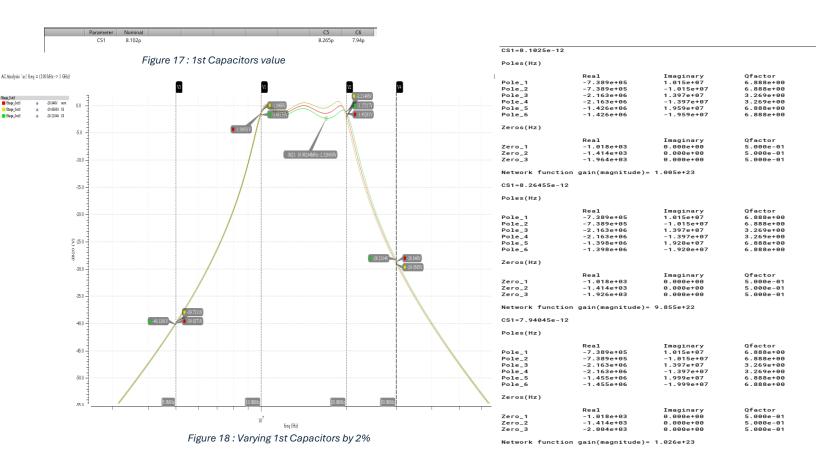
Cap (-2% change):

This means that TF has shifted slightly to high frequency because each stage will shift  $\omega_0^2 = \frac{1}{R_1^2 C^2}$  but quality factor will remain the same  $Q = \frac{R_2}{R_1}$ .

Cap (+2% change):

This means that TF has shifted slightly to low frequency because each stage will shift  $\omega_0^2 = \frac{1}{R_1^2 C^2}$  but quality factor will remain the same  $Q = \frac{R_2}{R_1}$ .

We notice that this small change in CAP value will be unobservable in output response but from our observations we can see that this change has a high effect because cascade of biquads highly sensitivity to component mismatch.



Varying the gain of the Op-amps to 1000 & 100

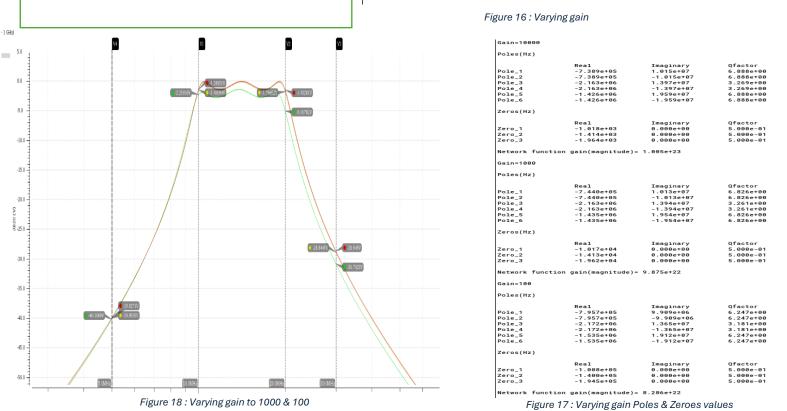


Figure 15: 2% 1st Capacitors Poles & Zeroes plot

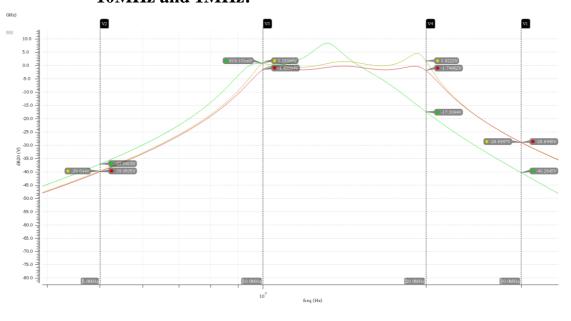
C4

100

#### Comment:

Decreasing the gain of Op-Amps leading to increasing in non-idealities in the Op-Amps. It also leads to increasing the number of poles and zeros as it is function of (GBW).

# Add a BW limitation for the Op-amps Set the gain at 1000 and vary BW to 10MHz and 1MHz:



#### Comment:

Decreasing the BW of Op-Amps leading to increasing in non-idealities in the Op-Amps. It also leads to increasing the number of poles and zeros as it is function of (GBW).

Figure 19 Varying BW

C_BW=0, R_BW=0				Zero_5	-1.607e+09	0.000e+00	5.000e-01
				Zero_6	-1.613e+09	0.000e+00	5.000e-01
Poles(Hz)				Zero_7	7.379e+09	2.326e+09	-5.243e-01
				Zero_8	7.379e+09	-2.326e+09	-5.243e-01
	Real	Imaginary	Qfactor	Zero_9	4.861e+09	6.236e+09	-8.133e-01
ole_1	-7.440e+05	1.013e+07	6.826e+00	Zero_10	4.861e+09	-6.236e+09	-8.133e-01
ole_2	-7.440e+05	-1.013e+07	6.826e+00	Zero_11	6.165e+08	8.165e+09	-6.640e+06
ole_3	-2.163e+06	1.394e+07	3.261e+00	Zero_12	6.165e+08	-8.165e+09	-6.640e+06
ole_4	-2.163e+06	-1.394e+07	3.261e+00	Zero_13	-4.001e+09	7.503e+09	1.063e+00
ole_5	-1.435e+06	1.954e+07	6.826e+00	Zero_14	-4.001e+09	-7.503e+09	1.063e+00
ole_6	-1.435e+06	-1.954e+07	6.826e+00	Zero_15	-7.528e+09	4.457e+09	5.811e-01
				Zero_16	-7.528e+09	-4.457e+09	5.811e-01
eros(Hz)				Zero_17	-8.845e+09	0.000e+00	5.000e-01
	Real	Imaginary	Qfactor	Network func	tion gain(magnitude)	= 4.157e+02	
ero_1	-1.017e+04	0.000e+00	5.000e-01		,		
ero_2	-1.413e+04	0.000e+00	5.000e-01	C_BW=1e-09,R	BW=1000		
ero_3	-1.962e+04	0.000e+00	5.000e-01	C_DM=10=05, K	_5#=1000		
etwork funct	ion gain(magnitude)	= 9.875e+22		Poles(Hz)			
					Real	Imaginary	Qfactor
_BW=1e-10,R_	BW=1000			Pole_1	6.938e+05	9.474e+06	-6.846e+06
				Pole_2	6.938e+05	-9.474e+06	-6.846e+06
oles(Hz)				Pole_3	7.260e+05	1.314e+07	-9.066e+06
				Pole_4	7.260e+05	-1.314e+07	-9.066e+06
	Real	Imaginary	Qfactor	Pole_5	2.839e+06	1.645e+07	-2.939e+06
ole_1	-5.822e+05	1.010e+07	8.689e+00	Pole_6	2.839e+06	-1.645e+07	-2.939e+06
ole_2	-5.822e+05	-1.010e+07	8.689e+00	Pole_7	-4.395e+07	0.000e+00	5.000e-01
ole_3	-1.864e+06	1.397e+07	3.782e+00	Pole_8	-5.059e+07	0.000e+00	5.000e-01
ole_4	-1.864e+06	-1.397e+07	3.782e+00	Pole_9	-5.261e+07	0.000e+00	5.000e-01
ole_5	-8.358e+05	1.942e+07	1.163e+01	Pole_10	-7.978e+07	0.000e+00	5.000e-01
ole_6	-8.358e+05	-1.942e+07	1.163e+01	Pole_11	-8.275e+07	0.000e+00	5.000e-01
ole_7	-5.084e+08	0.000e+00	5.000e-01	Pole_12	-8.417e+07	0.000e+00	5.000e-01
ole_8	-5.197e+08	0.000e+00	5.000e-01	Pole_13	-1.393e+08	0.000e+00	5.000e-01
ole_9	-5.251e+08	0.000e+00	5.000e-01	Pole_14	-1.622e+08	0.000e+00	5.000e-01
ole_10	-7.137e+08	0.000e+00	5.000e-01	Pole_15	-1.631e+08	0.000e+00	5.000e-01
ole_11	-7.502e+08	0.000e+00	5.000e-01	Pole_16	-1.654e+08	0.000e+00	5.000e-01
ole_12	-7.559e+08	0.000e+00	5.000e-01	Pole_17	-1.754e+08	0.000e+00	5.000e-01
ole_13	-1.393e+09	0.000e+00	5.000e-01	Pole_18	-1.810e+08	0.000e+00	5.000e-01
ole_14	-1.596e+09	0.000e+00	5.000e-01	Pole_19	-1.890e+08	0.000e+00	5.000e-01
ole_15	-1.596e+09	0.000e+00	5.000e-01	_			
ole_16	-1.598e+09	0.000e+00	5.000e-01	Zeros(Hz)			
ole_17	-1.610e+09	0.000e+00	5.000e-01	,			
ole_18	-1.616e+09	0.000e+00	5.000e-01		Real	Imaginary	Qfactor
ole_19	-1.626e+09	0.000e+00	5.000e-01	Zero_1	-9.561e+03	0.000e+00	5.000e-01
				Zero_2	-1.298e+04	0.000e+00	5.000e-01
eros(Hz)				Zero_3	-1.747e+04	0.000e+00	5.000e-01
				Zero_4	-1.695e+08	0.000e+00	5.000e-01
	Real	Imaginary	Ofactor	Zero_5	-1.734e+08	0.000e+00	5.000e-01
ero_1	-1.011e+04	0.000e+00	5.000e-01	Zero_6	-1.789e+08	0.000e+00	5.000e-01
ero_2	-1.400e+04	0.000e+00	5.000e-01	Zero_7	1.652e+09	0.000e+00	-5.000e-0
ero_2 ero_3	-1.4666+64 -1.938e+04	0.000e+00	5.000e-01	Zero_8	1.305e+09	1.014e+09	-6.333e-0
ero_3 ero_4	-1.603e+09	0.000e+00	5.000e-01	Zero_9	1.305e+09	-1.014e+09	-6.333e-0
				Zero_10	4.305e+08	1.613e+09	-1.939e+0
ero_5	-1.607e+09	0.000e+00	5.000e-01	Zero_10	4.305e+08	-1.613e+09	-1.939e+00
ero_6	-1.613e+09	0.000e+00	5.000e-01	Zero_11	-6.024e+08	1.583e+09	1.405e+00
ero_7	7.379e+09	2.326e+09	-5.243e-01	Zero_12 Zero_13	-6.024e+08	-1.583e+09	1.405e+00
ero_8	7.379e+09	-2.326e+09	-5.243e-01	Zero_13 Zero_14	-1.416e+09	9.631e+08	6.046e-01
ero_9	4.861e+09	6.236e+09	-8.133e-01	Zero_14 Zero_15	-1.416e+09	-9.631e+08	6.046e-01
ero_10	4.861e+09	-6.236e+09	-8.133e-01	2010_13			5.0466-61
	Figure 21 Pole	es & Zeros			Figure 2	20 Poles & Zeros	

#### We can see that there is a new poles and zeros appeared because of the non-ideality of op-amps.

• We can say that high quality factor of or system make this change more worth in our system.

•	<u>-15%</u>	<b>Nominal</b>	<u>15%</u>
Min Stopband Attenuation	1.3945	<u>1.433</u>	<u>1.398</u>
<b>Max Stopband Attenuation</b>	20.3	28.646	34.5

	<u>-2%</u>	<u>Nominal</u>	<u>2%</u>
Min Stopband Attenuation	<u>1.173</u>	<u>1.433</u>	<u>2.215</u>
Max Stopband Attenuation	28.21	28.646	29.0556

<u>Gain</u>	<u>100</u>	Nominal (10000)	<u>1000</u>
Min Stopband Attenuation	<u>5</u>	<u>1.433</u>	<u>1.75</u>
<b>Max Stopband Attenuation</b>	30.8	28.646	28.845

BW	<u>1M</u>	Nominal (Infinity)	<u>10M</u>
Min Stopband Attenuation	<u>17.3</u>	<u>1.75</u>	<u>1.822</u>
<b>Max Stopband Attenuation</b>	40.26	28.845	28.9

#### 4. Matlab Code

```
% Define the numerator and denominator coefficients for the transfer function H(s)
% These coefficients are specified for a high-order system.
numerator = [1.0055e+23, 0, 0, 0]; % Coefficients of the numerator polynomial of H(s)
denominator =
[1,54356436.5638108,2.81252429808991e+16,9.58909261436301e+23,2.22068017524791e+32,3.3886790896]
1806e+39,4.92231267110556e+47]; % Coefficients of the denominator polynomial of H(s)
% Create the transfer function H(s) using the 'tf' function
H = tf(numerator, denominator);
\mbox{\ensuremath{\$}} Compute the poles of the transfer function \mbox{\ensuremath{$H(s)$}} and convert them to \mbox{\ensuremath{$Hz$}}
% Poles are the roots of the denominator polynomial of the transfer function.
poles in_Hz = pole(H) / (2 * pi);
% Display the computed poles in Hz
disp('Poles of the transfer function in Hz:');
disp(poles in Hz);
^{\circ} Plot the Bode plot of the transfer function H(s)
% The Bode plot shows the magnitude and phase response of the system over a range of
frequencies.
figure:
bode(H), grid on;
title('Bode Plot of the Transfer Function H(s)');
xlabel('Frequency (Hz)');
ylabel('Phase (degrees)');
```

#### Our Repository and fall code

https://github.com/MGMA10/Biquad-BandPass-filter-based-on-Chebyshev-

#### Our MATLAB codes

https://github.com/MGMA10/Biquad-BandPass-filter-based-on-Chebyshev-/blob/main/prog.m https://github.com/MGMA10/Biquad-BandPass-filter-based-on-Chebyshev-/blob/main/IC\_P2.m