



GTU
Electronics Engineering

ELEC 331
Electronic Circuits 2

Fall Semester

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HW 5
Questions and Answers

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Assigned:

Due:

Answers Out:

Late Due:

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BJT Bias and SCTC

Malik 8.19

8.19 In Fig. P8.19, $\beta = 200$.

- Find I_B so that the transistor is biased at $I_C = 2.5$ mA.
- Find the numerical value of r_{π} .
- Write an equation for C so that the low-frequency pole is located at 100 rad/s.

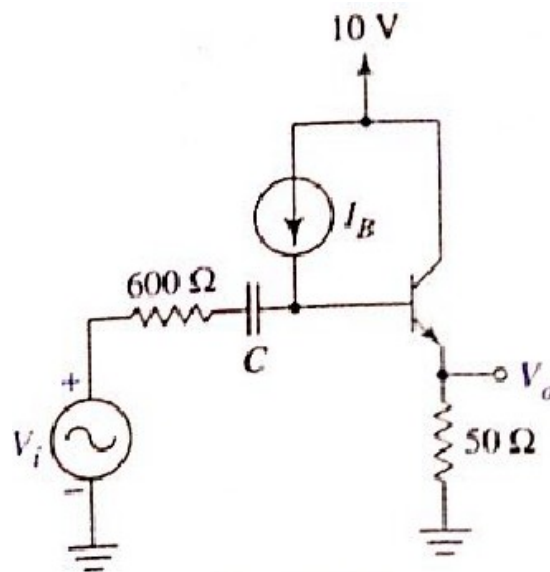


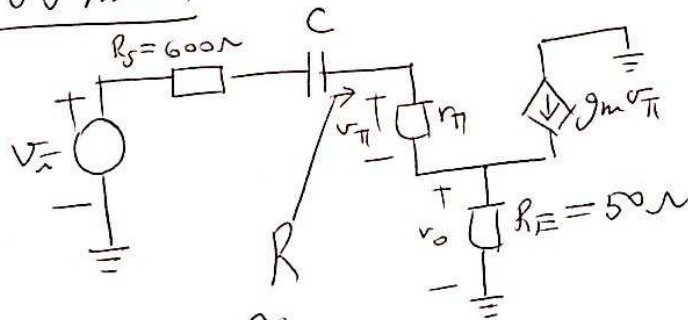
Figure P8.19

Necessary Knowledge and Skills: BJT biasing and small signal equivalent circuit, small signal impedance computations, method of SCTC (short-circuit time constants) for estimating the lower freq. cut off frequency (also interpreted as half-power freq.).

Mod 8.19

$$I_B = \frac{I_C}{\beta} = \frac{2.5 \text{ mA}}{200} = 1.25 \text{ mA} \cdot \frac{1}{100} = 12.5 \mu\text{A}$$

$$r_{\pi} = \frac{\beta}{g_m} = \frac{\beta V_T}{I_C} = \frac{200 \cdot 25 \text{ mV}}{2.5 \text{ mA}} = 2 \text{ k}\Omega$$

SS model

$$\begin{aligned} \frac{v_o}{v_s} &\approx \frac{R}{R_s + R + \frac{1}{C_s}} \cdot \frac{R_E}{\frac{1}{g_m} + R_E} \\ &= \frac{RC_s}{(R_s + R)C_s + 1} \cdot \frac{R_E}{\frac{1}{g_m} + R_E} \\ &= \frac{RC_s}{1 + \frac{1}{\frac{R_s + R}{C}}} \cdot \frac{R_E}{\frac{1}{g_m} + R_E} \end{aligned}$$

the pole is at $\Rightarrow \frac{1}{(R_s + R)C}$

①

min val for R

$$g_m = \frac{I_C}{V_T} = \frac{2.5 \text{ mA}}{25 \text{ mV}} = 100 \text{ mS}$$

Molik
8.19
cont.

$$R \approx (1 + g_m R_E) r_{\pi} \approx \cancel{10 \text{ Mega}\Omega} \quad R_f = 600 \Omega$$

$\swarrow \quad \downarrow \quad \uparrow$
 $100 \text{ mS} \quad 50 \Omega \quad 2 \text{ k}\Omega$

$$= 12 \text{ k}\Omega$$

$$R_f + R = 12.6 \text{ k}\Omega$$

$$\frac{1}{(12.6 \text{ k}\Omega)C} = 100 \text{ rad/s} \Rightarrow C = \frac{1}{(12.6 \text{ k}\Omega)(100 \text{ rad/s})}$$

$$= \frac{10^{-5}}{12.6} \text{ F}$$

$$\approx \frac{100}{12.5} \cdot 10^{-2} \cdot 10^{-5} \text{ F}$$

$$= 8 \times 10^{-7} = 0.8 \mu\text{F}$$

—————

BJT Bias and SCTC

Malik 8.20

8.20 Use short-circuit time constants to estimate the lower half-power frequency for Fig. P8.20; $\beta = 99$, $r_{\pi} = 100 \Omega$.

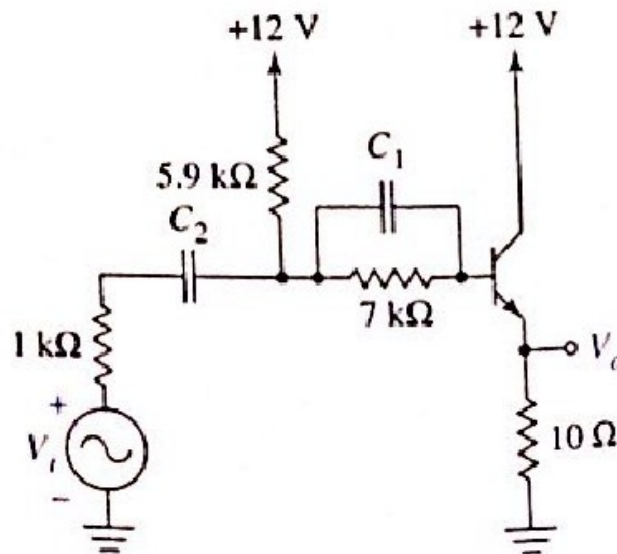


Figure P8.20

Necessary Knowledge and Skills: BJT biasing and small signal equivalent circuit, small signal impedance computations, method of SCTC (short-circuit time constants) for estimating the lower freq. cut off frequency (also interpreted as half-power freq.).

DC bias

$$I_E = (\beta + 1)I_B = 100I_B$$

$$(100I_B)(10\Omega) + 0.7 + (12.9k)I_B = 12V$$

$$(13.9k)I_B = 11.3V$$

$$I_B = \frac{11.3V}{13.9k\Omega}$$

$$I_E = 100I_B$$

time constant for C_2 (C_1 shorted)

$$\tau_2 = C_2 \left[R_S + R_1 \parallel \left[(1 + g_m R_E) r_{\pi} \right] \right]$$

time const. for C_1 (C_2 shorted)

$$\tau_1 = C_1 \left[R_2 \parallel \left[R_1 \parallel R_S + (1 + g_m R_E) r_{\pi} \right] \right]$$

$$W_L \approx \frac{1}{\tau_1} + \frac{1}{\tau_2}$$

method of short cir. time const.

lower half power freq

Note

$$R_J = 1k$$

$$R_E = 10\Omega$$

$$R_1 = 5.9k$$

$$R_2 = 7k$$

$$g_m = \frac{\beta}{r_{\pi}} = \frac{99}{100\Omega} = 990mS$$

$$\text{check } r_{\pi} = \frac{\beta V_T}{I_C}$$

$$= \frac{V_T}{I_B}$$

$$100\Omega = \frac{25mV}{I_B}$$

$$I_B = 0.25mA$$

does not check with the above value.

CS Amplifier Frequency Response

Sedra 4.94

4.94 In a particular MOSFET amplifier for which the mid-band voltage gain between gate and drain is -27 V/V, the NMOS transistor has $C_{gs} = 0.3$ pF and $C_{gd} = 0.1$ pF. What input capacitance would you expect? For what range of signal-source resistances can you expect the 3-dB frequency to exceed 10 MHz? Neglect the effect of R_G .

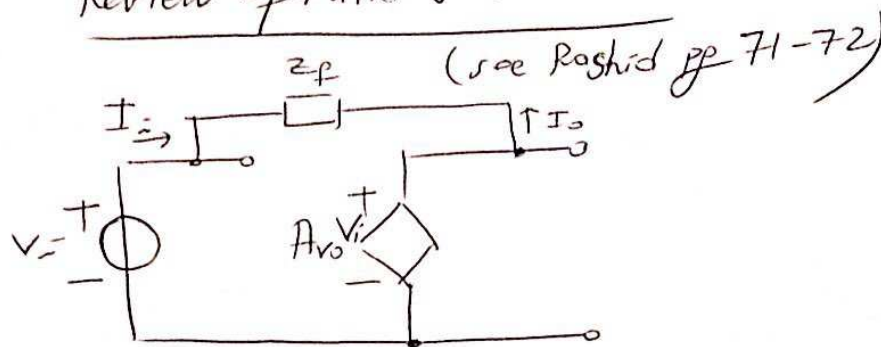
Note: Consider this question as of a common source amplifier configuration.

Additional Tasks: Review Miller's theorem, reprove it on paper.

Necessary Knowledge and Skills: Miller's effect in common source configuration, dominant pole determined by the Miller effect, OCTC method for computing the approximate high freq. cut-off, equivalent Thevenin impedance calculations, design for increasing bandwidth.

Review of Miller's theorem

Sedra
4.94



Z_f is going to be transformed into two separate impedances. I_i and I_o will each be required to flow into these generated impedances.

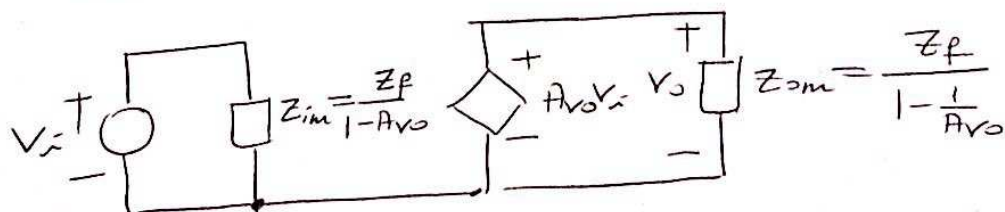
$$I_i = \frac{V_i - V_o}{Z_f} = \frac{V_i - A_{vo} V_i}{Z_f} = V_i \frac{(1 - A_{vo})}{Z_f}$$

$$\frac{V_i}{I_i} = \frac{Z_f}{1 - A_{vo}}$$

$$I_o = \frac{V_o - V_i}{Z_f} = \frac{V_o - \frac{V_o}{A_{vo}}}{Z_f}$$

$$\frac{V_o}{I_o} = \frac{Z_f}{1 - \frac{1}{A_{vo}}}$$

then we have



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For a typical amplifier assume

$$A_{Vo} < 0 \quad \text{and} \quad |A_{Vo}| > 1$$

and let $Z_f = \frac{1}{sC_f}$ (a capacitance)

then

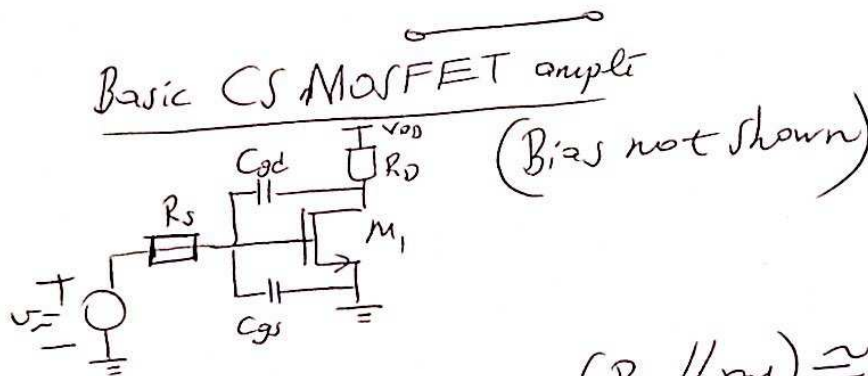
$$Z_{in} = \frac{1}{sC_f(1-A_{Vo})}$$

$$Z_{out} = \frac{1}{sC_f(1-\frac{1}{A_{Vo}})}$$

Corresponds to
a capacitance $\Rightarrow C_f(1-A_{Vo})$
(amplified)

Corresponds to
 $\Rightarrow C_f(1-\frac{1}{A_{Vo}})$
(if $|A_{Vo}| \gg 1$
then $\approx C_f$)

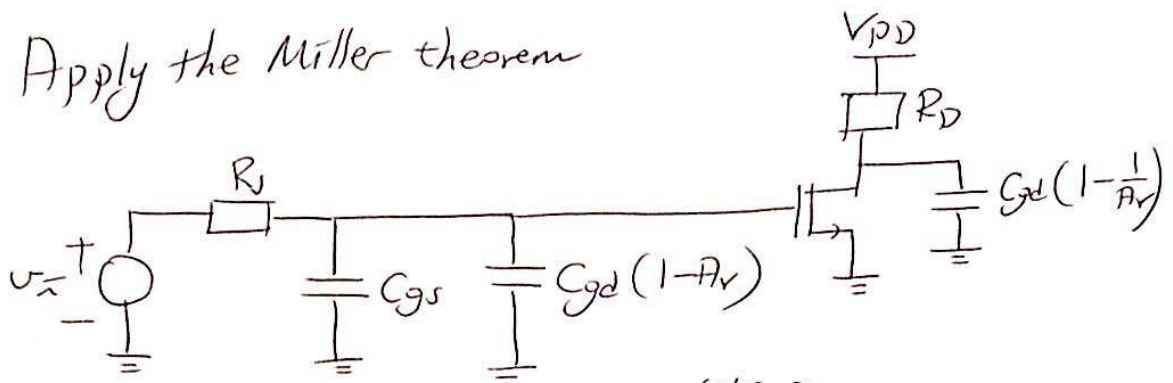
Basic CS MOSFET ampli



midband voltage gain $\Rightarrow -g_{m1}(R_D \parallel r_{o1}) \approx -g_{m1}R_D$
OR if R_D is replaced by a current source
with $R_{out} \gg r_{o1}$
then we have for the gain $\Rightarrow -g_{m1}r_{o1}$

We are given $-g_{m1} R_D$ or $-g_{m1} r_{o1}$ Sedra
4.94
cont.
as $A_V = -27 \text{ V/V}$

Apply the Miller theorem



Apply the method of OCTC ($v_{in}^{\text{set}} = 0$)

\Rightarrow the capacitance $C_1 = C_{gs} + C_{gd}(1 - A_V)$
sees $R_1 = R_S$ ($C_2 = (1 - \frac{1}{A_V})C_{gd}$ is open cir)

time constant $\tau_1 = C_1 R_1 = [C_{gs} + C_{gd}(1 - A_V)] R_S$

\Rightarrow the capacitance $C_2 = C_{gd}(1 - \frac{1}{A_V})$
sees $R_2 = R_D \parallel r_{o1}$ (could approximate to R_D or r_{o1} depending on the values)

time constant $\tau_2 = C_2 R_2$
 $= [C_{gd}(1 - \frac{1}{A_V})] [R_D \parallel r_{o1}]$

high
freq
cutoff

$$\omega_{3dB} \approx \frac{1}{\tau_1 + \tau_2} = \frac{1}{C_1 R_1 + C_2 R_2}$$

In this question it is expected that

$$\tau_1 \gg \tau_2$$

then $\omega_{3dB} \approx \frac{1}{\tau_1}$

Sedra
4.94
cont.

Numerical calculations

$$\omega_{3dB} = 2\pi f_{3dB} = 2\pi(10\text{MHz}) < \frac{1}{R_S [C_{gs} + C_{gd}(1 - A_v)]} = \frac{1}{\tau_1}$$

\downarrow \downarrow \downarrow
 0.3pF 0.1pF -27V/V

calculate a range for R_S

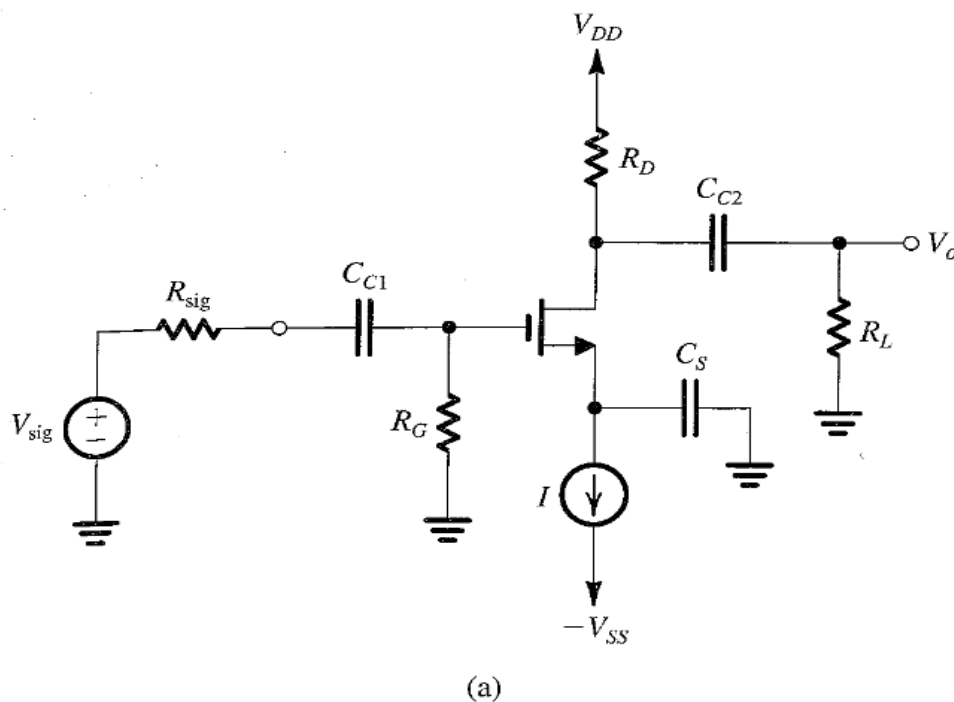
R_S should be smaller than some value

for $\omega_{3dB} > 2\pi(10\text{MHz})$

CS Amplifier OCTC, SCTC and Miller's Effect

Sedra 4.95

D4.95 In a FET amplifier, such as that in Fig. 4.49(a), the resistance of the source $R_{\text{sig}} = 100 \text{ k}\Omega$, amplifier input resistance (which is due to the biasing network) $R_{\text{in}} = 100 \text{ k}\Omega$, $C_{gs} = 1 \text{ pF}$, $C_{gd} = 0.2 \text{ pF}$, $g_m = 3 \text{ mA/V}$, $r_o = 50 \text{ k}\Omega$, $R_D = 8 \text{ k}\Omega$, and $R_L = 10 \text{ k}\Omega$. Determine the expected 3-dB cutoff frequency f_H and the midband gain. In evaluating ways to double f_H , a designer considers the alternatives of changing either R_{out} or R_{in} . To raise f_H as described, what separate change in each would be required? What midband voltage gain results in each case?



CS Amplifier OCTC, SCTC and Miller's Effect

Sedra 4.95

Note: This is a common source configuration.

Additional Tasks: Apply the SCTC method for computing the low freq. cut-off, iterate over the AC coupling capacitors, leave results in terms of the parameters used.

Necessary Knowledge and Skills: OCTC methods for computing the high freq cut-off, Thevenin equivalent impedance calculations, small signal equivalent circuits, bandwidth and gain trade-off, gain bandwidth product calculations, Miller's effect.

Sedra 4.95

Compute low freq cutoff (SCTC method)

\Rightarrow Note that V_{sig} is set to 0,
 V_{DD} and V_S are set to ∞
 I is open cir.

$$\Rightarrow \tau_{e,1} = C_{c1} \underbrace{R_{C_{c1}}}_{\parallel R_{sig} + R_G} \quad (C_{c2} \text{ and } C_S \text{ are short cir})$$

$$\Rightarrow \tau_{e,2} = C_{c2} \underbrace{R_{C2}}_{(R_D \parallel r_o + R_L)} \quad (C_{c1} \text{ and } C_S \text{ are short cir})$$

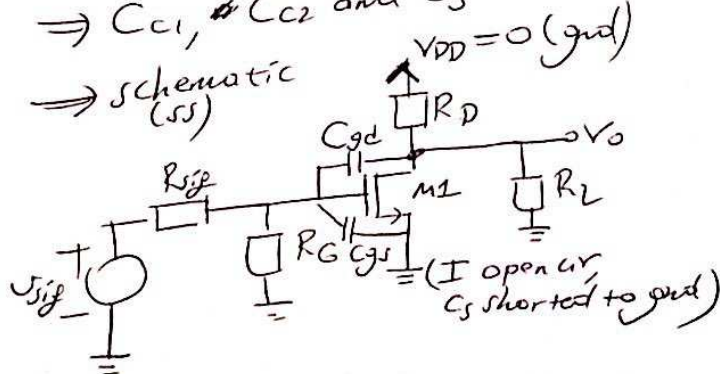
$$\Rightarrow \tau_{e,3} = C_S \underbrace{R_{C_S}}_{1/g_m} \quad (C_{c1} \text{ and } C_{c2} \text{ are short cir})$$

$$\Rightarrow \omega_L = \sum_{n=1}^3 \frac{1}{\tau_{e,n}} = \frac{1}{\tau_1} + \frac{1}{\tau_2} + \frac{1}{\tau_3}$$

Compute high freq cutoff (OCTC method)

$\Rightarrow C_{c1}, C_{c2}$ and C_S are effectively short cir

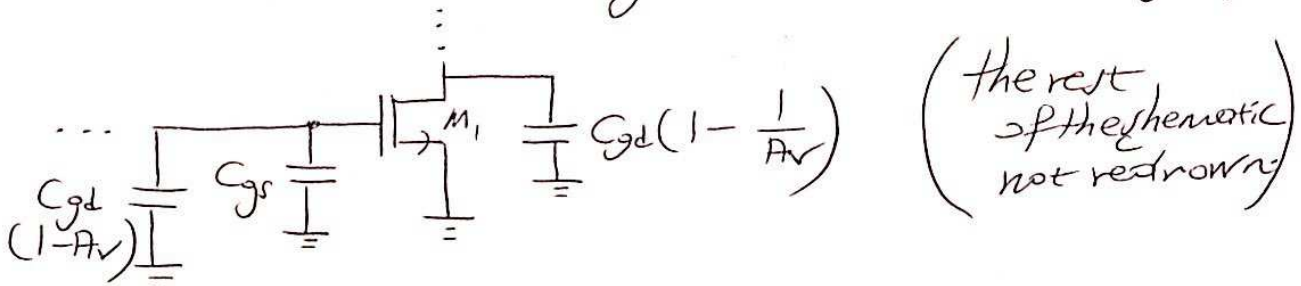
\Rightarrow schematic (ss)



⇒ Use Miller's theorem, but compute the midband gain first.

Sedra
4.95
cont.

$$A_V = \text{midband voltage gain} = \frac{R_G}{R_{sig} + R_G} (-g_m) [R_D \parallel R_L \parallel r_o] < 0 \quad (\text{negative})$$



⇒ Compute time constants

$$\tau_{H,1} = [C_{gs} + C_{gd}(1 - A_V)] [R_{sig} \parallel R_G]$$

(when $C_{gd}(1 - \frac{1}{A_V})$ is considered open cr.)

corresponds to this capacitance

$$\tau_{H,2} = [C_{gd}(1 - \frac{1}{A_V})] [R_D \parallel R_L \parallel r_o]$$

(when the other cap is considered open cr.)

$$W_H = \frac{1}{\sum_{n=1}^2 \tau_{H,n}} = \frac{1}{\tau_{H,1} + \tau_{H,2}}$$

if (as usually is the case)

$$\tau_{H,1} \gg \tau_{H,2} \Rightarrow \text{then } \tau_{H,1} + \tau_{H,2} \approx \tau_{H,1}$$

$$\text{then } W_H \approx \frac{1}{\tau_{H,1}}$$

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CE Amplifier OCTC, SCTC and Miller's Effect

Sedra 5.159

5.159 Consider the common-emitter amplifier of Fig. P5.159 under the following conditions: $R_{\text{sig}} = 5 \text{ k}\Omega$, $R_1 = 33 \text{ k}\Omega$, $R_2 = 22 \text{ k}\Omega$, $R_E = 3.9 \text{ k}\Omega$, $R_C = 4.7 \text{ k}\Omega$, $R_L = 5.6 \text{ k}\Omega$, $V_{CC} = 5 \text{ V}$. The dc emitter current can be shown to be $I_E \cong 0.3 \text{ mA}$, at which $\beta_0 = 120$, $r_o = 300 \text{ k}\Omega$, and $r_x = 50 \Omega$. Find the input resistance R_{in} and the midband gain A_M . If the transistor is specified to have $f_T = 700 \text{ MHz}$ and $C_\mu = 1 \text{ pF}$, find the upper 3-dB frequency f_H .

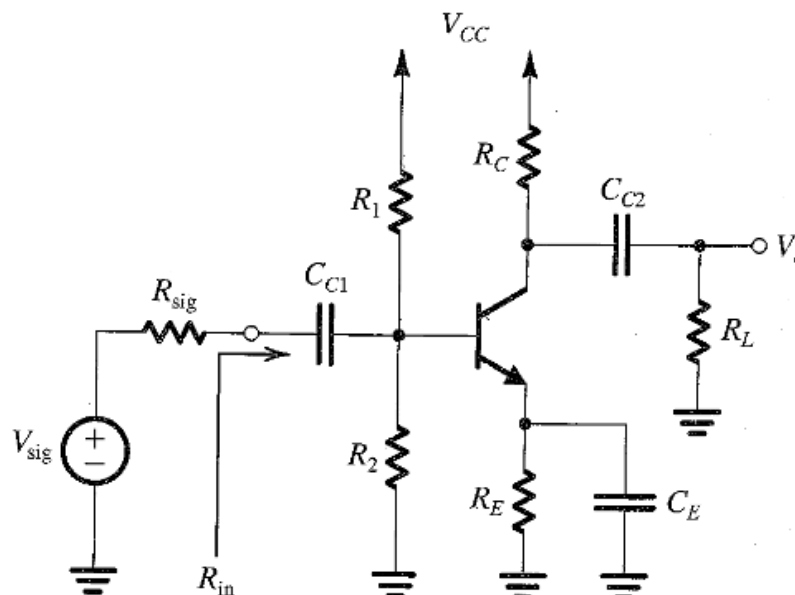


FIGURE P5.159

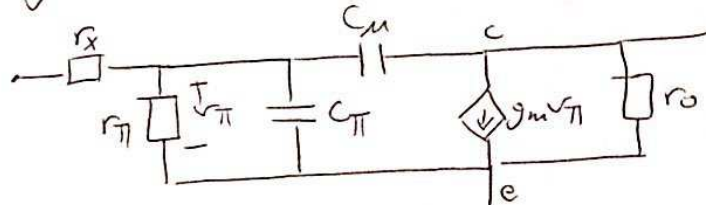
Notes: This is a common emitter configuration.

Additional Tasks: Apply the SCTC method for computing the low freq. cut-off, iterate over the AC coupling capacitors, leave results in terms of the parameters used.

Necessary Knowledge and Skills: OCTC methods for computing the high freq cut-off, Thevenin equivalent impedance calculations, small signal equivalent circuits, bandwidth and gain trade-off, gain bandwidth product calculations, Miller's effect.

Tasks in this questionSedra
5.159

- ⇒ Use the SCTC method to compute an approximate value for the low freq cut-off ω_L . Leave the result in terms of the parameters.
- ⇒ Compute the midband gain A_m
- ⇒ Use the OCTC method to compute an approximate value for the high freq cut-off ω_H . The result in terms of the parameters.
- ⇒ The high freq model for BJT is given as (naturally small signal)

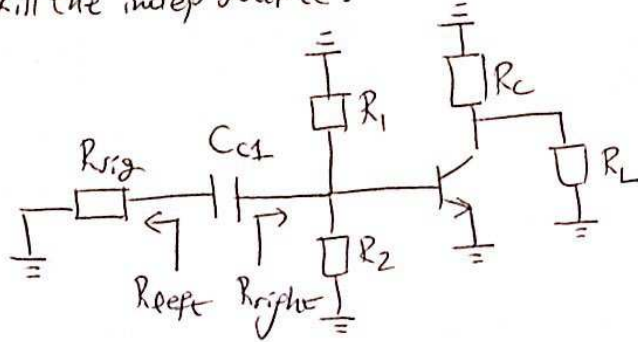


Compute the missing values for the parameters.

- ⇒ Compute ω_L , ω_H , A_m (midband gain) and R_{in} plugging in the values for the parameters.

SCTC for w_L Sedra
5.159

\Rightarrow given C_{C1} compute R_{C1} , short the other caps, kill the indep source.



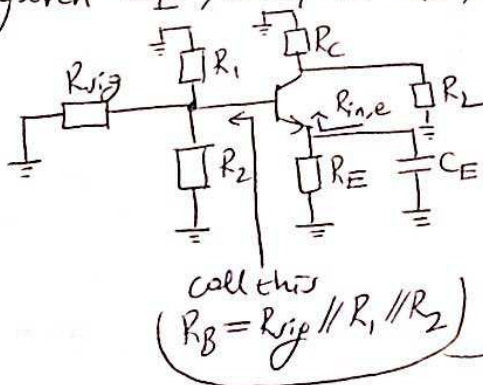
$$R_{C1} = R_{E_{eff}} + R_{right}$$

$$R_{E_{eff}} = R_{sig} \text{ (easy)}$$

$$R_{right} = R_1 // R_2 // r_{\pi} \text{ (easy)}$$

$$\text{time constant } \tau_{C1} = C_{C1} R_{C1}$$

\Rightarrow given C_E , compute R_{CE} , short other caps, kill indep src.



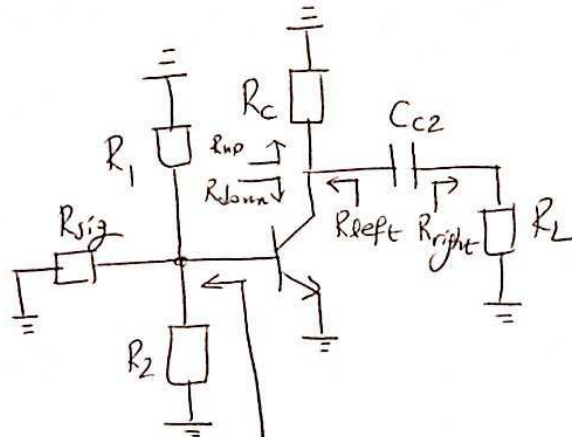
$$R_{in,e} = \frac{r_{\pi} + R_B}{1 + \beta}$$

(see derivations elsewhere, done many times)

$$\Downarrow$$

$$\text{Then } R_{CE} = R_{in,e} // R_E$$

$$\text{time constant } \tau_{CE} = C_E R_{CE}$$

SCTC for w_L (continued)Sadra
5-159 \Rightarrow given C_{c2} , compute R_{c2} , kill indep. src, short other caps.

$$R_{c2} = R_{left} + R_{right}$$

$$R_{right} = R_L$$

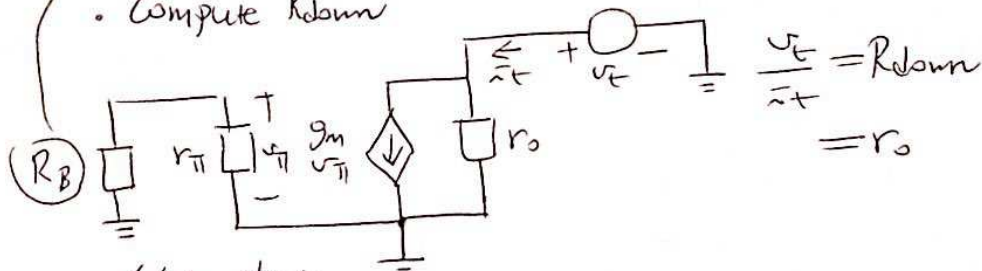
$$R_{up} = R_C$$

$$R_{left} = R_{up} \parallel R_{down}$$

$$R_{down} = ?$$

kill this

$$R_B = R_1 \parallel R_2 \parallel R_{sig}$$

• Compute R_{down} 

Note that
 there is no
 current over $r_{\pi} \Rightarrow v_{\pi} = 0 \Rightarrow g_m v_{\pi}$ open cir.

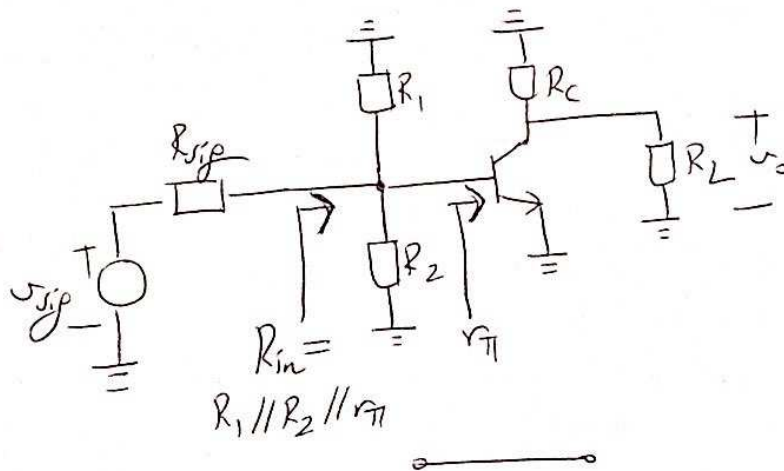
• time constant $\tau_{c2} = C_{c2} R_{c2}$

$$\text{SCTC formula} \Rightarrow w_L = \frac{1}{\tau_{c1}} + \frac{1}{\tau_{c2}} + \frac{1}{\tau_{cE}} \quad \left(\begin{array}{l} \text{all have} \\ \text{been} \\ \text{computed} \\ \text{above} \end{array} \right)$$

R_{in} (in midband computation)

Sedra
5.159

- \Rightarrow large valued C_{C1}, C_{C2}, C_E caps are all short cir in small signal in midband.
- \Rightarrow internal caps (BJT caps) are open cir in midband.
- \Rightarrow Draw schematic and compute R_{in}

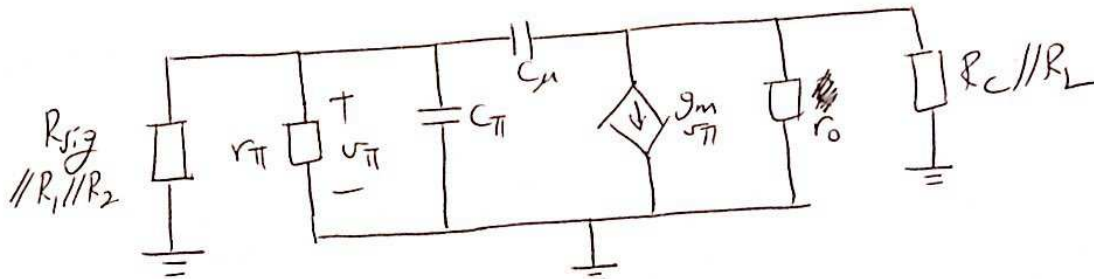
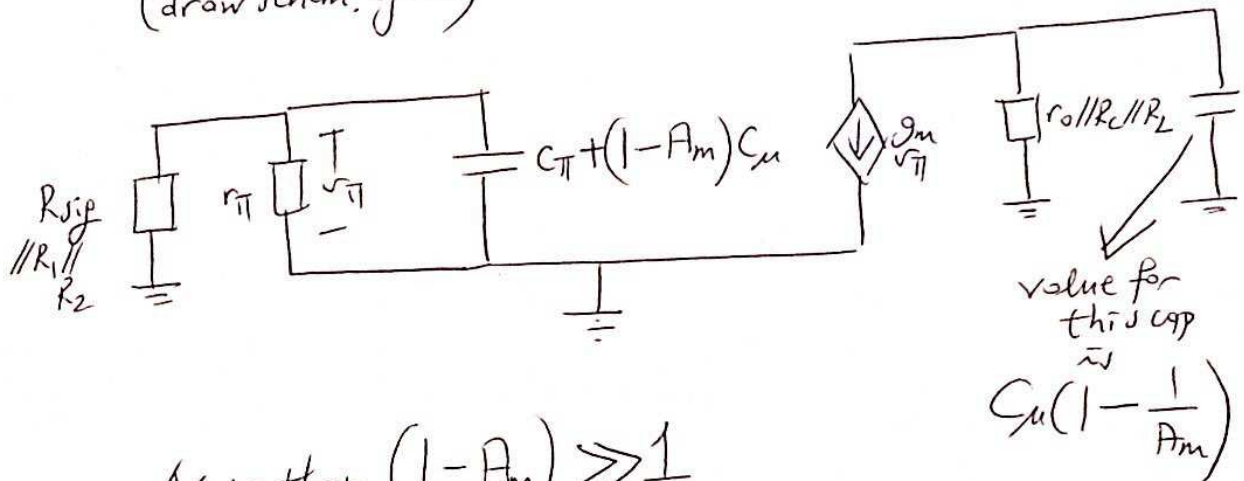


A_M (in midband)

- \Rightarrow coupling caps and C_E short cir in ss.
- \Rightarrow internal caps open cir.

$$\frac{v_o}{v_{sig}} = A_M = \underbrace{\frac{R_{in}}{R_{in} + R_{sig}}}_{\frac{v_b}{v_{sig}}} \underbrace{(-g_m)}_{\substack{\text{transcond.} \\ \text{of BJT}}} \underbrace{\left[R_C // r_o // R_L \right]}_{\substack{\text{load} \\ \frac{v_{out}}{i_{out}}}}$$

Note that R_{in} is computed above.

OCTC method for computing ω_H Sedra
5.159 \Rightarrow Draw schematic (kill indep. s.p.c., coupling caps are short cir) \Rightarrow Make use of Miller's thm
(draw schem. again)Note that $(1 - A_m) \gg 1$ and $1 < 1 - \frac{1}{A_m} < 2$ $(A_m \text{ computed above as midband gain})$ \Rightarrow call $C_1 = C_\pi + (1 - A_m)C_\mu$
 $C_2 = C_\mu(1 - \frac{1}{A_m})$ \Rightarrow open cir C_2 , compute R_{c1} corresponding to C_1

$$R_{c1} = R_{sig} \parallel R_1 \parallel R_2 \parallel r_\pi \quad \text{and} \quad \tau_{c1} = R_{c1} C_1$$

 \Rightarrow open cir C_1 , compute R_{c2} corresponding to C_2 Note that no current over $r_\pi \Rightarrow v_\pi = 0 \Rightarrow g_m v_\pi$ open cir
 $R_{c2} = r_o \parallel R_c \parallel R_L$ and $\tau_{c2} = R_{c2} C_2$

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5

OCTC for w_H computationSedra
5.159 \Rightarrow Apply the OCTC formula.

$$w_H = \frac{1}{\tau_{c1} + \tau_{c2}}$$

$\nwarrow \quad \nearrow$
 Both computed above

Numerical values \Rightarrow Left as an exercise but note the following:

$$g_m = \frac{I_C}{V_T} = \frac{\beta}{\beta+1} I_E \frac{1}{V_T} \rightarrow 25mV$$

$\underbrace{\quad}_{\text{very close to 1}}$
 since $\beta = 120$

- r_x can be neglected in the calculations, it is very small compared to $R_{sig} // R_1 // R_2$.

- f_T : transition frequency (see Rashid 504-506)

$$f_T = \frac{g_m}{2\pi(C_\pi + C_\mu)}$$

\nwarrow given
 \nearrow computed as above
 \nwarrow compute from this eqn.
 \nearrow given

BJT Differential Amplifier High-Freq. Response**Sedra 7.82**

7.82 A BJT differential amplifier operating with a 1-mA current source uses transistors for which $\beta = 100$, $f_T = 600$ MHz, $C_\mu = 0.5$ pF, and $r_x = 100 \Omega$. Each of the collector resistances is $10 \text{ k}\Omega$, and r_o is very large. The amplifier is fed in a symmetrical fashion with a source resistance of $10 \text{ k}\Omega$ in series with each of the two input terminals.

- (a) Sketch the differential half-circuit and its high-frequency equivalent circuit.
- (b) Determine the low-frequency value of the overall differential gain.
- (c) Use Miller's theorem to determine the input capacitance and hence estimate the 3-dB frequency f_H and the gain-bandwidth product.

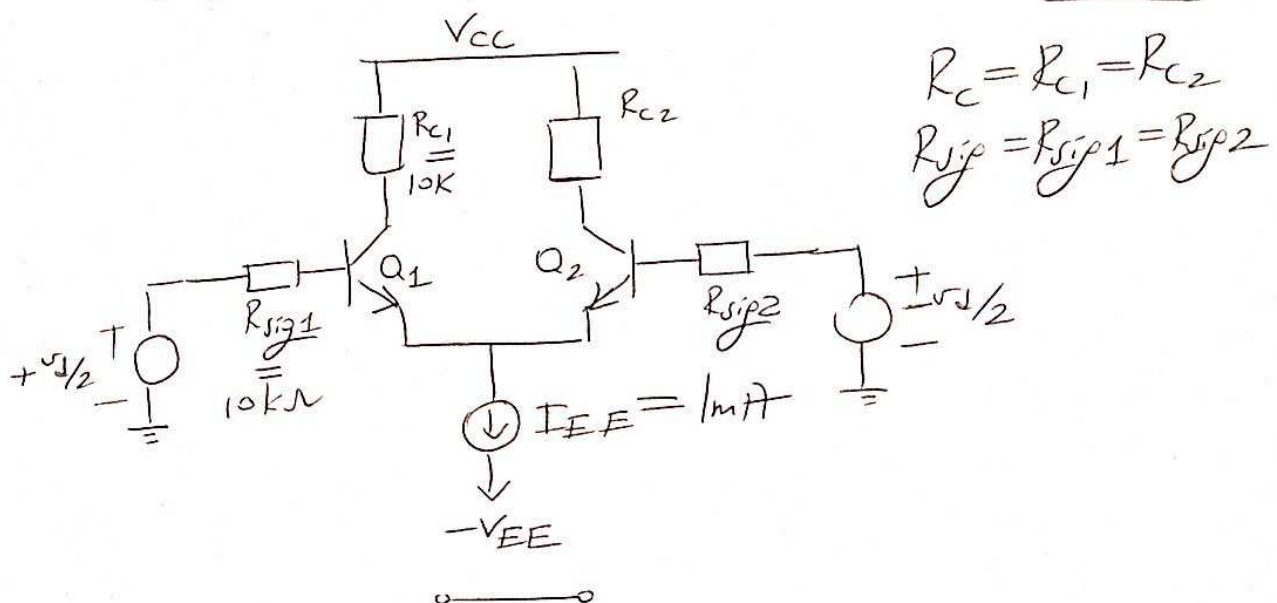
Notes: None.

Additional Tasks: None.

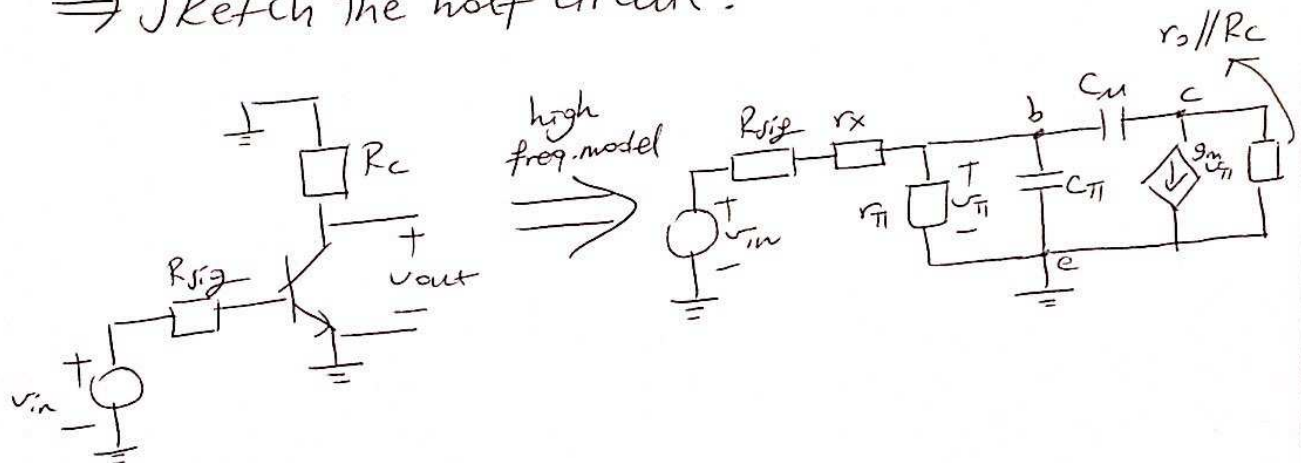
Necessary Knowledge and Skills: Differential amplifier, half circuit in differential mode, no emitter degeneration, small signal equivalent of BJT, differential voltage midband gain calculation, OCTC, Miller's effect, dominant pole approximation, gain bandwidth product.

⇒ Sketch the full schematic

Sedra
7.82



⇒ Sketch the half circuit.



⇒ Since $r_o \rightarrow +\infty$ (as given), we have $R_C // r_o = R_C$

⇒ midband gain of the common emitter stage

$$(A = \frac{v_c}{v_b} = -g_m R_C)$$

⇒ Overall midband gain $A_M = \frac{r_{\pi}}{r_{\pi} + R_{sig} + r_x} (-g_m R_C)$

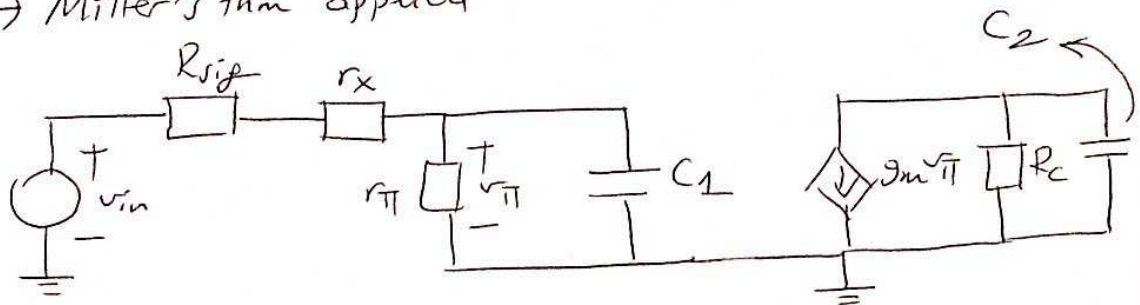
Handwritten annotations under the equation:
 $\frac{v_s}{v_{in}}$ under the first fraction, and $\frac{v_c}{v_b}$ under the second fraction.

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\Rightarrow Miller's thm and OCTC will be applied now to compute w_H or f_H .

Sedra
7-82

\rightarrow Miller's thm applied



$$C_1 = C_{\pi} + C_{\mu} \underbrace{(1 - A)}_{(1 + g_m R_c)}$$

$$C_2 = C_{\mu} \left(1 - \frac{1}{A}\right)$$

$$= C_{\mu} \left(1 + \frac{1}{g_m R_c}\right)$$

\rightarrow Apply OCTC (kill indep. src)

\cdot C_2 open cir, compute R_{c1} corresponding to C_1

$$R_{c1} = r_{\pi} \parallel (R_{sig} + r_x)$$

$$\tau_{c1} = R_{c1} C_1$$

\cdot C_1 open cir, compute R_{c2} corresponding to C_2

$$R_{c2} = R_c \quad (\text{no current through } r_{\pi} \Rightarrow v_{\pi} = 0)$$

$$\tau_{c2} = R_{c2} C_2$$

\cdot $w_H = \frac{1}{\tau_{c1} + \tau_{c2}} \rightarrow$ But in this config $\tau_{c1} \gg \tau_{c2}$ therefore $w_H \approx \frac{1}{\tau_{c1}}$

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Gain-Bandwidth product

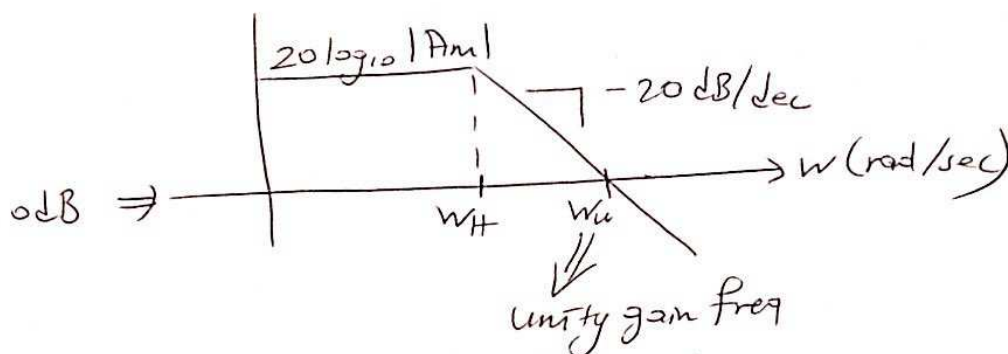
Sedra
7-82

$$GBW = |A_m| \cdot \frac{\omega_H}{2\pi}$$

$$= |A_m| \cdot f_H$$

$$\approx \left| \frac{r_\pi}{r_\pi + r_x + R_{sig}} (-g_m R_C) \right| \frac{1}{2\pi \tau_{c1}}$$

where τ_{c1} is given as above.



Note that $|A_m|_{\omega_H} = 1 \cdot \omega_u$

therefore $\frac{GBW}{2\pi} = \frac{\omega_u}{2\pi} = f_u$ (unity gain freq in Hz)

⇒ Numerical values comput. ⇒ exercise

Note the following:

$$I_{c1} = I_{c2} \approx \frac{I_{EE}}{2} = 0.5 \text{ mA}$$

$$g_m = \frac{I_c}{V_T} = \frac{0.5 \text{ mA}}{25 \text{ mV}}$$

$$f_T = \frac{g_m \rightarrow \text{computed}}{2\pi(C_{\mu} + C_{\pi})}$$

\downarrow given \downarrow given \downarrow compute

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