

Outline

- What is Classification?
- 2. K-Nearest-Neighbors
- 3. Decision Trees
- 4. Model Evaluation
- 5. Rule Learning
- 6. Naïve Bayes
- 7. Support Vector Machines
- 8. Artificial Neural Networks
- 9. Hyperparameter Selection

1. What is Classification?

 Goal: Previously unseen records should be assigned a class from a given set of classes as accurately as possible



– Approach:

- Given a collection of records (training set)
 - each record contains a set of attributes
 - one of the attributes is the class attribute (label) that should be predicted
- Learn a model for the class attribute as a function of the values of other attributes

– Variants:

- Binary classification (e.g. fraud/no fraud or true/false)
- Multi-class classification (e.g. low, medium, high)
- Multi-label classification (more than one class per record, e.g. user interests)

Introduction to Classification

A Couple of Questions:

- What is this?
- Why do you know?
- How have you come to that knowledge?

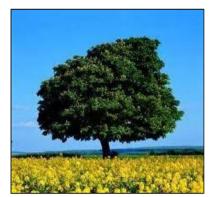


Introduction to Classification

- Goal: Learn a model for recognizing a concept, e.g. trees
- Training data:



"tree"



"tree"



"tree"



"not a tree"



"not a tree"



"not a tree"

Introduction to Classification

 We (or the learning algorithm) look at positive and negative examples (training data)

... and derive a model

e.g., "Trees are big, green plants that have a trunk and no wheels."

Goal: Classification of unseen instances















Tree?

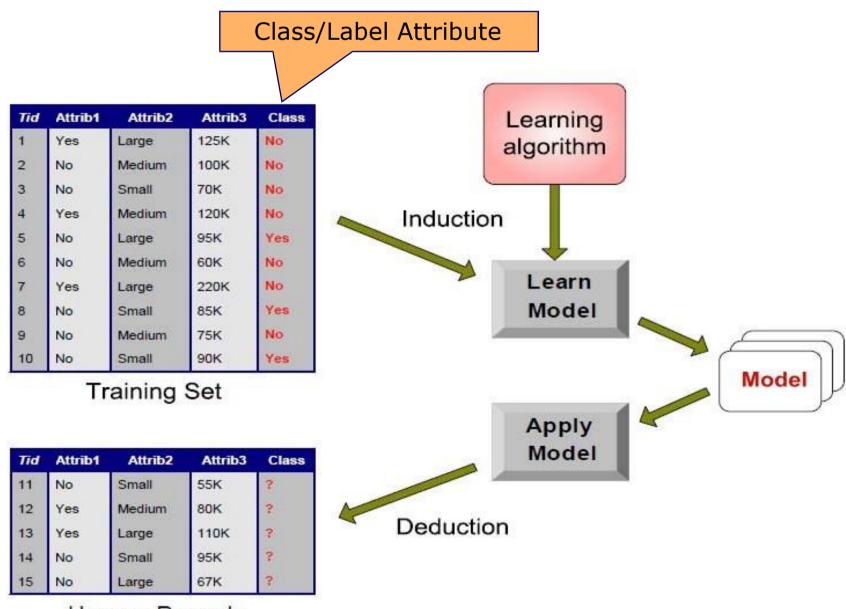
Tree?

Warning:

Models are only
approximating examples!

Not guaranteed to be
correct or complete!

Model Learning and Model Application Process



Unseen Records

Classification Examples

Credit Risk Assessment

- Attributes: your age, income, debts, ...
- Class: are you getting credit by your bank?

Marketing

- Attributes: previously bought products, browsing behavior
- Class: are you a target customer for a new product?

SPAM Detection

- Attributes: words and header fields of an e-mail
- Class: regular e-mail or spam e-mail?

Identifying Tumor Cells

- Attributes: features extracted from x-rays or MRI scans
- Class: malignant or benign cells

Classification Techniques

- 1. K-Nearest-Neighbors
- 2. Decision Trees
- 3. Rule Learning
- 4. Naïve Bayes
- 5. Support Vector Machines
- 6. Artificial Neural Networks
- 7. Deep Neural Networks
- 8. Many others ...

2. K-Nearest-Neighbors

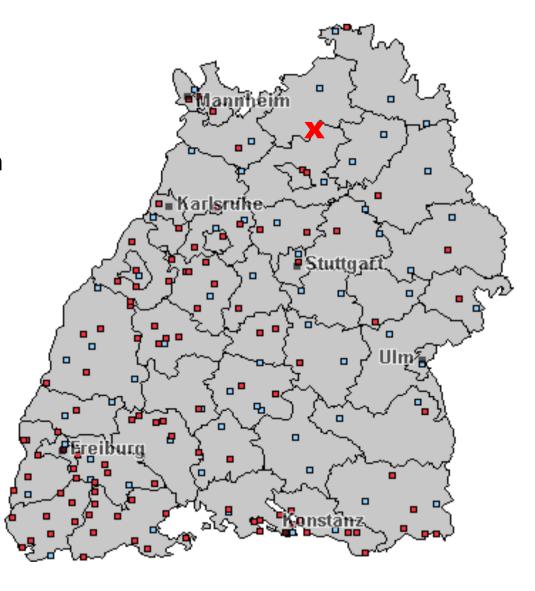
Example Problem

- Predict the current weather in a certain place
- where there is no weather station
- How could you do that?



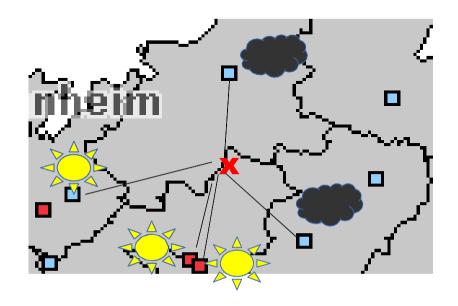






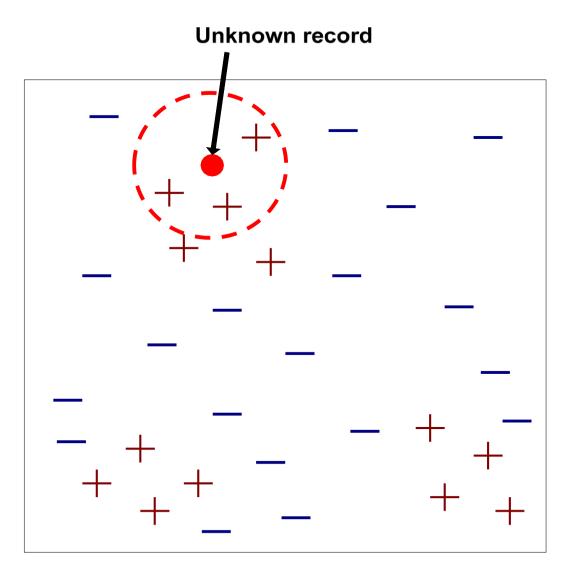
Basic Idea

- Use the average forecast of the nearest stations
- Example:
 - 3x sunny
 - 2x cloudy
 - result = sunny



- This approach is called K-Nearest-Neighbors
 - where k is the number of neighbors to consider
 - in the example: k=5
 - in the example: "near" denotes geographical proximity

K-Nearest-Neighbors Classifiers

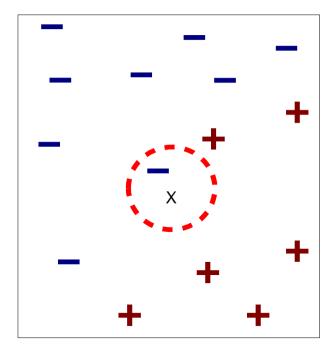


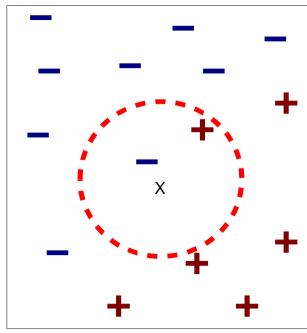
Require three things

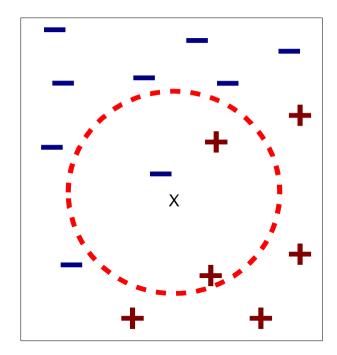
- A set of stored records
- A distance measure to compute distance between records
- The value of k, the number of nearest neighbors to consider
- To classify an unknown record:
 - 1. Compute distance to each training record
 - 2. Identify k-nearest neighbors
 - 3. Use class labels of nearest neighbors to determine the class label of unknown record
 - by taking majority vote or
 - by weighing the vote according to distance

Examples of K-Nearest Neighbors

The k-nearest neighbors of a record x are data points that have the k smallest distances to x







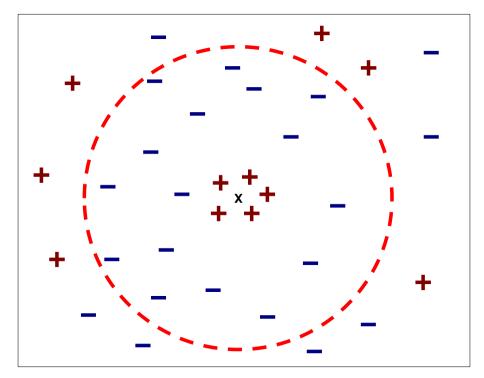
(a) 1-nearest neighbor

(b) 2-nearest neighbor

(c) 3-nearest neighbor

Choosing a Good Value for K

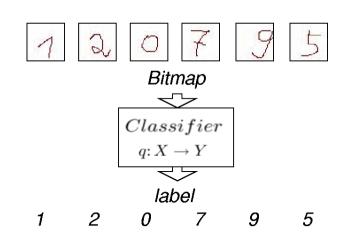
- If k is too small, the result is sensitive to noise points
- If k is too large, the neighborhood may include points from other classes



- Rule of thumb: Test k values between 1 and 20
 - setup: see section on Hyperparameter Selection

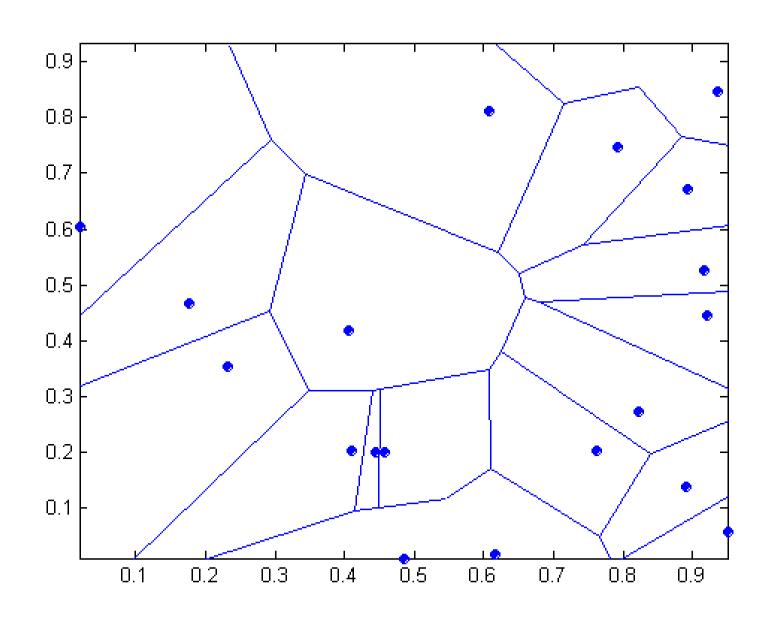
Discussion of K-Nearest-Neighbor Classification

- Often very accurate
 - for instance for optical character recognition (OCR)
- ... but slow
 - as unseen record needs to be compared to all training examples

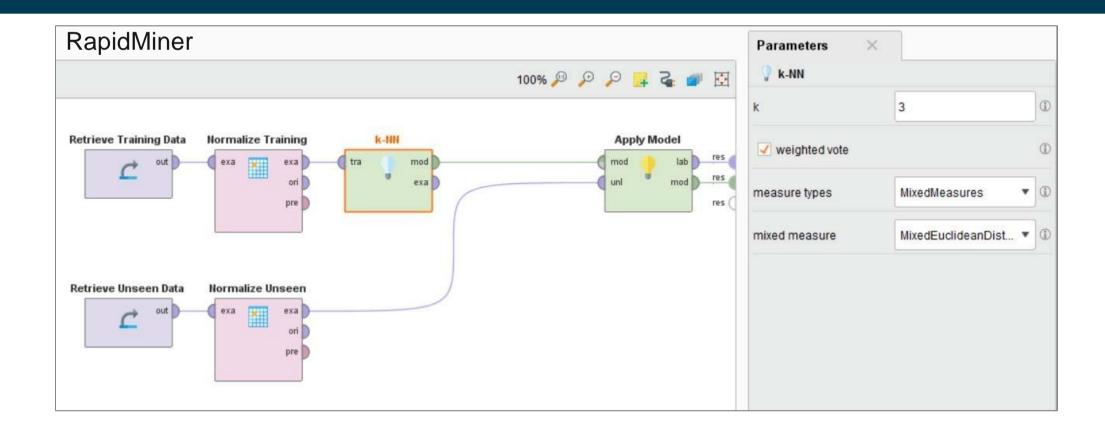


- Results depend on choosing a good proximity measure
 - attribute weights, asymmetric binary attributes, ...
 - see slide set Cluster Analysis
- KNN can handle decision boundaries which are not parallel to the axes (unlike decision trees)

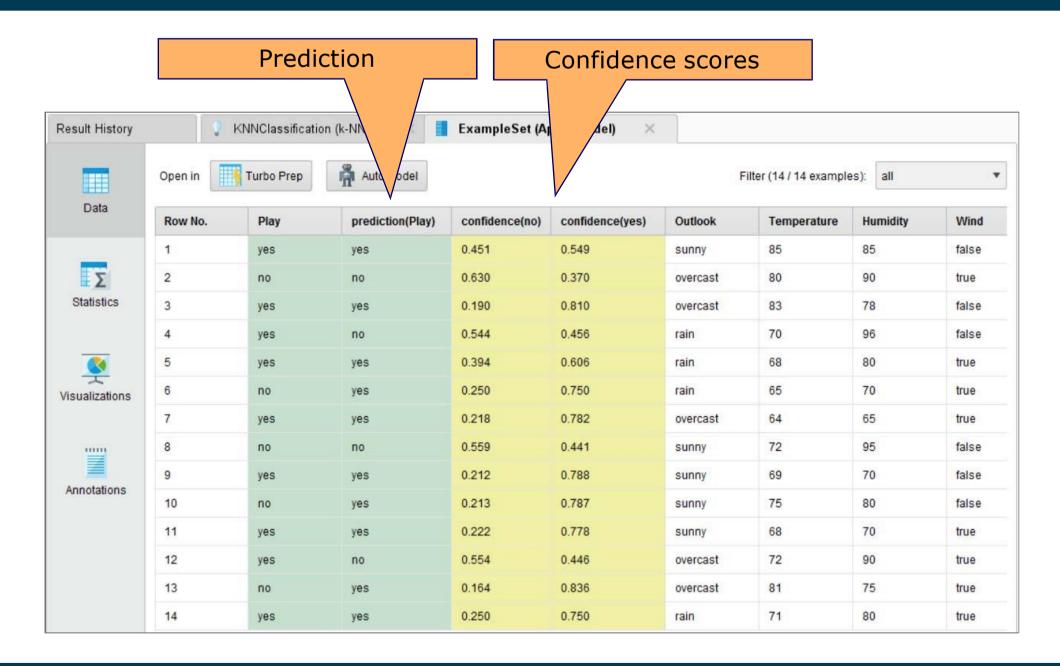
Decision Boundaries of a 1-NN Classifier



KNN Classification in RapidMiner and Python



Resulting Dataset



Lazy versus Eager Learning

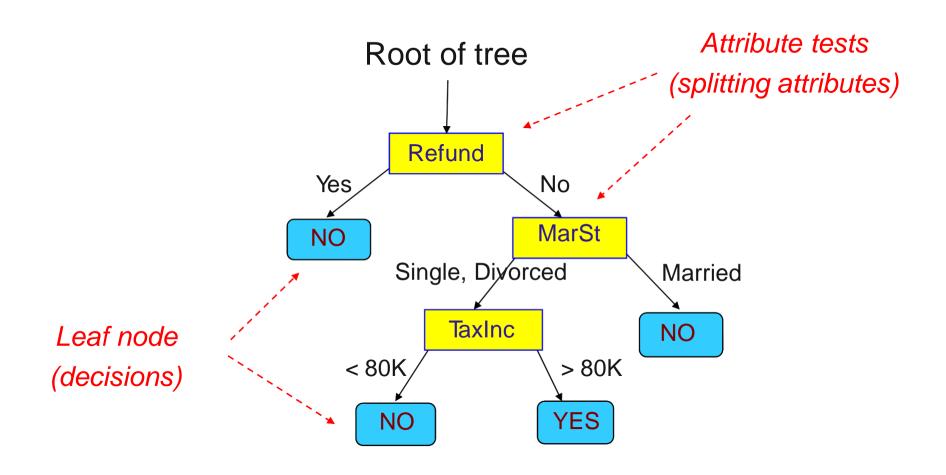
Lazy Learning

- Instance-based learning approaches, like KNN, are also called lazy learning as no explicit knowledge (model) is learned
- Single goal: Classify unseen records as accurately as possible

Eager Learning

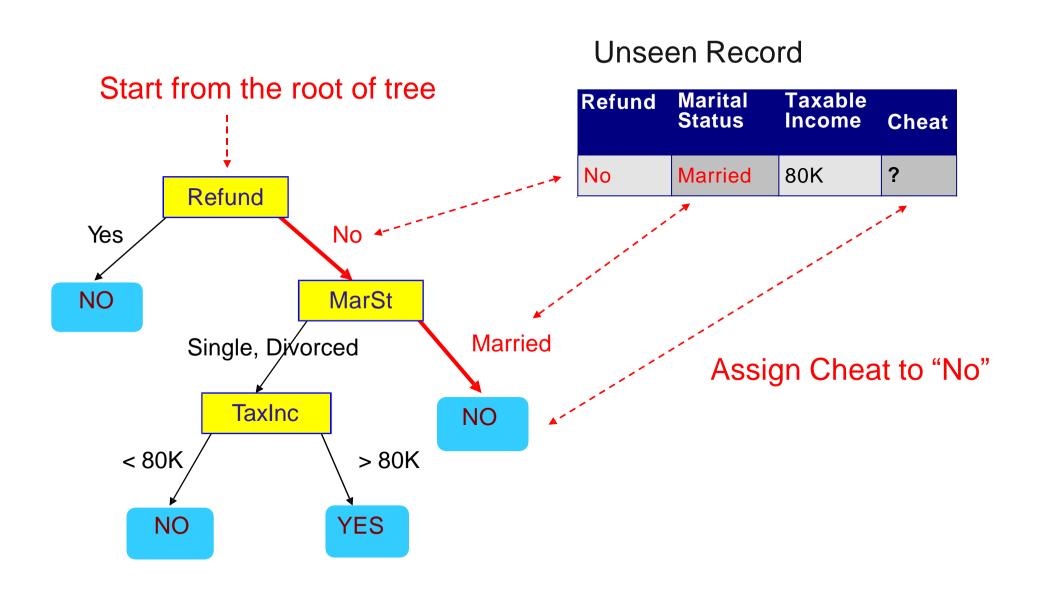
- but actually, we might have two goals
 - 1. classify unseen records
 - 2. understand the application domain as a human
- Eager learning approaches generate models that are (might be) interpretable by humans
- Examples of eager techniques: decision tree learning, rule learning

3. Decision Tree Classifiers

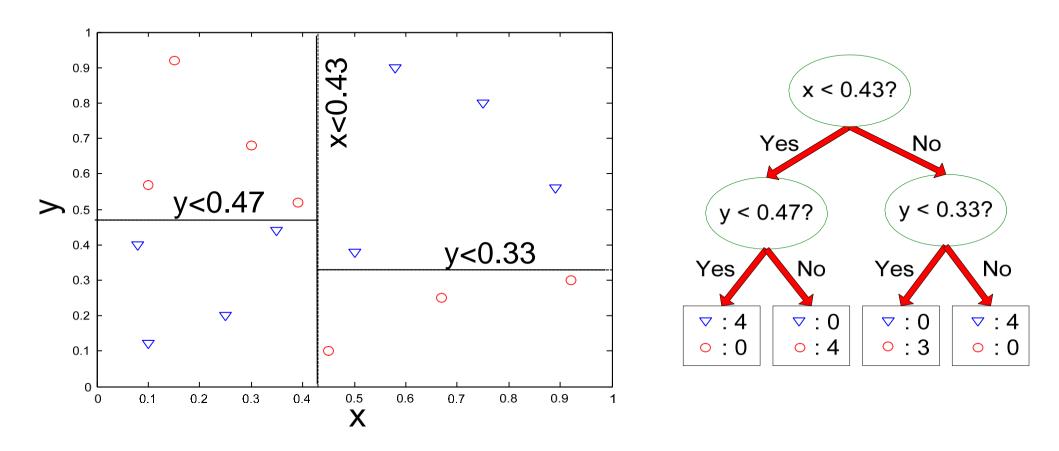


Decision trees encode a procedure for taking a classification decision

Applying a Decision Tree to Unseen Data



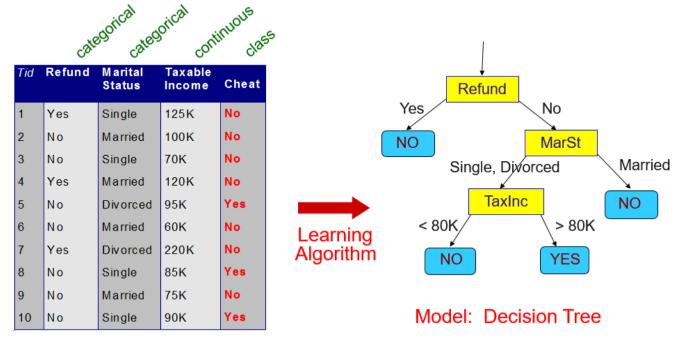
Decision Boundary



The decision boundaries are parallel to the axes because the test condition involves a single attribute at-a-time

Learning a Decision Tree

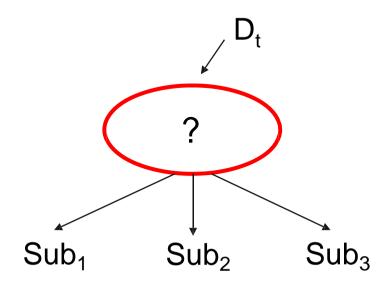
- How to learn a decision tree from training data?
 - finding an optimal decision tree is NP-hard
 - tree building algorithms thus use a greedy, top-down, recursive partitioning strategy to induce a reasonable solution
- Many different algorithms have been proposed:
 - Hunt's Algorithm
 - ID3
 - C4.5
 - CHAID



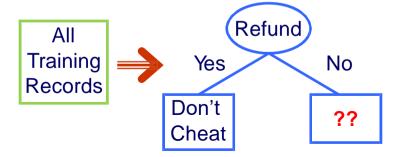
Training Data

Hunt's Algorithm

- Let D_t be the set of training records that reach a node t
- Generate leaf node or attribute test:
 - if D_t only contains records that belong to the same class y_t, then t is a leaf node labeled as y_t
 - if D_t contains records that belong to more than one class, use an attribute test to split the data into subsets having a higher purity.
 - for all possible tests: calculate purity of the resulting subsets
 - choose test resulting in highest purity
- Recursively apply this procedure to each subset



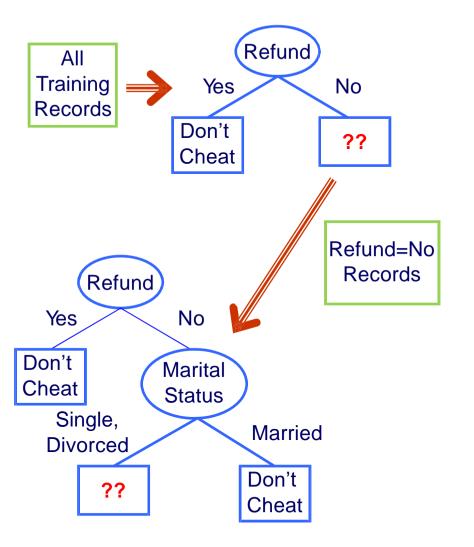
Hunt's Algorithm – Step 1



- We calculate the purity of the resulting subsets for all possible splits
 - Purity of split on Refund
 - Purity of split on Marital Status
 - Purity of split on Taxable Income
- 2. We find the split on Refund to produce the purest subsets

Tid	Refund	Marital Status	Taxable Income	Cheat	
1	Yes	Single	125K	No	
2	No	Married	100K	No	
3	No	Single	70K	No	
4	Yes	Married	120K	No	
5	No	Divorced	95K	Yes	
6	No	Married	60K	No	
7	Yes	Divorced	220K	No	
8	No	Single	85K	Yes	
9	No	Married	75K	No	
10	No	Single	90K	Yes	

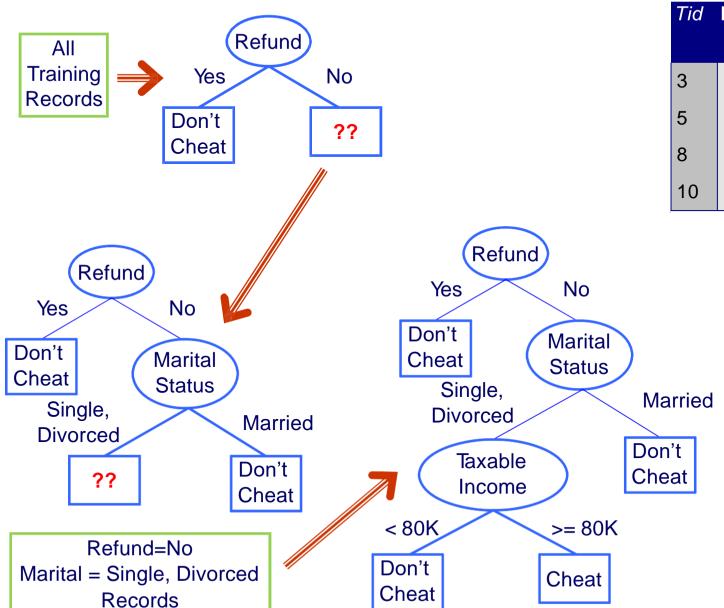
Hunt's Algorithm – Step 2



Tid	Refund	Marital Status	Taxable Income	Cheat	
2	No	Married	100K	No	
3	No	Single	70K	No	
5	No	Divorced	95K	Yes	
6	No	Married	60K	No	
8	No	Single	85K	Yes	
9	No	Married	75K	No	
10	No	Single	90K	Yes	

- We further examine the Refund=No records
- 2. Again, we test all possible splits
- 3. We find the split on Marital Status to produce the purest subsets

Hunt's Algorithm – Step 3



Tid	Refund	Marital Status	Taxable Income	Cheat	
3	No	Single	70K	No	
5	No	Divorced	95K	Yes	
8	No	Single	85K	Yes	
10	No	Single	90K	Yes	

- We further examine the Marital Status=Single or =Divorced records
- We find a split on
 Taxable Income
 to produce pure subsets
- We stop splitting as no sets containing different classes are left

Design Issues for Learning Decision Trees

1. How should training records be split?

- How to specify the attribute test condition?
 - Depends on number of ways to split: 2-way split, multi-way split
 - Depends on attribute data type: nominal, ordinal, continuous
- How to determine the best split?
 - Different purity measures can be used

2. When should the splitting procedure stop?

- Shallow trees might generalize better to unseen records
- Fully grown trees might overfit training data

Splitting Based on Nominal Attributes

Multi-way split: Use as many partitions as distinct values

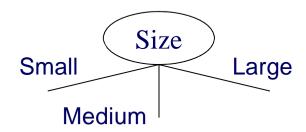


Binary split: Divides values into two subsets

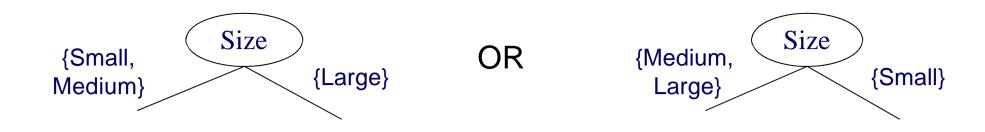


Splitting Based on Ordinal Attributes

Multi-way split: Use as many partitions as distinct values



 Binary split: Divides values into two subsets while keeping the order

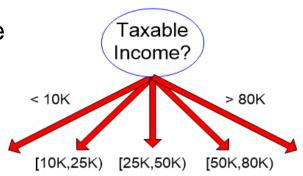


Splitting Based on Continuous Attributes

- Different ways of handling continuous attributes
 - Discretization to form an ordinal categorical attribute
 - equal-interval binning
 - · equal-frequency binning
 - binning based on user-provided boundaries



- usually sufficient in practice
- find the best splitting border v based on a purity measure (see below)
- can be compute intensive



(ii) Multi-way split



(i) Binary split

Discretization Example

- Values of the attribute, e.g., age of a person:
 - 0, 4, 12, 16, 16, 18, 24, 26, 28
- Equal-interval binning for bin width of e.g., 10:
 - Bin 1: 0, 4

- [-,10) bin
- Bin 2: 12, 16, 16, 18 [10,20] bin
- Bin 3: 24, 26, 28
- [20,+) bin
- denote negative infinity, + positive infinity
- Equal-frequency binning for bin density of e.g., 3:
 - Bin 1: 0, 4, 12

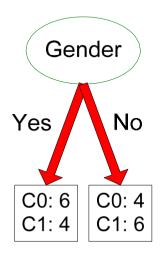
- [-, 14) bin
- Bin 2: 16, 16, 18
- [14, 21) bin
- Bin 3: 24, 26, 28
- [21,+] bin

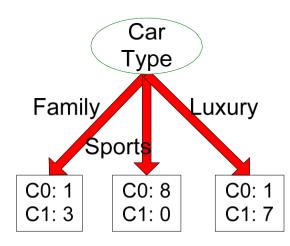
3.2 How to Find the Best Split?

Before splitting the dataset contains:

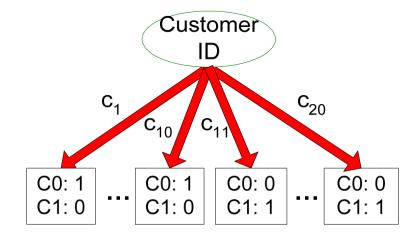
- 10 records of class C0 and
- 10 records of class C1

Which attribute test is the best?





Customer Id	Gender	Car Type	Shirt Size	Class
1	M	Family	Small	C0
2	M	Sports	Medium	C0
3	\mathbf{M}	Sports	Medium	C0
4	M	Sports	Large	C0
5	M	Sports	Extra Large	C0
6	M	Sports	Extra Large	C0
7	F	Sports	Small	C0
8	F	Sports	Small	C0
9	F	Sports	Medium	C0
10	F	Luxury	Large	C0
11	\mathbf{M}	Family	Large	C1
12	M	Family	Extra Large	C1
13	M	Family	Medium	C1
14	M	Luxury	Extra Large	C1
15	F	Luxury	Small	C1
16	F	Luxury	Small	C1
17	F	Luxury	Medium	C1
18	F	Luxury	Medium	C1
19	F	Luxury	Medium	C1
20	F	Luxury	Large	C1



How to Find the Best Split?

- Greedy approach: Test all possible splits and use the one that results in the most homogeneous (= pure) nodes
- Need a measure of node impurity:

C0: 5

C1: 5

Non-homogeneous

High degree of node impurity

C0: 9

C1: 1

Homogeneous

Low degree of node impurity

- Common measures of node impurity:
 - 1. GINI Index
 - 2. Entropy

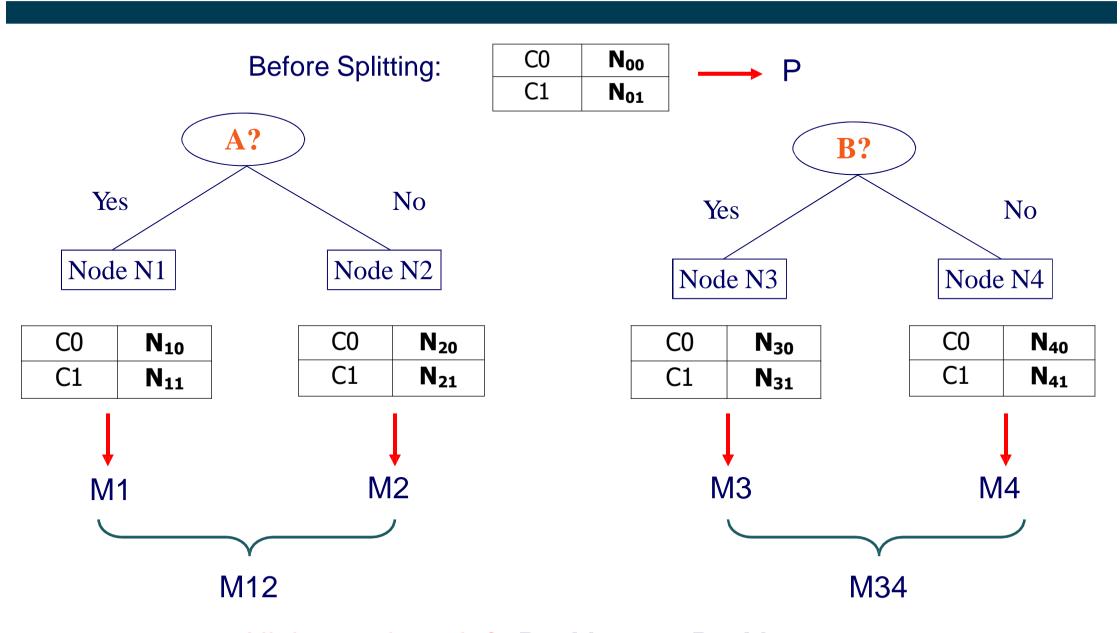
How to Find the Best Split?

- 1. Compute impurity measure (P) before splitting
- 2. Compute impurity measure (M) after splitting for all possible splits
 - compute impurity measure of each child node
 - M is the weighted impurity of children
- 3. Choose the attribute test condition (split) that produces the highest purity gain

$$Gain = P - M$$

or equivalently, lowest impurity measure after splitting (M)

Comparing Two Splits by Purity Gain



Higher purity gain? P - M12 or P - M34

3.2.1 Impurity Measure: GINI Index

– GINI Index for a given node t:

$$GINI(t) = 1 - \sum_{j} [p(j|t)]^{2}$$

 $p(j \mid t)$ is the relative frequency of class j at node t

- Minimum (0.0) when all records belong to one class
- Maximum (1 1/n_c) when records are equally distributed among all classes. n_c = number of classes

C1	0
C2	6
Gini=	0.000

C1	1
C2	5
Gini=	0.278

Gini=	0.444
C2	4
C1	2

C1	3
C2	3
Gini=	0.500

Examples for computing GINI

$$GINI(t) = 1 - \sum_{j} [p(j|t)]^{2}$$

$$P(C1) = 0/6 = 0$$
 $P(C2) = 6/6 = 1$

Gini =
$$1 - P(C1)^2 - P(C2)^2 = 1 - 0 - 1 = 0$$

$$P(C1) = 1/6$$
 $P(C2) = 5/6$

Gini =
$$1 - (1/6)^2 - (5/6)^2 = 0.278$$

$$P(C1) = 2/6$$
 $P(C2) = 4/6$

Gini =
$$1 - (2/6)^2 - (4/6)^2 = 0.444$$

Splitting Based on GINI

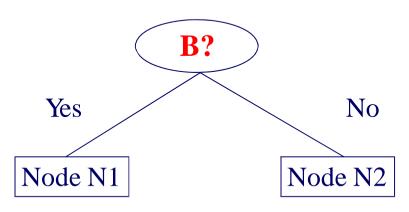
- When a node p is split into k partitions (subsets),
 the GINI index of each partition is weighted according to the partition's size
- The quality of the overall split is computed as:

$$GINI_{split} = \sum_{i=1}^{k} \frac{n_i}{n} GINI(i)$$

where: n_i = number of records at child i n = number of records at node p

Example: Calculating the Purity Gain of a Split

Split into two partitions



	Parent
C1	6
C2	6
Gini	= 0.500

GINI_{N1}

$$= 1 - (5/7)^2 - (2/7)^2$$

= 0.408

GINI_{N2}

$$= 1 - (1/5)^2 - (4/5)^2$$

= 0.32

	N1	N2					
C1	5	1					
C2	2	4					
Gini=0.371							

GINI_{Split}

$$= 7/12 * 0.408 +$$
Weights $5/12 * 0.32$

$$= 0.371$$

Purity Gain = 0.5 - 0.371 = 0.129

Categorical Attributes: Computing Gini Index

For each distinct attribute value, gather counts for each class

Multi-way split

		CarType							
	Family Sports Luxury								
C1	1	2	1						
C2	4 1 1								
Gini	0.393								

Two-way split (find best partition of values)

	CarType							
	{Sports, Luxury} {Family							
C1	3	1						
C2	2	4						
Gini	0.400							

	CarType						
	{Sports}	{Family, Luxury}					
C1	2	2					
C2	1	5					
Gini	0.419						

Continuous Attributes: Computing Gini Index

- How to find the best binary split for a continuous attribute?
- Efficient computation:
 - 1. sort the attribute on values
 - linearly scan these values, each time updating the count matrix and computing the gini index
 - 3. choose the split position that has the smalest gini index



Sorted Values
Split Positions

	Taxable Income																					
		60		70		7	5	85	5	90		9	5	10	00	12	20	12	25		220	
→	5	5	6	5	7	2	8	0	8	7	9	2	9	7	11	10	12	22	17	72	23	0
	<=	>	"	>	\=	>	<=	>	<=	>	\	>	\=	>	\=	>	"	>	\=	>	\=	>
Yes	0	3	0	3	0	3	0	3	1	2	2	1	3	0	3	0	3	0	3	0	3	0
No	0	7	1	6	2	5	3	4	3	4	3	4	3	4	4	3	5	2	6	1	7	0
Gini	0.4	20	0.4	100	0.3	75	0.3	43	0.4	17	0.4	100	<u>0.3</u>	<u>300</u>	0.3	843	0.3	375	0.4	00	0.4	20

Tid	Refund	Marital Status	Taxable Income	Cheat
1	Yes	Single	125K	No
2	No	Married	100K	No
3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
6	No	Married	60K	No
7	Yes	Divorced	220K	No
8	No	Single	85K	Yes
9	No	Married	75K	No
10	No	Single	90K	Yes

3.2.2 Alternative Impurity Measure: Information Gain

- Information gain relies on the entropy of each node
- Entropy of a given node t:

Entropy
$$(t) = -\sum_{j} p(j|t) \log_2 p(j|t)$$

 $p(j \mid t)$ is the relative frequency of class j at node t

- Entropy measures homogeneity of a node
 - Minimum (0.0) when all records belong to one class
 - Maximum (log₂ n_c) when records are equally distributed among all classes

Examples for Computing Entropy

Entropy
$$(t) = -\sum_{j} p(j|t) \log_2 p(j|t)$$

$$P(C1) = 0/6 = 0$$
 $P(C2) = 6/6 = 1$

Entropy =
$$-0 \log_2 0 - 1 \log_2 1 = -0 - 0 = 0$$

$$P(C1) = 1/6$$
 $P(C2) = 5/6$

Entropy =
$$-(1/6) \log_2(1/6) - (5/6) \log_2(5/6) = 0.65$$

$$P(C1) = 2/6$$
 $P(C2) = 4/6$

Entropy =
$$-(2/6) \log_2(2/6) - (4/6) \log_2(4/6) = 0.92$$

Splitting Based on Information Gain

Information Gain:

$$GAIN_{split} = Entropy(p) - \left(\sum_{i=1}^{k} \frac{n}{n} Entropy(i)\right)$$

Parent Node p is split into k partitions; n_i is number of records in partition i

- Information gain measures the entropy reduction of a split
- We choose the split with the largest reduction (maximal GAIN)

3. Alternative Splitting Criterion: GainRATIO

- GainRATIO is designed to overcome the tendency to generate a large number of small partitions
- GainRATIO adjusts information gain by the entropy of the partitioning (SplitINFO)
- Higher entropy of the partitioning (large number of small partitions) is penalized!

GainRATIO =
$$\frac{GAIN}{Split}$$
 = $\frac{GAIN}{Split}$ $SplitINFO$ = $-\sum_{i=1}^{k} \frac{n}{n} \log \frac{n_i}{n}$

Parent Node p is split into k partitions n_i is the number of records in partition i

3.3 Overfitting

- We want to learn models that are good at classifying unseen records
- Overfitting: Learned models can fit the training data too closely and thus work poorly on unseen data
- Model perfectly fitting the training data:
 - "Trees are big, green plants that have a trunk and no wheels"
- Unseen example:



Training data









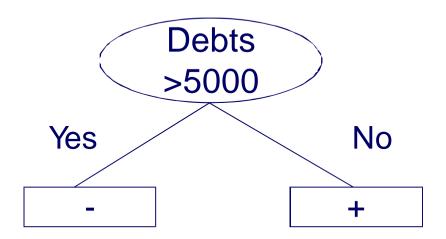




 Goal: Find good compromise between specificness and generality of the learned model

Overfitting: Second Example

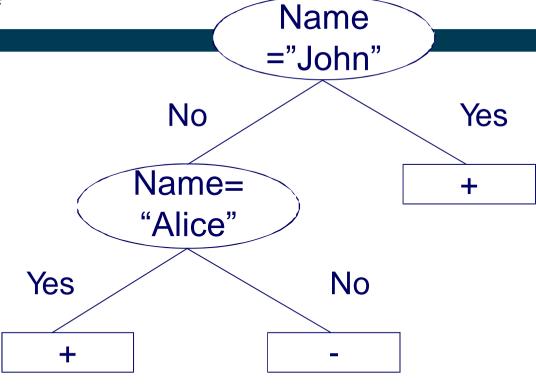
- Example: Predict credit rating
 - possible decision tree:



Name	Net Income	Job status	Debts	Rating
John	40000	employed	0	+
Mary	38000	employed	10000	-
Stephen	21000	self-employed	20000	-
Eric	2000	student	10000	-
Alice	35000	employed	4000	+

Overfitting: Second Example

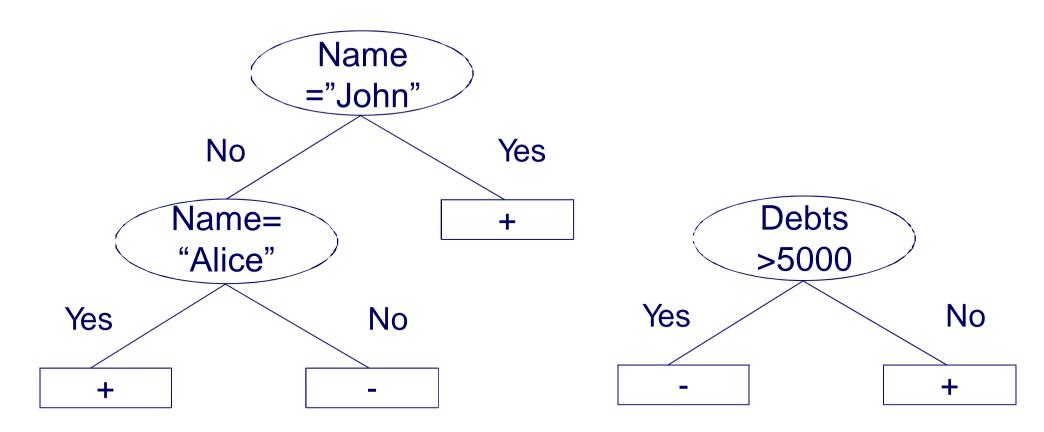
- Example: Predict credit rating
 - alternative decision tree:



Name	Net Income	Job status	Debts	Rating
John	40000	employed	0	+
Mary	38000	employed	10000	-
Stephen	21000	self-employed	20000	-
Eric	2000	student	10000	-
Alice	35000	employed	4000	+

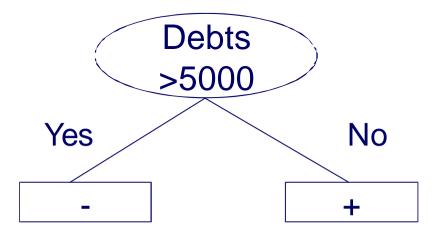
Overfitting: Second Example

- Both trees seem equally good
 - as they classify all instances in the training set correctly
- Which one do you prefer?



Occam's Razor

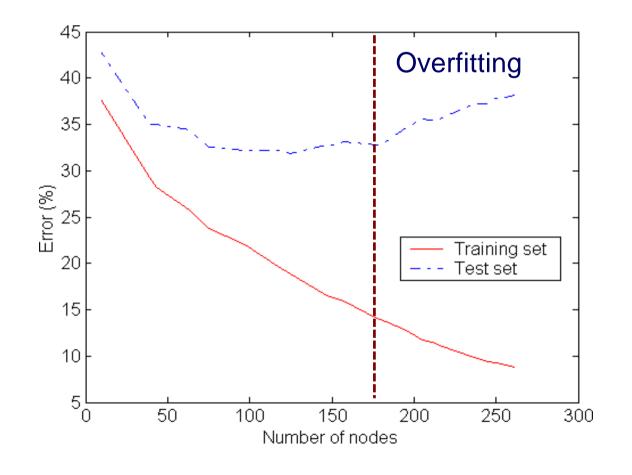
- Named after William of Ockham (1287-1347)
- A fundamental principle of science
 - if you have two theories
 - that explain a phenomenon equally well
 - choose the simpler one
- Tree that likely generalizes better according to Occam's razor





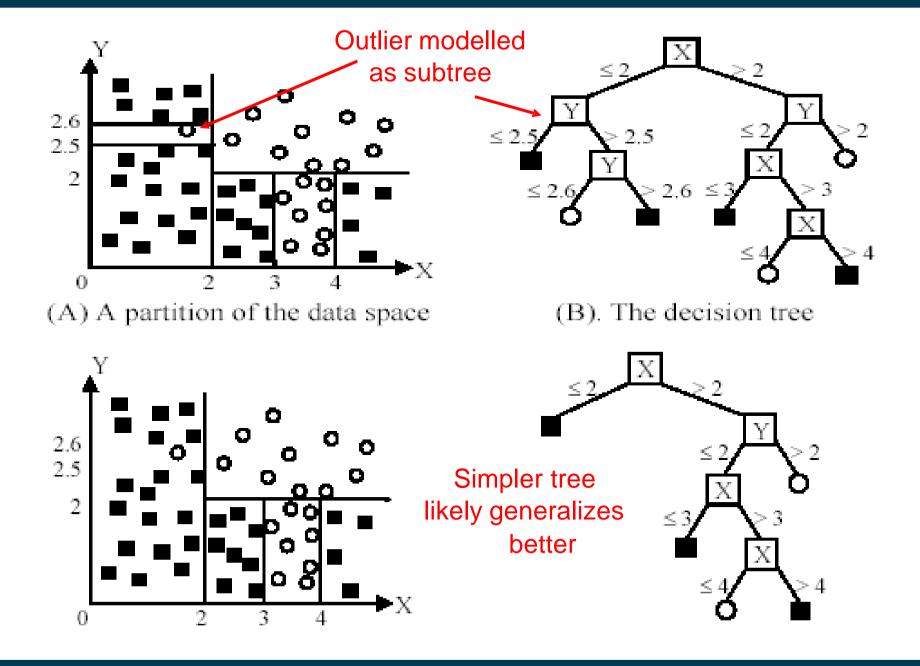
Overfitting: Symptoms and Causes

- Symptoms:
 - 1. decision tree too deep
 - 2. too many branches
 - model works well on training set but performs bad on test set
- Typical causes of overfitting
 - 1. too little training data
 - noise / outliers in training data
 - 3. high model complexity

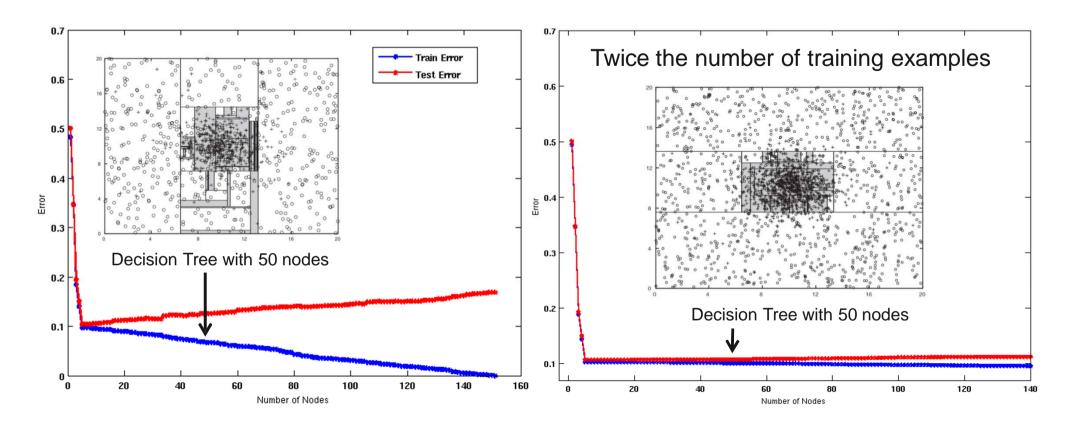


An overfitted model does not generalize well to unseen data.

Example of an Outlier causing Overfitting



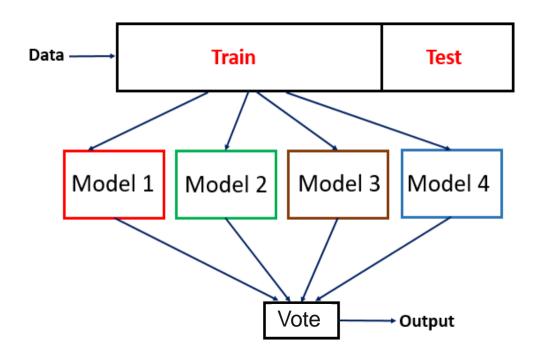
How to Prevent Overfitting 1: Use More Training Data



- If training data is under-representative, training errors decrease but testing errors increase on increasing number of nodes
- Increasing the size of training set reduces the difference between training and testing errors at a given number of nodes

How to Prevent Overfitting 2: Ensembles

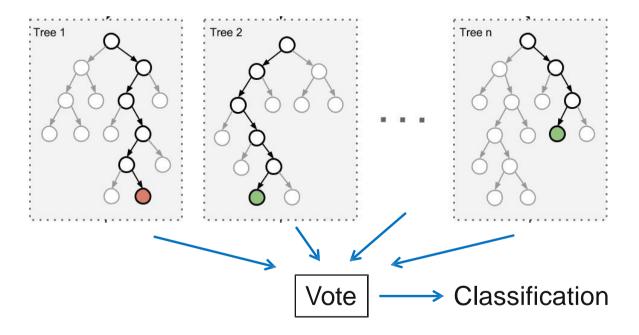
- Lean different models (base learners)
- Have them vote on the final classification decision



- Idea: Wisdom of the crowds applied to classification
 - A single classifier might focus too much on one aspect
 - Multiple classifiers can focus on different aspects

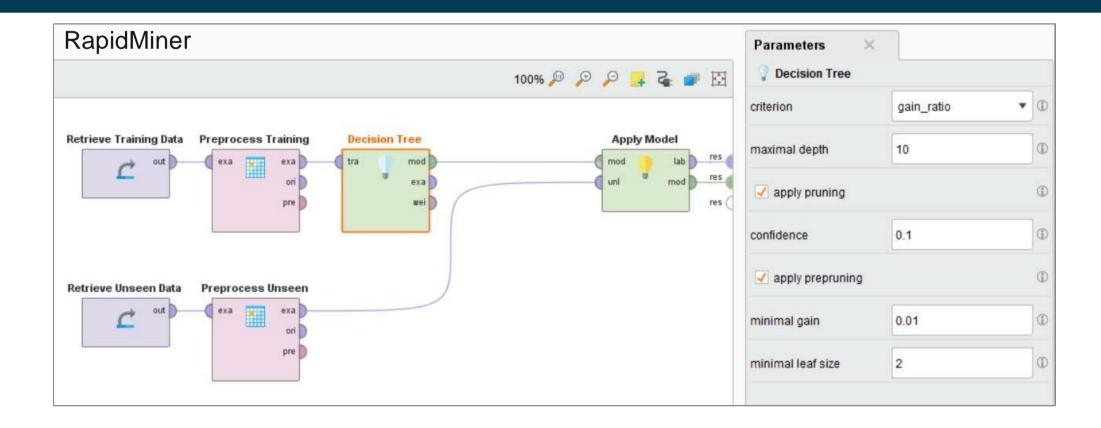
Random Forest

Ensemble consisting of a large number of different decision trees

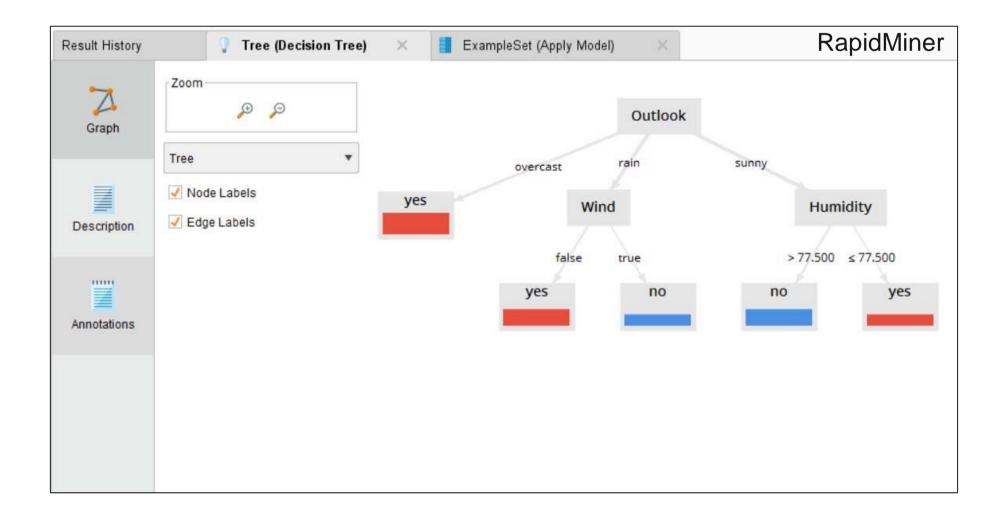


- Independence of trees achieved by introducing randomness into the learning process
 - only use an random subset of the attributes at each split
 - learn on different random subsets of the data (bagging)
- Random forests usually outperform single decision trees

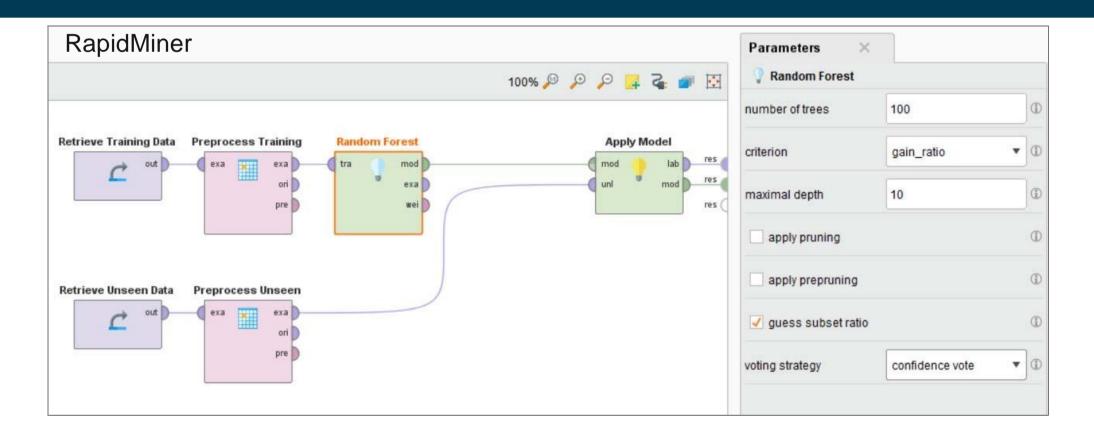
Decision Tree Classification in RapidMiner and Python



Examples of Learned Decision Trees



Random Forests in RapidMiner and Python



3.4 Discussion of Decision Trees

Advantages

- Inexpensive to construct
- Extremely fast at classifying unknown records
- Easy to interpret by humans for small-sized trees (eager learning)
- Can easily handle redundant or irrelevant attributes
- Accuracy is comparable to other classification techniques for many low dimensional data sets (not texts and images)

Disadvantages

- Space of possible decision trees is exponentially large.
 Greedy approaches are often unable to find the best tree
- Trees do not take into account interactions between attributes