

INFSCI 2591: Algorithm Design

Assignment #1

Due: September 13, 2016

1. Write a pseudocode for multiplying large numbers using the ala carte multiplication method.

Problem: multiply two large numbers (x and y) using the rectangle Ala Carte method.

Input: two integers x, y

Output: *result*, the product of the two numbers (x and y).

```
int ala_carte_multi(int x, int y)
{
    int result = 0;

    // get rid of the negative sign,
    // and change the corresponding flag to add them later.
    bool is_x_neg = false;
    bool is_y_neg = false;
    if(x < 0)
    {
        x_neg = true;
        x = x * -1;
    }
    if(y < 0)
    {
        y_neg = true;
        y = y * -1;
    }

    while(x > 0)
    {
        if(x % 2 != 0)
        {
            result += y;
        }
        x = floor(x / 2);
        y = y * 2;
    }

    // make sure the negative sign exists if needed
    if((is_x_neg && !is_y_neg) || (!is_x_neg && is_y_neg))
    {
        result = result * -1;
    }

    return result;
}
```

2. Write a pseudocode for multiplying large numbers using the rectangle multiplication method.

Problem: multiply two large numbers (x and y) using the rectangle multiplication method.

Input: two integers x, y

Output: *result*, the product of the two numbers (x and y).

```
int rectangle_multi (int x, int y)
{
    int result = 0;
    // get rid of the negative sign,
    // and change the corresponding flag to add them later.
    bool is_x_neg = false;
    bool is_y_neg = false;

    if(x < 0)
    {
        is_x_neg = true;
        x = x * -1;
    }
    if(y < 0)
    {
        is_y_neg = true;
        y = y * -1;
    }

    index i, j;
    int x_len = digits count of (x);
    int y_len = digits count of (y);
    int x_digits[1..x_len];
    int y_digits[1..y_len];

    // split x into digits
    for(i = x_len; i >= 1; i--)
    {
        x_digits[i] = x % 10;
        x /= 10;
    }
    // split y into digits
    for(i = y_len; i >= 1; i--)
    {
        y_digits[i] = y % 10;
        y /= 10;
    }

    // multiplying each two-corresponding digits
    // and storing the result in a table (2D array)
    int table_mult[1..y_len][1..(x_len * 2)];

    for(i = 1; i <= y_len; i++)
        for(j = 1; j <= x_len; j++)
        {
            int tmp_mult = y_digits[i] * x_digits[j];
            table_mult[i][(j*2)] = tmp_mult / 10;
            table_mult[i][(j*2)+1] = tmp_mult % 10;
        }
}
```

```
// summing up and store the result in array.
int result_arr_len = (x_len + y_len);
int result_arr[1..result_arr_len];
int sum;
index row, col;
bool iteration;

// first loop (zigzag traversal) in the sum operation
for(i = y_len; i >= 1; i--)
{
    sum = 0;
    row = i;
    col = (x_len * 2);
    iteration = false;

    while(row <= y_len && col >= 0)
    {
        sum += table_mult[row][col];

        if(!iteration)
            row++;
        col--;
        iteration = !iteration;
    }

    result_arr[(x_len + i)] = sum;
}

// second loop (zigzag traversal) in the sum operation
for(j = x_len; j >= 1; j--) {

    sum = 0;
    col = (j * 2);
    row = 0;
    iteration = true;

    while(row <= y_len && col >= 0)
    {
        sum += table_mult[row][col];

        if(!iteration)
            row++;
        col--;
        iteration = !iteration;
    }

    result_arr[j] = sum;
}

// summing up the carryout/leftover with the next number.
for(i = result_arr_len; i >= 1; i--)
{
    if(result_arr[i] > 10)
    {
        result_arr[i-1] += (result_arr[i] / 10);
        result_arr[i] = result_arr[i] % 10;
    }
}
```

```
// preparing the numbers to final stage
// by giving them its actual value (weight).
for(i = 1; i <= result_arr_len; i++)
    for(j = i; j <= (result_arr_len - 1); j++)
        result_arr[i] *= 10;

// sum all items inside the result array
for(i = 1; i <= result_arr_len; i++)
    result += result_arr[i];

// make sure the negative sign exists if needed
if((is_x_neg && !is_y_neg) || (!is_x_neg && is_y_neg))
{
    result = result * -1;
}

return result;
}
```