[100 Points] Modify the Caesar Shift Cipher Python Implementation Listed Such That Takes the Script Takes as Input a Binary File and Encrypts/Decrypts the Output to Another Binary File

```
message = 'This is my secret message'
key = 11
mode = 'encrypt'
SYMBOLS='ABCDEFGHIJKLMNOPQRSTUVWXYZ abcdefghijklmnopqrstuvwxyz1234567890!?.'
translated=''
for symbol in message:
    if symbol in SYMBOLS:
        symbolIndex=SYMBOLS.find(symbol)
        if mode =='encrypt':
            translatedIndex=(symbolIndex+key)%len(SYMBOLS)
        elif mode == 'decrypt':
            translatedIndex=(symbolIndex-key)%len(SYMBOLS)
        translated+=SYMBOLS[translatedIndex]
    else:
        translated+=symbol
print(translated)
```

Sweigart, A.(2018). *Cracking Odes with Python.* San Francisco, CA: No Starch Press

Below is the Python script I wrote for the caesar cipher, I utilized "Affine_Cipher.py" as the test input to verify functionality.

```
print("Homework 1: byte-wise caesar cypher")

def Caesar_Bytewise(shift, inFile, outFile):
  with open(inFile, "rb") as f:
    with open(outFile, "wb") as output:
      byte = f.read(1)
      while byte != b"":
        # Convert byte into an integer value
        value = int.from_bytes(byte, byteorder='big')
        # Calculate the output value given the shift
        out_value = ( value + shift) % 256
        # Write the output value to the output file, as a byte
        output.write( out_value.to_bytes(1, byteorder='big', signed=False))
        byte = f.read(1)
      output.close()
    f.close()

def main():
  Caesar_Bytewise(100, "Affine_Cipher.py", "HW1_output.txt")

  # Used for testing:
  #Caesar_Bytewise(156, "HW1_output.txt", "HW1_outputVerification.txt")


if __name__ == "__main__":
  main()
```

Modified function for byte-wise caesar cipher, written to be portable to larger python script

[5 Points] Represent in binary using Two's complement (signed) - Calculators, Internet allowed

Converting to Two's complement:
If positive: $2's\,Complement(x) = x$; if negative: $2's\,Complement(x) = x \oplus \texttt{0xFF} + 1$

a) 127:

$$127 = \boxed{0111\,1111}$$

b) -128:

$$128 = 10000000 \rightarrow 01111111 + 1 = \boxed{10000000}$$

c) -1:

$$1 = 00000001 \rightarrow 11111110 + 1 = \boxed{11111111}$$

[5 Points] Represent the following decimal numbers in hexadecimal (unsigned) - Calculators, Internet allowed

a) 10:

$$10 = \boxed{\texttt{0xA}}$$

b) 33:

$$33 = 16 \cdot 2 + 1 = \boxed{\texttt{0x21}}$$

c) 120:

$$120 = 16 \cdot 7 + 8 = \boxed{\texttt{0x78}}$$

[5 Points] Find two different words (plainText_1, plainText_2) that are at least 4 characters long such that the cipher-texts produced using the Caesar Cipher algorithm are identical ($\text{cipherText}_1 = \text{cipherText}_2$) provided that they use two different keys (key_1, key_2). List the two plain-text words (plainText_1, plainText_2), and their corresponding keys (key_1, and key_2).

The below pairing was found by using a brute force approach with two online Caesar Cipher algorithms. For the first, I chose a four letter word at random, and shifted it by some key x. This produced $\text{plainText}_1 \rightarrow \text{cipherText}_1$ with $key = x$. I then used cipherText_1 as the input to the second Caesar Cipher, and checked each key to see if it produced a corresponding English word, let this key be x'. This would indicate that $key_2 = 26 - x'$.
The words, cipher texts, and keys are as follows:

Plain Text	Cipher Text	Key
cows	htbx	5
semi	htbx	15

[10 Points] Fill in the blank (all from the book):

a) Symmetric Encryption Participants share a secret key to encrypt and decrypt and decryption is the inverse operation of encryption.

b) Asymmetric/Public Key Encryption Participants share a public portion of the key, but a private portion is retained by a single participant for secure encryption and decryption and digital signatures.

c) Cryptography The science of secret writing.

d) Cryptanalysis The science and art of breaking the secure properties of crypto systems.

e) Moore's Law The concept that computational power doubles every eighteen months so that brute force attacks against cryptosystems will be faster in the future.

f) Kerckhoffs' Principle The concept that a cryptosystem should be secure even if the attacker knows all the details (but not the keys) of the targeted cryptosystem.

1.9 [25 Points] Compute x as far as possible without a calculator. Where appropriate, make use of a smart decomposition of the exponent as shown in the example in Sect. 1.4.1:

a) $x = 3^2 \mod 13$

$$\boxed{x = 9}$$

b) $x = 7^2 \mod 13$

$$x = 49 = 13 \cdot 3 + 10 \rightarrow \boxed{x = 10}$$

c) $x = 7^{100} \mod 13$

$$x = 7^{100} \mod 13 = (7^2)^{50} \mod 13 = 10^{50} \mod 13$$

$$10^2 \mod 13 = 9$$

$$10^3 \mod 13 = 10^2 \cdot 10 \mod 13$$

$$10^3 \mod 13 = 90 \mod 13 = 12$$

$$x = 10^{50} \mod 13 = (10^2 \cdot 10^3)^{10} \mod 13$$

$$x = (9 \cdot 12)^{10} \mod 13$$

$$9 \cdot 12 \mod 13 = 108 \mod 13 = 4$$

$$x = 4^{10} \mod 13 = (4^2)^5 \mod 13$$

$$4^2 \mod 13 = 3$$

$$x = 3^5 \mod 13 = 3^2 \cdot 3^3 \mod 13$$

$$3^3 \mod 13 = 27 \mod 13 = 1$$

$$x = 9 \cdot 1 \mod 13$$

$$x = 7^{100} \mod 13 = \boxed{9 = x}$$

d) This last problem is called a *discrete logarithm* and points to a hard problem which we discuss in Chap. 8. The security of many public-key schemes is based on the hardness of solving the discrete logarithm for large numbers, e.g., with more than 1000 bits.
$7 \times x = 11 \mod 13$

$$\begin{aligned} 7 \cdot x &= 11 \mod 13 \\ 7 \cdot 9 &= 63 \\ 63 &\mod 13 = 11 \\ \boxed{x = 9} & \end{aligned}$$

1.11 [25 Points] This problem deals with the affine cipher with the key parameters $\alpha = 7$, $\beta = 22$.

I utilized a python script to solve this problem, and the code I wrote is included in Appendix A.

a) Decrypt the following text: `falszztysyjzyjkywjrztyjztyynaryjkyswarztyegyyj`

The decrypted text is as follows: **firstthesentenceandthentheevidencesaidthequeen**

b) Who wrote the line?

Lewis Caroll in *Alice's Adventures Under Ground*

1.13 [25 Points] In an attack scenario, we assume that the attacker Oscar manages somehow to provide Alice with a few pieces of plaintext that she encrypts.Show how Oscar can break the affine cipher by using two pairs of plaintext-ciphertext, (x_1, y_1) and (x_2, y_2). What is the condition for choosing x_1 and x_2?

Remark: Inpractice,such an assumption turns out to be valid for certain settings, e.g., encryption by Web servers, etc. This attack scenario is,thus,very important and is denoted as a *chosen plaintext* attack.

One must select x_1 and x_2 such that $y_1 \neq y_2$. This would then give you the following equations:

$$\alpha \cdot x_1 + \beta \mod 26 = y_1 \tag{1}$$

$$\alpha \cdot x_2 + \beta \mod 26 = y_2 \tag{2}$$

With (1) and (2), Oscar has two equations with two unknowns: α and β. Thus, this system of equations can be solved, giving Oscar the keys α and β.

Appendix A: Python Script

```
import string
import math

def ModularInverse(alpha):
  running = True
  inv_alpha = 1
  while running:
    if ( (alpha * inv_alpha) % 26 == 1):
      print( "Modular inverse of {0} is: {1}".format(alpha, inv_alpha) )
      running = False
      return inv_alpha
    else:
      inv_alpha += 1


def affineDecrypt(inv_alpha, beta, input):
  output = ""
  for letter in input:
    in_index = string.ascii_lowercase.index(letter)
    out_index = ( inv_alpha * (in_index - beta) ) % 26
    output += string.ascii_lowercase[out_index]
  return output

def affineEncrypt(alpha, beta, input):
  output = ""
  for letter in input:
    in_index = string.ascii_lowercase.index(letter)
    out_index = ( in_index * alpha + beta) % 26
    output += string.ascii_lowercase[out_index]
  return output

def main():
  encrypt = True
  alpha = 7
  beta = 22
  if encrypt:
    print("Starting encrypt with alpha = {0} and beta = {1}: \n".format(alpha, beta))
    input = "firstthesentenceandthentheevidencesaidthequeen"
    output = affineEncrypt(alpha, beta, input)
  else:
    print("Starting decrypt with alpha = {0} and beta = {1}: \n".format(alpha, beta))
    input = "falszztysyjzyjkywjrztyjztyynaryjkyswarztyegyyj"
    output = affineDecrypt(ModularInverse(alpha), beta, input)

  print( "The output is: \n" + output )

if __name__ == "__main__":
  main()
```