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# PREDICTING REAL ESTATE PRICES IN MONTREAL USING MACHINE LEARNING METHODS

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## ABSTRACT

Machine Learning. The indispensable part of twenty-first century technology's development. Methods of ML are helpful in many fields of our daily life. We decided to utilize ML powerful methods in analyzing real estate market in Montreal. Based on collected data, we want to predict the value of real assets in one of the biggest and most popular cities in Canada.

**Keywords** Machine Learning · Artificial Intelligence · ML models · housing market · real estate · business · predicting · Data Science

## 1 Introduction

## 2 Data

Our dataset consists of six data frames. The core data frame is 'listings.csv', as it contains key attributes for real estates sold in Montreal. During data exploratory analysis we have discovered that some columns contain largely nulls, so we have decided to drop them. Additionally, columns with the same value for all records were also rejected as they did not provide any information. The variable we want to predict is **BuyPrice**, we observed that some records contained the price per foot or square meter while the rest contained the total price of the property. In addition, we have calculated that the purchase price is mostly correlated with the potential gross income, the number of bathrooms, bedrooms, and rooms.

The next data frames that were analyzed, were 'policeCoord.csv' and 'firestations.csv'. ~~The next data frames that were analyzed were "policeCoord.csv" and "firestations.csv".~~ These data frames only contained the coordinates of the police and fire departments. It seems useful to calculate the distance to the nearest police and fire station for each property.

Next, we examined the file "montreal\_hpi.csv" which contained the house price index measures. Due to the significant correlation (greater than 0.99) between the variables, we concluded that only one column should be used from the mentioned dataframe.

In order to add socio-demographic data, we have analyzed 'sociodemo.csv'. A data frame with information about population, nearby schools, average income, etc.

The last data frame was 'extra\_data.csv' which provided additional information for some properties in 'listings.csv', unfortunately this frame was contained vast majority of null values. However, some columns, such as LivingArea, found themselves truly relevant.

### 3 Selected models

After exact EDA (exploratory data analysis) we started next step which was building and testing different models. We have built several RandomForest, XGBoost, LightGBM and CatBoost models. Our models were trained using Grid Search and Random Search. Then were selected only the best models based on RMSE. For each algorithm mentioned before we have selected five models with different hyperparameters which have reached the best scores. Then we have tried PCA to reduce dimension of the dataset and this significantly improved scores of our models. Below is a table with the best scores on test data sets from the four selected algorithms.

RMSE	RandomForest	XGBoost	LightGBM	CatBoost
PCA	87 740.23	360.06	74 396.47	46 023.39
WITHOUT PCA	334 091.74	228890.90	282 358.90	246 424.10

All hyperparameters were set to avoid overfitting and underfitting so models presented above have similar scores on training and test data sets. Then we selected the best algorithm for our models, which, as we can see in the table above, turned out to be XGBoost.

Below we can see the best 3 models built on XGboost's algorithm and their hyperparameters

Model	RMSE train	RMSE test	booster	eta	max_depth	gamma	min_child_weight	subsample	colsample_bytree
xgboost 1	101.90	360.07	gbtree	0.05	7	0	1	1	1
xgboost 2	430.97	881.18	gbtree	0.09	8	4	1	1	1
xgboost 3	808.91	1 477.11	gbtree	0.12	6	6	1	1	1

Next, we created residual plots to check how our predictions looked like. What is really satisfying is that almost all predictions are very accurate. Residual plots are presented below.

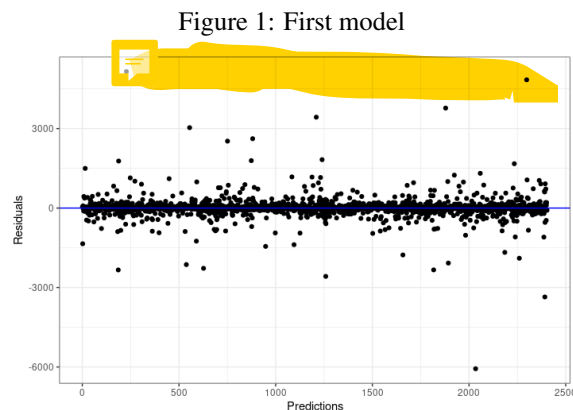


Figure 2: Second model

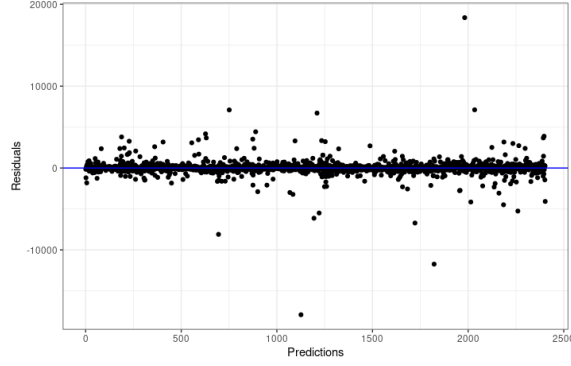
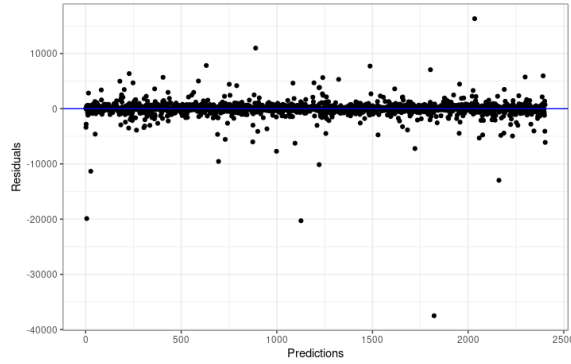


Figure 3: Third model



So as we can see these three XGBoost models were very accurate and reached very low RMSE. But how about the other metrics? That was our next step in choosing accurate model. We have measured the predictions using MAE,  $R^2$  and the mentioned before RMSE. In the following formulas,  $y_i$  stands for real value of i-th observation in dataset and  $\hat{y}_i$  stands for the model's prediction of this value.

MAE is defined as  $\sum_{i=1}^n |y_i - \hat{y}_i|$ ,

$R^2$  is defined as  $\frac{\sum_{i=1}^n (\hat{y}_i - \bar{y})(y_i - \bar{y})}{\sum_{i=1}^n (y_i - \bar{y})^2}$ ,

and the RMSE is defined as  $\sqrt{\frac{\sum_{i=1}^n (\hat{y}_i - y_i)^2}{n}}$

So now we can present our results:

Model name	RMSE test	MAE test	R2
xgboost1	360.07	135.74	0.9998625
xgboost2	881.18	289.28	0.9995856
xgboost3	1 477.11	520.25	0.9978164

All three models achieve very good metrics and will also be further analyzed using XAI methods. But there is one change that must be performed. As we have used the PCA method to reduce dimension of our data sets we have lost the interpretability of our data. So we need to decide what is more important: increasing the accuracy of the prediction or preserving the interpretability and an insight into the influence of individual variables on the predictions. In the next steps, where we are analyzing our models using XAI methods, we are using the data set without PCA.

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### 3.1 Headings: second level

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$$\xi_{ij}(t) = P(x_t = i, x_{t+1} = j | y, v, w; \theta) = \frac{\alpha_i(t) a_{ij}^{w_t} \beta_j(t+1) b_j^{v_{t+1}}(y_{t+1})}{\sum_{i=1}^N \sum_{j=1}^N \alpha_i(t) a_{ij}^{w_t} \beta_j(t+1) b_j^{v_{t+1}}(y_{t+1})} \quad (1)$$

#### 3.1.1 Headings: third level

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## 4 Examples of citations, figures, tables, references

### 4.1 Citations

Citations use natbib. The documentation may be found at

<http://mirrors.ctan.org/macros/latex/contrib/natbib/natnotes.pdf>

Here is an example usage of the two main commands (`citet` and `citep`): Some people thought a thing [Kour and Saabne, 2014a, Hadash et al., 2018] but other people thought something else [Kour and Saabne, 2014b]. Many people have speculated that if we knew exactly why Kour and Saabne [2014b] thought this...

### 4.2 Figures

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<sup>1</sup>Sample of the first footnote.

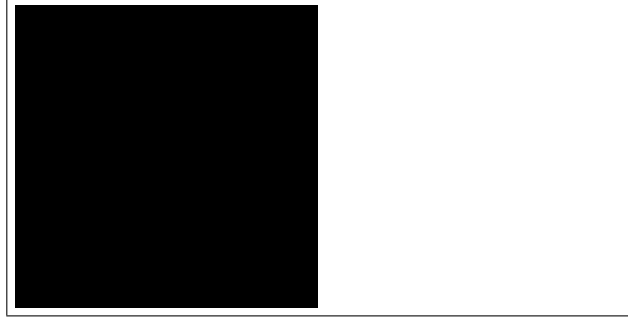


Figure 4: Sample figure caption.

Table 1: Sample table title

Part		
Name	Description	Size ( $\mu\text{m}$ )
Dendrite	Input terminal	$\sim 100$
Axon	Output terminal	$\sim 10$
Soma	Cell body	up to $10^6$

### 4.3 Tables

See awesome Table 1.

The documentation for booktabs (‘Publication quality tables in LaTeX’) is available from:

<https://www.ctan.org/pkg/booktabs>

### 4.4 Lists

- Lorem ipsum dolor sit amet
- consectetur adipiscing elit.
- Aliquam dignissim blandit est, in dictum tortor gravida eget. In ac rutrum magna.

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