

Unit 3:- Number System

(Marks:-18)

Q.1. What is Number system? And explain the types of number system?

Ans.

Number system:-

In computer system data is store in specific format is called number system.

Base:-

Base is defined as number of symbol available in number system.

➤ There are **four** types of number system.

- i. Binary Number System.
- ii. Octal Number System.
- iii. Decimal Number System.
- iv. Hexa Decimal Number System.

I. Binary Number System:-

A number system have in base is two is called binary number system.

Base: - 2.

Range:-0 to 1.

II. Octal Number System:-

A number system have in base is eight is called octal number system.

Base: - 8.

Range:-0 to 7.

III. Decimal Number System:-

A number system have in base is ten is called Decimal number system.

Base: - 10.

Range: - 0 to 9.

IV. Hexa Decimal Number System:-

A number system have in base is sixteen is called Hexa Decimal Number System.

Base:-16.

Range:- 0 to 15.

0 to 9 and A to F

A=10, C= 12 E=14.

B=11, D= 13, F=15.

1. Non positional Number System:-

A number system in which digits or value has not fix position is called Non-positional Number System.

2. Positional Number System:-

A number system in which digits or value has fix position is called Positional Number System.

Sum:-

1. Octal to binary:-

$$\sim (7436.231)_8====(?)_2$$

$$\underline{111} \underline{100} \underline{011} \underline{110} . \underline{010} \underline{011} \underline{001}$$

$$\text{Ans. } (7436.231)_8====(111\ 100\ 011\ 110.010\ 011\ 001)_2$$

2. Binary to octal:-

$$\sim (110010101010.11010110)_2====(?)_8$$

$$\underline{110} \underline{010} \underline{101} \underline{010} . \underline{110} \underline{101} \underline{100}$$

$$6\ 2\ 5\ 2\ .\ 6\ 5\ 4$$

$$\text{Ans. } (110010101010.11010110)_2====(6252.654)_8$$

3. Hexa Decimal to binary:-

$$\sim (A896F.48E)_{16}====(?)_2$$

$$108915.4814$$

$$\underline{1010} \underline{1000} \underline{1001} \underline{0110} \underline{1111} . \underline{0100} \underline{1000} \underline{1110}$$

$$\text{Ans. } (A896F.48E)_{16}====(1010\ 1000\ 1001\ 0110\ 1111\ .0100\ 1000\ 1110)_2$$

4. Binary to hexa decimal:-

$$\sim (1101011010100.1110101)_2====(?)_{16}$$

$$\underline{0001} \underline{1010} \underline{1101} \underline{0100} . \underline{1110} \underline{1010}$$

$$1\ A\ D\ 4\ .\ E\ A$$

$$\text{Ans. } (1101011010100.1110101)_2====(1AD4.EA)_{16}$$

5. Binary to decimal:-

$$\sim (0010110100110001111000011000.110011100110)_2 \\ ===== (?)_{10}$$

0010 1101 0011 0001 1110 0001 1000 1100 1110 0110

2 D 3 1 E 1 8 C E 6

2D31E18CE6

Ans. $(0010110100110001111000011000.110011100110)_2 =====$

$(2D31E18CE6)_{10}$

6. Decimal to binary:-

$$\sim (744.58)_{10} ===== (?)_2$$

2	744		0.58*2=1.16	1
2	372	0	0.16*2=0.32	0
2	186	0	0.32*2=0.64	0
2	93	0	0.64*2=1.28	1
2	46	1	0.28*2=0.56	0
2	23	0		
2	11	1		
2	5	1		
2	2	1		
2	1	0		
	0	1		

1 0 1 1 1 0 1 0 0 0

512 256 128 64 32 16 8 4 2 1

Ans. $(744.58)_{10}====(1011101000.10010)_2$

7. Decimal to octal:-

~ $(376.44)_{10}====(?)_8$

8	376		$0.44*8=3.52$	3
8	47	0	$0.52*8=4.16$	4
8	5	7	$0.16*8=1.28$	1
	0	5		

Ans. $(376.44)_{10}====(570.341)_8$

8. Decimal to Hexa Decimal:-

~ $(2348.30)_{10}====(?)_{16}$

16	2348	
16	146	12
16	9	2
	0	9

$0.30*16= 4.80$ 4

$0.80*16= 12.8$ 12

$$0.80 \times 16 = 12.8 \quad 12$$

$$\text{Ans. } (2348.30)_{10} = (92C.4CC)_{16}$$

9. Hexa Decimal to Octal:-

$$\sim (B973.29C)_{16} = (?)_8$$

$$\underline{001} \underline{011} \underline{100} \underline{101} \underline{110} \underline{011} . \underline{001} \underline{010} \underline{011} \underline{100}$$

$$1 \quad 3 \quad 4 \quad 5 \quad 6 \quad 3 \quad . \quad 1 \quad 2 \quad 3 \quad 4$$

$$\text{Ans. } (B973.29C)_{16} = (134563.1234)_8$$

10. Octal to Hexa Decimal:-

$$\sim (732.351)_8 = (?)_{16}$$

$$\underline{0001} \underline{1101} \underline{1010} . \underline{0111} \underline{0100} \underline{1000}$$

$$1 \quad D \quad A \quad . \quad 7 \quad 4 \quad 8$$

$$\text{Ans. } (732.351)_8 = (1DA.748)_{16}$$

11. Binary to Decimal:-

$$\sim (110010.0110)_2 = (?)_{10}$$

$$\text{➤ } \underline{5 \ 4 \ 3 \ 2 \ 1 \ 0}$$

$$1 \ 1 \ 0 \ 0 \ 1 \ 0$$

$$= 2^5 \times 1 + 2^4 \times 1 + 2^3 \times 0 + 2^2 \times 0 + 2^1 \times 1 + 2^0 \times 0$$

$$= 32 \times 1 + 16 \times 1 + 8 \times 0 + 4 \times 0 + 2 \times 1 + 1 \times 0$$

$$= 50.$$

$$\text{➤ } \underline{1 \ 2 \ 3 \ 4}$$

$$\begin{aligned}
 &0110 \\
 &= 2^{-1} \cdot 0 + 2^{-2} \cdot 1 + 2^{-3} \cdot 1 + 2^{-4} \cdot 0 \\
 &= 0.5 \cdot 0 + 0.25 \cdot 1 + 0.125 \cdot 1 + 0.0625 \cdot 0 \\
 &= 0 + 0.25 + 0.125 + 0 \\
 &= 0.375.
 \end{aligned}$$

$$\text{Ans. } (110010.0110)_2 = (50.375)_{10}$$

11. Octal to Decimal:-

$$\sim (723.27)_8 = (?)_{10}$$

$$\triangleright \begin{array}{c} 210 \\ \hline 723 \end{array}$$

$$= 8^2 \cdot 7 + 8^1 \cdot 1 + 8^0 \cdot 3$$

$$= 64 \cdot 7 + 16 \cdot 1 + 1 \cdot 3$$

$$= 448 + 16 + 3$$

$$= 467$$

$$\triangleright \begin{array}{c} 12 \\ \hline 27 \end{array}$$

$$= 8^{-1} \cdot 2 + 8^{-2} \cdot 7$$

$$= 0.125 \cdot 2 + 0.0625 \cdot 7$$

$$= 0.250 + 0.4375$$

$$= 0.6875$$

$$\text{Ans. } (723.27)_8 = (467.6875)_{10}$$

12. Hexa Decimal to Decimal:-

$$\sim (B829.F2)_{16} = (?)_{10}$$

$$\begin{array}{r} \text{➤ } \underline{3210} \\ \text{B829} \end{array}$$

$$=16^3*11+16^2*8+16^1*2+16^0*9$$

$$=4096*11+256*8+16*2+1*9$$

$$=45056+2048+32+9$$

$$=47145$$

$$\begin{array}{r} \text{➤ } \underline{12} \\ \text{F2} \end{array}$$

$$=16^{-1}*1+16^{-2}*2$$

$$=0.0625*1+0.0039*2$$

$$=0.0625+0.0078$$

$$=0.6328$$

$$\text{Ans. } (B829.F2)_{16}====(47145.6328)_{10}$$

❖ Addition:-

1. $63+20=(?)$

$$\begin{array}{r} 1 1 \\ 0110 \ 0011 \\ 0010 \ 0000 \\ \hline 1000 \ 0011 \\ \hline 8 \qquad 3 \end{array}$$

3. $537+241=(?)$

$$\begin{array}{r} 0101 \ 0011 \ 0111 \\ 0010 \ 0100 \ 0001 \\ \hline 0111 \ 0111 \ 1000 \\ \hline 7 \quad 7 \quad 8 \end{array}$$

2. $843+521=(?)$

$$\begin{array}{r} 1000 \ 0100 \ 0011 \\ 0101 \ 0010 \ 0001 \\ \hline 1 \\ 1101 \ 0110 \ 0100 \\ 0110 \ 6 \quad 4 \\ \hline 0001 \ 0011 \ 6 \quad 4 \\ \hline 1 \quad 3 \quad 6 \quad 4 \end{array}$$

Values	Sum	Carry
0+0	0	0
0+1	1	0
1+1	0	1
1+1+1	1	1

❖ Subtraction:-

1. $54-32=?$

$$\begin{array}{r} 0101\ 0100 \\ 0011\ 0010 \\ \hline 0010\ 0010 \\ \hline \end{array}$$

2 2

3. $111100-000101=?$

$$\begin{array}{r} 111\ 100 \\ 000\ 101 \\ \hline 111\ 011 \\ \hline \end{array}$$

7 3

2. $63-20=?$

$$\begin{array}{r} 0110\ 0011 \\ 0010\ 0000 \\ \hline 0100\ 0011 \\ \hline \end{array}$$

4 3

Value	Difference	Barrow
0-0	0	0
0-1	1	1
1-0	1	0
1-1	0	0