

Linear Algebra

a) $A: 2 \times 3$

$B: 4 \times 3$

$C: 1 \times 5$

$D: 2 \times 2$

$E: 1 \times 1$

$F: 5 \times 1$

$G: 3 \times 3$

b) Square Matrices: D, E, G

c) Symmetric: E, G

d) $B,$

e) A, B

f) E, F

g) C, E

h) $A_T = \begin{bmatrix} -1 & 0 \\ 2 & -2 \\ 1 & -11 \end{bmatrix}, C_T = \begin{bmatrix} -3 \\ 2 \\ 9 \\ -5 \\ 7 \end{bmatrix}$

$E_T = [3]$ $G_T = \begin{bmatrix} -5 & -4 & 2 \\ -4 & -3 & 4 \\ 2 & 4 & 1 \end{bmatrix} = G$

2)

$$AB = \begin{bmatrix} 3 & -1 & -2 \\ -1 & 4 & -5 \end{bmatrix}$$

$$FE = \begin{bmatrix} -25 \\ -55 \\ 55 \end{bmatrix}$$

3) Determ.

$$|M| = 15 \times 2 - 30 = -15$$

$$|M_2| = 2(-2-5) - 3(1-9) + 1(-2-5) \\ = -24 + 24 - 8 = \boxed{-8}$$

4) Inverse

$$\text{inverse}(A) = \frac{1}{-9+5} \begin{bmatrix} 2 & 3 \\ -3 & -8 \end{bmatrix}$$

$$= \begin{bmatrix} -1 & \frac{3}{4} \\ 1 & 2 \end{bmatrix}$$

$$\det(A_2) = -1$$

$$\text{coFactor} : \begin{bmatrix} 0 & 1 & -1 \\ 1 & 0 & -1 \\ -1 & -1 & 1 \end{bmatrix}$$

$$\text{adj}(A) = \begin{bmatrix} 0 & 1 & -1 \\ 1 & 0 & -1 \\ -1 & -1 & 1 \end{bmatrix}$$

$$\text{Inverse}(A_2) = \begin{bmatrix} 0 & -1 & 1 \\ -1 & 0 & 1 \\ 1 & 1 & -1 \end{bmatrix}$$

$$(5) [6]$$