

For the network in Figure 2b, the output can be given by

$$\tilde{a}^{(1)} = \tilde{W} \cdot \tilde{a}^{(0)} + \tilde{b}$$

To establish two networks equivalent, the following equations need to be set up

$$\vec{a}^{(3)} = \tilde{a}^{(1)}$$

$$\vec{a}^{(0)} = \tilde{a}^{(0)}$$

So, we need to list the equation between  $\vec{a}^{(3)}$  and  $\vec{a}^{(0)}$ .

Known by the background, the equation can be given by

$$\vec{a}^{(3)} = W^{(3)} \cdot W^{(2)} \cdot W^{(1)} \cdot \vec{a}^{(0)} + W^{(3)} \cdot W^{(2)} \cdot \vec{b}^{(1)} + W^{(3)} \cdot \vec{b}^{(2)} + \vec{b}^{(3)}$$

Therefore, Network 2's weights ( $\tilde{W}$ ) and bias ( $\tilde{b}$ ) can be given by

$$\tilde{W} = W^{(3)} \cdot W^{(2)} \cdot W^{(1)}$$

$$\tilde{b} = W^{(3)} \cdot W^{(2)} \cdot \vec{b}^{(1)} + W^{(3)} \cdot \vec{b}^{(2)} + \vec{b}^{(3)}$$