

# Larmor precession

Angular momentum of a spin in a magnetic field (in the z-direction), equation of motion is

$$\frac{\hbar d\mathbf{I}}{dt} = \boldsymbol{\mu} \times \mathbf{B} \quad \text{or} \quad \frac{d\boldsymbol{\mu}}{dt} = \gamma_n \boldsymbol{\mu} \times \mathbf{B}$$

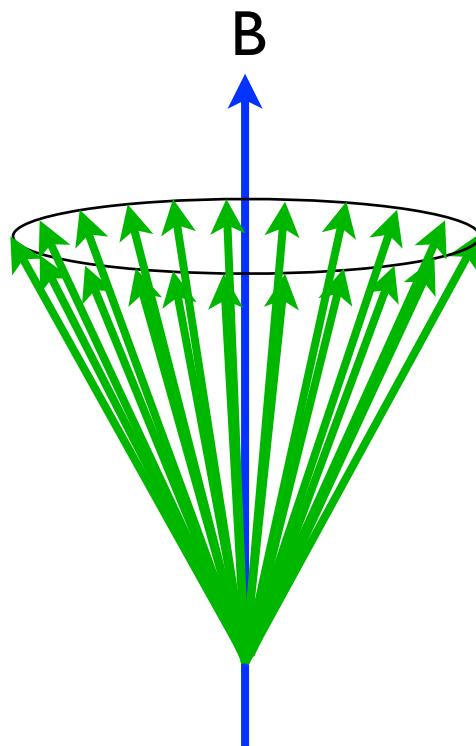
Where the gyromagnetic ratio,  $\gamma_n$ , is the ratio of the magnetic moment to the angular momentum

This gives oscillatory solutions of the form

$$\mu_x = |\mu| \cos \omega_L t \quad \mu_y = -|\mu| \sin \omega_L t$$

describing a precession of the spin around the field direction, with an angular frequency of  $\omega_L$ , the **Larmor precession frequency**

$$\omega_L = \gamma_n B$$



# Adiabatic rotation

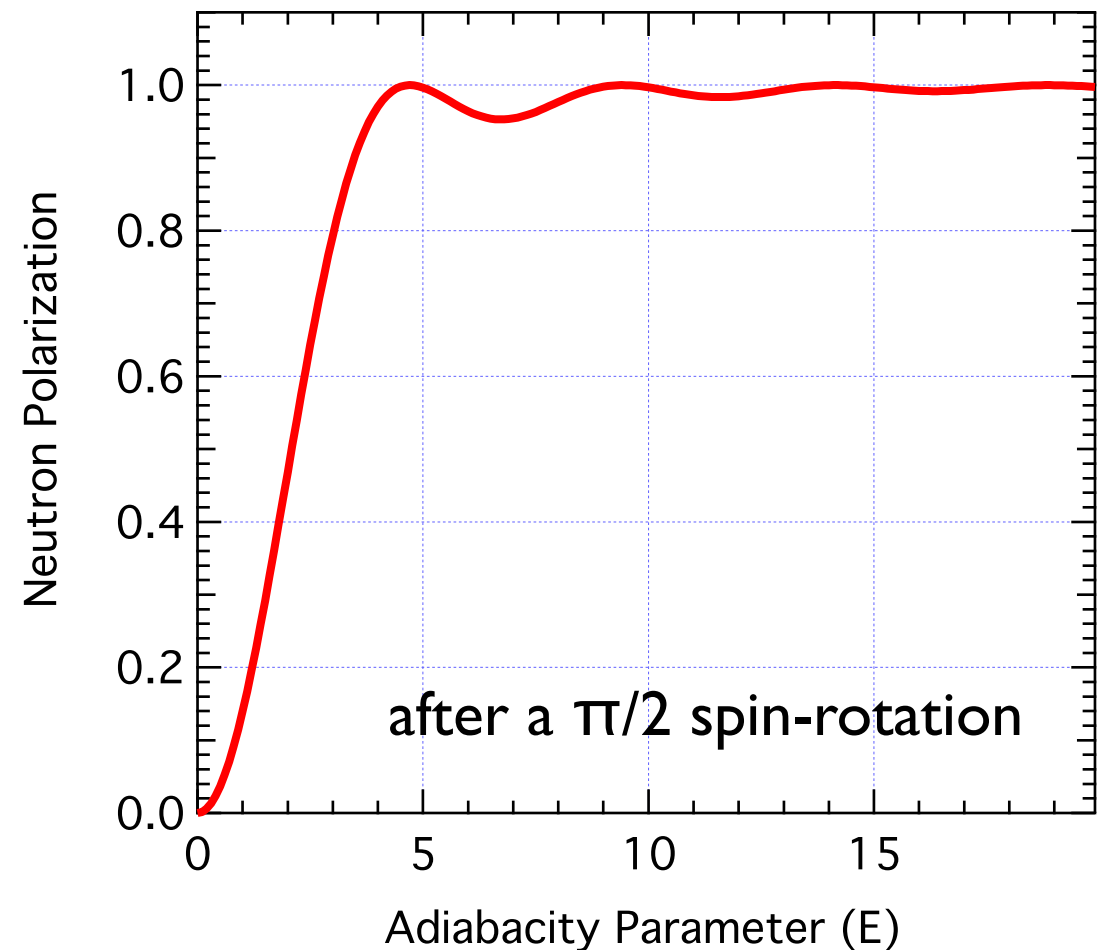
The rate of angular rotation,  $\omega_B$ , of the field along the y-axis in the rest frame of the neutron is:

$$\omega_B = \frac{d\theta_B}{dt} = \frac{d\theta_B}{dy} \cdot \frac{dy}{dt} = \frac{d\theta_B}{dy} v$$

where  $v$  is the neutron velocity

We can therefore define an adiabaticity parameter,  $E$ , where

$$E = \frac{\omega_L}{\omega_B} = \frac{|\gamma_n| B}{\frac{d\theta_B}{dy} v}$$



For an adiabatic rotation without loss of polarization we require  $E > 10$  (by bitter experience)

This inequality corresponds to  $\frac{d\theta_B}{dy} < 2.65 B \lambda$  degrees/cm

with  $B$  in mT,  $\theta$  in degrees, distance  $y$  in cm and neutron wavelength,  $\lambda$  in Å

