

Cooling Down a Coke Can Experiment study

Fluid Mechanics and Transport Processes

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"Cooling down a coke can"

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Chapitre 1

Introduction

This report outlines the physics behind an experiment produced during the MECA-H-3001 "Fluid Mechanics and Transport Processes" course of the ULB (Université Libre de Bruxelles) on Friday, the sixteenth of October 2015.

The experiment can be found at this address ¹ and was described as following:

- Three coke cans were available as well as a bucket of ice and water (at 0°C) and a drill to spin the can inside the bucket.
- One of the cans was used to determine the initial temperature (16°C) of the fluid (essentially water) inside the can.
- One can was left inside the bucket for 60 seconds and a final temperature of 11.9°C was measured as a result of the conductive heat transfer with the surrounding fluid.
- One can was spun inside the bucket for 60 seconds at about 1000 rounds per minute, and a final temperature of 11°C was measured as a result of the convective and conductive heat transfer.

In the first chapter, convective and conductive processes that are related to the experiment will be described. Those phenomena will then be applied to the problem via a mathematical model, including a discussion of simplifications brought to the problem in order to simplify calculations. This model will be compared to the experimental results, then a discussion on it's reliability followed by a conclusion on mathematical models in general will be presented.

^{1.} https://www.youtube.com/watch?v=MSwc_IAPh3E

Chapitre 2

Heat transfer processes

They are three different ways of transferring heat: conduction, convection and radiation. Due to its nature (heat exchange between two distant bodies at very different temperatures), radiation can be neglected for this experiment and will thus not be presented here.

2.1 Conduction

Thermal conduction is a heat transfer process without macroscopic movement of matter. It is initiated by a difference of temperature between contiguous bodies (or inside a body). This difference of temperature implies a difference of internal energy: the energy is higher in the warmer area than in the cooler. By diffusion and collisions between the particles, which can be molecules in a fluid or conduction electrons in a solid, particles in the warmer area transfer kinetic energy to the other particles, making them moving or vibrating faster. This creates a heat flow from the warmer area to the cooler until the system reaches thermal equilibrium. Furthermore, conduction is an irreversible process.

Conduction is described by the following general equation, which is demonstrated in Professor Jean-Marie Buchlin's course[2], Chapter 13.

$$\frac{\delta T}{\delta t} = \nabla \cdot (\alpha \nabla T) + \dot{Q}_v \tag{2.1}$$

This equation can not be used by itself because of it's nature (second degree partial derivative equation). It thus needs boundary conditions linked to properties of the system. Those can be geometrical, physical, temporal or border conditions.

Boundary conditions used and simplifications of the above general equation will be discussed in chapter 3

2.2 Convection

Convection refers to particular heat transfers in fluids. Convection occurs when some fluid is in movement. The movement lead to an advection (heat is transported by moving matter).

Convection is described as following:

$$Convection = Conduction + Advection (2.2)$$

Seeing this, it is easy to understand that convection is superior than conduction in fluids in a flux situation.

An important distinction can be made in convective heat transfers: convection can be natural or forced. Natural convection occurs mainly due to temperature differences which modify fluids density. Increasing the temperature amplifies thermal agitation which leads to a volume expansion along with a decreasing of density. Cold components are thus heavier and fall down while lighter hot components rise. This created a bulk fluid motion initiating a convective heat transfer called natural convection. Forced convection refers to a convective heat transfer due to surface forces which generates a movement in the fuid. Those surfaces forces can can be applied by either artificial ways such as fans or natural ways such as blowing wind. Both natural and forced convection can happend simultaneously.

The flow properties also have a major impact on convective heat transfers and can be expressed through dimensionless numbers. As convection depends on the flow (laminar, turbulent,...), we will discuss the equation to use in the next chapter (Mathematical model, chapter 3).

Chapitre 3

Mathematical model

The idea behind mathematical models is to create a simplified version of a problem, that is accurate enough to predict the behaviour of a system, but simple enough to be resolved with few calculations.

This means that some simplifications of the equations seen before can be made, using the properties of the studied system.

General simplifying assumptions for the experiment will first be described and their validity will be discussed, then two simplified models will be presented : one for the non-spinning can and one for the spinning can.

3.1 General simplifying assumptions

The first assumption that will be considered is that the fluid contained in the can has properties similar to water. Coke is indeed an aqueous solution containing sugar and other ingredients, but at relatively low concentrations. Properties of water can be found in annex A and are extracted from "Perry's Chemical Engineers' Handbook"[1].

Another assumption is that the can is a perfect cylinder with an height of h=116mm and a diameter of $d=66mm^{-1}$. In the reality, the shape of a can is a bit different to support pressure but difference should not be significant in present calculations. The material used for cans is Aluminium and since it is extremely thin(less than 1mm) and has an excellent thermal conductivity (> $200\frac{W}{K.m}$), its influence on heat transfers can be neglected. The considered model will thus be a cylinder of water laid under water maintained at another temperature and without any matter exchange, as shown in figure 3.1.

Furthermore, the hypothesis that all heat exchanges between the can and surrounding ice-cold water take place on de sides of the can and not on it's top or bottom will be assumed. The total

^{1.} dimensions are standard ones for European Aluminium 330ml cans, those can be found on webpackaging.com

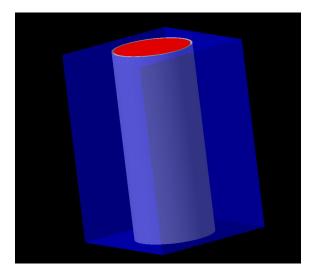


FIGURE 3.1 – The red cylinder is hotter water, the blue box is colder water. No matter exchanges, only heat transfer.

surface of the can is given by:

$$Surface = 2.Surface_{circle} + Surface_{rectangularside}$$

$$\Leftrightarrow S = 2(\pi(\frac{d}{2})^2) + \pi dh$$

$$\Leftrightarrow S = 30.8944cm^3$$
(3.1)

Bottom and top circular surfaces have a total surface of $2xSurface_{circle} = 2(\pi(\frac{d}{2})^2) = 6.8424cm^3$, this is thus about 22.14% of total surface. Reason why it was decided to ignore such a large portion of the can's area is because half of it is not even in contact with ice during the experiment (the system holding the can covers it's top and non-spinning can is not totally in ice), reducing the area to consider at about 11% of total exchange area. This can still be seen as a large percentage, but as it is on the bottom of the can and as we are trying to cool down a liquid, the liquid in contact with the bottom part will be cooler, making heat transfer far less efficient there because cold fluids tend to be more dense than hot fluids.

The last general simplification made for this experiment is to consider the mix of ice and water surrounding the can as a continuous layer of water maintained at 0°C. This should be correct enough considering that there is a large quantity of melting ice in an isolated box; and as liquid water is more flexible than ice, the can has a larger surface in contact with molten ice (and thus water) than with ice itself.

3.2 Simplified models

With these four simplifications in mind, two models will now be build, one for the non-spinning can and one for the spinning can.

3.2.1Non-spinning can

Heat transfer processes in presence are conduction and natural convection. Natural convection appears because of the density change of fluid related to temperature: the cooler the fluid, the denser it is. There is no forced convection because there is no flux in the fluid.

The convective heat transfer coefficient for natural convection (in the can) is given by:

$$h_x = Ra^{\alpha} = cGr^{\alpha}Pr^{\alpha} \tag{3.2}$$

Where Gr is the Grashof number and Pr the Prandtl number. Prandtl can be found in annex A: water being at 16°C(about 290K), it gives Pr = 7.56.

Grashof number is calculated using the following formula (taken from annex B):

$$Gr = \frac{\beta g \Delta T_{ref} d^3}{\nu^2} \tag{3.3}$$

- β is the volume expansion coefficient, given by $\frac{1}{\rho} \frac{\delta \rho}{\delta T}$. Using the tables in annex A, the following approximation can be made : $\beta = 1.001 \times 10^{-3} \frac{\frac{1}{1.000 \times 10^{-3}} - \frac{1}{1.001 \times 10^{-3}}}{5} = 1.998 \times 10^{-4} K^{-1}$.
- $g=9.81\frac{m^2}{s}$ is gravity. $\Delta T_{ref}=16-0=16$ °C is the difference of temperature between the water inside the can and the ice-cold water outside of it.
- $d=33\times 10^{-3}m$ is the diameter of the cylinder. $\nu=\frac{\mu}{\rho}=\frac{1080\times 10^{-6}}{\frac{1}{1.001\times 10^{-3}}}=1.081\times 10^{-6}\frac{m^2}{s}$ is water's kinematic viscosity.

All values used come from annex A.

Rayleigh number is thus:

$$Ra = GrPr = 7.56 \times \frac{1.998 \times 10^{-4} \times 9.81 \times 16 \times (66 \times 10^{-3})^3}{(1.081 \times 10^{-6})^2} = 5.8329 \times 10^7$$
 (3.4)

Since $Ra < 10^9$, the laminar case should be considered. Assuming that the ice-cold water around the can is at a constant temperature, it is now needed to determine which equation to use for Nusselt number.

The easiest approximation is to describe the cylinder as a rectangular enclosure, with H (the height of the enclosure) equal to h = 116mm and L (the characteristic length of the enclosure) equal to $\frac{d}{2} = 33mm$. This gives an H on L ratio of $\frac{H}{L} = 3.352$. The equation 9-53 at page 555 of "Heat and Mass Transfer: Fundamentals and Applications" [3], chapter 9-5 will thus be used:

$$Nu = 0.22(\frac{Pr}{0.2 + Pr}Ra)^{0.28}(\frac{H}{L})^{-1/4}$$

$$\Leftrightarrow Nu = 2.3835 \times 10^{1}$$
(3.5)

and:

$$Nu = \frac{hL}{k}$$

$$\Leftrightarrow h = \frac{Nuk}{L} = \frac{2Nuk}{d}$$

$$\Leftrightarrow h = 4.3191 \times 10^2 \frac{W}{m^2 K}$$
(3.6)

Biot number is given by $Bi = \frac{hL}{k} = \frac{hd}{2k} = 23.8347 > 1$. This indicates that the system can not be considered as a Lumped system, the temperature inside the can is not homogeneous. But, as the temperature is measured manually by putting a thermometer inside the can, and as the size of the thermometer is not negligible compared to the small radius of the can, the system will be simplified by using the equations for a Lumped system in the case of sensible heat transfer:

$$\rho C_p V \frac{dT}{dt} = -hS_{tot}(T - T_{ext})$$

$$\Leftrightarrow \frac{hS_{tot}}{\rho C_p V} dt = \frac{1}{(T_{ext} - T)} dT$$

$$\Leftrightarrow \frac{4h}{\rho C_p d} dt = \frac{1}{(T_{ext} - T)} dT$$

$$\Leftrightarrow \frac{4h}{\rho C_p d} t = \ln(\frac{T_0 - T_{ext}}{T_f - T_{ext}})$$

$$\Leftrightarrow e^{\frac{4h}{\rho C_p d} t} = \frac{T_0 - T_{ext}}{T_f - T_{ext}}$$

$$\Leftrightarrow T_f = T_{ext} + \frac{T_0 - T_{ext}}{e^{\frac{4h}{\rho C_p d} t}}$$
(3.7)

This, when using the parameters of the experiment, would have given $T_f = 284.14K = 10.99$ °C after t = 60s.

This value is quite far from what is observed in the experiment. This is due to some simplifications made here, like, for example, using the Lumped system equations, or some of the parameters choice.

Looking at the parameters, the approximation made for β can be refined if, instead of using the value approximated over the temperature interval, the value for β at 15°C given in Appendix A-1, table A-9 of "Heat and Mass Transfer: Fundamentals and Applications" [3]: $\beta = 1.38 \times 10^{-4} K^{-1}$ is used. Injecting this in the model already adds some accuracy, with a temperature of 11.40°C (284.55K).

Moreover, the values of β and Pr are not fixed, they depend on temperature. To get even more accurate results, "mean values" of those two numbers will now be taken. In order to do so, since their evolution is small in the interval of temperatures $(1.38 \times 10^{-4} \text{ to } 0.733 \times 10^{-4} \text{ for } \beta \text{ and } 8.09 \text{ to } 9.45 \times 10^{-4} \text{ for Prandtl}^2)$, the assumption is made that their variation is linear and that the linear mean value on the interval can be used. In the end, it gives $\beta = 1.056 \times 10^{-4} K^{-1}$ and Pr = 8.77.

To be even more accurate, the same correction can be made for k, ρ and C_p ; values for those parameters becoming $k=0.584\frac{W}{mK}$, $\rho=999.4\frac{kg}{m^3}$ and $C_p=4189.5\frac{J}{kgK}$. Those corrections, when injected in the model, give $T_f=284.77K=11.62^{\circ}\mathrm{C}$ after t=60s. Biot

Those corrections, when injected in the model, give $T_f = 284.77K = 11.62^{\circ}\text{C}$ after t = 60s. Biot number for this case is Bi = 20.8, still high. Even with this high Biot number, the value obtained seems acceptable, considering the simplifications made on the system. The error compared to the experimental result is about 2.38% (when taken in degrees Celsius), and the fact that the temperature measurement made during the experiment where not immediate and that the thermometer itself was warm has to be taken in account.

^{2.} Be warned that the values for Prandtl are different than the one used before: this is due to the fact it was decided to use values from the same source ("Heat and Mass Transfer: Fundamentals and Applications" [3]) here to ensure they are calculated the same way. This also shows the differences that can be observed for the same number, depending of the source and the temperatures it uses as standards

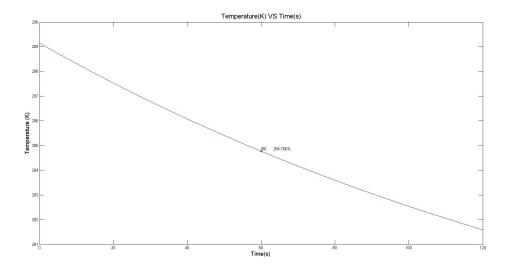


FIGURE 3.2 – Graph of temperature versus time for the non-spinning can. The star marks the 60s point.

The code used for this part of the model can be found in annex C.1

Graph 3.2 gives the evolution of temperature (K) with time (s) for the last model with enhanced approximations of Prandtl and β .

3.2.2 Spinning can

For this model, we will be using simplifying assumptions made in section 3.2.1 concerning Prandtl number (Pr), the density of water (ρ) , the volume expansion coefficient for water (β) , the specific heat of water (C_p) and thermal conductivity of water (k).

For this case, our hotter water cylinder shown in red on figure 3.1 is spinning at $\Omega = 1000 rpm = 1.6667 \times 10^{1} \frac{rounds}{s}$. This can be considered as a flow along a plate, the plate being the interface between hot and cold water, at a certain speed U.

The speed's distribution outside of the can is decreasing quickly, with a maximum on the can's surface. This maximum is given by $U_{max} = \Omega \pi d = 3.4558 \frac{m}{s}$. The speed quickly drops to zero since ice is slowing the water. The We will again use the linear approximation made before and consider that the flow has a "mean" speed of $U = \frac{U_{max}}{2} = 1.7279 \frac{m}{s}$.

Knowing our speed, we can now calculate Reynolds number $Re = \frac{\rho UL}{\mu}$. The characteristic length L for this problem is the circumference of the can, since the speed is tangent to it, so we have $L = \pi d$. ν is the dynamic viscosity of water and can be found on table 9, Annex-1 of "Heat and Mass Transfer: Fundamentals and Applications" [3]. We will use the same approach as before and consider the "mean" value of μ on our interval, which is $\mu = 1.2225 \times 10^{-3}$. Reynolds is thus $\Re = \frac{999.4 \times 1.7279 \times 0.116}{1.2225 \times 10^{-3}} = 1.6386 \times 10^5$.

We will now use the formula for a flow on a flat plate (see annex B page 4). We have $Re < 3 \times 10^5$,

meaning we are in laminar regime:

$$Nu_{out} = \frac{1}{2}0.332Pr^{\frac{1}{3}}\sqrt{Re}$$

$$Nu_{out} = 1.3857 \times 10^{2}$$
(3.8)

We can now calculate h:

$$h_{out} = \frac{Nu_{out}k}{L} = 3.9029 \times 10^2 \frac{W}{m^2 K}$$
 (3.9)

Biot number is given by $Bi = \frac{h_{out}}{\frac{4k}{d} + h_{in}}$ where h_{in} was calculated for natural convection in the non-spinning case 3.2.1. We thus have $Bi = 9.671 \times 10^{-1}$, which is lower than the critical value of 1. Using the lumped system equation is perfectly correct:

$$\rho C_p V \frac{dT}{dt} = -hS_{tot}(T - T_{ext})$$

$$\Leftrightarrow \frac{hS_{tot}}{\rho C_p V} dt = \frac{1}{(T_{ext} - T)} dT$$

$$\Leftrightarrow \frac{4h}{\rho C_p d} dt = \frac{1}{(T_{ext} - T)} dT$$

$$\Leftrightarrow \frac{4h}{\rho C_p d} t = \ln(\frac{T_0 - T_{ext}}{T_f - T_{ext}})$$

$$\Leftrightarrow e^{\frac{4h}{\rho C_p d} t} = \frac{T_0 - T_{ext}}{T_f - T_{ext}}$$

$$\Leftrightarrow T_f = T_{ext} + \frac{T_0 - T_{ext}}{e^{\frac{4h}{\rho C_p d} t}}$$
(3.10)

With $h = h_{out} + h_{in}$ and for t = 60s, we have T = 281.42K = 8.27°C.

Graph 3.3 shows the relation between temperature and time for different rotation speeds, ranging from $\Omega = 0rpm$ to $\Omega = 1750rpm$, with steps of 250rpm. We can clearly see that at higher speeds, the can is cooled down more quickly.

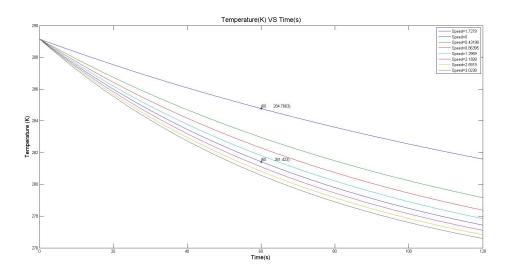


FIGURE 3.3 – Graph of temperature versus time for the spinning can for speeds ranging from $\Omega=0rpm$ to $\Omega=1750rpm$, steps of 250rpm

Chapitre 4

Comparison between reality and the mathematical model

Chapitre 5

Conclusion

Annexe A

Water Thermo-Physical Properties

These chart can be are extracted from "Perry's Chemical Engineers' Handbook", Chapter 2[1].

TABLE 2-352 Saturated Water Substance—Temperature (SI units)

Tomp	K. K	150	160 170 180 200	210 220 230 240 250	255 260 265 270 273.15	273.15 275 280 285 290	295 300 305 310 315	320 325 330 335 340	345 350 355 365 365	370 373.15 375 380 385	390 400 420 430
Surface tension,	Condensed					0.0755 0.0753 0.0748 0.0743	0.0727 0.0717 0.0709 0.0700 0.0692	0.0683 0.0675 0.0666 0.0658 0.0649	0.0641 0.0632 0.0623 0.0614 0.0605	0.0595 0.0589 0.0586 0.0576 0.056	0.0556 0.0536 0.0515 0.0494 0.0472
no.	Vapor					0.815 0.817 0.825 0.833 0.841	0.849 0.857 0.865 0.873 0.883	0.894 0.901 0.908 0.916 0.925	0.933 0.942 0.951 0.960 0.969	0.978 0.984 0.987 0.995 1.004	1.013 1.033 1.054 1.075 1.10
Prandtl no.	Condensed					12.99 12.22 10.26 8.81 7.56	6.62 5.83 5.20 4.62 4.16	3.77 3.42 3.15 2.88 2.66	2.45 2.29 2.14 2.02 1.91	1.80 1.76 1.70 1.61 1.53	1.47 1.34 1.24 1.16 1.09
ductivity, K)	Vapor					0.0182 0.0183 0.0186 0.0189 0.0193	0.0195 0.0196 0.0201 0.0204 0.0207	0.0210 0.0213 0.0217 0.0220 0.0223	0.0226 0.0230 0.0233 0.0237 0.0237	0.0245 0.0248 0.0249 0.0254 0.0258	0.0263 0.0272 0.0282 0.0293 0.0304
Thermal conductivity, W/(m·K)	Condensed	3.73	3.52 3.34 3.18 3.04 2.91	2.79 2.59 2.50 2.42	2.38 2.35 2.31 2.27 2.26	0.569 0.574 0.582 0.590 0.598	0.606 0.613 0.620 0.628 0.634	0.640 0.645 0.650 0.655 0.660	0.665 0.668 0.671 0.674	0.679 0.680 0.681 0.683 0.685	0.686 0.688 0.688 0.688 0.685
Ns/m²	Vapor					8.026 8.096 8.296 8.496 8.696	8.896 9.096 9.296 9.496 9.696	9.896 10.096 10.296 10.496	10.896 11.096 11.296 11.496 11.696	11.896 12.026 12.096 12.296 12.496	12.696 13.056 13.426 13.796 14.146
Viscosity, Ns/m ²	Condensed					17506 16526 14226 12256 10806	9596 8556 7696 6956	5776 5286 4896 4536 4206	3896 3656 3436 3246 3066	2896 2796 2746 2606 2486	2376 2176 2006 1856 1736
eat,	Vapor					1.854 1.855 1.858 1.861 1.864	1.868 1.872 1.877 1.882 1.888	1.895 1.903 1.911 1.920 1.930	1.941 1.954 1.968 1.983 1.999	2.017 2.029 2.036 2.037 2.080	2.104 2.158 2.221 2.291 2.369
Specific heat, C _p , kJ/(kg·K)	Condensed	1.155	1.233 1.311 1.389 1.467 1.545	1.623 1.701 1.779 1.857 1.935	1.974 2.013 2.052 2.091 2.116	4.217 4.211 4.198 4.189 4.184	4.181 4.179 4.178 4.178 4.179	4.180 4.182 4.184 4.186 4.188	4.191 4.195 4.199 4.203	4.214 4.217 4.220 4.226 4.232	4.239 4.256 4.278 4.302 4.331
(kg·K)	Vapor	16.54	15.49 14.57 13.76 13.03 12.38	11.79 11.20 10.79 10.35 9.954	9.768 9.590 9.461 9.255 9.158	9.158 9.109 8.980 8.857 8.740	8.627 8.520 8.417 8.318 8.224	8.151 8.046 7.962 7.881 7.804	7.729 7.657 7.588 7.521 7.456	7.394 7.356 7.333 7.275 7.218	7.163 7.058 6.959 6.865 6.775
Entropy, kJ/(kg·K)	Condensed	-2.187	-2.106 -2.026 -1.947 -1.868 -1.789	-1.711 -1.633 -1.555 -1.478 -1.400	-1.361 -1.323 -1.281 -1.296 -1.221	0.000 0.028 0.104 0.178 0.251	0.323 0.393 0.462 0.530 0.597	0.649 0.727 0.791 0.854 0.916	0.977 1.038 1.097 1.156 1.214	1.271 1.307 1.328 1.384 1.439	1.494 1.605 1.708 1.810 1.911
kJ/kg	Vapor	2273	2291 2310 2328 2347 2366	2384 2403 2421 2440 2459	2468 2477 2486 2496 2502	2502 2505 2514 2523 2532	2541 2550 2559 2568 2577	2586 2595 2604 2613 2622	2630 2639 2647 2655 2663	2671 2676 2679 2687 2684	2702 2716 2729 2742 2753
Enthalpy, kJ/kg	Condensed	-539.6	-525.7 -511.7 -497.8 -483.8	-451.2 -435.0 -416.3 -400.1 -381.5	-369.8 -360.5 -351.2 -339.6 -333.5	0.0 7.8 28.8 49.8 70.7	91.6 112.5 133.4 154.3 175.2	196.1 217.0 237.9 258.8 279.8	300.7 321.7 342.7 363.7 384.7	405.8 419.1 426.8 448.0 469.2	490.4 532.9 575.6 618.6 661.8
m³/kg	Vapor	9.55.+9	9.62.+8 1.08.+8 1.55.+7 2.72.+6 5.69.+5	1.39.+5 3.83.+4 1.18.+4 4.07.+3 1.52.+3	956.4 612.2 400.4 265.4 206.3	206.3 181.7 130.4 99.4 69.7	51.94 39.13 27.90 22.93 17.82	13.98 11.06 8.82 7.09 5.74	4.683 3.846 3.180 2.645 2.212	1.861 1.679 1.574 1.337 1.142	0.980 0.731 0.553 0.425 0.331
Volume, m³/kg	Condensed†	1.0733	1.0743 1.0763 1.0773 1.0783 1.0793	1.0813 1.0823 1.0843 1.0853 1.0873	1.0873 1.0883 1.0893 1.0903 1.0913	1.0003 1.0003 1.0003 1.0003 1.0013	1.0023 1.0033 1.0053 1.0073 1.0093	1.0113 1.0133 1.0163 1.0183 1.0213	1.0243 1.0273 1.0303 1.0343 1.0383	1.0413 1.0443 1.0453 1.0493 1.0533	1.0583 1.0673 1.0773 1.0883 1.0993
Process	_	6.3011	7.7210 7.299 5.388 3.237 1.626	7.016 2.655 8.915 3.724 7.594	1.233 1.963 3.063 4.693 6.113	0.00611 0.00697 0.00990 0.01387 0.01917	0.02617 0.03531 0.04712 0.06221 0.08132	0.1053 0.1351 0.1719 0.2167 0.2713	0.3372 0.4163 0.5100 0.6209 0.7514	0.9040 1.0133 1.0815 1.2869 1.5233	1.794 2.455 3.302 4.370 5.699
Tomp	K K	150	160 170 180 190 200	210 220 230 240 250	255 260 265 270 273.15	273.15 275 280 285 290	295 300 305 310 315	320 325 330 335 340	345 350 355 365	370 373.15 375 380 385	390 400 420 430

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440	490	540	590	630
450	500	550	600	635
460	510	560	610	640
470	520	570	620	645
480	530	580	625	647.3‡
0.0451	0.0339	0.0221	0.0105	0.0026
0.0429	0.0316	0.0197	0.0084	0.0015
0.0407	0.0293	0.0173	0.0063	0.0008
0.0385	0.0269	0.0150	0.0045	0.0001
0.0362	0.0245	0.0128	0.0035	0.0000
1.12	1.25 1.28 1.31 1.35 1.39	1.43 1.47 1.52 1.59 1.68	1.84 2.15 2.60 3.46 4.20	4.8 6.0 9.6 26
1.04 0.99 0.95 0.92 0.89	0.87 0.85 0.84 0.84	0.86 0.90 0.94 0.99	1.05 1.14 1.30 1.52 1.65	2.0 2.7 12 8
0.0317	0.0401	0.0540	0.0841	0.130
0.0331	0.0423	0.0583	0.0929	0.141
0.0346	0.0447	0.0637	0.103	0.155
0.0363	0.0475	0.0698	0.114	0.178
0.0381	0.0506	0.0767	0.121	0.238
0.682	0.651	0.594	0.513	0.412
0.678	0.642	0.580	0.497	0.392
0.673	0.631	0.563	0.467	0.367
0.667	0.621	0.548	0.444	0.331
0.660	0.608	0.528	0.430	0.238
14.506	16.236	18.16	21.56	28.06
14.856	16.596	18.66	22.76	30.06
15.196	16.956	19.16	24.16	32.06
15.546	17.336	19.76	25.96	37.06
15.886	17.726	20.46	27.06	45.06
1626 1526 1436 1366 1296	124.–6 118.–6 113.–6 108.–6 104.–6	1016 976 946 916 886	846 816 776 726	676 646 596 546 456
2.46 2.56 2.79 2.94	3.10 3.27 3.47 3.70 3.96	4.27 4.64 5.09 5.67 6.40	7.35 8.75 11.1 15.4 18.3	22.1 27.6 42
4.36 4.40 4.44 4.48 4.53	4.59 4.66 4.74 4.84 4.95	5.08 5.24 5.43 5.68 6.00	6.41 7.00 7.85 9.35 10.6	12.6 16.4 26 90
6.689	6.312	5.953	5.569	5.115
6.607	6.233	5.882	5.480	5.025
6.528	6.163	5.808	5.318	4.912
6.451	6.093	5.733	5.259	4.732
6.377	6.023	5.654	5.191	4.443
2.011	2.479	2.948	3.419	3.875
2.109	2.581	3.039	3.520	3.950
2.205	2.673	3.132	3.627	4.037
2.301	2.765	3.225	3.741	4.223
2.395	2.856	3.321	3.805	4.443
2764	2799	2792	2717	2515
2773	2801	2784	2682	2466
2782	2802	2772	2641	2401
2789	2801	2757	2588	2292
2795	2798	2737	2555	2107
705.3	929.1	1170	1443	1734
749.2	975.6	1220	1506	1783
793.5	1023	1273	1573	1841
838.2	1071	1328	1647	1931
883.4	1119	1384	1697	2107
0.261	0.0922	0.0375	0.0163	0.0075
0.208	0.0766	0.0317	0.0137	0.0066
0.167	0.0631	0.0269	0.0015	0.0057
0.136	0.0525	0.0228	0.0094	0.0045
0.111	0.0445	0.0193	0.0085	0.0032
1.1103 1.1233 1.1373 1.1523 1.1673	1.1843 1.2033 1.2223 1.2443 1.2683	1.2943 1.3233 1.3553 1.3923 1.4333	1.4823 1.5413 1.6123 1.7053	1.8563 1.9353 2.0753 2.3513 3.1703
7.333	21.83	52.38	108.3	179.7
9.319	26.40	61.19	123.5	190.9
11.71	31.66	71.08	137.3	202.7
14.55	37.70	82.16	159.1	215.2
17.90	44.58	94.51	169.1	221.2
440	490	540	590	630
450	500	550	600	635
460	510	560	610	640
470	520	570	620	645
480	530	580	625	647.3‡

 $^{\circ}$ 1 bar = $10^5\,N/m^2$. †Above the solid line, the condensed phase is solid; below it, liquid.

Critical temperature.

Worrs: The notations of paras is sont, 5-cond, and a second conditions of the c

Annexe B

Formula Sheet

The following formula sheet was given and demonstrated at Pr. Parente's course "MECA-H3001 : Fluid mechanics and transfer processes".

Formula sheet MECA-H-300

Transport Phenomena

October 2015

The definition of the dimensionless numbers as well as the physical understanding of the terms of the equations must be known.

Part I: Momentum

1

Local Equations

Newton's Law:

$$\tau_{xy} = -\mu \frac{\partial u}{\partial y}$$

Mass conservation:

$$\frac{\partial \rho}{\partial t} + \nabla . \left(\rho \overset{r}{V} \right) = 0$$

• Navier-Stokes equations:

- Laminar flow, incompressible and Newtonian fluid:

$$\frac{DV}{Dt} = -\frac{1}{\rho}\nabla P + \frac{\mu}{\rho}\nabla^2 V + F$$

• Euler equation:

$$\rho \frac{DV}{Dt} = -\nabla P + \rho F$$

• Bernoulli equation

$$\rho \frac{V^2}{2} + P + \rho gz = C^{te} = P_{tot}$$

• Laminar boundary layer equation for a flat plate:

$$\frac{\partial u^2}{\partial x} + \frac{\partial uv}{\partial y} = \frac{\mu}{\rho} \cdot \frac{\partial^2 u}{\partial y^2}$$

- Boundary layer thickness: $\delta = \frac{5x}{\sqrt{Re_x}}$

- Friction coefficient: $C_f = \frac{0,664}{\sqrt{Re_v}}$

Integral method:

• Mass conservation:

$$\frac{d[m]_{tot}}{dt} = \langle \rho V_n \rangle_1 S_1 - \langle \rho V_n \rangle_2 S_2$$

$$\begin{split} \frac{d\left[m\right]_{tot}}{dt} = & <\rho V_n >_1 S_1 - <\rho V_n >_2 S_2 \\ & \bullet \quad \textbf{Momentum:} \\ \frac{d\cancel{P}_{tot}}{dt} = & -\Delta_1^2 \left[<\rho V^2 > + P \right] \overset{r}{S} - \overset{r}{F}_{paroi} + m_{tot} \overset{r}{g} \end{split}$$

• Boundary layer:

- Boundary layer thickness:
$$\delta^{**} = \delta \int_{0}^{1} \left(\frac{u}{U_{ext}} - \frac{u^{2}}{U_{ext}^{2}} \right) \cdot d\left(\frac{y}{\delta} \right)$$

- Friction coefficient:
$$C_f = 2 \frac{d\delta^{**}}{dx}$$

• Pressure drops

• Distributed pressure drops:
$$\Delta P_{tot} = \lambda \frac{L}{D} \frac{\rho U^2}{2}$$

- Laminar regime:
$$\lambda == \frac{64}{Re_{D_h}}$$

- Turbulent regime, smooth walls: **Blasius**
$$\lambda = \frac{0.316}{Re_{D_h}^{0.25}}$$

- Turbulent regime, smooth/rough transition: Colebrook
$$\frac{1}{\sqrt{\lambda}} = 1{,}14 - 0{,}87 \ln \left(\frac{9{,}34}{\text{Re}_{\text{D}_{\text{b}}} \sqrt{\lambda}} \right)$$

- Turbulent regime, rough walls: **Nikuradse**
$$\frac{1}{\sqrt{\lambda}} = 1,14 - 0,87 \ln \left(\frac{R}{2} \right)$$

• Concentrated pressure drops:
$$\Delta P_{tot} = K \frac{\rho U_2^2}{2}$$

- Values of K for different configurations:

Elbow

r _c /D	K _c
1	0,35
2	0,19
4	0,16
6	0,21
8	0,28
10	0,32
· ·	· ·

Contraction

D_2/D_1	K _e
0	0,5
0,2	0,49
0,4	0,42
0,6	0,27
0,8	0,20
0,9	0,1

Diffuser

D_1/D_2	$\mathbf{K}_{\mathbf{E}}$
0	1
0,2	0,87
0,4	0,70
0,6	0,41
0.8	0.15

Part II: Energy

Local equations

• Fourier's Law:

$$q_y = -k \cdot \frac{dT}{dy}$$

• Heat transfer with heat source (k=C^{te}):

$$\rho C \frac{\partial T}{\partial t} = k \nabla^2 T + \mathcal{O}_v$$

- Laplacian in Cartesian coordinates $\nabla^2 T = \frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2}$
- Laplacian in cylindrical coordinates: $\nabla^2 T = \frac{\partial^2 T}{\partial x^2} + \frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial T}{\partial r} \right)$
- Laplacian in spherical symmetry: $\nabla^2 T = \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial T}{\partial r} \right)$
 - **◆** Boundary conditions:

Diriclet: $T_{paroi} = T_o(s_{paroi}, t)$

Neuman: $q_{paroi} = -k \frac{\partial T}{\partial n} \bigg|_{paroi} = q_o(s_{paroi}, t)$

Mixed: $q_p = -k \frac{\partial T}{\partial n} \Big|_p = h \left(T_p - T_f \right)$

- h = convective heat transfer coefficient

• Semi-infinite Solid

- Step of temperature: $\Theta = \frac{T T_f}{T_o T_f} = \frac{2}{\sqrt{\pi}} \operatorname{erf} \left(\frac{x}{2\sqrt{\alpha t}} \right)$
 - α = thermal diffusivity
- Periodic perturbation (ω) with amplitude A_o : $\Theta = \frac{T T_o}{A_o} = e^{-x\sqrt{\frac{\omega}{2\alpha}}} \cos\left(\omega t x\sqrt{\frac{\omega}{2\alpha}}\right)$

• Heat equation for a moving fluid 2D:

- Laminar flow, incompressible and Newtonian fluid, constant thermal conductivity:

3

$$\rho C_{p} \left(u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} \right) = k \frac{\partial^{2} T}{\partial y^{2}} + \mu \left(\frac{\partial u}{\partial y} \right)^{2}$$

Global equations

• Thermal Resistance:

- Series:
$$\Re_{\text{th,tot}} = \frac{T_1 - T_2}{\mathcal{E}} = \sum_{i=1}^{N} \Re_{\text{th,i}} = \sum_{i=1}^{N} \frac{\delta_i}{Sk_i}$$

- Parallel:
$$\frac{\&}{T_1 - T_2} = \frac{1}{\Re_{th,tot}} = \sum_{i=1}^{N} \frac{1}{\Re_{th,i}}$$

- Global exchange coefficient:
$$\frac{1}{h_{tot}} = S\Re_{th,tot} = \sum_{i=1}^{N} \frac{\delta_i}{k_i} + \sum_{i=1}^{N} \frac{1}{h_i}$$

Lumped systems

$$\frac{dU}{dt} = hS_{tot}(T_{ext} - T)$$

1. Sensible heat transfer (heating up or cooling down):

$$\rho_s C_s V \frac{dT}{dt} = -h S_{tot} (T - T_{ext})$$

2.Latent heat transfer (fusion or evaporation):

$$\rho \mathcal{L}_{SL} S \frac{de}{dt} = h S_{tot} (T - T_{ext})$$

Contact temperature

$$T_c = \frac{b_1 T_1 + b_2 T_2}{b_1 + b_2} \neq f(t)$$

Effusivity $b = \sqrt{k\rho C}$

• Forced convection correlation (gas and liquids)

- Flat plate, laminar regime
$$Re_x < 3 \cdot 10^5$$

$$Nu_x = \frac{h_x x}{k_f} = 0,332 Pr^{1/3} \sqrt{Re_x}$$

$$Nu_x = \frac{h_x x}{k_f} = 0,029 \, Pr^{0,43} \, Re_x^{0,8}$$

$$\overline{Nu}_{L} = \frac{1}{n} \cdot Nu_{x} (en \ x = L)$$

• n exponent of Re_x

$$\overline{Nu}_{L} = \frac{\overline{h} \cdot L}{k_{c}} = 0,664 \cdot Pr^{1/3} \cdot \sqrt{Re_{L}}$$

- Laminar then turbulent boundary layer

$$\overline{\text{Nu}}_{\text{L}} = 0.036 \cdot \text{Pr}^{0.43} \left(\text{Re}_{\text{L}}^{0.8} - \text{Re}_{\text{c}}^{0.8} \right) + 0.664 \cdot \text{Pr}^{1/3} \cdot \text{Re}_{\text{c}}^{0.5}$$

•
$$Re_c = 2 \times 10^5$$

- Around a cylinder
$$40 \le \text{Re}_{\text{D}} \le 10^5$$
:

$$\overline{\text{Nu}}_{\text{D}} = \left(0.4 \, \text{Re}_{\text{D}}^{0.5} + 0.06 \, \text{Re}_{\text{D}}^{2/3}\right) \text{Pr}^{0.4}$$

- Around a sphere
$$3.5 \le \text{Re}_D \le 8.10^4$$
:

$$\overline{Nu}_{sph} = 2 + \overline{Nu}_{cyl}$$

• Laminar with
$$T_{wall} = C^{te}$$
:

$$Nu_D = 3,66$$

• Laminar with
$$q_{wall} = C^{te}$$
:

$$Nu_D = 4,36$$

$$Nu_D = 0.023 Re_D^{0.8} Pr^{0.4}$$

• Natural convection correlations (gas and liquids)

- Isothermal vertical flat plate

o Laminar
$$10^4 < Ra < 10^9$$
: $Nu_L = 0.59Ra_L^{1/4}$
o Turbulent $10^9 < Ra < 10^{13}$: $Nu_L = 0.10Ra_L^{1/3}$

- Constant heat flux vertical flat plate

o Laminar
$$10^5 < \text{Ra} < 10^{11}$$
: $\text{Nu}_{\text{L}} = 0,750 \left[\text{Ra}_{\text{L}}^* \right]^{0,20}$
o Turbulent $2 \cdot 10^{13} < \text{Ra} < 10^{16}$: $\text{Nu}_{\text{L}} = 0,645 \left[\text{Ra}_{\text{L}}^* \right]^{0,22}$

- Around a vertical cylinder

y	linder		Nu	$= CRa_D^n$
	Ra_D	C	n	
	$10^{-10} - 10^{-2}$	0,675	0,058	
	$10^{-2} - 10^2$	1	0,148	
	$10^2 - 10^4$	0.85	0,188	
	$10^4 - 10^7$	0,48	1/4	
	$10^7 - 10^{12}$	0,125	1/3	

- Around a sphere $10^5 \le Ra_D \le 10^9$

$$Nu_D = 2 + 0.5Ra_D^{1/4}$$

- Vertical plate in confined space

$$Nu_e = \frac{k_e}{k_f} = C \cdot Ra_e^n \cdot \left[\frac{L}{e}\right]^{-m}$$

	Ra _e	C	n	m
Gas				
	2000-2.10 ⁵	0,197	1/4	1/9
	$2.10^5 - 10^7$	0,073	1/3	1/9
Liquid	< 2000	1	0	0
	$10^4 - 10^7$	0,45	1/4	0,3
	10 ⁶ -10 ⁹	0,046	1/3	0

- Horizontal plate in confined space

$$Nu_e = \frac{k_e}{k_f} = C \cdot Ra_e^n$$

	Ra _e	С	n
Gas	< 1700	1	0
	1700 - 7000	0,059	0,4
	7000 - 3,2 10 ⁵	0,212	1/4
	> 3,2 10 ⁵	0,061	1/3
Liquid	< 1700	1	0
	1700 - 6000	0,012	0,6
	6000 - 3,7 10 ⁴	0,375	0,2
	3,7 10 ⁴ - 10 ⁸	0,13	0,3
	> 108	0,057	1/3

• Energy balance by radiation
$$\alpha_{\lambda} + \tau_{\lambda} + r_{\lambda} = 1$$

• Stefan-Boltzmann Law's
$$M^{\circ} = \int_{0}^{\infty} M_{\lambda}^{\circ} d\lambda = \sigma T^{4} \text{ avec } \sigma = 5,67 \text{ } 10^{-8} \text{ W/m}^{2}.\text{K}^{4}$$

• Radiosity of a grey body
$$J = \varepsilon M^{\circ} + rE$$

• Heat flux density lost by a grey body
$$q_{perdue} = \epsilon M^{\circ} - \alpha E = J - E$$

• Radiative heat transfer coefficient
$$h_r = G(\epsilon, F) \cdot \sigma \cdot (T_1^2 + T_2^2) (T_1 + T_2)$$

• Total energy equation

$$\frac{d\left[E_c + E_i + E_p\right]_{tot}}{dt} = -\Delta_1^2 \left[< \rho \left(\frac{V^2}{2} + e_i + \frac{P}{\rho} + gz\right) V_n > S \right] + \mathcal{E} + \overline{\mathcal{W}}$$

• Mechanical energy equation for an incompressible fluid

$$\frac{d\left[E_{c}+E_{p}\right]_{tot}}{dt}=-\boldsymbol{\Delta}_{1}^{2}\left[<\rho\left(\frac{V^{2}}{2}+\frac{p}{\rho}+gz\right)V_{n}>S\right]+\overline{\hat{W}}-\underline{\hat{W}}_{v}$$

• Generalized Bernoulli equation for a flow in a pipe

$$-\Delta_1^2 \left[< \rho \left(\frac{V^2}{2} + \frac{p}{\rho} + e_p \right) V_n > S \right] = \mathcal{E}_v$$

• Internal energy equation for an incompressible fluid

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$$\frac{d[E_i]_{tot}}{dt} = -\Delta_1^2 \left[< \rho e_i V_n > S \right] + e^* + e^* v$$

Part III: Mass

• Fick's Law

$$j_A(x) = -\rho \mathcal{D}_{AB} \cdot \frac{d\omega_A}{dx} \qquad \text{with} \quad \mathcal{D}_{AB} = \mathcal{D}_{BA} = \mathcal{D}$$

• Diffusion into a moving fluid

$$\begin{split} &\overset{r}{n_{A}} - \omega_{A} \begin{pmatrix} \overset{r}{n_{A}} + \overset{r}{n_{B}} \end{pmatrix} = -\rho \mathcal{D} \nabla \omega_{A} & \text{with} \quad \omega_{A} = \frac{\rho_{A}}{\rho} \\ &- & \text{Absolute flux density} \quad \overset{r}{n_{A}} = \rho_{A} \overset{r}{u_{A}} = \overset{i}{j_{A}} + \rho_{A} \overset{i}{U} \\ &- & \text{Barycentric velocity} \quad \overset{r}{U} = \frac{\rho_{A} \overset{i}{u_{A}} + \rho_{B} \overset{i}{u_{B}}}{\rho} \end{split}$$

• Molecular diffusion evaporation of a liquid in a column L

- Mass fraction distribution
$$\frac{1 - \omega_{A}(z)}{1 - \omega_{A,0}} = \left[\frac{1 - \omega_{A,L}}{1 - \omega_{A,0}}\right]^{\frac{z}{L}}$$

- Evaporation mass flow
$$\Re_{A} \approx \left[2 \frac{M_{A}}{RT} \cdot \frac{S}{L} \right] \left(P_{sat}(T) - P_{A,L} \right)$$

- Saturation pressure (T in °C):
$$p_{sat}(T) = 10^{7,625} \frac{T}{241+T} + 2,787$$

- Mass Diffusivity (T in °C et P in Pa) :
$$\mathcal{D} = \frac{2,26}{P} \left(\frac{T + 273,15}{273,15} \right)^{1,81}$$

Mass boundary layer

$$u\frac{\partial \rho_{A}}{\partial x} + v\frac{\partial \rho_{A}}{\partial y} = \mathcal{D}\frac{\partial^{2} \rho_{A}}{\partial y^{2}}$$

Correlation of forced convection mass transfer

$$j_{A,p} = -\mathcal{D}_{AB} \cdot \frac{d\rho_A}{dy} \bigg|_{y=0} = h_m \left(\rho_{A,p} - \rho_{A,ext} \right)$$

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Same expressions of the heat transfer, replacing Nu with Sh and Pr with Sc.

• Perfect gas equation:

$$p_v = \rho_v \frac{\mathcal{R}}{M_v} T_v$$
 with $\mathcal{R} = 8314 \text{ J/kmol.K}$

Annexe C

Codes

The following codes where used to calculate the models and obtain the different graphs. The reader should be advised this code is only usable for this work and should not be reused as it takes in account parameters and simplifying assumptions made for this particular experiment.

C.1 Non-spinning model

```
t = linspace(0,120,1210);
Pr = 8.77
beta = 1.056*10^{(-4)}
rho=999.4;
k = .584;
Cp = 4189.5;
Ra=Pr*(beta*9.81*16*(.066)^(3))/(1.081*10^(-6))^2
Nu = 0.22*(Pr*Ra/(0.2+Pr))^(0.28)*(0.116/0.033)^(-1/4)
h = Nu * k / .033
T60 = (16./(exp((4*h*60)/(rho*4184*.066))))
Tf = 273.15 + (16./(exp((4*h*t)/(rho*Cp*.066))));
plot(t,Tf,60,T60+273.15,'*')
strValues = num2str([60 T60+273.15]);
text(60, T60+273.15, strcat('(', strValues, ')'),'
   VerticalAlignment', 'bottom');
title('Temperature(K) VS Time(s)')
xlabel('Time(s)')
ylabel('Temperature (K)')
```

C.2 Non-spinning model

```
t = linspace(0,120,1210);
Pr=8.77;
beta=1.056*10^(-4);
```

```
rho=999.4;
k = .584:
Cp = 4189.5;
mu = .0012225;
U = 1.7279;
Ra=Pr*(beta*9.81*16*(.066)^(3))/(1.081*10^(-6))^2;
Nuin=0.22*(Pr*Ra/(0.2+Pr))^(0.28) *(0.116/0.033)^(-1/4);
hin = Nuin * k / .033;
Re = rho * U * .116 / mu;
Nuout = .5*.332*Pr^(1/3)*sqrt(Re);
hout = Nuout * k / . 2073451151;
h=hin+hout;
T60 = (16./(exp((4*h*60)/(rho*4184*.066))))
Tf = 273.15 + (16./(exp((4*h*t)/(rho*Cp*.066))));
U0=0;
Re0 = rho * U0 * .116 / mu;
Nuout0 = .5*.332*Pr^{(1/3)}*sqrt(Re0);
hout0 = Nuout0 * k / .2073451151;
h0=hin+hout0;
T600 = (16./(exp((4*h0*60)/(rho*4184*.066))))
Tf0=273.15 + (16./(exp((4*h0*t)/(rho*Cp*.066))));
U2 = .25 * U; U3 = .5 * U; U4 = .75 * U; U5 = 1.25 * U; U6 = 1.5 * U; U7 = 1.75 * U;
Re2=rho*U2*.116/mu; Re3=rho*U3*.116/mu; Re4=rho*U4*.116/mu; Re5
   =rho*U5*.116/mu; Re6=rho*U6*.116/mu; Re7=rho*U7*.116/mu;
Nuout2 = .5*.332*Pr^{(1/3)}*sqrt(Re2);
Nuout3 = .5*.332*Pr^{(1/3)}*sqrt(Re3);
Nuout4=.5*.332*Pr^(1/3)*sqrt(Re4);
Nuout5 = .5*.332*Pr^{(1/3)}*sqrt(Re5);
Nuout6 = .5*.332*Pr^{(1/3)}*sqrt(Re6);
Nuout7 = .5*.332*Pr^{(1/3)}*sqrt(Re7);
hout2=Nuout2*k/.2073451151;
hout3 = Nuout3 * k / . 2073451151;
hout4 = Nuout4 * k / . 2073451151;
hout5 = Nuout5 * k / . 2073451151;
hout6 = Nuout6 * k / . 2073451151;
hout7 = Nuout7 * k / . 2073451151;
h2=hin+hout2; h3=hin+hout3; h4=hin+hout4; h5=hin+hout5; h6=hin+
   hout6; h7=hin+hout7;
Tf2=273.15 + (16./(exp((4*h2*t)/(rho*Cp*.066))));
Tf3=273.15 + (16./(exp((4*h3*t)/(rho*Cp*.066))));
Tf4=273.15 + (16./(exp((4*h4*t)/(rho*Cp*.066))));
Tf5=273.15 + (16./(exp((4*h5*t)/(rho*Cp*.066))));
Tf6 = 273.15 + (16./(exp((4*h6*t)/(rho*Cp*.066))));
Tf7 = 273.15 + (16./(exp((4*h7*t)/(rho*Cp*.066))));
```

```
plot(t,Tf,t,Tf0,'b',t,Tf2,t,Tf3,t,Tf4,t,Tf5,t,Tf6,t,Tf7,60,
   T60+273.15, 'b*', 60, T600+273.15, 'b*')
strValues = num2str([60 T60+273.15]);
text(60,T60+273.15,strcat('(',strValues,')'),'
   VerticalAlignment', 'bottom');
strValues0 = num2str([60 T600+273.15]);
text(60, T600+273.15, strcat('(', strValues0, ')'), '
   VerticalAlignment','bottom');
legend(strcat('Speed=',num2str(U)),strcat('Speed=',num2str(
   U0)),strcat('Speed=',num2str(U2)),strcat('Speed=',num2str
   (U3)), strcat('Speed=',num2str(U4)), strcat('Speed=',
   num2str(U5)),strcat('Speed=',num2str(U6)),strcat('Speed='
   ,num2str(U7)));
title('Temperature(K) VS Time(s)')
xlabel('Time(s)')
ylabel('Temperature (K)')
```

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