# Measuring malapportionment, gerrymander, and turnout effects in multi-party systems

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#### Motivation

### Empirical procedure to measure and analyze the difference between the **votes** and **seats** that parties win in general elections

Central concern of electoral reform debates Kendall&Stuart 1950, Rae 1967, Erikson 1972, Tufte 1973, Taagepera 1973, Johnston 1979, Gudgin&Taylor 1980, Grofman 1983, Cain 1985, Niemi&Fett 1986, King&Browning 1987, Gelman&King 1994, Balinski&Young 2001, Cox&Katz 2002, Engstrom 2006...

Methods exist, but limited to (exceptional) two-party competition

#### Contributions

- Extension to multi-party competition
- 2 Overcome small-N obstacle
- 3 Apply to recent Mexican elections

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### Overview

Key quantity of interest is the system's  $partisan\ bias = undue$  advantage conferred to some party in the conversion of votes into legislative seats

 $\rightarrow$  Potential distortion wherever districts are drawn to allocate seats

Theory highlights three sources of partisan bias

- Gerrymanders (e.g., Cox&Katz 2002)
- Turnout differentials (Rosenstone&Hansen 1993)
- Malapportionment and demographic shifts (Johnston 1979)

Procedure measures three sources

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# UK general election 2015

|                         | V    | 5    | s-v   |
|-------------------------|------|------|-------|
| Conservative            | .369 | .509 | +.140 |
| Labour                  | .305 | .357 | +.052 |
| UK Independence Party   | .126 | .002 | 125   |
| Liberal Democrat        | .079 | .012 | 066   |
| Scottish National Party | .047 | .086 | +.039 |
| Green                   | .038 | .002 | 036   |

|                  | small | large |
|------------------|-------|-------|
| too concentrated | helps | hurts |
| too dispersed    | hurts | helps |

### Overview: approach & results

#### Three models

- lacksquare Grofman, Koetzle & Brunell (1997) ightarrow partisan bias breakdown
- King (1990)  $\rightarrow$  multi-party partisan bias
- Linzer (2012) → data scarcity

### **Findings**

- Persistent bias against the right
- Components of bias often larger than the whole
- Gerrymanders have offset PRI's large turnout advantage

### Road map

- 1 Partisan bias: sources, measurement
- 2 Mexican Cámara de Diputados elections
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### What is partisan bias

It is the excess/defect seat share that a party with half of the votes wins:

$$\lambda = (s \mid v = .5) - .5$$

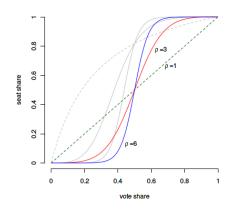
- Two-party, balanced system assumed
- .5 threshold inappropriate for multi-party/imbalanced competition
- Alternative threshold not evident
- Relative quantity preferable

Fitting votes—seats curves: s = f(v)

$$\frac{s}{1-s} = \left(\frac{v}{1-v}\right)^3$$

$$\frac{s}{1-s} = \lambda \left(\frac{v}{1-v}\right)^{\rho} \iff \log \operatorname{id}(s) = \ln \lambda + \rho \operatorname{logit}(v)$$

District responsiveness  $\rho$  (and party bias  $\lambda > 0$  in grey)



# Three sources of partisan bias

|            |        |         | Raw votes |       |       | Vote | shares | Seat  | shares |       |
|------------|--------|---------|-----------|-------|-------|------|--------|-------|--------|-------|
| Districts  | Pop.   | Turnout | left      | right | total |      | left   | right | left   | right |
| Gerryman   | der    |         |           |       |       |      |        |       |        |       |
| 1 and 2    | 420    | .5      | 147       | 63    | 210   |      | .7     | .3    | 1      | 0     |
| 3, 4 and 5 | 420    | .5      | 84        | 126   | 210   |      | .4     | .6    | 0      | 1     |
| nationwide | 2100   | .5      | 546       | 504   | 1050  |      | .52    | .48   | .4     | .6    |
| Turnout    |        |         |           |       |       |      |        |       |        |       |
| 1 and 2    | 420    | .70     | 200       | 100   | 300   |      | .67    | .33   | 1      | 0     |
| 3, 4 and 5 | 420    | .35     | 50        | 100   | 150   |      | .33    | .67   | 0      | 1     |
| nationwide | 2100   | .5      | 550       | 500   | 1050  |      | .52    | .48   | .4     | .6    |
| Malappor   | tionme | nt      |           |       |       |      |        |       |        |       |
| 1 and 2    | 600    | .5      | 200       | 100   | 300   |      | .67    | .33   | 1      | 0     |
| 3, 4 and 5 | 300    | .5      | 50        | 100   | 150   |      | .33    | .67   | 0      | 1     |
| nationwide | 2100   | .5      | 550       | 500   | 1050  |      | .52    | .48   | .4     | .6    |

### Obstacle 1: partisan bias breakdown

Grofman, Koetzle & Brunell (1997): Three ways to aggregate district returns nationwide

$$v_p = \sum_{d} v_{dp} \times \frac{\text{raw vote}_d}{\text{total raw vote}} \tag{1}$$

$$\bar{v}_p = \sum_d v_{dp} \times \frac{1}{\text{total districts}}$$
 (2)

$$\bar{w}_p = \sum_d v_{dp} \times \frac{\text{population}_d}{\text{total population}}$$
 (3)

Fitting votes-seats curve with (1), (2), or (3) yields components

- $\rightarrow$  with v you get raw partisan bias
- $\rightarrow$  with  $\bar{v}$  you get **gerrymander**-based
- ightarrow with  $\bar{w}$  you get **gerrymander** + **malapportionment**-based

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### Obstacle 1: partisan bias breakdown

Trick is to estimate  $\lambda$  with each national vote measure in turn

#### Formulas:

- a raw partisan bias =  $\lambda^{\nu}$
- ${}_{ar{\mathbf{b}}}$  gerrymander-based  $=\lambda^{ar{\mathbf{v}}}$
- d turnout-based =  $\lambda^{v} \lambda^{\bar{w}}$
- a = b + c + d

### Obstacle 2: multi-party competition

King (1990) is a votes-seats curve for a P-party system ( $P \ge 2$ )

$$E(s_p) = \frac{e^{\lambda_p} v_p^{\rho}}{\sum_{q=1}^{P} e^{\lambda_q} v_q^{\rho}}$$

- Akin to switch from dichotomous to multinomial logit regression
- lacksquare Restricting  $\lambda_1=0$  expresses bias relative to party p=1

#### In sum:

Fit equation above using v, then  $\bar{v}$ , then  $\bar{w}$ ; rely on subtraction formulas to get measures of raw partisan bias and its components

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## Background on Mexico

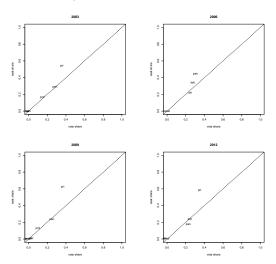
- Hegemonic party 1929–1997
- Three major parties: PRD PRI PAN and minors
- Lower chamber of Congress elected every 3 years, concurrent w presidential race every 6 years
- Mixed system: 300 SMD + 200 PR seats
- Single-term limits removed in 2018
- Independent board (IFE) manages elections and redistricting

### Obstacle 3: small-N

- A general election with *P* parties offers *P* data points to fit a votes-seats curve
- P typically small
- Multi-year approach: pool historic record... may compare apples/oranges in long-haul
- Single-election approach preferable... but requires data multiplication strategy

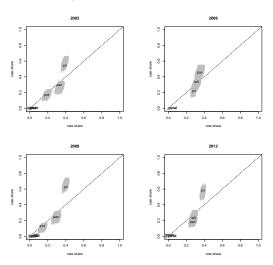
### Monte Carlo simulation

- Linzer (2012): approximates prob. distribution of national party vote returns from observed district outcomes (FMM)
- Use to simulate 1,000 elections



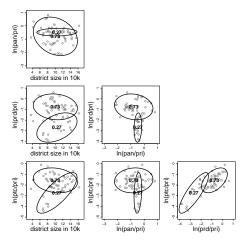
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### Mixture model

- Combines the properties of two or more prob. density functions: can approximate any arbitrary distribution
- Seek components (multivariate normals) and weights of log-ratio votes shares



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### One Mexican-one vote?

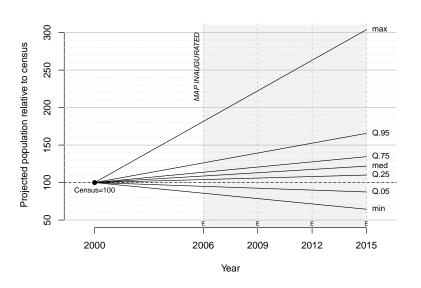
Malapportionment occurs when sparsely populated areas get the same representation as the densely populated

Can arise by commission or by omission (or by accident)

Census lag: most recent decennial census must be used

- ... but no obligation to redistrict as soon as available
- 6-year lag on average: 199**7**, 200**6**, 201**5**
- 2015 map abandoned
- board considers  $\pm 15\%$  imbalance normal (!)

## District populations: linear projection

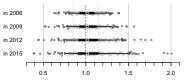


Plus: bureaucratic leeway in new district sizes

### Malapportionment is substantial

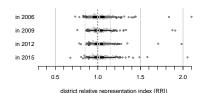
$$RRI = \frac{nat.pop./300}{district size}$$

#### 2006 map (drawn with 2000 census)



district relative representation index (RRI)

#### 2015 map (drawn with 2010 census)



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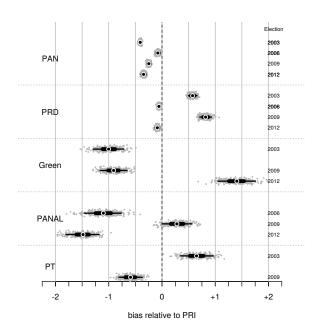
### Estimation

Votes-seats curve fitted with MCMC (Jags via R)

100k iterations of 3 chains, every 500th obs. of last 50k used to sample posterior density

Visual inspection of model parameters to verify chain convergence

# Results: raw partisan bias



| Actual map    |               |                 |              | Нурс        | othetical   | map          |
|---------------|---------------|-----------------|--------------|-------------|-------------|--------------|
| partisan bias | pan-pri       | prd-pri         | min–pri      | pan-pri     | prd-pri     | min–pri      |
| 2003 election | 1             |                 |              | (wit        | h 2006 m    | ap)          |
| raw           | 37 (0)        | +.72<br>(0)     | -1.01 (0)    | 41<br>(0)   | +.57 (0)    | -1.00 (0)    |
| gerrym.       | 09<br>(0)     | $^{+.69}_{(0)}$ | 88<br>(0)    | 13<br>(0)   | +.62        | 90<br>(0)    |
| turnout       | 26<br>(0)     | $11_{(0)}$      | 08<br>(0)    | 26<br>(0)   | 09<br>(0)   | 09<br>(0)    |
| malapp.       | 01<br>(.11)   | +.14 (0)        | 05<br>(0)    | 02<br>(.12) | +.05<br>(0) | 02<br>(0)    |
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| raw           | 08<br>(0)     | 06<br>(0)       | -1.10<br>(0) |             |             |              |
| gerrym.       | +.28          | +.30            | 62<br>(0)    |             |             |              |
| turnout       | 36<br>(0)     | 41<br>(0)       | 43<br>(0)    |             |             |              |
| malapp.       | 00<br>(.42)   | +.05            | 05<br>(0)    |             |             |              |
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| gerrym.       | 28<br>(0)     | 07<br>(0)       | +1.41 (0)    | 24<br>(0)   | 05<br>(.06) | +1.02<br>(0) |
| turnout       | 07<br>(.02)   | 08<br>(0)       | +.02         | 08<br>(.26) | 09<br>(0)   | +.01 (0)     |
| malapp.       | +.01<br>(.42) | +.06            | 02<br>(0)    | 00<br>(.38) | +.01<br>(0) | +.00         |

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- Malapp. always pro-left
- Redistricting abates malapp
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| Actual map Hypothetical map |               |                    |              |             |                 | map          |
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|---------------|---------------|-------------------------|--------------|-------------|-------------------------|-----------|--|--|
| partisan bias | pan-pri       | pan-pri prd-pri min-pri |              |             | pan-pri prd-pri min-pri |           |  |  |
| 2003 election | n             |                         |              | (wit        | th 2006 m               | ap)       |  |  |
| raw           | 37 (0)        | +.72<br>(0)             | -1.01 (0)    | 41<br>(0)   | +.57 (0)                | -1.00 (0) |  |  |
| gerrym.       | 09<br>(0)     | $^{+.69}_{(0)}$         | 88<br>(0)    | 13<br>(0)   | +.62                    | 90<br>(0) |  |  |
| turnout       | 26<br>(0)     | 11<br>(0)               | 08<br>(0)    | 26<br>(0)   | 09<br>(0)               | 09<br>(0) |  |  |
| malapp.       | 01 (.11)      | +.14<br>(0)             | 05 (0)       | 02<br>(.12) | +.05<br>(0)             | 02<br>(0) |  |  |
| 2006 election | n             |                         |              | , ,         |                         |           |  |  |
| raw           | 08<br>(0)     | 06 (0)                  | -1.10<br>(0) |             |                         |           |  |  |
| gerrym.       | +.28<br>(0)   | +.30<br>(0)             | 62<br>(0)    |             |                         |           |  |  |
| turnout       | 36<br>(0)     | 41<br>(0)               | 43<br>(0)    |             |                         |           |  |  |
| malapp.       | 00<br>(.42)   | +.05                    | 05<br>(0)    |             |                         |           |  |  |
| 2009 election | n             |                         |              | ļi          |                         |           |  |  |
| raw           | 25<br>(0)     | +.82                    | 91 (0)       |             |                         |           |  |  |
| gerrym.       | 11<br>(0)     | +1.01<br>(0)            | 79<br>(0)    |             |                         |           |  |  |
| turnout       | 14<br>(0)     | 24<br>(0)               | 12<br>(0)    |             |                         |           |  |  |
| malapp.       | 00<br>(.36)   | +.05                    | 00<br>(0)    |             |                         |           |  |  |
| 2012 election | n             |                         |              | (wit        | h 2015 m                | ap)       |  |  |
| raw           | 35<br>(0)     | 09<br>(0)               | +1.40<br>(0) | 32<br>(0)   | 13<br>(0)               | +1.03     |  |  |
| gerrym.       | 28<br>(0)     | 07<br>(0)               | +1.41        | 24<br>(0)   | 05<br>(.06)             | +1.02     |  |  |
| turnout       | 07<br>(.02)   | 08<br>(0)               | +.02         | 08<br>(.26) | 09<br>(0)               | +.01      |  |  |
| malapp.       | +.01<br>(.42) | +.06                    | 02<br>(0)    | 00<br>(.38) | +.01                    | +.00      |  |  |

- Turnout always pro-PRI
- Malapp. always pro-left
- Redistricting abates malapp.
- Possibly cancelling effects

# Road map

- 1 Partisan bias: sources, measurement
- 2 Mexican Cámara de Diputados elections
- 3 Malapportionment
- 4 Results
- 5 Final remarks

## The bigger project

Draw Mexico project = offspring of Public Mapping Project in U.S.

Remove opaqueness from redistricting process

DistrictBuilder is open-source, web-based software

- enables widespread DIY redistricting thru cloud computing
- internet lets anyone draw/inspect maps: crowdsourcing
- $\blacksquare$  redistricting contests in 6 US states  $\rightarrow$  hundreds of legal plans

Application to Mexico (Donations anyone?)

### Findings & next steps

- I Rel. to the right, persistent pro-PRI, and esp. pro-left raw bias
- Malapportionent effects are (surprisingly) small
- Pro-PRI turnout-based bias
- 4 Gerrymander effects large and volatile
- District lines can compensate for turnout disadvantage
- To-do: add PR-tier to analysis
- To-do: inspect inter-election volatility

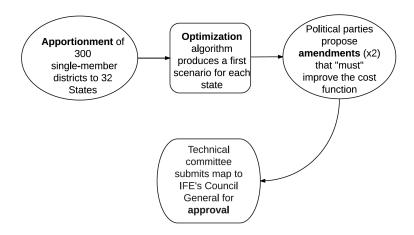
Thank you!

## Findings & next steps

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### Thank you!

### The redistricting process



### The redistricting process

$$\label{eq:score} \begin{aligned} \texttt{Score} &= .4 \times \texttt{PopBalance} + .3 \times \texttt{MunicBoundaries} \\ &+ .2 \times \texttt{TravelTime} + .1 \times \texttt{Compactness} \end{aligned}$$

Plus: minority representation (40 % indigenous pop.)

Board tolerates  $\pm 15\%$  imbalance to accommodate this

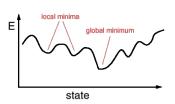
### Optimization algorithm

Simulated annealing = probabilistic meta-heuristic for optimization locates a good approximation to the global optimum of the cost function in a large search space

Thousands of iterations using electoral secciones

Combinatorial optimization algorithm used to generate the first scenario in each state

#### Simulated Annealing



IFE claims that this is a public process, but the operation and procedures are done behind closed doors

### Party amendments

