The Effects of Automated Redistricting and Partisan Strategic Interaction on Representation: The Case of Mexico*

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Abstract

In the U.S. redistricting is deeply politicized and often synonymous with gerrymandering — the manipulation of boundaries to promote the goals of parties, incumbents, and racial groups. In contrast, Mexicos redistricting since 1996 has been done with automated algorithms devised by the federal electoral regulator (the IFE) in consultation with parties. In this setting, parties generate counterproposals to the computer-generated map, in a closed-door process not revealed outside the bureaucracy. Applying geospatial statistics and large-scale optimization to a novel dataset that has never been available outside the IFE, we analyze the effects of automated redistricting and partisan strategic interaction on representation. Our dataset comprises the entire set of plans generated by the automated algorithm, as well as all the counterproposals made by each political party during the 2013 redistricting process. Additionally, we inspect the 2006 map with new data and two proposals to replace it towards 2015 in search for partisan effects and political distortions. Our analysis offers a unique insight into the internal workings of the purportedly autonomous IFE and the partisan effects of automated redistricting on representation.

A fundamental principle of democratic governance is that the will of the people is the main engine of public policy. Usually, electoral institutions serve the purpose of translating the peoples' will, expressed by their votes, into the selection of representatives, who enact policies. In redistricting — the periodic drawing of electoral

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boundaries, ostensibly to achieve seemingly apolitical goals such as balancing districts' populations — the causal chain can be reversed. The drawing of new electoral boundaries may allocate voters to districts in ways that affect the number of legislative seats parties are expected to win, the careers of incumbents, and representation for racial and other interest groups. With so much at stake, scholars have found the redistricting process can distort representation, through an eponymous strategy known as gerrymandering (Cox and Katz 2002, Engstrom 2006, Erikson 1972, Mayhew 1974).

Some state governments have sought to remove the opportunity for politicians to engage in gerrymandering by shifting redistricting authority from state legislatures to commissions; although some commissions' rules and membership continue to produce highly politicized outcomes, while others less so (McDonald 2004, Trelles and Martínez 2012). Mexicans similarly decided to overcome this challenge by delegating redistricting authority to the Federal Electoral Institute (IFE), an independent election management board created in 1990. Mexico has innovated beyond the U.S. by employing self-tailored automated algorithms to find redistricting plans deemed optimal on a priori criteria, and for political parties to react by offering counter-proposals (Trelles and Martínez 2012). Here, we examine the extent to which technocrats have supplanted politicians (Lujambio and Vives Segl 2008) by analyzing a novel dataset describing partisan interaction within IFE in the 2013 redistricting process.

Despite that electoral officials may claim to be politically neutral, scholars find the rules by which they operate may not constrain political manipulation (Estévez, Magar and Rosas 2008, Lijphart 1990, Rossiter, Johnston and Pattie 1997). Furthermore, criteria may embody subtle second order biases that produce a predictable political outcome (Parker 1990). Rather than removing political bias, redistricting by commission may perpetuate it in a different guise. In particular, IFE conducts redistricting behind closed doors, without public scrutiny, much less public participation (Trelles and Martínez 2008). The media and public are provided insufficient information to assess if the final plan embodies political mischief — for example, how the plan produced by automation methods differs from the final plan — before the new plan is formally adopted by IFE's Council General and takes effect.

In 2013, as in 1996 and 2005, IFE employed an algorithmic redistricting process

¹The lack of information in previous redistricting rounds, even within the IFE, generated non-functional districts. In 1996 and 2004, for instance, electoral commissioners received complains — from several local IFE commissions and party representatives in states like Sonora and Chihuahua — arguing that they where not allowed to participate in the redistricting process and that several districts, despite being "optimal," where splitting communities or had major geographical accidents making them dysfunctional for organizational and campaign purposes (Trelles and Martínez 2008).

based upon criteria agreed amongst IFE's electoral commissioners before plans were drawn. IFE used the 2005 algorithm (a simulated annealing combinatorial optimization heuristic) with the same four input parameters (population balance, compactness, municipal integrity and traveling time), but with a slightly re-weighted overall scoring function to optimize (Federal Electoral Institute 2013, Trelles and Martínez 2008). As in 2005, the base geography was modified so that the algorithm could not partition minority municipalities and 25 districts where created with at least 40% of indigenous population.

The last redistricting process towards the 2015 election offers an opportunity to assess the robustness of Mexico's redistricting process. For the first time, IFE created a web-based map sharing tool, which allows us to analyze all redistricting plans formally introduced throughout the process. A large number of plans were produced, more than in any previous redistricting, as IFE invited two sets of institutional actors to participate in the process: the seven national parties represented in the National Surveillance Commission (NSC) and the same seven parties represented in each of the 32 state-based Local Surveillance Commissions (LSC). IFEs Technical Redistricting Committee enabled strategic interaction between entities by allowing them to observe counter-proposals formulated by other parties through the platform. Observations and counter-proposals took place in the first and second — out of three — stages of the process.²

In the end, despite consensus within party representatives at IFE to endorse the final plan (they actively participated in the process), unexpected partisan resistance in the three major national party headquarters (PAN, PRI and PRD) stalled adoption of IFE's final plan and ushered in a set of reforms to the Mexican electoral system in early 2014. The way that redistricting has played out so far in Mexico and the last set of electoral reforms — specially the reintroduction of legislative reelection starting in 2015 — raise a number of questions: Are the adopted redistricting criteria politically neutral? Were the plans produced algorithmically optimal with respect to the selected criteria? How did partisan counter-proposals differ from the bureaucratic solution? What influence did parties have on the final plan?

²The idea of partisan interaction was introduced in the International Redistricting Seminar celebrated at IFE in Mexico City in November 2012. IFE had allowed parties to formulate observations in 1996 and 2005, but no interaction platform existed so that parties could observe what others were proposing. The authors of this paper introduced the idea during the presentation of the Public Mapping Project Mexico (www.publicmapping.org), an open source web based platform that allows citizens and parties to analyze redistricting scenarios, observe what other users are proposing, and formulate counterproposals in order to optimize the criteria established by the legal framework and allow the authority in charge of redistricting to automatically rank and evaluate counterproposals.

In this work we answer these questions and assess Mexico's redistricting process in search of partisan effects on representation by inspecting data that has never been available outside of the Mexican government. It comprises the machine generated plans and two rounds of strategic counter-proposals made by political parties.

1 Automated redistricting and party input

Mexico adopted a mixed-member electoral system for the lower house of Congress for the 1979 congressional election. Three hundred single-member districts were drawn to elect three-fourths of the chamber by plurality rule. That proportion fell to three-fifths since 1985, but the number of single-member districts has not changed. No boundary lines are drawn for the compensatory, proportional representation seats; accordingly, we leave them out of the analysis, and by seats/districts, in the paper, we always refer to the single-member kind. The original district map was redrawn in 1997, coinciding with the first free and fair congressional election (Lujambio and Vives Segl 2008). Redistricting occurred again in 2006, and was meant to be undertaken, but aborted, in 2015.

We use years to name the different maps, sticking to the convention of using not the date when boundaries were actually redrawn and accepted, but that of the first election the map was (or would have been) used. Thus, there is a "1979 map" actually drawn in 1978, a "1997 map" drawn in 1996, a "2006 map" drawn in 2004–05, and a "2015 map" drawn in 2013, but never used.

The method adopted has relied on machine-assisted mapping since 1997. Details have changed, but the broad lines have not (Trelles and Martínez 2008). We describe the three major stages of the redistricting process: the apportionment of seats to states; the design of an optimization algorithm; and the strategic assessment of computer-generated district blueprints by a technocrats with active, but limited involvement of political parties.

Apportionment. This stage redistributes a fixed number of seats among the 32 states.³ Restrictions, reminiscent of the U.S., apply: no state may have fewer than two seats; the sole redistributive criterion above that minimum is state population; and no district may cross state boundaries. The next section elaborates the apportionment method used and some problems for representation.

Optimization. This stage adopts a set of desiderata for a new map drawn from

³The Federal District, where Mexico City resides, is not a state proper, but is treated as one for the purpose of apportionment and redistricting.

the base geography. The process makes marginal changes to boundaries, repeatedly reassigning geographical blocks between districts, systematically checking tradeoffs between criteria in a formal cost function, and iterating it all with different random seeds. Cost-minimizing district maps for each state are thus generated. The building blocks are more than 66 thousand secciones electorales into which the Mexican territory is subdivided. Secciones are analogous to U.S. census tracts, but somewhat bigger. Median sección population in the 2010 census was 1,280 persons, with a maximum at 79,232. Restrictions also apply: contiguity is a must, no district can have exclaves; as are guarantees for minority representation, municipios (the lowest elected offices, similar to counties in the U.S.) with sizeable indigenous populations cannot be partitioned.

More refined optimization algorithms have been used in each redistricting round. The algorithm described in the last paragraph, used for the 2015 map, replaced a method of simulated annealing used for the 2006 map. The most recent cost function included four criteria (and relative weights): population balance (.4), municipal boundary preservation (.3), travelling times inside the district (.2), and district compactness (.1). IFE would tolerate population deviations of up to 15% across districts, and deviations above that threshold with proper justification. The tecnical committee made a 2015 map proposal ("scenario 1") on July 17, 2013.

Assessment. The third stage begins once the first scenario has been formally presented by IFE's technical committee — appointed by the Council General — and distributed to the parties. It involves two rounds where technical experts comment on the maps and political parties observe and suggest modifications to the maps.⁴ Amendments are proposed to the first scenario, and those that are adopted by the technical committee are then used as a starting point for another round of partisan observations to produce a second scenario. Parties are invited again to propose a second round of amendments and, once they have been analyzed and discussed by the technical committee again, a final plan is presented to the Council General to be formally approved.

It is at this stage where parties interact strategically with mapmakers, and other parties. Parties propose amendments to the computer-generated plans, but these amendments must improve the overall cost score to be considered for adoption. Table 1 summarizes the two rounds of amendments that took place in preparation for the 2015 map. The number of proposals increased significantly over previous redistricting, because IFE expanded participation to the its state offices, giving the parties two

⁴This stage took approximately 4 months. It began in July 2013 and concluded in October 2013.

Party	national	state	total 1st	national	state	total 2nd	Total
PAN	17/22	2/20	19/42	17/24	4/16	21/40	40/82
PRI	0/0	2/28	2/28	8/30	6/26	14/56	16/84
PRD	3/27	2/21	5/48	5/29	5/18	10/47	15/95
PT	1/12	1/20	2/32	3/15	1/16	4/31	6/63
PVEM	0/0	1/20	1/20	7/28	3/17	10/45	11/65
MC	1/17	0/21	1/38	6/32	2/16	8/48	9/86
PNA	0/1	1/18	1/19	4/11	3/17	7/28	8/47
IFE	0/0	1/9	1/9	0/0	5/13	5/13	6/22
Total	22/79	10/157	32/236	50/169	29/139	43/308	111/544

Table 1: Counter-proposals to the first and second scenarios at the National and Local Surveillance Committees. Denominator reports the number of counter-proposals made, numerator how many were adopted. Prepared by authors with information from the Federal Electoral Institute.

channels to deliver simultaneous counter-proposals. There were a total of 534 counterproposals made for the 2015 map (more than twice of the counterproposals made for the 1997 and 2006 maps). 236 counterproposals were made to the first scenario (157 from the LSC and 79 form the NSC) and 308 were made to the second scenario (139 by the LSC and 169 by NSC).

Parties actively challenged proposed districts, making 75 counter-proposals each on average. Although we expected that all 7 parties would behave as rational selfinterest maximizers and strategically make competitive counter-proposals to the first scenario, the right-of-center PAN was, by far, the most successful. Nearly half of their 82 proposals were accepted, compared to about one-fifth for the other major parties (PRI and PRD). Amendments originated in both national (7 parties at the National Surveillance Commission) and state level (same 7 parties represented at 32 Local Surveillance Commissions).⁵ Activity at the amendment stage was enhanced by the adoption of an internal web-based map-sharing tool, which standardized counterproposals and enabled parties to observe each others' amendments — improving information for strategic behavior. The final proposal for Council General approval was presented on October 15, 2013. In the midst of a major electoral reform that took place in December that year, the Council General, driven by the pressure of the three major parties (PAN, PRI and PRD), chose not to decide before the end of the year. The 2015 midterm election, it was soon after learned, would be held with significantly outdated districts.

 $^{^5{\}rm The}$ full set of parties represented in each committee were PAN, PRI, PRD, PT, PVEM, MC and PNA.

We investigate how the 2015 redistricting process unfolded in Figure 1. For each of Mexico's thirty-two states we plot the overall score for each proposed redistricting plan (the value of the algorithm's cost function for the three scenarios are black points, numbered). The optimization objective is to produce a plan with the least cost, so plans with lower values are better than plans with higher values. The first scenario resulted from the optimization algorithm prior to party feedback, the second and third from party amendments. Colored points are party counteproposals to the second scenario, blue for the PAN, red for the PRI, yellow for the PRD, grey for the best offer by a minor party.⁶ Brown points represent two or more counter-proposals with equal scores, with one protruding petal for each plan. The cost function is expressed relative to the value of the second proposal.

In all but one state (Baja California Sur, BCS), the progression of scenarios is towards improving the cost function, as the third and final scenario has a lower score than either of the two prior scenarios. We observe numerous instances where humans "beat" the machine, by offering counter-proposals that improve the first scenario's score. These plans demonstrate how redistricting is a complex integer optimization problem where optimization algorithms can become stuck in local optima (Altman and McDonald 2011). Where the adopted amendments to the first scenario improve the score greatly — as is the case in Hidalgo (Hgo), Puebla (Pue) and San Luis Potosí (San) — the second round of counterproposals fails to further improve the previous round given that the margin to make changes becomes narrower. We cannot know for certain if these final plans are the global optimum since the algorithm departed from a randomly chosen seed and redistricting is such a challenging optimization problem.

There are three instances where the PRD offered a counter-proposal improving upon the first scenario and all other amendments, but the amendment was rejected: Durango (Dgo), Morelos (Mor), and Quereíaro (Que). Two identical plans proposed in Tabasco (Tab) similarly are the objectively best plans, but are rejected. In these three instances, a second round of partisan observations fails to find better plans. This provides further evidence of how automated algorithms are challenged by the complexities of redistricting. More importantly, the existence of these better plans demonstrates that politics is present in the process, likely to the detriment of the PRD.

There are several proposals that have identical scores to the first scenario, and

⁶The same analysis for party reactions to the first proposal would reveal another interesting aspect of negotiation. A successful amendment in the first round sets the starting point for the optimization process towards the second round, and this might lend important proposal power. PAN was, by far, the most successful party in the first round.

Proposals and counterproposals

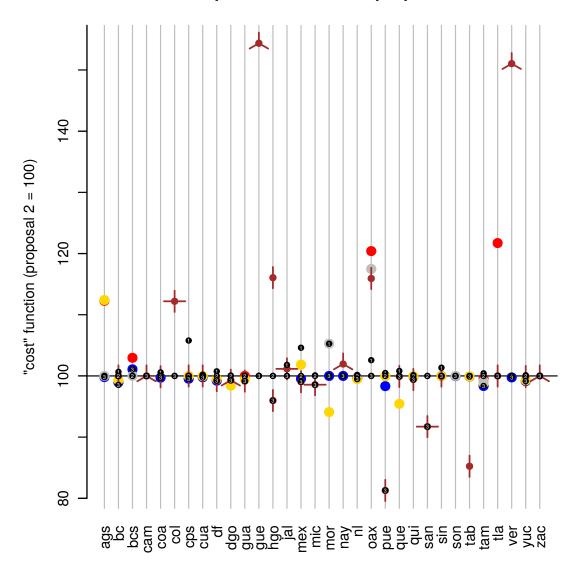


Figure 1: Map proposals towards 2015 by state. Black, numbered points indicate the value of the algorithm's cost function for the three map scenarios. The cost function is expressed relative to the value of the second proposal. Colored points are party counterproposals to the second proposal, blue for the PAN, red for the PRI, gold for the PRD, grey for the best offer by a minor party. Brown points report overlaps of two or more counter-proposals, one protruding petal for each overlap.

Similarity between	\min	25%	median	75%	max
first 2015 proposal and status quo	0.128	0.419	0.584	0.755	1
final 2015 proposal and status quo	0.125	0.437	0.643	0.805	1
first and final 2015 proposals	0.174	0.705	0.967	1	1

Table 2: District similarity before and after the failed 2015 redistricting

several instances where two proposals have identical scores. If two scenarios were tied, the technical committee would adopt the proposal that had lower cost values associated to the most relevant criteria — population, followed by municipal integrity, traveling time and compactness at the end (Federal Electoral Institute 2013). Further investigation may reveal subtle differences between these seemingly-similar plans, such as the assignment of two secciones to different districts that has minimal changes on the overall score. We also observe numerous instances where parties propose plans that score worse than the first scenario. In many cases, as in 2005, parties decided — even if the cost function of their counterproposal was higher than the departing scenario — to present their plan and try to argue that their plan represented better specific communities or that responded better to geographical or socioeconomic characteristics not considered by the optimization algorithm.

In another key respect, all processes have remained opaque activities between electoral regulators and party representatives. New technology letting anyone interested, with little more than an Internet connection, see proposals, react, and improve them through crowd-sourcing or an open web based platform (Altman and McDonald 2011, Trelles 2015), remains to be adopted. We observe evidence to suggest such transparency may not be welcome by all parties, as the PRD proposed objectively better plans that were never adopted.

2 The 2006 Map and the 2015 Proposals

A new map is a full description of district boundary changes. The common way to visualize a map is by drawing it. We look at maps differently, with focus not in the physical lines and line changes but in their political consequences. Putting the 2006 map and the 2015 final proposal drawings side to side reveals boundary shifts. But unless the drawing is more data rich, assessing even the relatively simple question of how similar districts were before and after redistricting visually is a challenge.

But a similarity index (Cox and Katz 2002:15–7) offers ground for assessment. Measurement identifies the parent district or single largest contributor of population

to every new district. The similarity index divides the population that parent and new district share in common by their joint population: s = c/(p + n - c). The range is zero (district shares no population at all with parent) to one (districts are identical). Table 2 describes the change that the 2015 map would have brought in the 300 single member districts, comparing IFE's initial and final proposals with the 2006 map. Also compared are the final and initial 2015 proposals themselves.

Six percent of districts entertained no change in boundaries whatsoever vis-à-vis the status quo (18 districts in the initial proposal, 19 in the final), and twice as many had at least nine-tenths of the population in common (40 districts in the initial, 44 in the final proposal). Inspecting which districts were a priori chosen for marginal or no change might reveal systematic distortions of the automated redistricting algorithm. Party feedback left 39 percent of districts in IFE's first proposal intact, and 62 percent with up from nine-tenths of the population in common. Inspecting which districts the parties targeted for major amendment — presumably a partial reinstatement of a preferred status quo district — should shed further light into the subject. Note how median district similarity with the 2006 map augmented from first to final proposal. So did the third quartile. Accepted counter-proposals therefore reconstituted portions of status quo districts. This seems consistent with a view where parties protect strongholds that the algorithm may have split, but further analysis must be done.

Noting that victory margins began widening in the mid-1960s, Mayhew (1974) saw gerrymandering as one possible explanation, incumbents influencing the preservation of safe districts. While the argument opened the heated incumbency advantage debate, the intuition may guide our inquiry. District volatility should capture a key element for analysis of map similarities. District d volatility is $v_d = 1/2\sqrt{\sum_{p=1}^{P}\sum_{t=2}^{3}(v_{d,p,t}-v_{d,p,t-1})^2}$ with p indexing the competing parties and t = 1, 2, 3 for the 2006, 2009, and 2012 congressional elections respectively.

Mexican party strength is not proportional to the formidable entry barriers they enjoy and massive public subsidies they receive yearly (Magar 2015). Evidence of this is their inability to cultivate loyal voters. District volatility is remarkably high, as shown in Table 3. The median district saw 25 percent of votes change party hands between 2006 and 2012 (not exactly how the index reads, but close enough). With so many volatile districts around, parties should have attempted to redress strongholds that automated redistricting split beyond recognition. How much were strongholds

⁷The measure of volatility proposed is inspired in measures of disproportionality, replacing the seats–votes difference with vote first differences. It is a squared version of a Loosemore-Hanby index (Gallagher 1991, Loosemore and Hanby 1971).

	min.	25%	median	75%	max
district volatility	.08	.19	.25	.31	.52
mean PAN margin	49	23	10	.01	.28
mean PRI margin	43	09	01	.07	.28
mean PRD margin	51	31	21	04	.39

Table 3: 2006 map district volatility and party margins in three congressional elections

affected by the initial 2015 proposal? To what extent did party counter-proposals redress them? This should be a promising line of inquiry.

3 Conclusion

** To be written **

Mexico's federal districts exhibit no party bias when analyzed at the state level. Big system responsiveness, typical of first-past-the-post system in units with few federal districts, is associated with the districts. So PRI's tendency to be over-represented more than PAN and PRD, and the PRI's winning of a couple extra seats with the redistricting proposal is not the product of partisan bias. If the PRI wins more this is due to its status as the largest party in more states that the other two major parties combined.

Appendix

Elasticity

How elastic a district is to a party's statewide (nationwide?) vote swings is interesting. Elasticity should shape redistricting preferences. A district is highly elastic for the PAN when small shifts in the party's vote statewide correspond to sharp district vote hikes. It is inelastic when it corresponds to more modest district vote changes. Negative elasticity is even conceivable, the district vote growing when the rest of the state shrinks. Local effects on mobilization and voting can move against state effects. If every sección in the district is a microcosm of the state's electorate, unit elasticity ensues.

The measure regresses a party's three-year vote change in the sección Δ_s on the

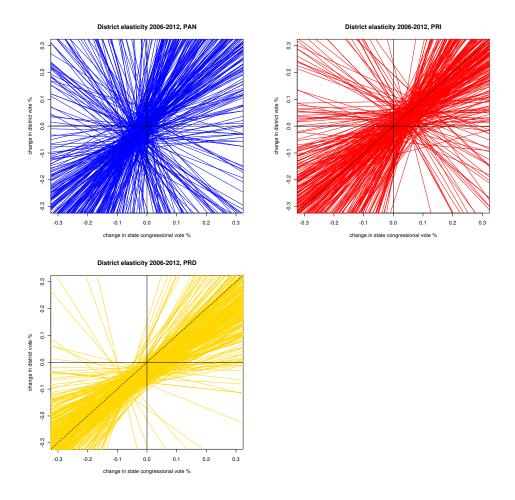


Figure 2: Parties' district elasticities

the parent state vote change Δ_e thus:

$$\Delta_s = \sum_{d=1}^{D_e} \alpha_d + \beta_d \Delta_e. \tag{1}$$

Fixed effects for each district are considered, fitting separate α_d and β_d regression coefficients for every district (indexed d). The model is estimated for every state separately because doing it nationwide involves too many secciónes (67k) and parameters (600) for my machine.

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