

Day 3 - Python Programming

Recursion
State Machines
Classes
From Idea to Business
Project Time

Recursion

What is Recursion?

A programming technique whereby a function calls itself either directly or indirectly.

Recursion Example

Fibonacci numbers: 0, 1, 1, 2, 3, 5, 8, 13, . . .

Mathematically:

$$F(0) = 0$$

$$F(1) = 1$$

$$F(n) = F(n-1) + F(n-2)$$

Recursion Example

Fibonacci numbers: 0, 1, 1, 2, 3, 5, 8, 13, . . .

Mathematically:

$$F(0) = 0$$

$$F(1) = 1$$

$$F(n) = F(n-1) + F(n-2)$$

```
def fibonacci(n):  
    if n == 0:  
        return 0  
    elif n == 1:  
        return 1  
    else:  
        return fibonacci(n-1) + fibonacci(n-2)
```

Recursion vs Iteration

```
def fib(n):  
    if n == 0:  
        return 0  
    elif n == 1:  
        return 1  
    else:  
        return fib(n-1)+fib(n-2)
```

```
def fib(n):  
    if n == 0 or n == 1:  
        return n  
    else:  
        a = 1  
        b = 1  
        for i in range(1, int(n)-1):  
            temp = a + b  
            a = b  
            b = temp  
        return b
```

Benefits of Recursion

1. Simpler and more elegant solutions
2. Easier to visualize problems
3. Sometimes more efficient

Laws of Recursion

1. Requires a base case
2. Requires a recursive case
3. Recursive call must progress problem towards base case

Laws of Recursion

1. Requires a base case

Path through the code which does not call the function again

2. Requires a recursive case

3. Recursive call must progress problem
towards base case

Laws of Recursion

1. Requires a base case

2. Requires a recursive case

Code that calls the function from within the function

3. Recursive call must progress problem
towards base case

Laws of Recursion

1. Requires a base case
2. Requires a recursive case
3. Recursive call must progress problem
towards base case
i.e. must reduce problem

Recursion Example

```
def fibonacci(n):
```

```
    if n == 0:  
        return 0
```

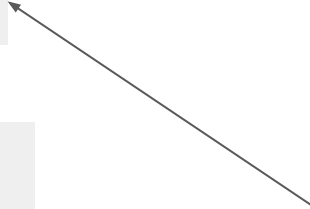
Base case

```
    elif n == 1:  
        return 1
```

Base case

```
    else:  
        return fibonacci(n-1) + fibonacci(n-2)
```

Recursive case



Drawbacks of Recursion

Function calls can be costly

- use up memory
- use up time

Common Pitfalls...

1. No base case
2. No progress towards base case
3. Infinite loop
4. Too costly

Common Pitfalls...

1. No base case
2. No progress towards base case
3. Infinite loop
4. Too costly

```
def fib(n):  
    return fib(n-1) + fib(n-2)
```

What does this function know?

Common Pitfalls...

1. No base case
2. No progress towards base case
3. Infinite loop
4. Too costly

```
def fib(n):
```

```
    if n == 0 or n == 1:
```

```
        return n
```

```
    else:
```

```
        return (n-1) + (n-2)
```

Is the base case being used by the else?

Common Pitfalls...

1. No base case
2. No progress towards base case
3. Infinite loop
4. Too costly

```
def fib(n):
```

```
    if n == 0 or n == 1:
```

```
        return n
```

```
    else:
```

```
        return f(n+1) + f(n+2)
```

When will this end?

Common Pitfalls...

1. No base case
2. No progress towards base case
3. Infinite loop
4. Too costly

Especially when function being recursed:

- has many operations
- has many variable assignments

Recursion Optimization: Memoization

“Memorized” results from previous runs used in subsequent repeated calls.

```
def fibonacci(n):  
    if n == 0:  
        return 0  
    elif n == 1:  
        return 1  
    else:  
        return fibonacci(n-1) + fibonacci(n-2)
```

How can we optimize this solution?

Recursion Optimization: Memoization

“Memorized” results from previous runs used in subsequent repeated calls.

```
memo = {}  
def fibonacci(n):  
    if n == 0:  
        return 0  
    elif n == 1:  
        return 1  
    else:  
        if n not in memo:  
            memo[n] = fibonacci(n-1) + fibonacci(n-2)  
        return memo[n]
```


Recursion Exercise 1: Factorial

Given that $n \geq 1$, return the factorial of n . Compute the result recursively (without loops).

$\text{factorial}(n) = n * (n-1) * (n-2) * \dots * 1$

$\text{factorial}(1) \rightarrow 1$ (1)

$\text{factorial}(2) \rightarrow 2$ (2 * 1)

$\text{factorial}(3) \rightarrow 6$ (3 * 2 * 1)

Factorial Solution

$\text{factorial}(n) = n * (n-1) * (n-2) * \dots * 1$

```
def factorial(n):  
    if n == 1:  
        return 1  
    else:  
        return n * factorial(n-1)
```

Recursion Exercise 2: PowerN

Given a base and n and both are ≥ 0 , compute recursively (no loops) the value of base to the n power, so is 9 (3 squared).

$$\text{powerN}(3, 2) = 3 \wedge 2 = 9$$

$$\text{powerN}(2, 3) = 2 \wedge 3 = 8$$

$$\text{powerN}(9, 0) = 9 \wedge 0 = 1$$

PowerN Solution

$\text{powerN}(n) = \text{base}^n$

```
def powerN (b, n):  
    if n == 0:  
        return 1  
    else:  
        p = b * powerN(b, n-1)
```

PowerN Solution

$\text{powerN}(n) = \text{base}^n$

```
def powerN (b, n):  
    if n == 0:  
        return 1  
    else:  
        p = powerN(b, n//2)  
        if n%2 == 0:  
            return p * p  
        else:  
            return b * p * p
```

~Break~

State Machines




State Machines

Mathematical computation model

Abstract machine (theoretical idea of model)

Change states by specific inputs

Examples of State Machines:

- Vending Machine
 - Traffic Lights
 - Combination Locks
 - Elevators
- 

Elevator

2F

1F



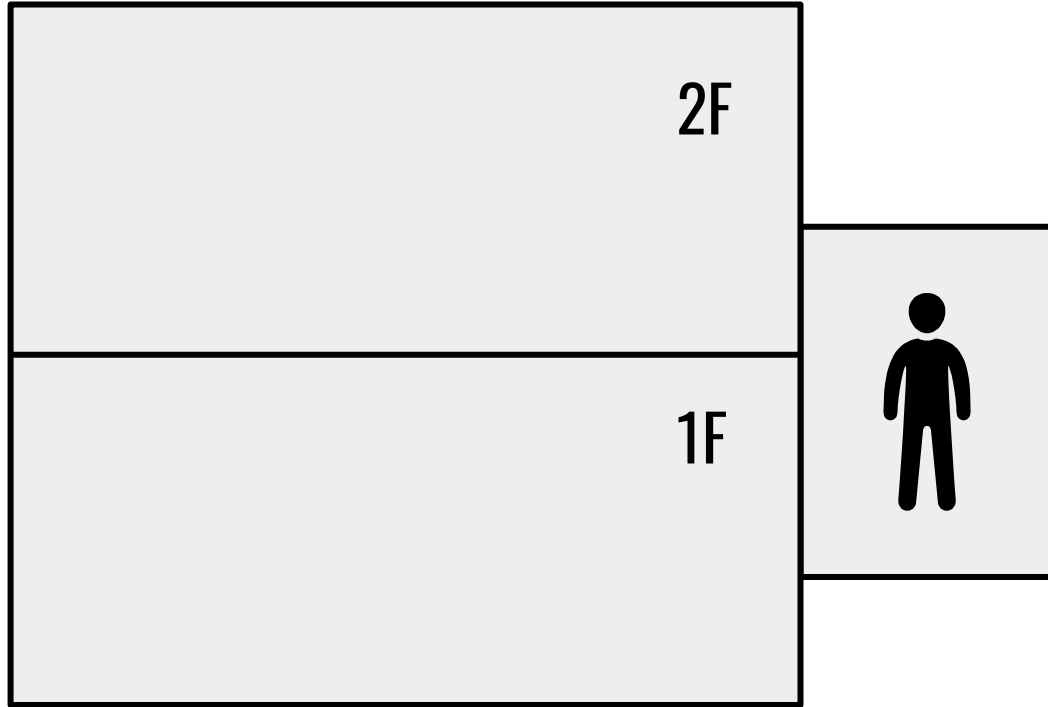
Elevator

2F

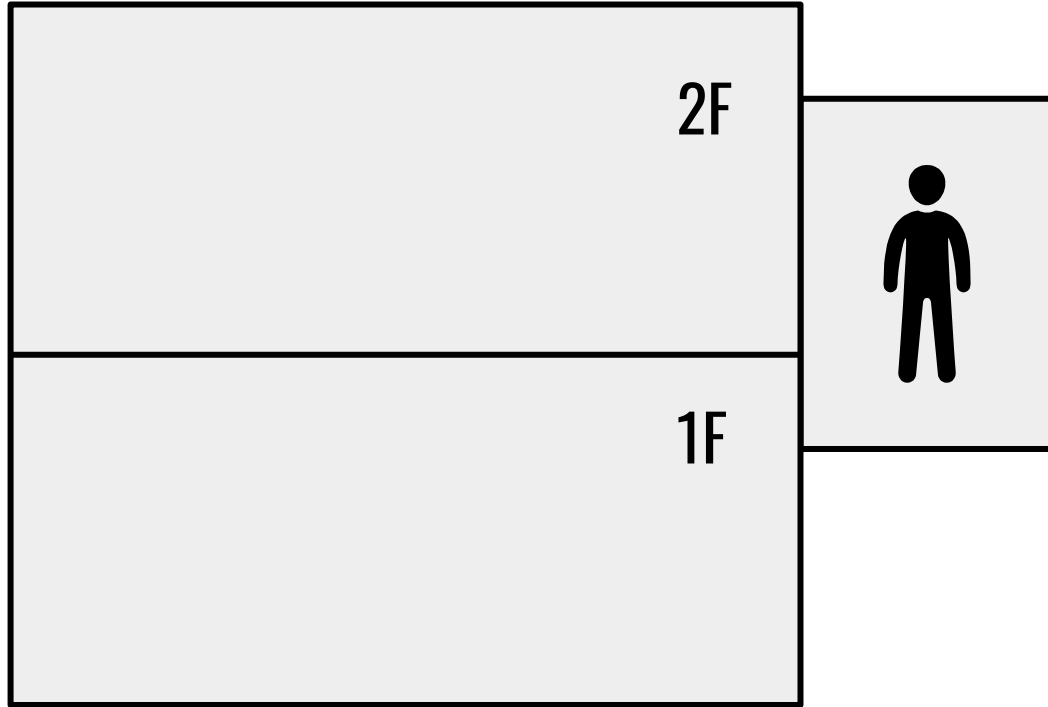
1F



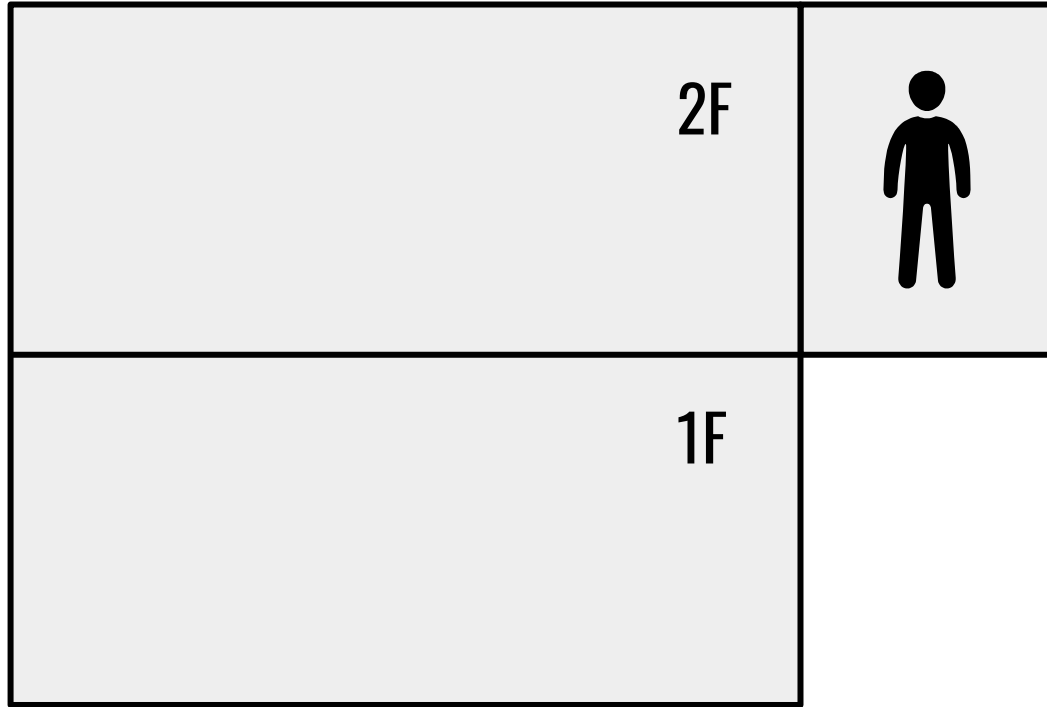
Elevator



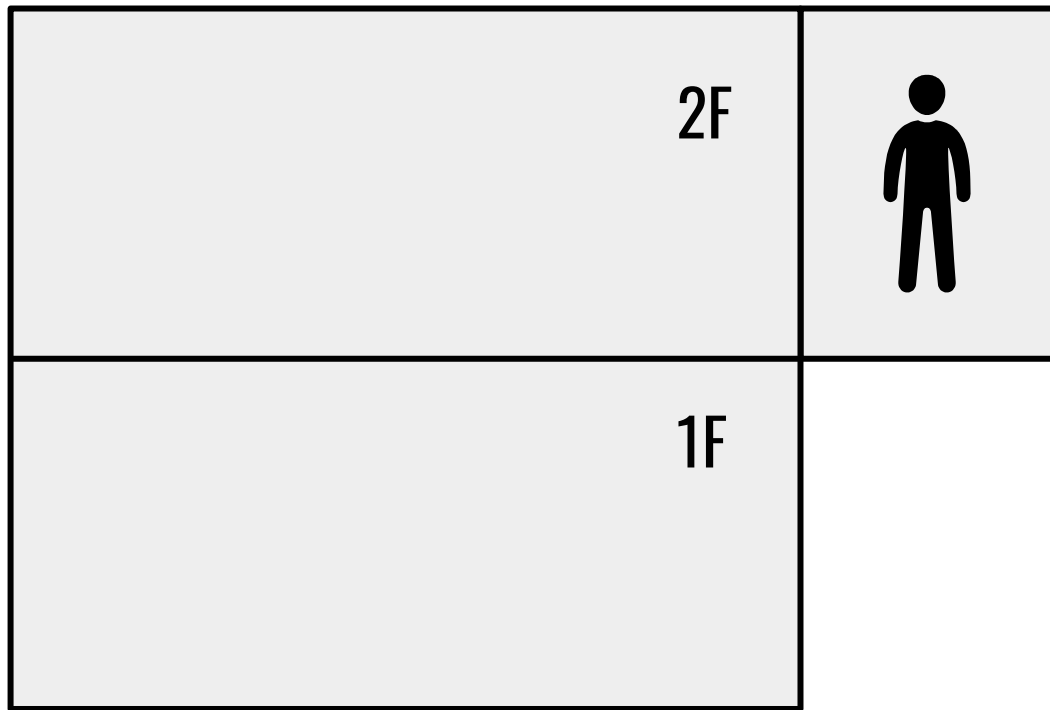
Elevator



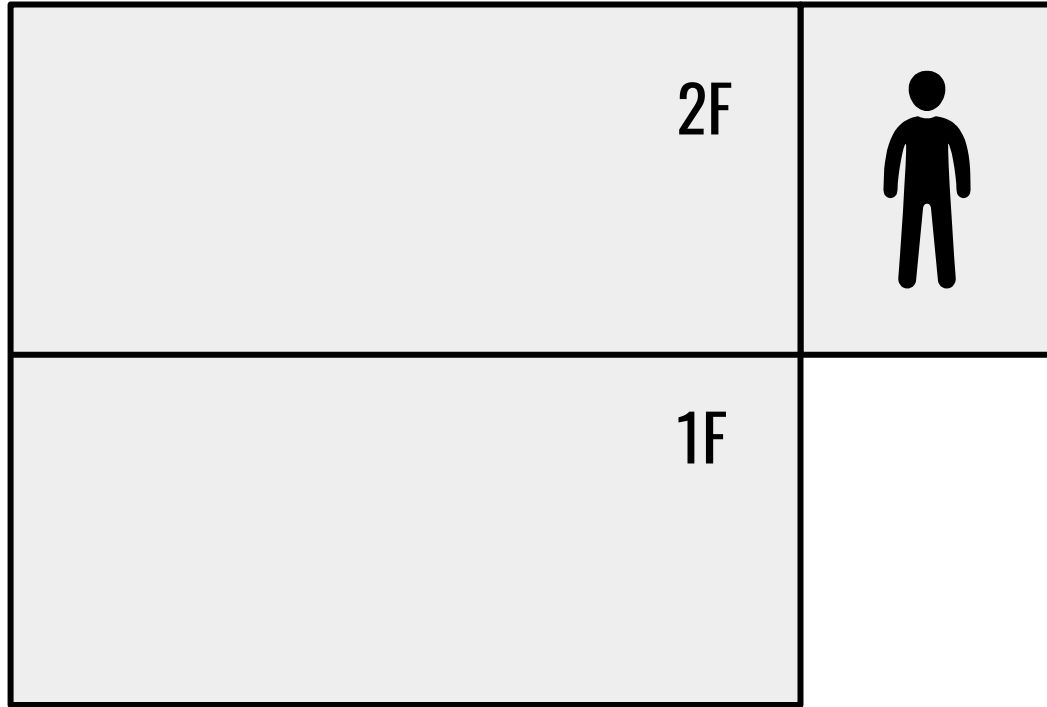
Elevator



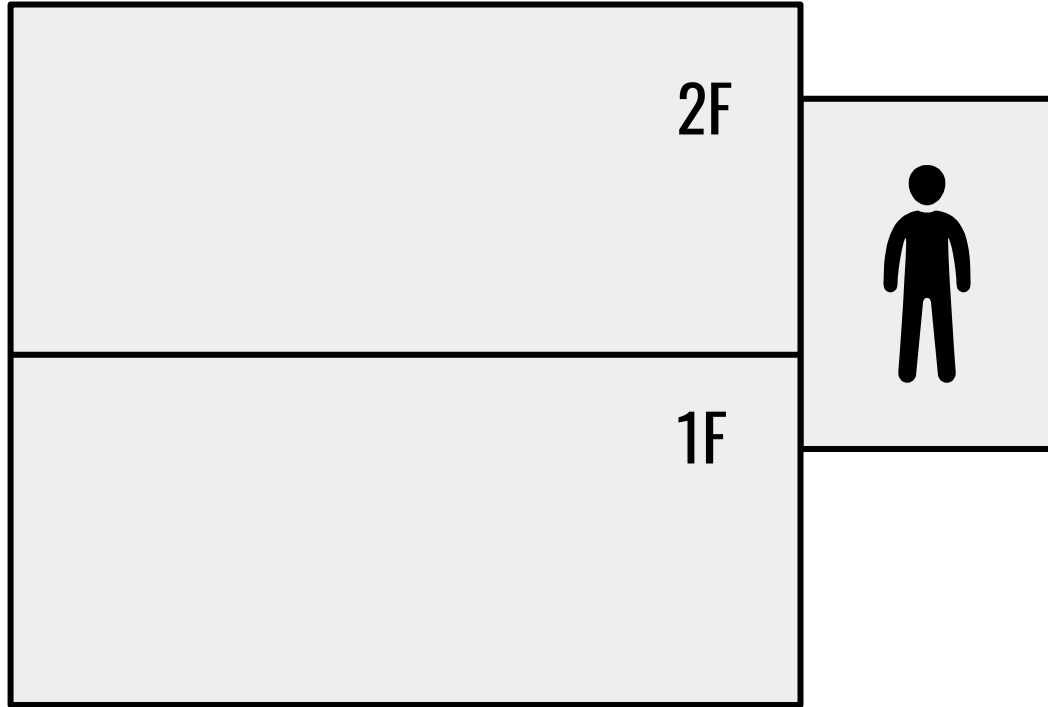
Elevator



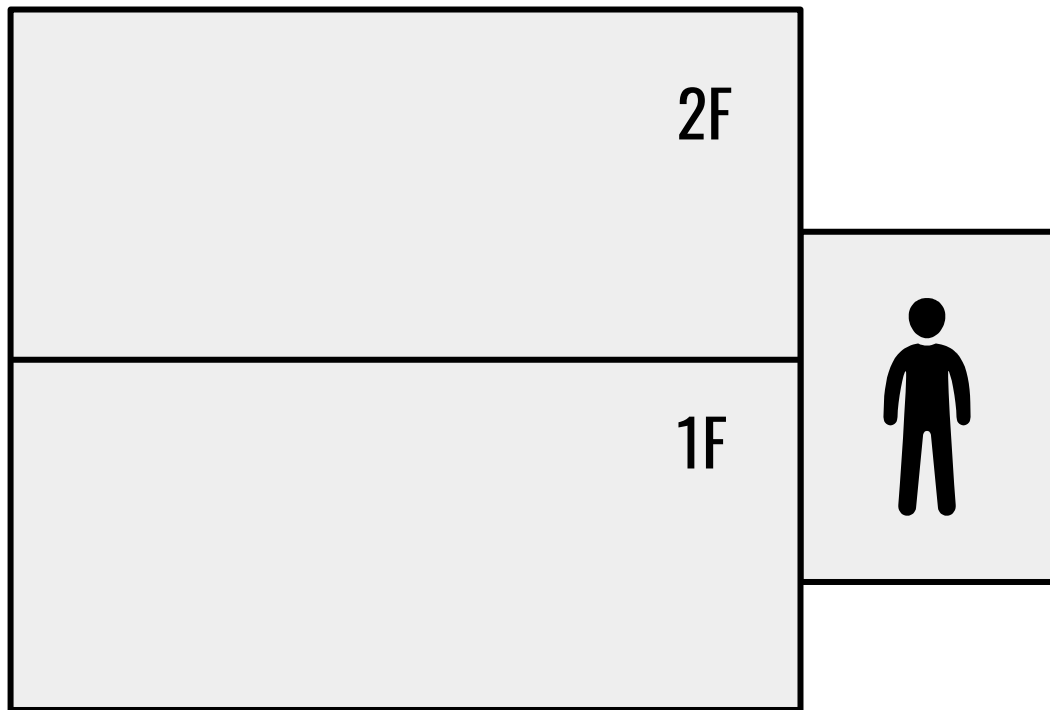
Elevator



Elevator



Elevator



Elevator

2F

1F



Elevator

2F

1F

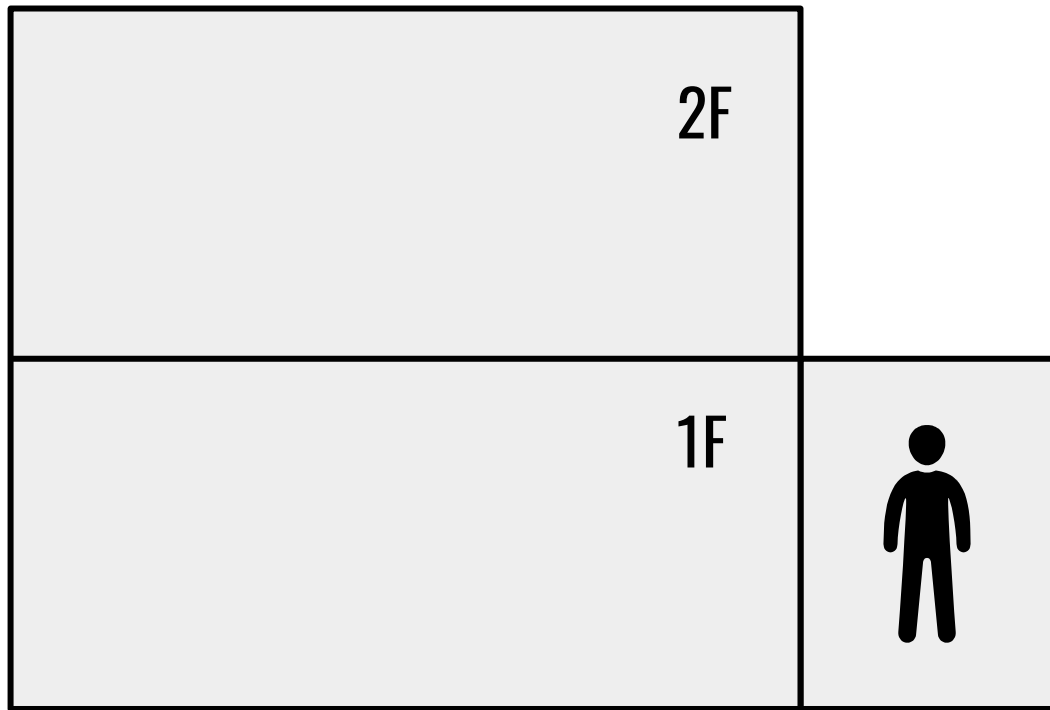


A cluster of overlapping geometric shapes in the top-left corner, including a cyan parallelogram, an orange parallelogram, a blue parallelogram, a teal parallelogram, and a light blue parallelogram.

Elevator as a State Machine!

A cluster of overlapping geometric shapes in the bottom-right corner, including a cyan parallelogram, an orange parallelogram, a blue parallelogram, a teal parallelogram, a light blue parallelogram, and a black parallelogram.

Elevator

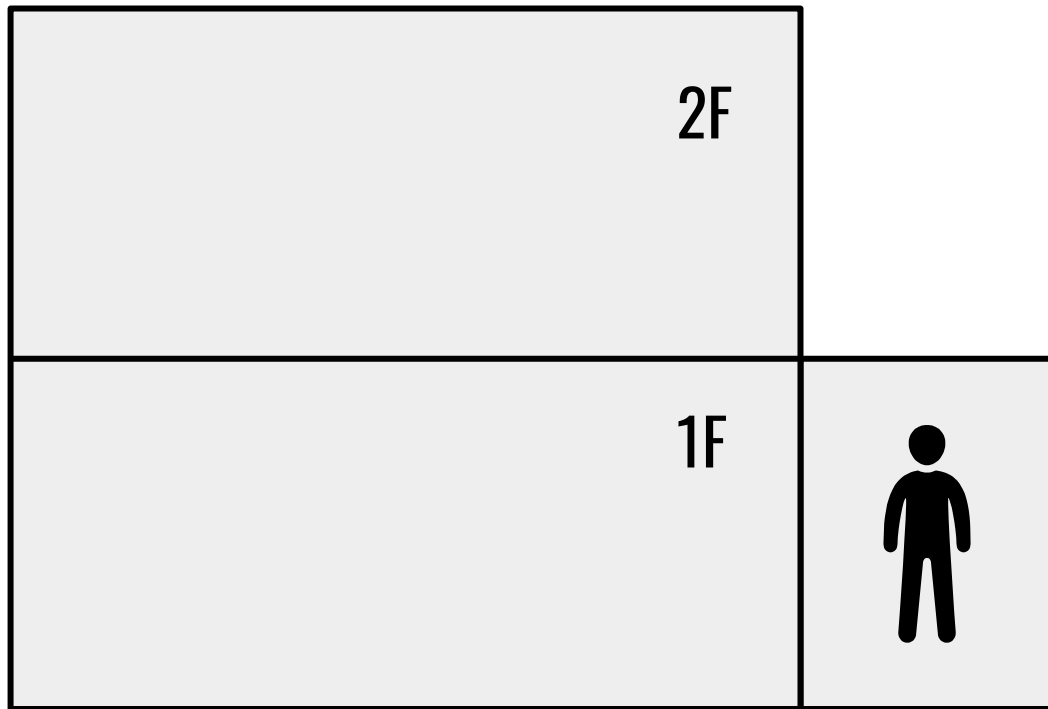


moving = 0

up = 0

down = 0

Elevator

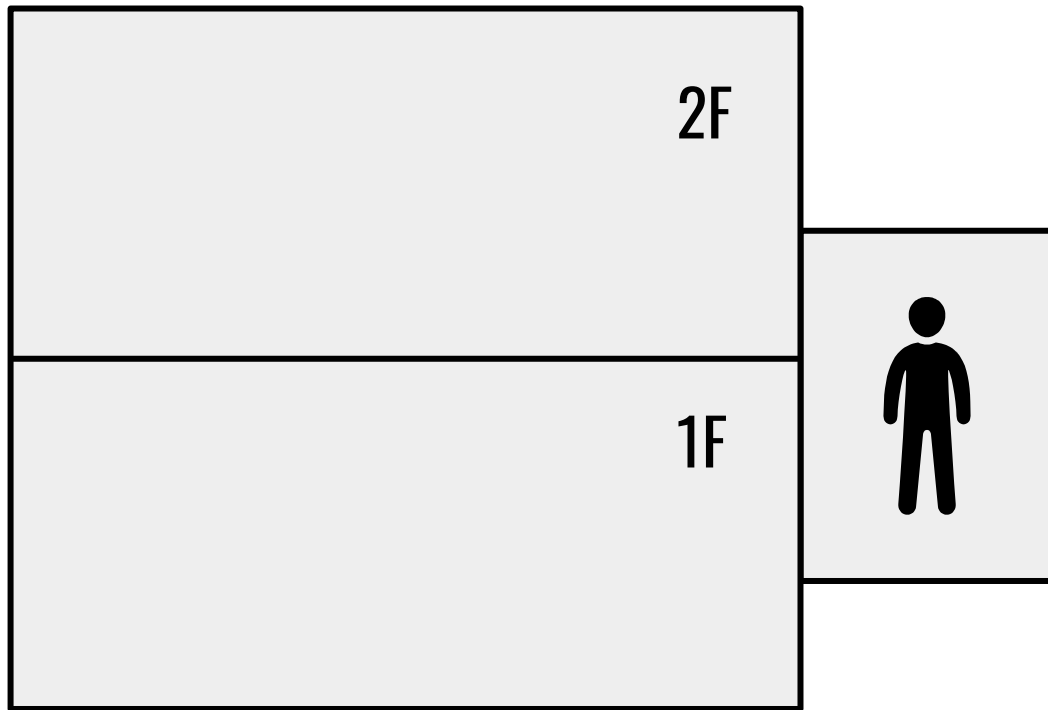


moving = 0

up = 1

down = 0

Elevator

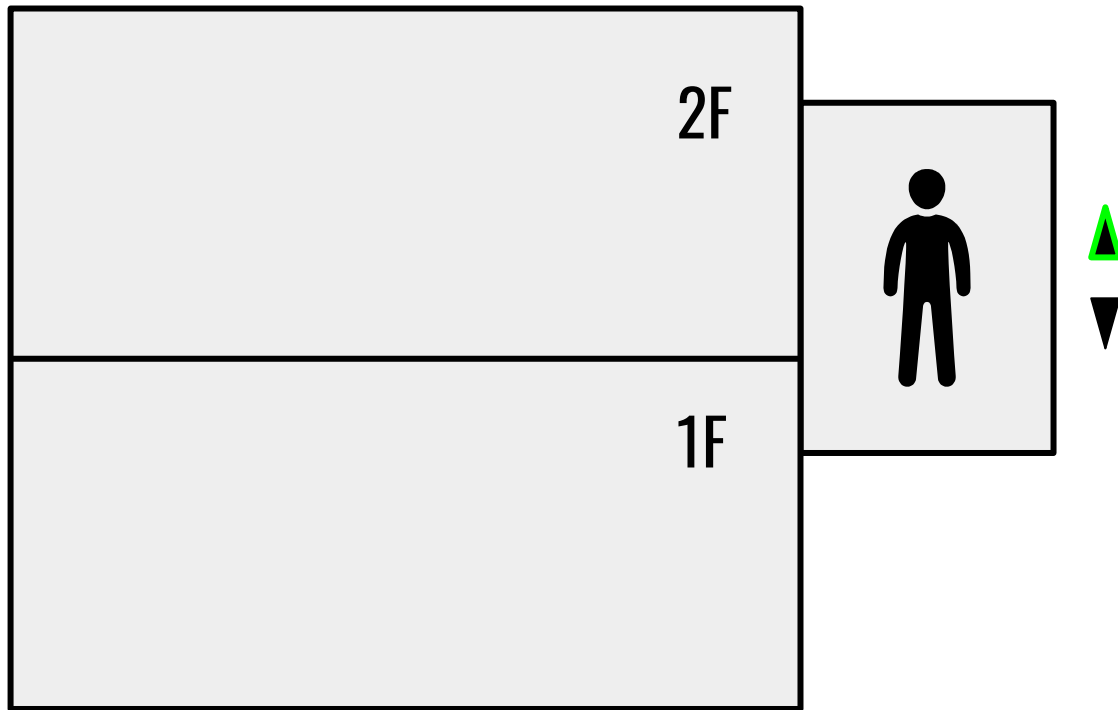


moving = 1

up = 1

down = 0

Elevator

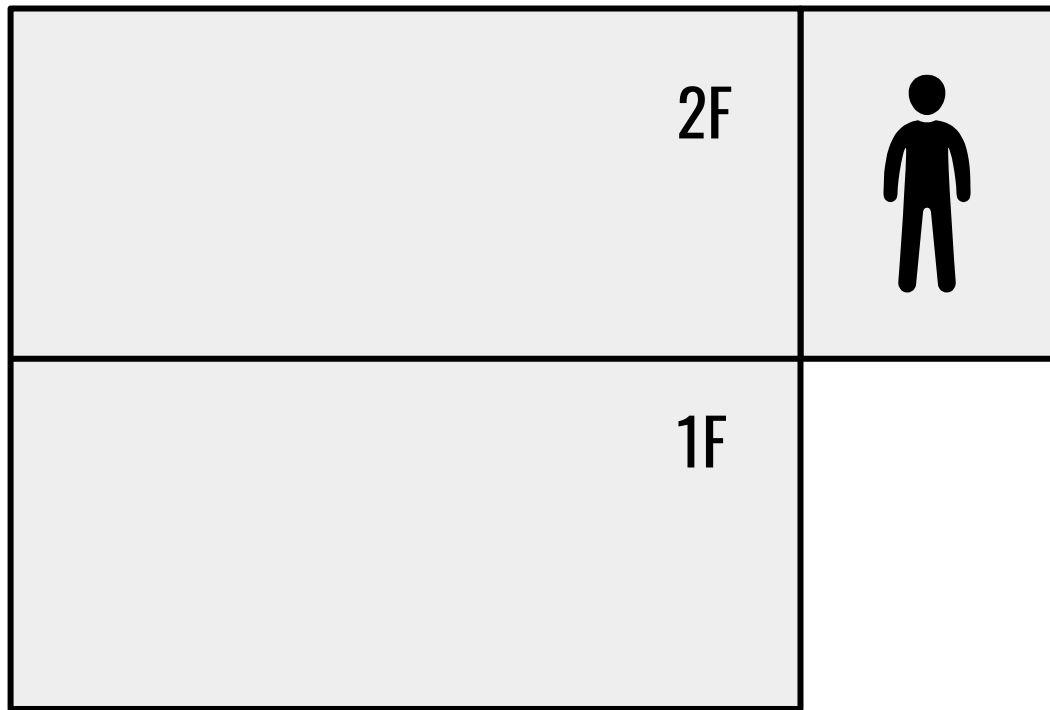


moving = 1

up = 1

down = 0

Elevator

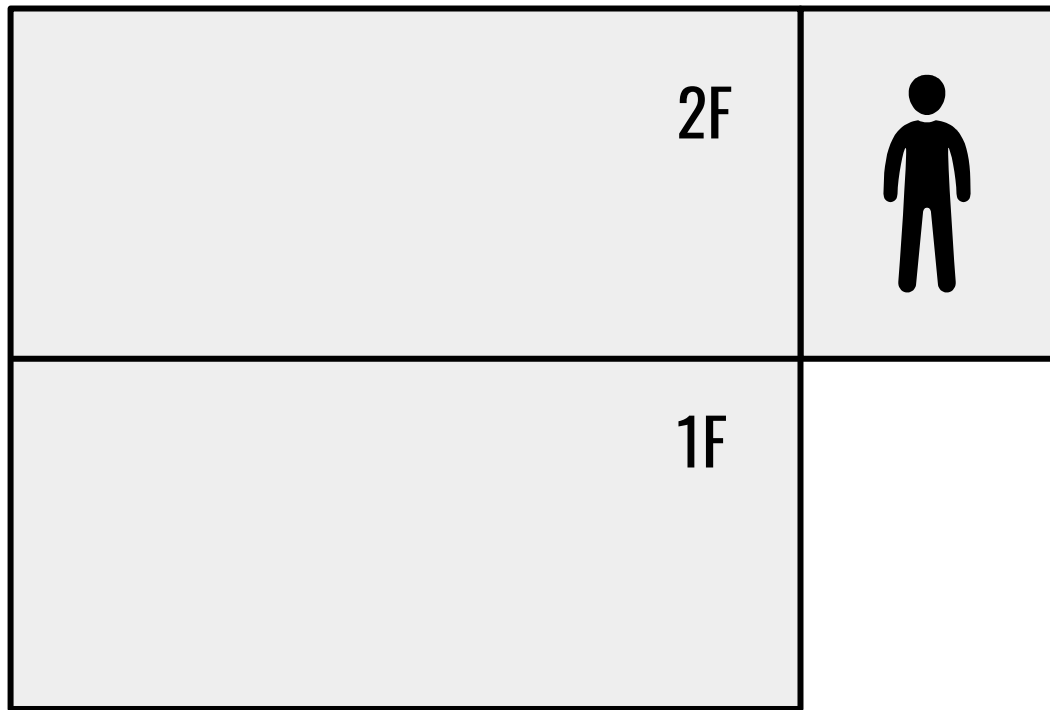


moving = 0

up = 1

down = 0

Elevator

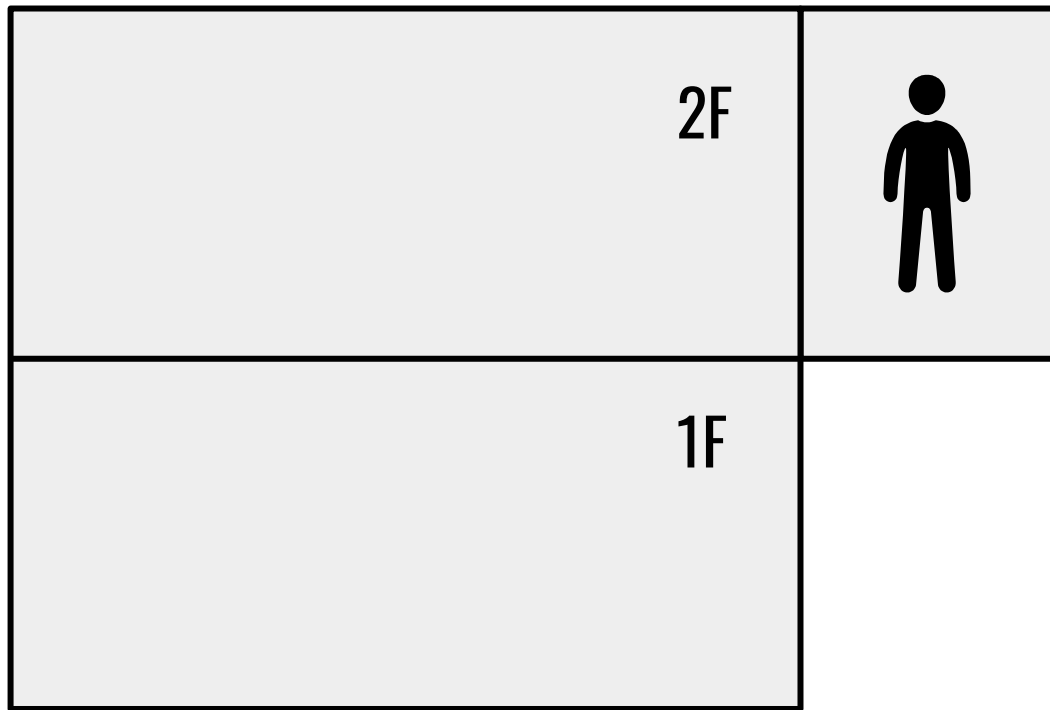


moving = 0

up = 0

down = 0

Elevator

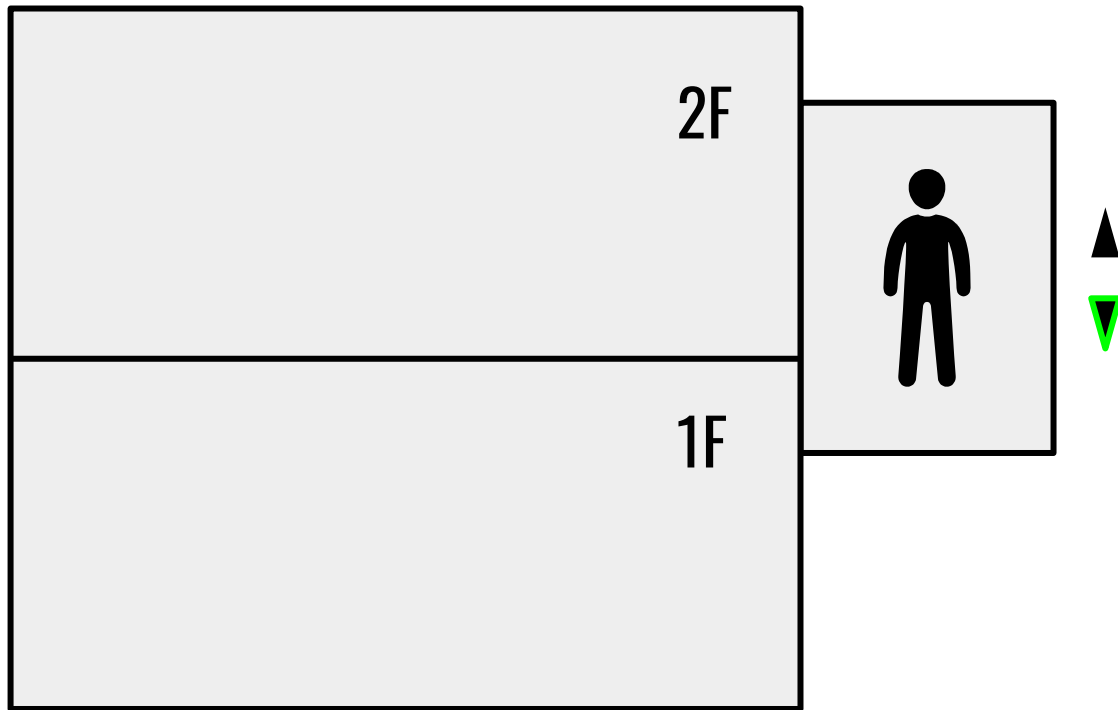


moving = 0

up = 0

down = 1

Elevator

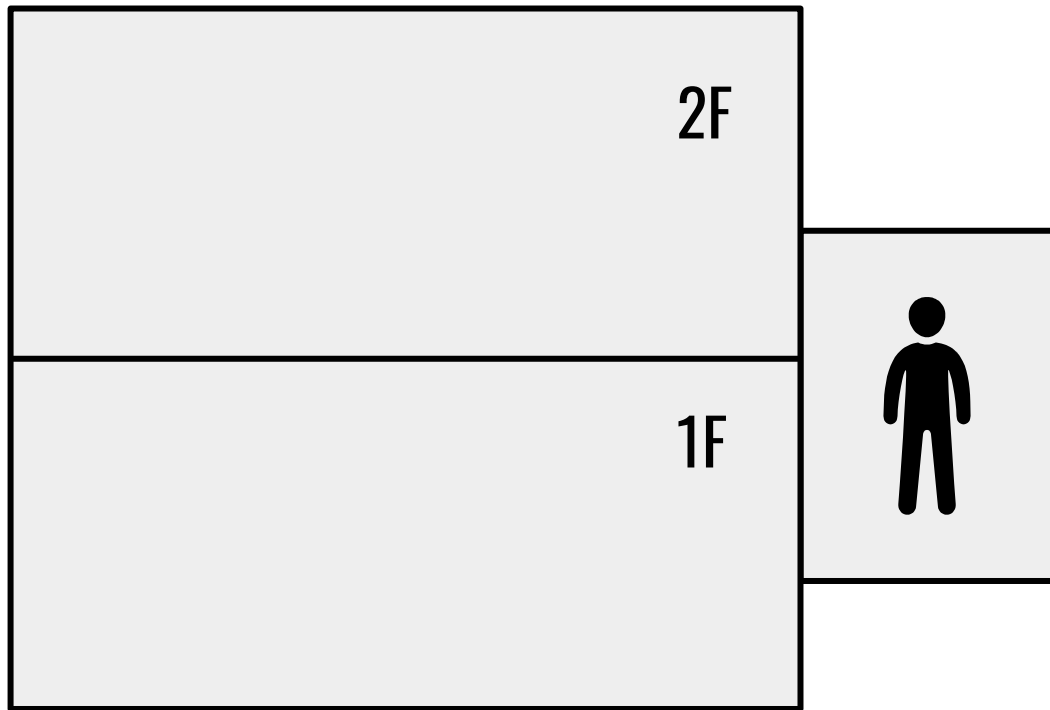


moving = 1

up = 0

down = 1

Elevator

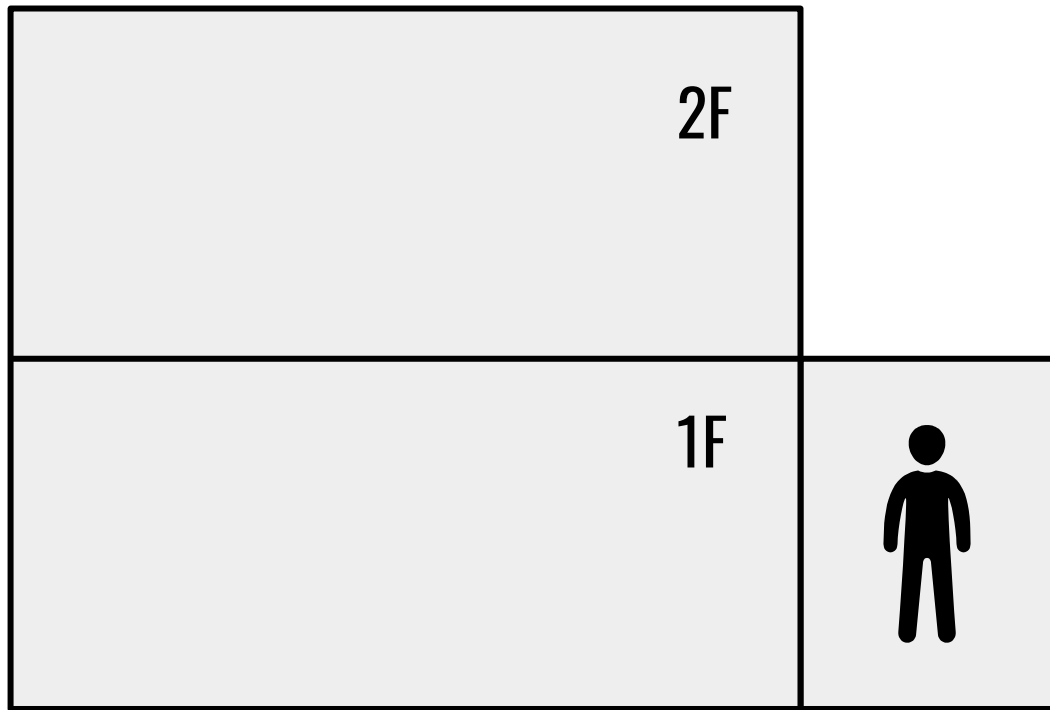


moving = 1

up = 0

down = 1

Elevator

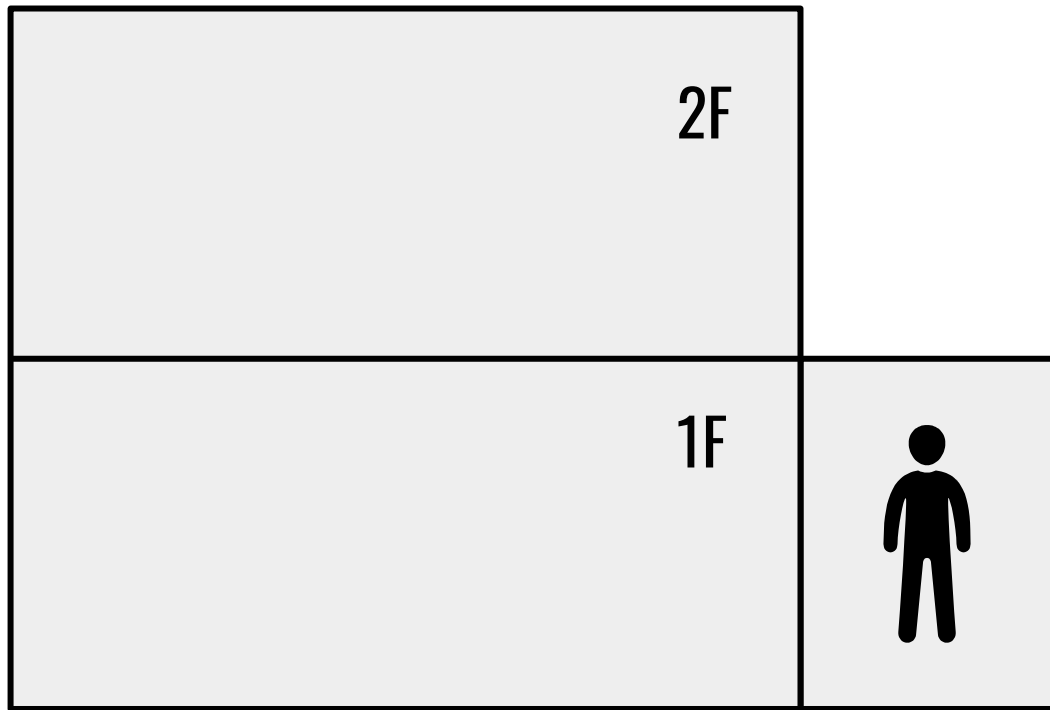


moving = 0

up = 0

down = 1

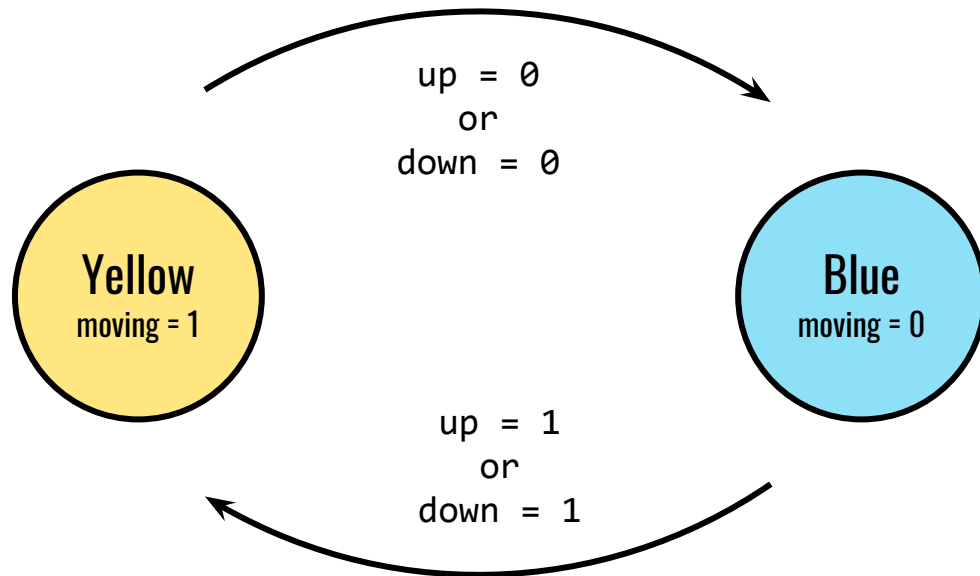
Elevator



moving = 0

up = 0

down = 0



A cluster of overlapping geometric shapes in the top-left corner, including a cyan triangle, an orange parallelogram, a blue parallelogram, and a teal parallelogram.

Your Turn!

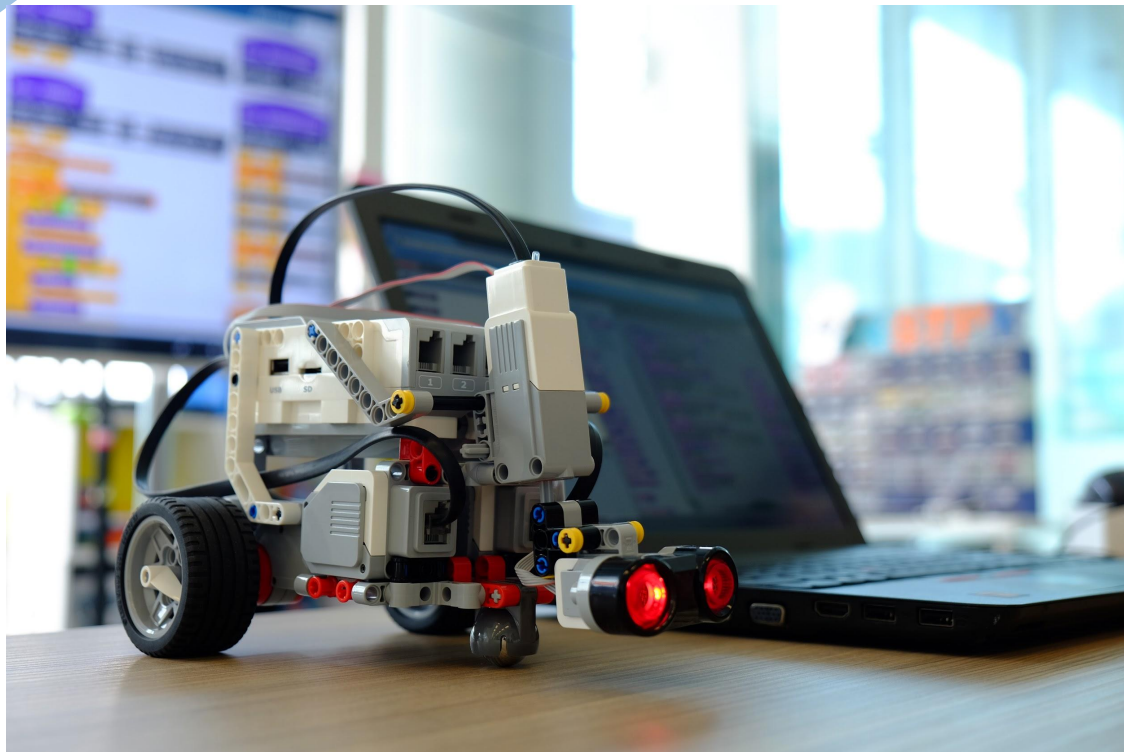
Write a state machine for being hungry

A cluster of overlapping geometric shapes in the bottom-right corner, including a cyan triangle, an orange parallelogram, a blue parallelogram, a teal parallelogram, and a light blue parallelogram.

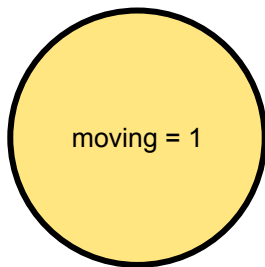
A cluster of overlapping geometric shapes in the top-left corner, including a cyan triangle, an orange parallelogram, a blue parallelogram, a teal rectangle, and a light blue parallelogram.

Why is this relevant?

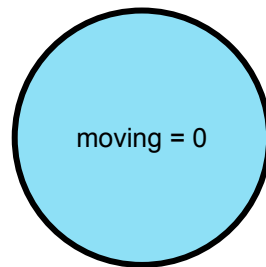
A cluster of overlapping geometric shapes in the bottom-right corner, including a cyan parallelogram, an orange parallelogram, a blue parallelogram, a teal rectangle, a light blue parallelogram, and a black parallelogram.



Move forward
and sense
surroundings



too close to
object



Check left and
right for open
space

turn







```
state = 0
```

```
if state == 0:
    game.reset()
elif state == 1:
    #level one
    player.battle(snakes)
    if player.win():
        print('next level!')
        state += 1
    else:
        print('start over')
        state = 1
```

```
elif state == 2:
    #level two
    player.battle(dinosaurs)
    if player.win():
        print('next level!')
        state += 1
    else:
        print('start over')
        state = 1
```

```
elif state == 3:
    #level one
    player.battle()
    if player.win():
        print('yay!')
    else:
        print('game over')
        state = 0
```






```
state = 0
lives = 3

if state == 0:
    game.reset()
elif state == 1:
    #level one
    player.battle(snakes)
    if player.win():
        print('next level!')
        state += 1
    else:
        lives -= 1
        if lives > 0:
            level.reset()
        else:
            print('start over')
            state = 1
```

```
elif state == 2:
    #level two
    player.battle(dinosaurs)
    if player.win():
        print('next level!')
        state += 1
    else:
        lives -= 1
        if lives > 0:
            level.reset()
        else:
            print('start over')
            state = 1
```

```
elif state == 3:
    #level one
    player.battle()
    if player.win():
        print('yay!')
    else:
        lives -= 1
        if lives > 0:
            level.reset()
        else:
            print('game over')
            lives = 3
    state = 0
```



A cluster of overlapping geometric shapes in the top-left corner, including a cyan triangle, an orange parallelogram, a blue parallelogram, a teal rectangle, and a light blue parallelogram.

Classes and Objects

A cluster of overlapping geometric shapes in the bottom-right corner, including a cyan parallelogram, an orange parallelogram, a blue parallelogram, a teal rectangle, a light blue parallelogram, and a small black triangle.

```
1 class Charleen:
2     food = "Watermelon"
3
4     def dance(self):
5         print("Catch a crayon")
6
7 # Create a new class object
8 charleen1 = Charleen()
9 print(charleen1)
10 print(charleen1.food) # Access public variables
11 print(charleen1.dance()) # Call functions
12
13 # Create another object
14 charleen2 = Charleen()
15 print(charleen2)
16 charleen2.food = "Mango"
17
18 # Two objects
19 # Same Class, Different Values
20 print(charleen1.food)
21 print(charleen2.food)
22
```



```
1 class Sprite:
2     name = "default_name"
3     hometown = "default_hometown"
4
5     # Make sure to use 'self' as a parameter
6     # And use it when calling class variables
7     def get_description(self):
8         result = ""
9         result += "Name: " + self.name + "\n"
10        result += "Hometown: " + self.hometown + "\n"
11        return result
12
13    # Different from 'self' class vars and input parameter
14    def set_name(self, name):
15        self.name = name
16
17    def set_hometown(self, hometown):
18        if (hometown == "NYC"):
19            hometown = "NYC (da best)"
20            self.hometown = hometown
21
22    # Without 'self' parameter, it is a Static class function
23    def generic_greeting():
24        return "Hi, how are you?"
25
```

```
1 ▼ class Player:
2     name = ""
3     power = 0
4     speed = 0
5
6     # Class Constructors in python
7 ▼ def __init__(self, name, power, speed):
8     self.name = name
9     self.power = power
10    self.speed = speed
11
12    # Calling methods from other objects in the same class
13 ▼ def attack(self, other):
14    if (self.speed < other.speed):
15        return "Attack failed! Too slow!"
16 ▼    else:
17        if (self.power >= other.power):
18            return self.name + " successfully attacked " + other.name
19        else:
20            return self.name + "'s attack on " + other.name + " failed"
21
22    def speed_boost(self):
23        self.speed *= 2
24
25
26    Spiderman = Player("Peter Parker", 50, 2)
27    Hawkeye = Player("Clint Barton", 20, 3)
28
29    battle1 = Spiderman.attack(Hawkeye)
30    print(battle1)
31
32    Spiderman.speed_boost()
33    battle2 = Spiderman.attack(Hawkeye)
34    print(battle2)
```

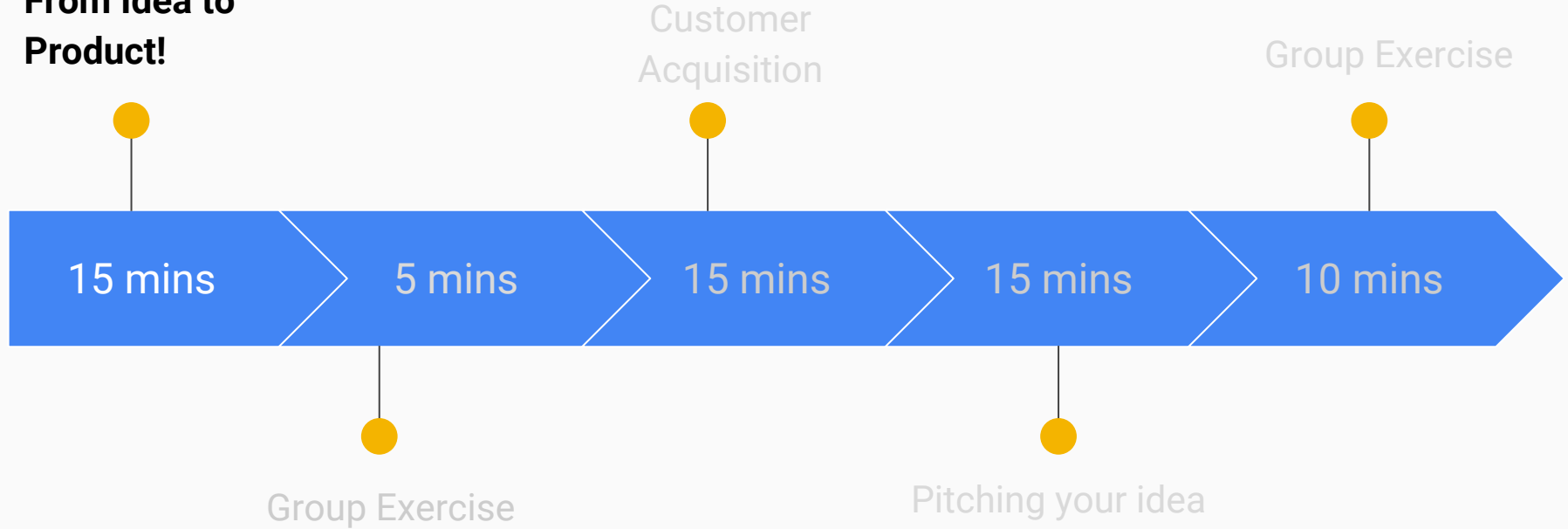
Turning an Idea into a Business

Objectives

Learn how to get from an idea into a product with a customer.

Learn how to pitch/sell your product.

From Idea to Product!





Product Development Process

From an Idea into a Product with a Customer

What is a Product?

- It is not an idea!

What is a Product?

- It is not an idea
- It is not code!

What is a Product?

- It is not an idea
- It is not code
- It is not a prototype!

product

A good, idea, method, information, object or service created as a result of a process and serves a need or satisfies a ...



BusinessDictionary

Example: Is this a product?

- I think that an app that notifies you of free cool events near you would be very helpful!

NO!

Idea

- I have code that can compute if I am meeting my saving/retirement goals.

NO!

Code

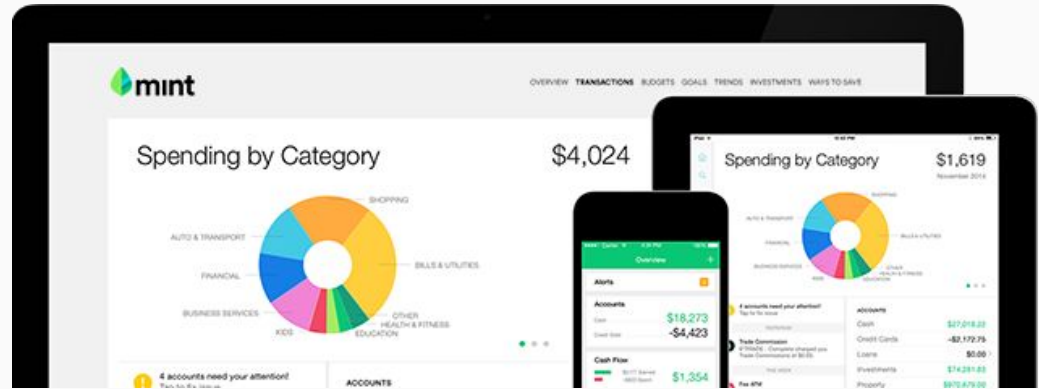
Idea → Product

- I think that an app that notifies you of free cool events near you would be very helpful!



Code Product

- I have code that can compute if I am meeting my saving/retirement goals.



A product is the result of a Process



Example: Mint



Idea

It would great if people could track and visualize their saving goals and progress.

Concept

The application would collect all of one's bank accounts data and analyze against user set budgets and saving goals.

Prototype

Code that can get data from all of one's back accounts.

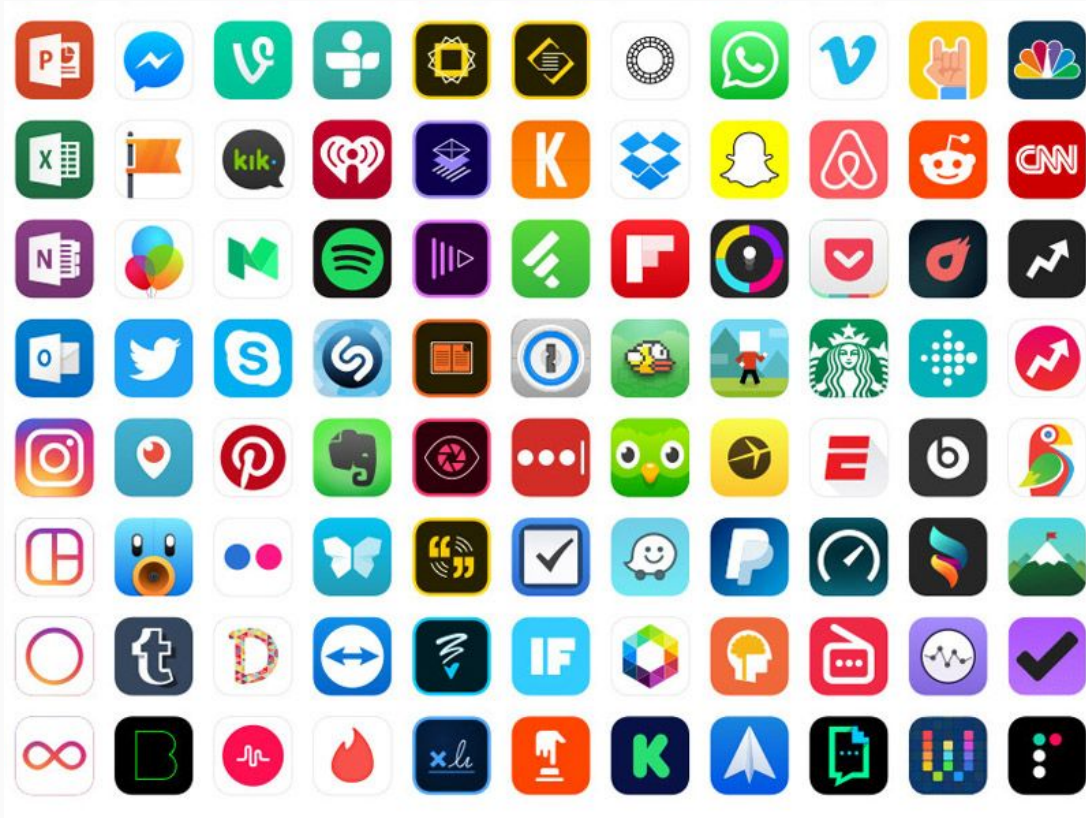
Product

Mint app (android & iphone)



Product Development Process

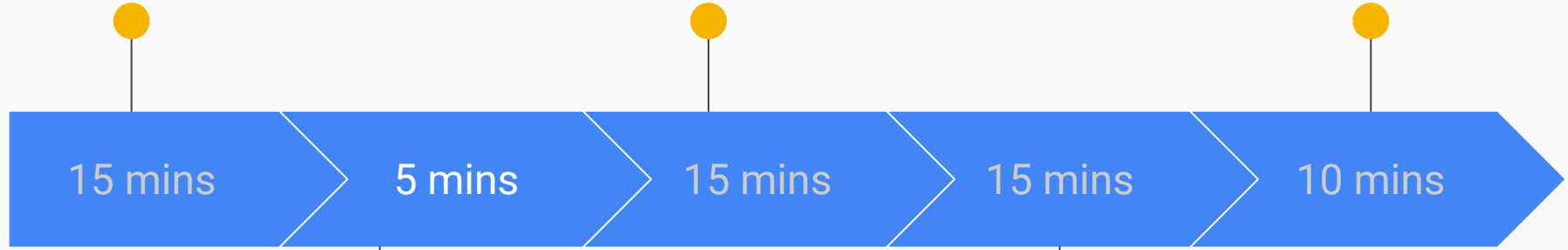
Once, they were ideas!



From Idea to
Product!

Customer
Acquisition

Group Exercise



Group Exercise

Pitching your idea

Group Exercise!!!

In your groups, take 5 minutes to:

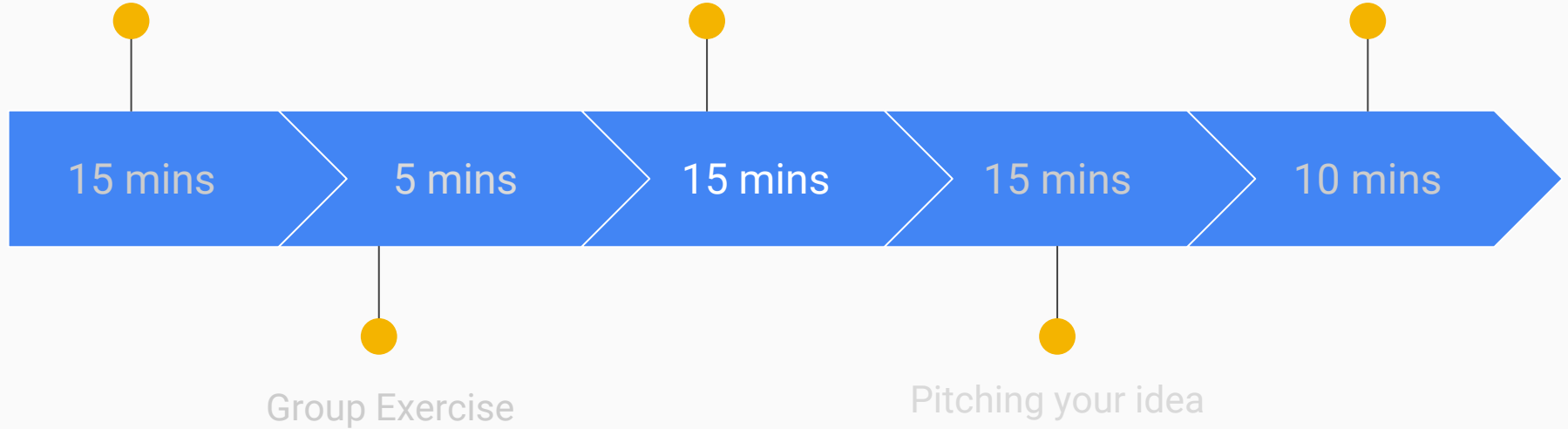
- 1) Clearly state your final idea.
- 2) Determine a product from your idea.
- 3) Discuss a potential prototype.



From Idea to
Product!

**Customer
Acquisition**

Group Exercise





Process of Acquiring a Customer

Who is a Customer?

- It is a user willing to pay for your product

Who is a Customer?

- It is a user willing to pay for your product
- It is not someone who says “your idea is so cool!”

Who is a Customer?

- It is a user willing to pay for your product
- It is not someone who says “your idea is so cool!”
- It is not someone who just listens to you and nods yes yes yes!

There are 4 Types of Customers

A) Early adopters

- Always quick/first to try new ideas/products/tech
- Do it for the reputation
- Very few
- Often have money/voice/power

There are 4 Types of Customers

A) Early adopters

B) Early majority

- Relatively quick to adopt new ideas/products/tech
- Make decisions based on utility and practical benefits over coolness

There are 4 Types of Customers

A) Early adopters

B) Early majority

C) Late majority

- Average at adopting new ideas/products/tech
- Share a lot of traits with early majority but tend to be overly cautious before committing

There are 4 Types of Customers

A) Early adopters

B) Early majority

C) Late majority

D) Laggards

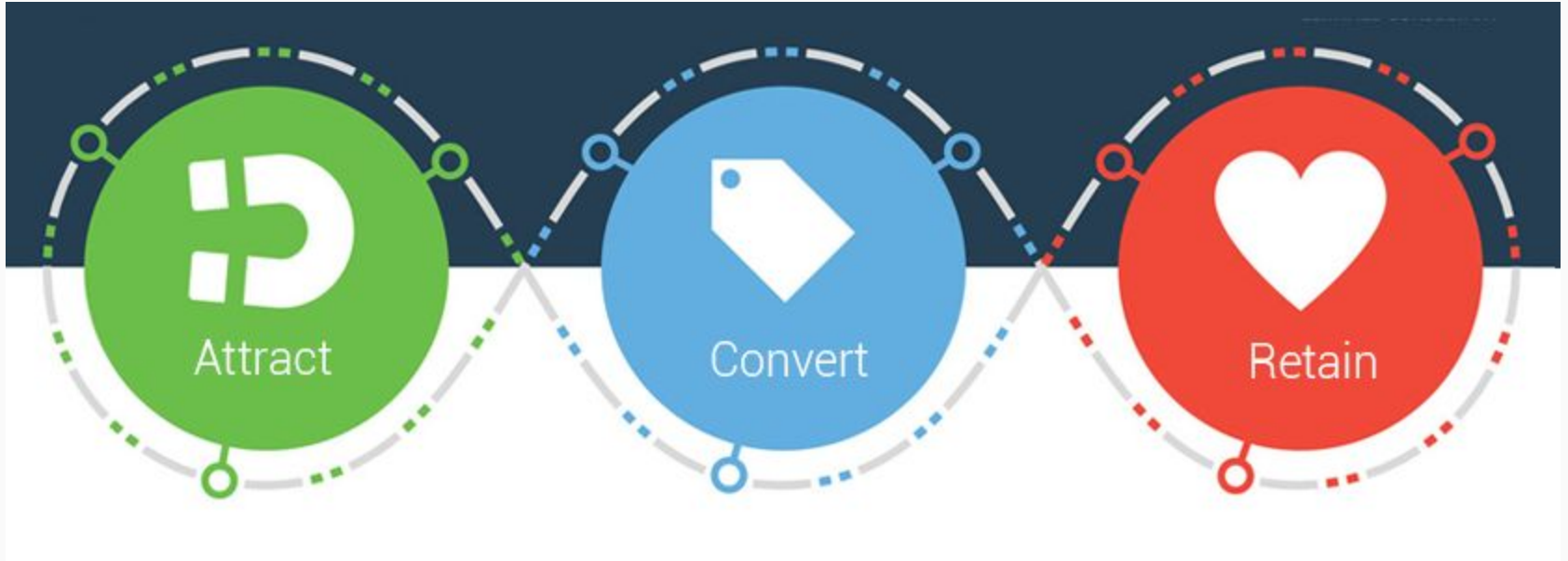
- Most people
- Last to adopt new ideas/products/tech
- When forced to or product is now famous/proved to be a great product

Who is your Customer?



Your customer ...

- Is not everyone!
- Is not all your friends and family and classmates and ...
- Must be very specific, for example:
 1. Children from Asian middle-class families who know/speak very limited English.
 2. Women who like reading Steve Harvey's books.
 3. Couples that frequently travel together to tropical destinations and spend about \$1000 on vacation annually.



Customer Acquisition



Customer Engagement

Customer Acquisition: COCA & LTV

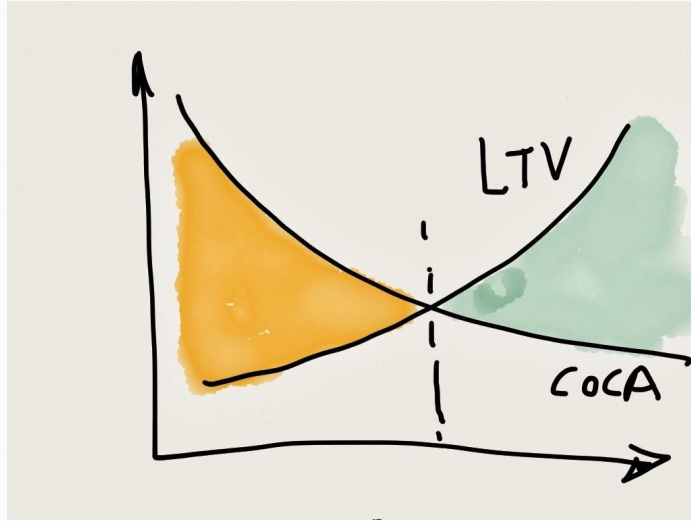
COCA:

- Cost Of Customer Acquisition
- $$\frac{\text{sales \& marketing costs}}{\text{\# of new customers}}$$

LTV:

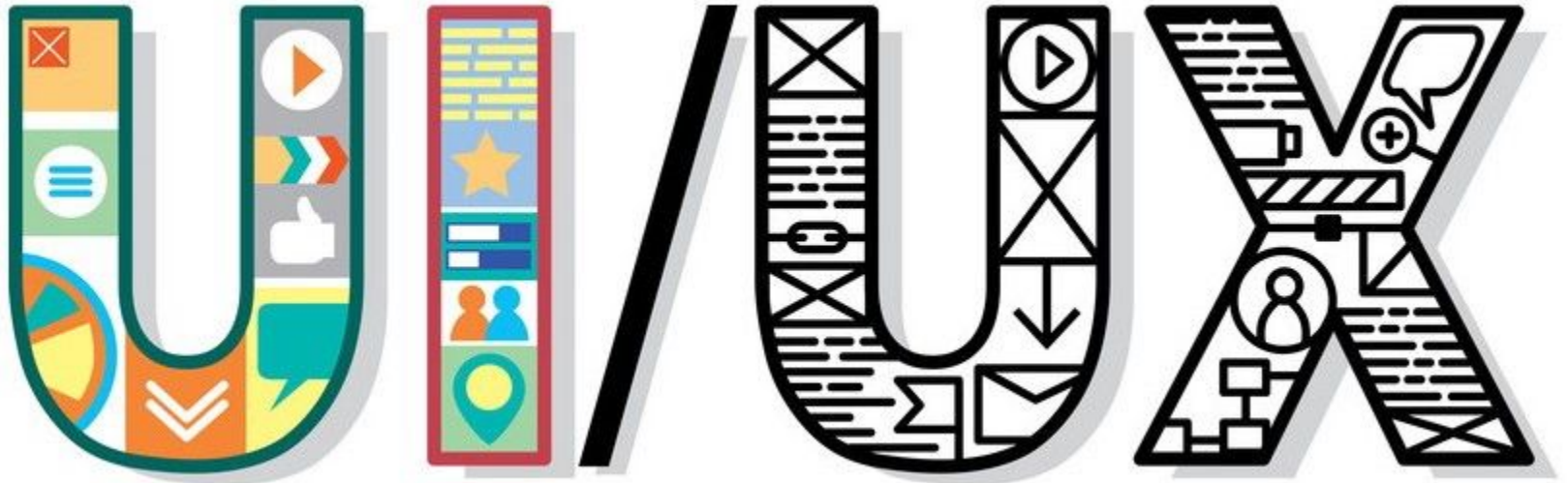
- Life Time Value of a customer
- Total lifetime profit you expect to make from a customer

Product successful when ...



$$LTV \geq 3 * COCA$$

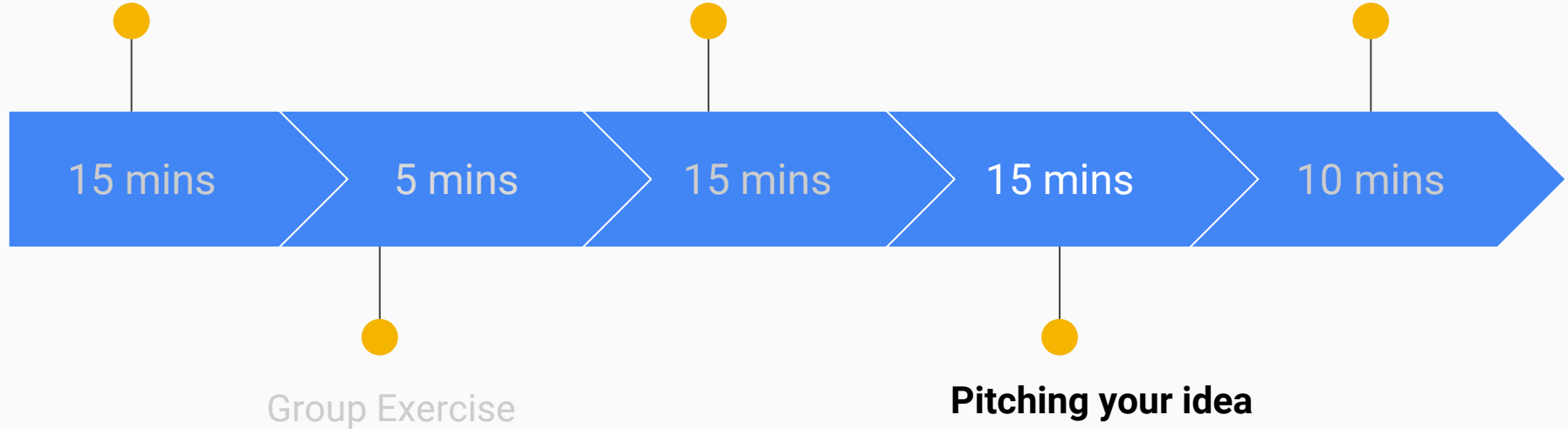
Companies spend millions



From Idea to
Product!

Customer
Acquisition

Group Exercise





Pitching your Idea/Product

Different Pitch for Different Audiences



Customer



Investor



Sponsor



Different Pitch for Different Audiences

Customer

My idea is solving your problem of/meeting your need of ...

Investor

Sponsor

Different Pitch for Different Audiences

Customer

My idea is solving your problem of/meeting your need of ...

Investor

Business Plan: problem, solution, customer, value added, finances, team behind product

Sponsor

Different Pitch for Different Audiences

Customer

My idea is solving your problem of/meeting your need of ...

Investor

Business Plan

Sponsor

Elevator Pitch: 30-60 sec of what your idea/product is

Different Pitch for Different Audiences

Customer

My idea is solving your problem of/meeting your need of ...

Investor

Business Plan

Sponsor

Elevator Pitch

Any pitch should:

- State problem & solution



Any pitch should:

- State problem & solution
- Be clear & concise!



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- Be persuasive!



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- Be passionate!



Any pitch should:

- State problem & solution
- Be clear & concise!
- Be persuasive!
- Be passionate!
- Extend an invite to continue conversation!



Any pitch should:

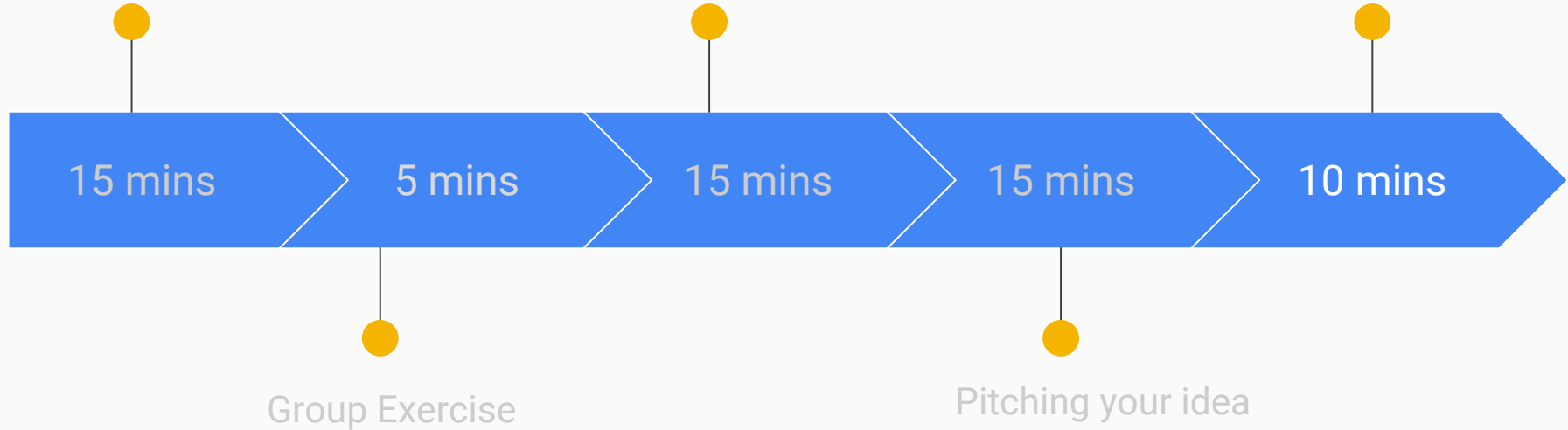
- State problem & solution
- Be clear & concise!
- Be persuasive!
- Be passionate!
- Extend an invite to continue conversation!



From Idea to
Product!

Customer
Acquisition

Group Exercise



Friday Final Deliverables

1. **Presentation:** You will pitch your idea to us!
2. **Prototype:** A working portion of your product/idea!

THEME: Community

Group Exercise!!!

In your groups, take 10 minutes to:

- 1) Identify what need your idea is solving.
- 2) Define 2-3 potential customers. Be very specific!
- 3) Determine 3 things you'd tell an investor in order to get capital for your idea.





Project Work Time!



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[charleenwang](#)

Charleen



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Leon Cheng

Invite someone



A cluster of overlapping geometric shapes in the top-left corner, including a cyan parallelogram, an orange parallelogram, a blue parallelogram, a teal parallelogram, and a light blue parallelogram.

Survey Time!

A cluster of overlapping geometric shapes in the bottom-right corner, including a cyan parallelogram, an orange parallelogram, a blue parallelogram, a teal parallelogram, a light blue parallelogram, and a black parallelogram.



<https://goo.gl/4NoUeq>