1.1.(i)

$$rac{\partial y_i}{\partial \gamma} = \hat{x_i}$$
 $rac{\partial y_i}{\partial \beta} = 1$

1.1.(ii)

$$rac{\partial y_j}{\partial x_i} = \left\{egin{array}{c} 0, i
eq j ee r_j$$

1.1.(iii)

$$rac{\partial g(z)_j}{\partial z_i} = \left\{ egin{array}{c} rac{e^{z_i} (\Sigma_{j=1}^k e^{z_j}) - e^{2z_i}}{(\Sigma_{j=1}^k e^{z_j})^2}, i = j \ -rac{e^{z_i + z_j}}{(\Sigma_{j=1}^k e^{z_j})^2}, i
eq j \end{array}
ight.$$

1.2.(i)

$$egin{aligned} z_{FC_{1a}} &= heta_{1a} x + b_{1a} \ a_{FC_{1a}} &= ReLU(z_{FC_{1A}}) \ a_{DP_{1a}} &= M igodots a_{FC_{1a}} \ \hat{y}_a &= a_{FC_{2a}} = heta_{2a} a_{DP_{1a}} + b_{2a} \ z_{FC_{1b}} &= heta_{1b} x + b_{1b} \ a_{FC_{1b}} &= ReLU(z_{FC_{1b}}) \ a_{BN_{1b}} &= BN_{\gamma,eta}(a_{FC_{1b}}) \ z_{FC_{2b}} &= heta_{2b}(a_{BN_{1b}} igodots a_{FC_{2a}}) + b_{2b} \ \hat{y}_b &= a_{FC_{2b}} &= Softmax(z_{FC_{2b}}) \ L(x,y_a,y_b; heta) &= rac{1}{m} \sum_{i=1}^m [rac{1}{2} ||(\hat{y}_{ai} - y_{ai})||_2^2 - \sum_{j=1}^{n_{yb}} y_{bi}^j log(\hat{y}_{bi}^j)] \end{aligned}$$

1.2.(ii)

$$\begin{split} \frac{\partial L}{\partial z_{FC_{2b}}} &= \frac{1}{m} \Sigma_{i=1}^m (\hat{y}_b^{(i)} - y_b^{(i)}), \text{得到残差} \delta^{(FC_{2b})} \\ &\frac{\partial L}{\partial \theta_{2b}} = \delta^{(FC_{2b})} (a_{BN_{1b}} \oplus \hat{y}_a)^T \\ &\frac{\partial L}{\partial a_{BN_{1b}}} = \delta^{(FC_{2b})} \theta_{2b}^T, \text{得到残差} \delta^{(BN_{1b})} \frac{\partial L}{\partial \gamma} = \delta^{(BN_{1b})} \hat{a}_{FC_{1b}}^T \\ &\frac{\partial L}{\partial \beta} = \Sigma_{i=1}^{n_{ya}} \delta_i^{(BN_{1b})} \\ &\text{对于} BN_{\mathbb{R}} \text{,记输出} a_{BN_{1b}} \text{为} y \text{,记输入} a_{FC_{1b}} \text{为} x \text{,则有} \\ &\frac{\partial y_j}{\partial x_i} = \begin{cases} \gamma(\sigma_b^2 + \epsilon)^{-3/2} ((1 - \frac{1}{m})(\sigma_b^2 + \epsilon) - \frac{1}{m}(x_j - \sigma_B)(x_i - \sigma_B), i = j \\ \gamma(\sigma_b^2 + \epsilon)^{-3/2} (-\frac{1}{m}(\sigma_b^2 + \epsilon) - \frac{1}{2}(x_j - \sigma_B)(x_i - \sigma_B), i \neq j \end{cases} \\ &\frac{\partial L}{\partial a_{FC_{1b}}} = \Sigma_{j=1}^m \delta^{(BN_{1b})} \frac{\partial y_j}{\partial x_i} \end{split}$$

$$\begin{split} \frac{\partial a_{FC_{1b}i}}{\partial z_{FC_{1b}i}} &= sgn(z_{FC_{1b}i}) \\ \frac{\partial L}{\partial z_{FC_{1b}i}} &= \Sigma_{j=1}^m \delta^{(BN_{1b})} \frac{\partial y_j}{\partial x_i} \bigodot sgn(z_{FC_{1b}i}), \ \text{记为残差} \, \delta^{(FC_{1b})} \\ \frac{\partial L}{\partial \theta_{1b}} &= \delta^{(FC_{1b})} x^T \\ \\ \frac{\partial L}{\partial \hat{y}_a} &= \frac{1}{m} \sum_{i=1}^m (\hat{y}_a^{(i)} - y_a^{(i)}) + \delta^{(FC_{2b})} \theta_{2b}^T, \ \text{组合得到残差} \, \delta^{(ya)} \\ \\ \frac{\partial L}{\partial \theta_{2a}} &= \delta^{(ya)} a_{DP_{1a}}^T \\ \\ \frac{\partial L}{\partial a_{DP_{1a}}} &= \delta^{(ya)} \theta_{2a}^T, \ \text{组合得到残差} \, \delta^{(dp)} \\ \\ \frac{\partial L}{\partial a_{FC_{1a}}i} &= \begin{cases} 0, r_i$$