

MAE 3780/3783: Mechatronics  
February 5, 2024

# Logistics Updates

- This week in lab – **office hours**
  - **Lab 2** will occur next week – details released (including pre-lab) soon
- HW 2 (resistors) due **Friday, February 9, 11 pm**
- HW 3 (RLC) released asap – Due **Friday, February 23, 11 pm**
- Office hours schedule viewable on shared Google calendar

Let's add numbers!

$$V_S = 3\text{ V}$$

$$R_1 = 300\ \Omega$$

$$R_2 = 1\text{ k}\Omega$$

$$R_3 = 100\ \Omega$$

$$I_S = 0\text{ A}$$

what is  $V_{R_3}$ ?

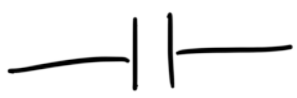
from node analysis:

$$\begin{bmatrix} \frac{1}{300} + \frac{1}{100} & -\frac{1}{100} & 0 \\ \frac{1}{100} & -\left(\frac{1}{100} + \frac{1}{1000}\right) & 1 \\ 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} V_A \\ V_B \\ i \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 3 \end{bmatrix}$$

$$\begin{bmatrix} V_A \\ V_B \\ i \end{bmatrix} = \begin{bmatrix} \frac{9}{4} \text{ V} \\ 3 \text{ V} \\ \frac{21}{2000} \text{ A} \end{bmatrix}$$

$$\begin{aligned} V_{R_3} &= V_A - V_B = \frac{9}{4} - 3 \\ &= -\frac{3}{4} \text{ V} \end{aligned}$$

# Energy Storing Devices

capacitor:  $C$   farad (F)  
typically 1pf - 1mf

$$C_{tot} = C_1 + C_2 + \dots C_n \text{ (in parallel)}$$

$$\frac{1}{C_{tot}} = \frac{1}{C_1} + \frac{1}{C_2} + \dots \frac{1}{C_n} \text{ (in series)}$$

$$I-V: I_C = C \frac{dV_C}{dt}$$

$$V_C(t) = \frac{1}{C} \int_{-\infty}^t I_C(t') dt'$$

given  $V_c(t=t_0) = V_0$  then

$$V_c(t) = \frac{1}{C} \int_{t_0}^t I_c(t') dt' + V_0$$

$\forall t \geq t_0$

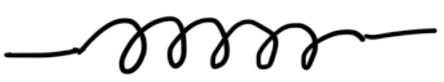
properties:

- at steady state,  $I_c(t \rightarrow \infty) = 0$   
(open circuit)

- continuity:  $V_c$  cannot jump

$$V_c(t^-) = V_c(t^+)$$

$I_c$  can jump

inductor:  $L$   Henry (H)

$$L_{\text{tot}} = L_1 + L_2 + \dots L_N \quad (\text{in series})$$

$$\frac{1}{L_{\text{tot}}} = \frac{1}{L_1} + \frac{1}{L_2} + \dots \frac{1}{L_N} \quad (\text{in parallel})$$

$$\text{I-V: } V_L = L \frac{dI_L}{dt}$$

$$I_L(t) = \frac{1}{L} \int_{-\infty}^t V_L(t') dt'$$

given  $I_L(t=t_0) = I_0$  then

$$I_L(t) = \frac{1}{L} \int_{t_0}^t V_L(t') dt' + I_0$$

$\forall t \geq t_0$

properties:

— at steady state  $V_L(t \rightarrow \infty) = 0$   
(short circuit)

— continuity:  $I_L$  cannot jump

$$I_L(t^-) = I_L(t^+)$$

$V_L$  can jump



circuit analysis:

① KVL, KCL, ohm's law to write ODE

② Solve ODE:

- bring to canonical form

- find initial condition

$$x(t=0) = x_0$$

- find steady state

$$x(t \rightarrow \infty) = x_\infty$$

- use formula in ODE handout

first order system:

$$\tau \frac{dx(t)}{dt} + x(t) = K_s F(t)$$

$$\text{solution: } x(t) = (x_0 - x_\infty) e^{-\frac{t}{\tau}} + x_\infty$$