

mesh analysis:

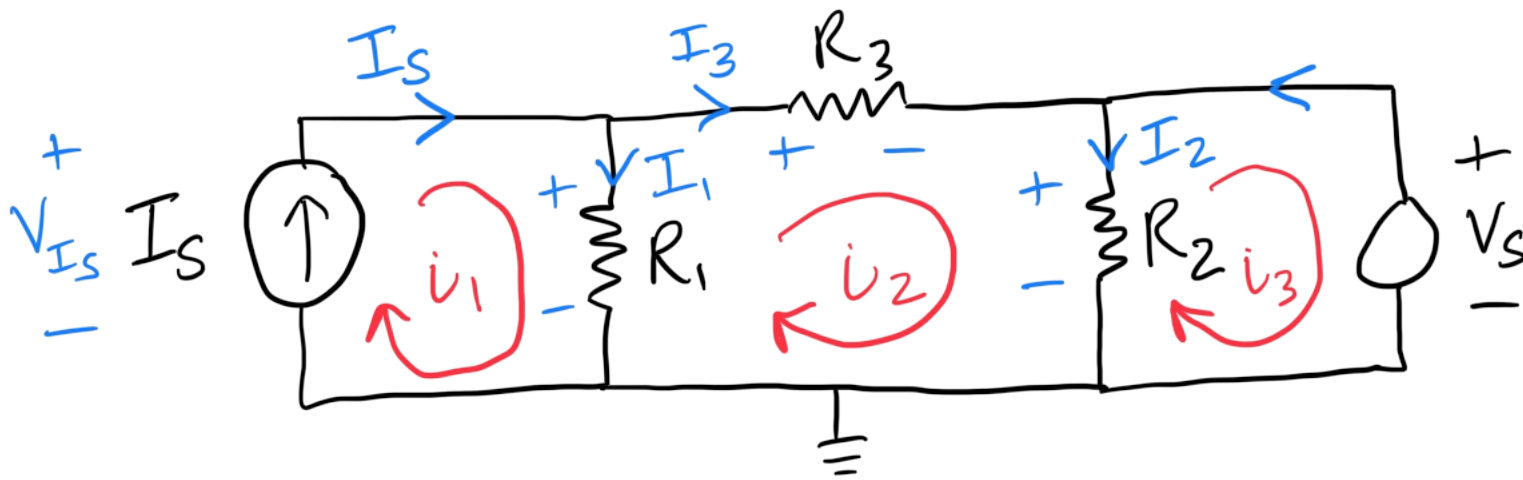
unknowns: ① mesh currents

② voltage across current sources

known: ① sources

equations to use:

- KVL represented using mesh currents
- current sources



unknowns: i_1 , i_2 , i_3 , V_{Is}

KVL on meshes:

mesh 1: $-V_{Is} + V_{R_1} = 0$

ohm's law: $-V_{Is} + R_1(i_1 - i_2) = 0$

this is the correct equation;
check for yourselves! :)

$R_1 i_1 - R_1 i_2 - V_{Is} = 0$

known

$$\text{mesh 2: } -V_{R_1} + V_{R_3} + V_{R_2} = 0$$

$$\text{ohm's law: } -R_1(i_1 - i_2) + R_3 i_2 + R_2(i_2 - i_3) = 0$$

$$-R_1 i_1 + (R_1 + R_2 + R_3) i_2 - R_2 i_3 = 0 \quad \text{known}$$

$$\text{mesh 3: } -V_{R_2} + V_S = 0$$

$$\text{ohm's law: } -R_2(i_2 - i_3) + V_S = 0$$

$$-R_2 i_2 + R_2 i_3 = -V_S \quad \text{known}$$

$$\text{current source: } I_S = i_1$$

together: originally incorrectly written in
lecture; this is correct

$$\begin{bmatrix} R_1 & -R_1 & 0 & -1 \\ -R_1 & R_1+R_2+R_3 & -R_2 & 0 \\ 0 & -R_2 & R_2 & 0 \\ 1 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \\ i_3 \\ V_{I_s} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ -V_s \\ I_s \end{bmatrix}$$

$A \qquad \qquad \qquad x \qquad \qquad \qquad b$

$$Ax = b \implies x = A^{-1}b$$

Let's add numbers!

$$V_S = 3\text{ V}$$

$$R_1 = 300\ \Omega$$

$$R_2 = 1\text{ k}\Omega$$

$$R_3 = 100\ \Omega$$

$$I_S = 0\text{ A}$$

what is V_{R_3} ?