

Solution Sketch for PS6

1. Solution

- (a) MR,MR,MB,MB
- (b) Everyone will guess the urn contains a majority of the color that they observed.
- (c) MR,MR,MR,MR. Note: P4 only knows P2 and P3 both guessed MR, so it is necessarily true that they know player 3's guess is uninformative. Indeed from P4's perspective, P1-P3 may have observed the following balls (each with prob. $1/3$): (B,R,R), (R,R,B), (R,R,R), which means the conditional probability should be $(P[MB|BRRB] + P[MB|RRBB] + P[MB|RRRB])/3 = (1/2 + 1/2 + 1/5)/3 = 2/5 < 1/2$

2. Solution

- (a) $b/(a+b) < p \leq 1$
- (b) Player 2 will always guess Urn A regardless
- (c) Player 3 will guess Urn A since $P(\text{Urn A}|BRB) = 9/17 > P(\text{Urn B}|BRB) = 8/17$
- (d) Player 3 will guess Urn B since $P(\text{Urn A}|BRB) = 3/7 < P(\text{Urn B}|BRB) = 4/7$
- (e) $q \geq b/(a+b)$

3. Solution

- (a) $4 \times 4 = 16$
- (b) $A = \{(1,1), (1,2), (2,1), (2,2), (2,3), (3,2), (3,3), (3,4), (4,3), (4,4)\}$
 $B = \{(1,1), (1,2), (1,3), (1,4), (3,1), (3,2), (3,3), (3,4)\}$
 $A \cap B = \{(1,1), (1,2), (3,2), (3,3), (3,4)\}$.
- (c) $P(A) = 5/8, P(B) = 1/2, P(A \cap B) = 5/16, P(A|B) = 5/8, P(B|A) = 1/2$.