

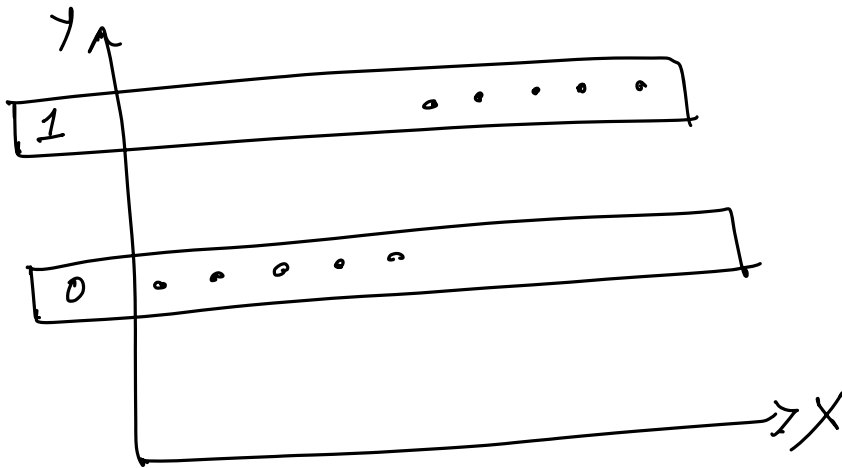
# Logistic Regression (LR)

→ Logistic regression is a special case of regression analysis and is used when dependent variable is nominally scaled.

Eg: Variable purchase decision : buys a product or does not buy a product.

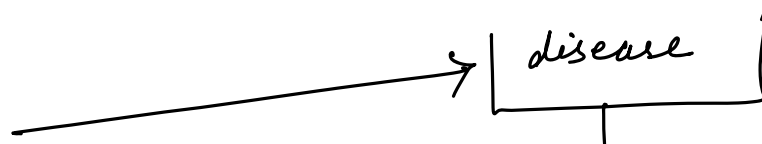
→ With LR, it is now possible to explain the dependent variable or estimate the probability of occurrence of the categories of the variable.

→ In the basic form of LR, dichotomous variable (0 or 1) can be predicted. For this purpose, the probability of occurrence of value = 1 (characteristic present is estimated).



Age,  
Gender,  
Smoking status

↓  
Independent variable



↓  
dependent variable

01 → diseased

00 → not diseased

(How likely is it that the disease is present if the person under consideration has a certain age, sex and smoking status).

Calculate LR:

To build a LR model, the linear regression eqn. is used as the starting point.

$$\hat{y} = b_1 x_1 + b_2 x_2 + \dots + b_k x_k + a$$

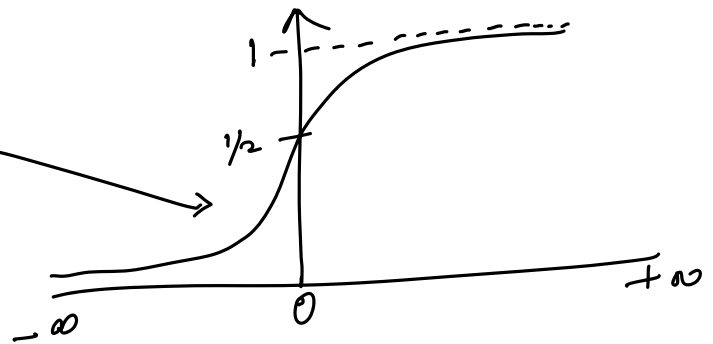
independent variable

reg. coefficients

Logistic function -

The logistic model is based on logical functions.

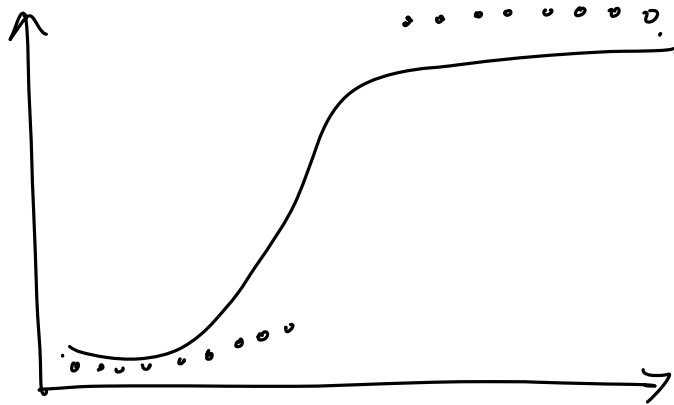
$$f(z) = \frac{1}{1 + e^{-z}}$$



$$\hat{y} = b_1 x_1 + b_2 x_2 + \dots + b_k x_k + a$$

$$f(z) = \frac{1}{1 + e^{-z}} = \frac{1}{1 + e^{-(b_1 x_1 + b_2 x_2 + \dots + b_k x_k + a)}}$$

This now ensures that no matter in which range the  $x$  values are located, only values between 0 and 1 will come out. The new graph now looks like this:



The probability that for given values of the independent variable the dichotomous dependent variable  $y$  is 0 or 1 is given by:

$$P(y=1 | x_1, x_2, \dots, x_k) = \frac{1}{1 + e^{-(b_1 x_1 + b_2 x_2 + \dots + b_k x_k + a)}}$$

$$P(y=0 | x_1, x_2, \dots, x_k) = 1 - \frac{1}{1 + e^{-(b_1 x_1 + \dots + b_k x_k + a)}}$$