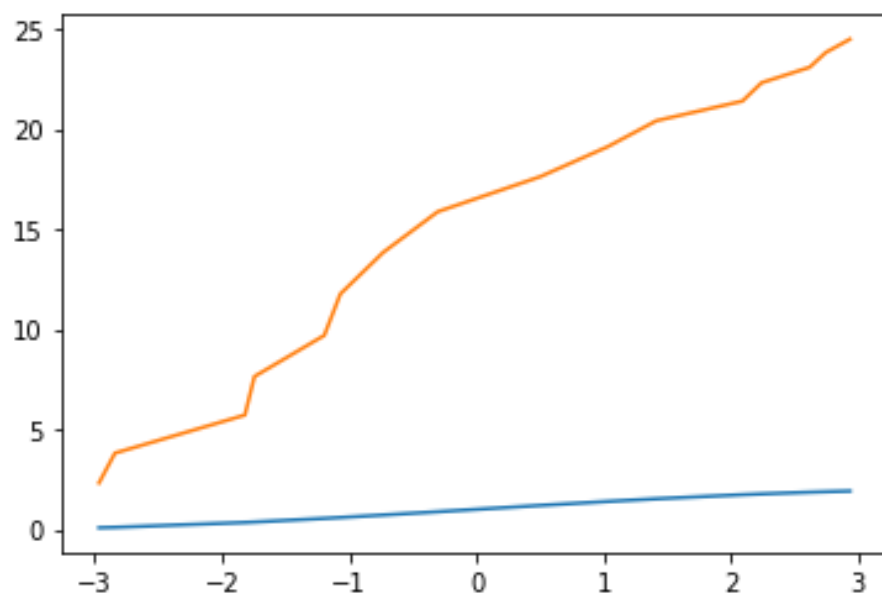


## Κεφάλαιο 13

### Πρόβλημα 13

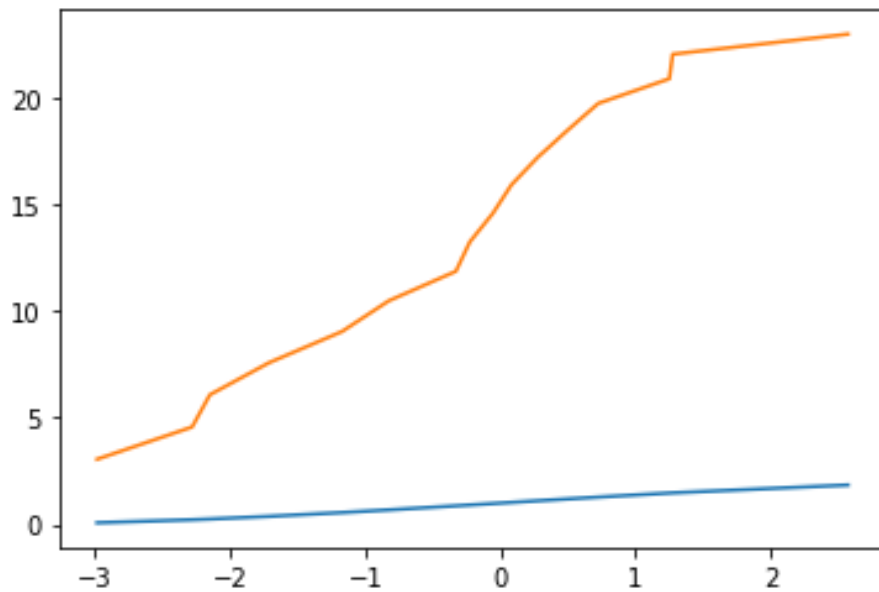
---



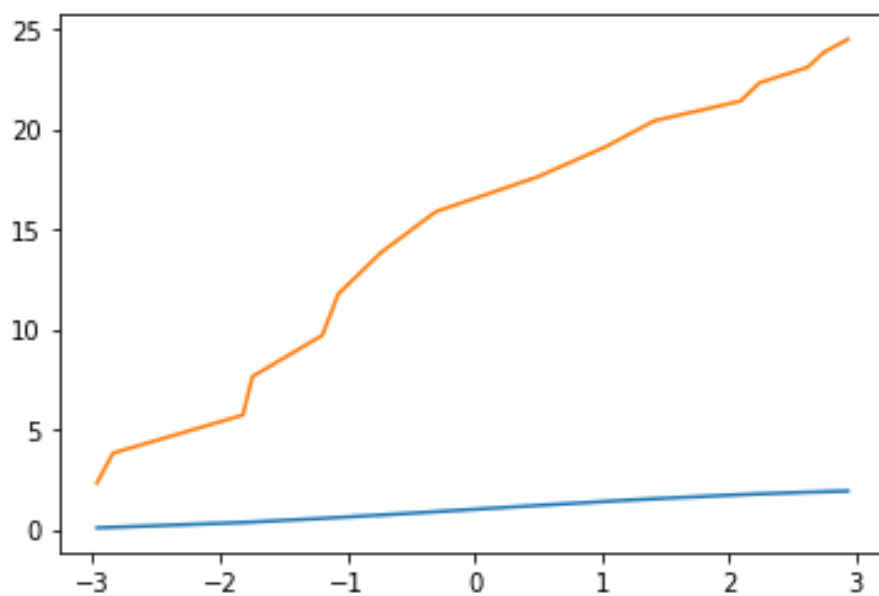
Εικόνα 13.1: *Network Response S=4*

#### 13.1 Python Code

```
1 import matplotlib.pyplot as plt
2
3 from math import sin, pi, exp, sqrt
4 from random import uniform
5
6 # Initialize input vectors
7
8 p = [uniform(-3.0, 3.0),uniform(-3.0, 3.0),uniform(-3.0, 3.0),uniform(-3.0, 3.0),uniform(-3.0, 3.0),
9       uniform(-3.0, 3.0),uniform(-3.0, 3.0),uniform(-3.0, 3.0),uniform(-3.0, 3.0),uniform(-3.0, 3.0),
10      uniform(-3.0, 3.0),uniform(-3.0, 3.0),uniform(-3.0, 3.0),uniform(-3.0, 3.0),uniform(-3.0, 3.0),
11      uniform(-3.0, 3.0)]
12 p.sort()
13 learning_rate = 0.01
14
15 def g_function(p):
```



Εικόνα 13.2: *Network Response S=8*



Εικόνα 13.3: *Network Response S=16*

```

13     return 1+sin(p*(pi/8))
14
15 def radbas(n):
16     return exp(-n*n)
17
18 def purelin(n):
19     return n
20
21 def purelin_der(n):
22     return 1
23
24 def radbas_der(n):

```

```

25     return -2*n*exp(-n*n)
26
27 S = 4
28
29 # Initialize weights and biases
30
31 for k in range(3):
32     print(f"For S = {S}")
33     w1 = []
34     b1 = []
35     w2 = []
36     for i in range(S):
37         w1.append(uniform(0, 0.5))
38         b1.append(uniform(0, 0.5))
39         w2.append(uniform(0, 0.5))
40     b2 = uniform(0, 0.5)
41
42 # Start training
43
44 while True:
45     sum_sq_error = 0
46     for i in range(10):
47         n1 = []
48         a1 = []
49         n2 = b2
50         for j in range(S):
51             n = sqrt((p[i]-w1[j])*(p[i]-w1[j]))+b1[j])
52             n1.append(n)
53             a = radbas(n)
54             a1.append(a)
55             n2 += a * w2[j]
56         a2 = purelin(n2)
57
58         # Calculate error
59
60         e = g_function(p[i])-a2
61         sum_sq_error = sum_sq_error + e*e
62
63         # Calculate sensitivities and recalculate weights and biases
64
65         s2 = -2*purelin_der(n2)*(e)
66         s1 = []
67         for j in range(S):
68             s1.append(radbas_der(n1[j])*w1[j]*s2)
69
70         w2[j] -= learning_rate*s2*a1[j]
71     b2 -= learning_rate*s2
72
73     for j in range(S):
74         w1[j] -= learning_rate*s1[j]*p[i]
75         b1[j] -= learning_rate*s1[j]
76

```

```
77     # Check sum square error threshold
78
79     if sum_sq_error <= 1.2:
80         break
81
82     # Classify vectors
83
84     result = []
85     g = []
86     print( f"points: {p}")
87     for i in range(16):
88         for j in range(S):
89             n = p[i]*w1[j]+b1[j]
90             a = radbas(n)
91             n2 += a * w2[j]
92             a2 = purelin(n2)
93             result.append(a2)
94             g.append(g_function(p[i]))
95
96     # Design plot
97
98     plt.plot(p, g)
99     plt.plot(p, result)
100     plt.show()
101
102     S = S * 2
```