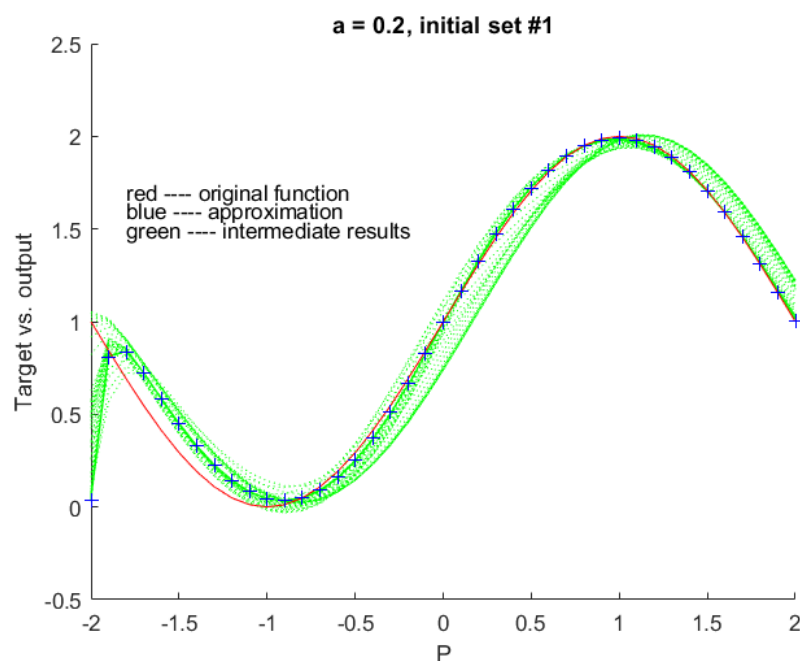


## Κεφάλαιο 3

### Πρόβλημα 3

---

#### 3.1 $S^1 = 2$



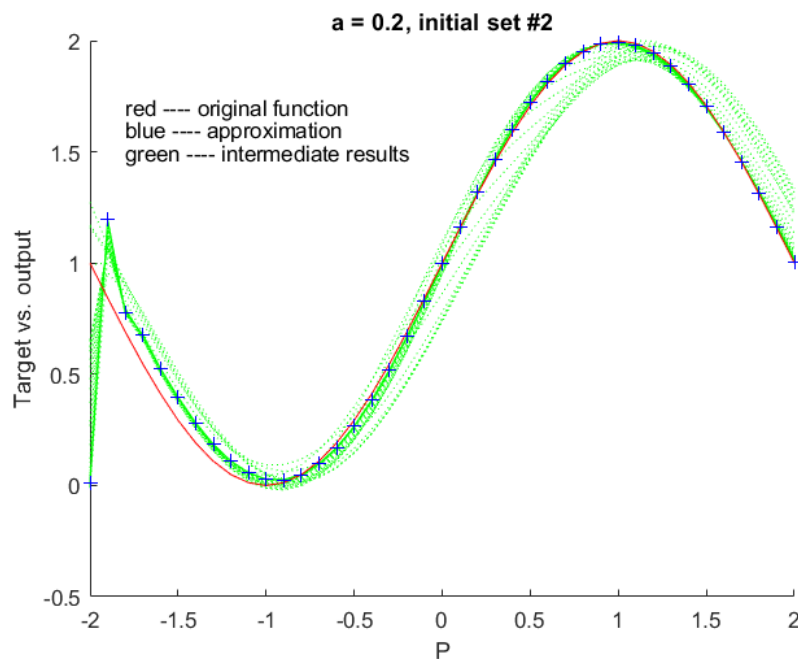
Εικόνα 3.1:  $S^1 = 2, a = 0.2$ , Initial set 1

#### 3.2 $S^1 = 10$

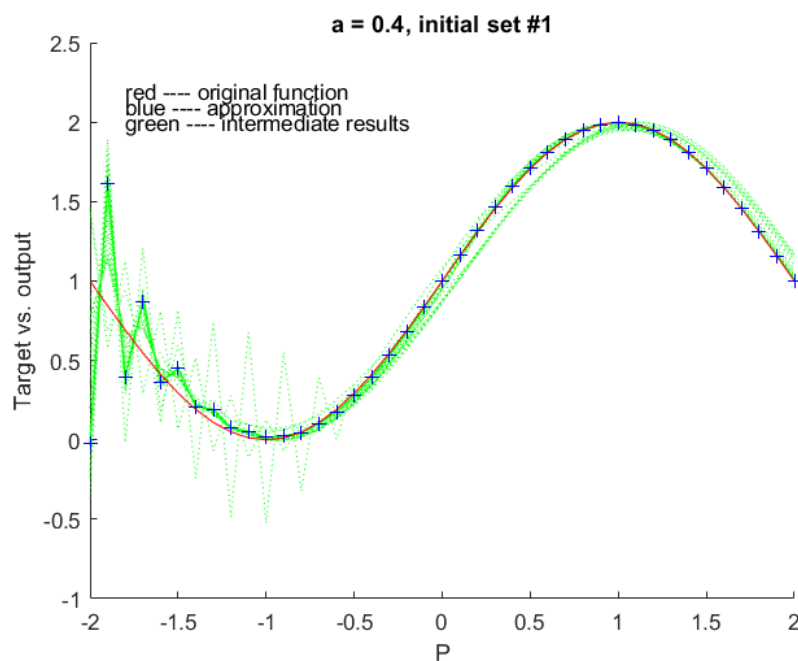
The code was modified and tested for  $S^1 = 10$  and led us to the following conclusions .

#### 3.3 Discuss the convergence properties of the algorithm as the learning rate changes

1. The higher the learning rate is, the faster the iteration process converges
2. When  $a > 0.6$ , the solution becomes unstable. e.g.  
When  $a = 0.8$  is used, the converging process is very unstable, and takes a long time



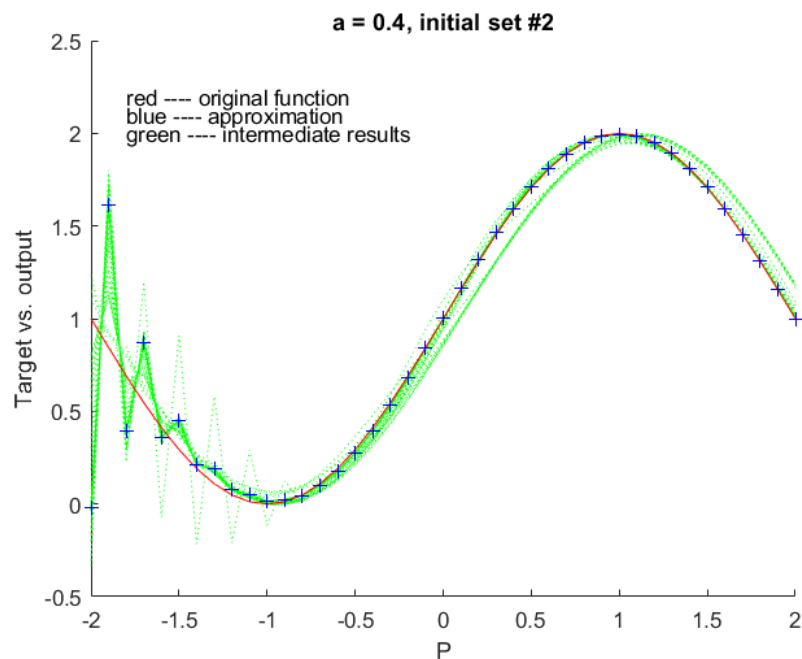
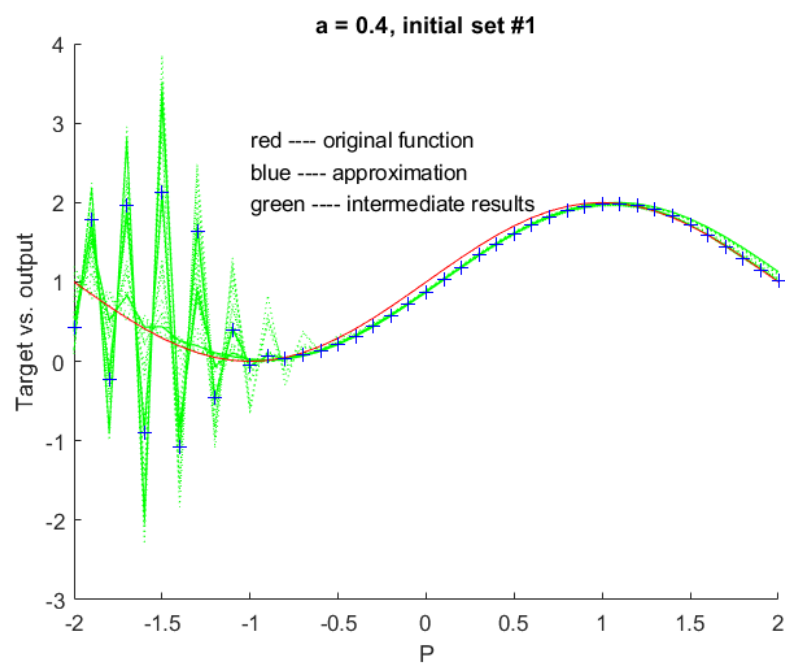
Εικόνα 3.2:  $S^1 = 2, a = 0.2$ , Initial set 2



Εικόνα 3.3:  $S^1 = 2, a = 0.4$ , Initial set 1

3. The initial weights and biases affects the converging speed and the final results
4. The momentum backpropagation variance would probably be applied successfully in this model

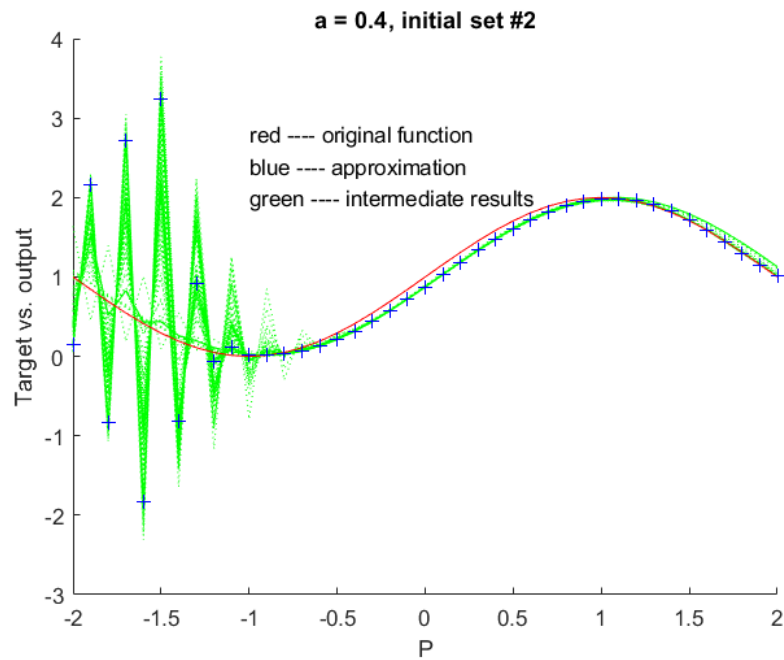
### 3.4 MATLAB Code

Εικόνα 3.4:  $S^1 = 2, a = 0.4$ , Initial set 2Εικόνα 3.5:  $S^1 = 2, a = 0.6$ , Initial set 1

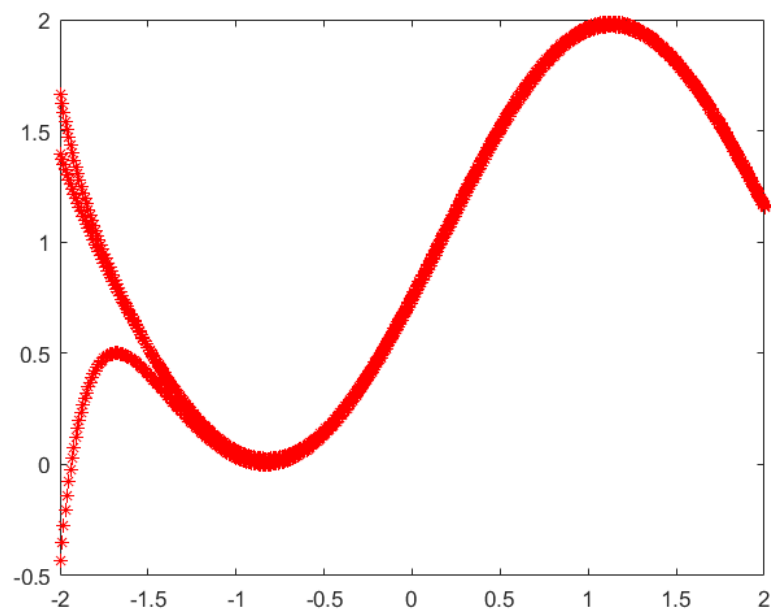
```

1 clear
2 %Initialize data
3 W1 = rand(2,1) - 0.5;
4 W2 = rand(1,2) - 0.5;
5 b1 = rand(2,1) - 0.5;
6 b2 = rand - 0.5;
7 a1 = zeros(2,1);
8

```



Εικόνα 3.6:  $S^1 = 2, a = 0.6$ , Initial set 2

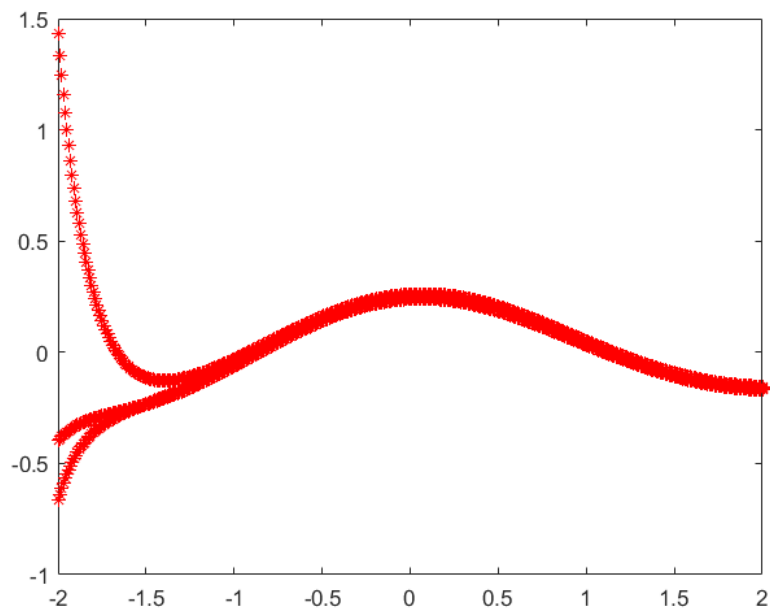
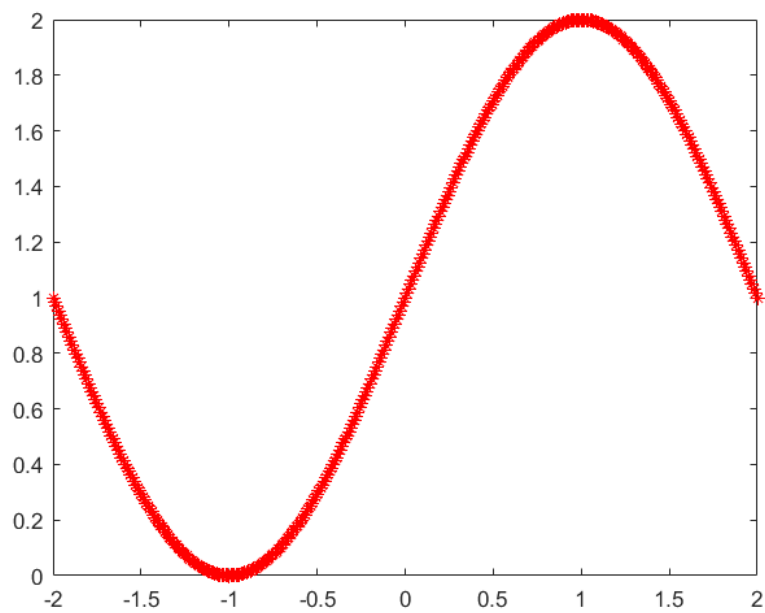


Εικόνα 3.7:  $S^1 = 10$ , approximation

```

9 %Output the initial set
10 w1_0 = w1
11 b1_0 = b1
12 w2_0 = w2
13 b2_0 = b2
14
15 alfa = 0.6; %learning rate
16 tol = 0.1; %tol: tolerance

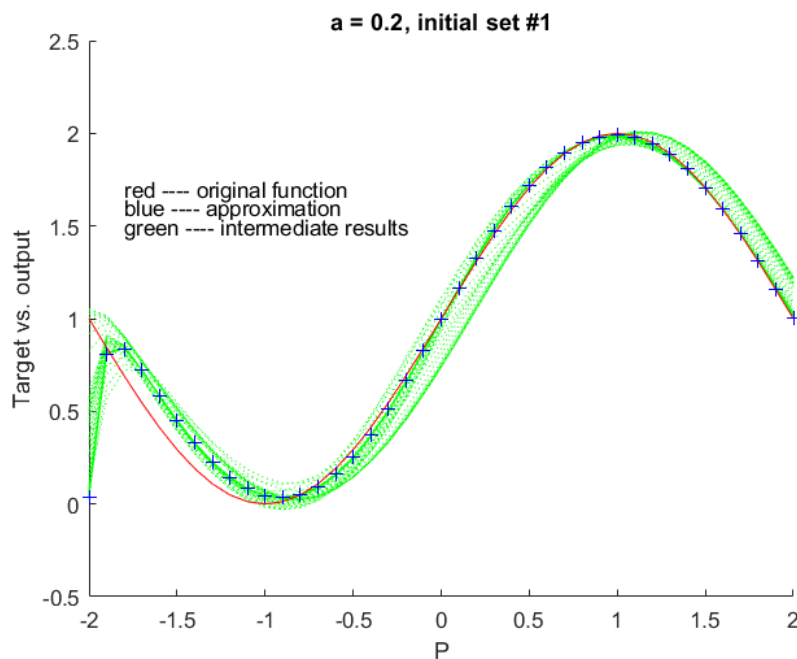
```

Εικόνα 3.8:  $S^1 = 10$ , *error*Εικόνα 3.9:  $S^1 = 10$ , *realfunctionvalue*

```

17 mse = 1;           %mse: mean square error
18 iter = 0;
19
20 figure;
21 while (mse > tol && iter < 1000)
22     mse = 0;
23     i = 0;
24     iter = iter + 1;

```

Εικόνα 3.10:  $S^1 = 2, a = 0.2$ , Initial set 1

```

25  for P = -2 : .1 : 2
26      i = i + 1;
27      T = 1 + sin(pi*P/2);
28      a1 = logsig(W1*P + b1);
29      a2 = purelin(W2*a1 + b2);
30      mse = mse + (T - a2)^2;
31      A(i) = a2;
32
33      dlogsig = [(1 - a1(1))* a1(1) 0;0 (1 - a1(2))* a1(2)];
34      s2 = -2 * (T - a2);
35      s1 = dlogsig * W2' * s2;
36
37      W2 = W2 - alfa * s2 * a1';
38      W1 = W1 - alfa * s1 * P;
39      b2 = b2 - alfa * s2;
40      b1 = b1 - alfa * s1;
41  end
42  P = -2 : .1 : 2;
43  if (mod(iter,10) == 0)
44      plot(P,A,'g:')
45  end
46  hold on;
47 end
48
49 %Display in graph
50 P = -2 : .1 : 2;
51 T = 1 + sin(pi*P/2);
52 %figure;
53 plot(P,T,'r-',P,A,'b+')
54 title('a = 0.4, initial set #2');

```

```

55 text(-1.0,2.8,'red ---- original function');
56 text(-1.0,2.4,'blue ---- approximation');
57 text(-1.0,2.0,'green ---- intermediate results');
58 xlabel('P'), ylabel('Target vs. output');
59 W1
60 b1
61 W2
62 b2
63 iter

1 clf; clc; clear;
2
3 % Init min/max
4 xMax = 0.5;
5 xMin = -xMax;
6 difference = xMax-xMin;
7
8 % Init w1, b1, w2, b2
9
10 W1(:, 1) = xMin + rand(1, 10)*difference; % For the first layer (logsig)
11 B1(:, 1) = xMin + rand(1, 10)*difference; % The new values of the weights, biases will be added to each
    column
12
13 W2(1, :) = (xMin+rand(1,10)*difference)'; % For the second layer (purelin)
14 B2(1) = xMin + rand(1, 1)*(difference); % The new values of the weights, biases will be added to each row
15
16 i = 1;
17 learningRate = 0.01;
18
19 while (1)
20     for p = -2:0.01:2
21
22         % FEED-FORWARD PHASE
23
24         product = (W1(:, i).* p + B1(:, i)); % Compute activation for 1st layer
25         A1(:, i) = 1./(1+exp(-product));
26         A2(i) = W2(i, :)*A1(:, i) + B2(1); % Compute activation for 2nd layer
27
28         % COMPUTE ERROR THROUGH THE COST FUNCTION
29
30         error = 1 + sin(p * (pi/2)) - A2(i);
31
32         % BACKPROPAGATION PREPARATION
33
34         % Compute derivative for 1st activation, compute sensitivities
35         derivative = [];
36         for row = 1:10
37             element = (1-A1(row,i))*A1(row,i);
38             derivative = [derivative element];
39         end
40         R = diag(derivative);
41
42         s2 = -2 * 1 * error;

```

```
43     s1 = R * W2(i, :) * s2;
44
45     % UPDATE WEIGHTS AND BIASES
46
47     W1(:, i+1) = W1(:, i) - learningRate * s1 * p;
48     B1(:, i+1) = B1(:, i) - learningRate * s1;
49
50     W2(i+1, :) = W2(i, :) - learningRate * s2 * A1(:,i)';
51     B2(i+1) = B2(i) - learningRate * s2;
52
53     figure(1);
54     plot(p, error, '*b');
55     hold on;
56
57     figure(2);
58     plot(p, A2(i), '*g');
59     hold on;
60
61     figure(3)
62     plot(p, 1 + sin(p*(pi/2)), '*r');
63     hold on;
64
65     i = i + 1;
66
67 end
68
69 if (abs(error) < 0.1 || i>1000)
70     return % End if absolute error is smaller than the predefined threshold
71 end
72
73 end
```