STA2201H Winter 2024 Assignment 1

Due: 11:59pm, 5 February 2023

What to hand in: .qmd or .Rmd file and the compiled pdf

How to hand in: Submit files via Quercus

1 Overdispersion

Suppose that the conditional distribution of outcome Y given an unobserved variable θ is Poisson, with a mean and variance $\mu\theta$, so

$$Y|\theta \sim \text{Poisson}(\mu\theta)$$

- a) Assume $E(\theta) = 1$ and $Var(\theta) = \sigma^2$. Using the laws of total expectation and total variance, show $E(Y) = \mu$ and $Var(Y) = \mu(1 + \mu\sigma^2)$.
- b) Assume θ is Gamma distributed with α and β as shape and scale parameters, respectively. Show the unconditional distribution of Y is Negative Binomial.
- c) In order for $E(Y) = \mu$ and $Var(Y) = \mu(1 + \mu \sigma^2)$, what must α and β equal?

2 Child support payments

Consider the situation where we are interested in the effect of divorced fathers' income on their child support payments. In this question we will be simulating the 'true' relationship between these two factors in a population, simulating survey data, then calculating the estimated relationship based on that surveyed data.

- a) Simulate data on income and child support payments for a population of 1000 fathers. Simulate both variables on the log scale, and assume
 - Log of Income is normally distributed with a mean of log(10000) and a standard deviation of log(100)
 - Log of Payments are normally distributed with a mean of log(3500) and a standard deviation of log(30)

Plot a histogram of both variables.

- b) Create a scatter plot of log payments versus log income and add a line of best fit. Briefly describe what you observe.
- c) Simulate a set of fathers who are surveyed from total population in the following way:
 - Transform log income and log payments to z-scores
 - Create a new variable called **survey** that is a logical variable equal to TRUE if the sum of the two z-scores, plus some random noise (i.e. plus a draw from a standard normal distribution) is greater than 0.

Explain what the calculation for **survey** is doing, and what real-life sampling situation it is emulating. Summarize the mean payments and income for surveyed and non-surveyed fathers, and briefly comment.

- d) Illustrate with the regressions and a plot the estimated effect of income on payments for the surveyed fathers. How does this differ to the same relationship estimated from the total population?
- e) Discuss briefly what you observe and broader implications for drawing inferences from survey data.

Note: this example was inspired by a classic paper in sociology:

Lin, I. F., & Seltzer, J. A. (1999). Causes and effects of nonparticipation in a child support survey. Journal of Official Statistics, 15(2), 143

3 Hurricanes

In 2014 the following paper was published in PNAS:

Jung, K., Shavitt, S., Viswanathan, M., & Hilbe, J. M. (2014). Female hurricanes are deadlier than male hurricanes. Proceedings of the National Academy of Sciences, 111(24), 8782-8787.

As the title suggests, the paper claimed that hurricanes with female names have caused a greater loss of life. In this question you will be investigating the data set used for the regression part of their analysis.

You can download the data from the paper's supporting information here: https://www.pnas.org/doi/10.1073/pnas.1402786111#supplementary-materials

You should skim the whole paper but you will probably find it useful to read the sections on the Archival Study in the most depth (both in the main text and 'Materials and Methods' section).

- a) Create three graphs in ggplot that help to visualize patterns in deaths by femininity, minimum pressure, and damage. Discuss what you observe based on your visualizations.
- b) Run a Poisson regression with deaths as the outcome and femininity as the explanatory variable. Interpret the resulting coefficient estimate. Check for overdispersion. If it is an issue, run a quasi-Poisson regression with the same variables. Interpret your results.
- c) Reproduce Model 4 (as described in the text and shown in Table S2). Report the estimated effect of femininity on deaths assuming a hurricane with median pressure and damage ratings.
- d) Using Model 4, predict the number of deaths caused by Hurricane Sandy. Interpret your results
- e) Describe at least two strengths and two weaknesses of this paper, focusing on the archival analysis. What was done well? What needed improvement?
- f) Are you convinced by the results? If you are, explain why. If you're not, describe what additional data and/or analyses you would like to see to further test the author's hypothesis.

¹I was able to reproduce the coefficient estimates using the data available but the standard errors were slightly different, so don't worry if that is what you find.

4 Commuting behavior

This question relates to commuting behavior in Canadian communities. We are interested in exploring factors that are associated with differences in the likelihood of commuting via public transit in Canadian census metropolitan areas.

- You can download the data here: https://www150.statcan.gc.ca/t1/tbl1/en/tv.action?pid=9810046801 (to download, select Download Options, the CSV, Download entire table)
- a) You will need to tidy up the dataset to get it in a more useable for to run your analyses. Here are some suggested things to do:
- Remove unwanted columns and clean up column names
- Filter the dataset to just include Census Metropolitan Areas (CMAs), to remove upper and lower 95% bounds, and to remove any total counts in the age, gender, visible minority, and commuting columns
- Collapse the immigrant counts to just be just two categories: **immigrant** (which is the sum of the immigrant and non-permanent residents) and **non-immigrant**. You will also need to collapse the commute type categories to be just two: **public** and **non-public**
- Reshape your dataset so it is in 'long' format: geography, visible minority status, age, gender, and immigrant status are all different columns showing all possible categories, and then there are 'public commute', 'non-public commute', and 'total' columns which show counts of populations in each group.

Show the first few rows of your dataset as output in your assignment.

- b) Perform some exploratory data analysis (EDA) using the commuting dataset, focusing on differences in public transit commuting. Summarize your observations with the aid of 3-4 key tables or graphs.
- c) Build a regression model at the CMA level to help investigate patterns in public commuting. There is no one right answer here, but you should justify the outcome measure you are using (e.g. counts, proportions, rates, etc) and your distributional assumptions about the outcome measure (e.g. binary, poisson, normal, etc). You should also discuss briefly your model building strategy; what covariates you considered and why (motivated by your EDA), and how the candidate model was chosen.² Interpret your findings, including visualizations where appropriate.
- d) Use your model from c) to predict the proportion of men in Edmonton who are aged 35-44, are not from a visible minority, and are not immigrants, who take public transit. Compare this prediction to the same demographic group in Toronto. Briefly discuss how good you think this prediction is, and why.
- e) Give a brief summary of your analysis. What could this model be used for? What are the limitations? What other variables may be of interest to investigate in future?

²Note that province, while not explicitly in the dataset, could be an interesting covariate.