

Tipología y ciclo de vida de los datos - Práctica 2

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Contents

1	Descripción del Dataset	1
2	Integración y selección de los datos de interés a analizar	2
2.1	Primer contacto con el juego de datos, visualizamos su estructura.	2
3	Limpeza de los datos	3
3.1	Trabajamos en los atributos con valores vacíos	3
3.2	Identificación y tratamiento de valores extremos	8
3.2.1	Variable age	8
3.2.2	Variable Education.num	8
3.2.3	Variable Capital.gain	9
3.2.4	Variable Capital.loss	11
3.2.5	Variable hours.per.week	13
4	Análisis de los datos	15
4.1	Selección de los grupos de datos	15
4.1.1	Correlation of numeric variables	15
4.1.2	Category variables	16
4.2	Comprobación de la normalidad y homogeneidad de la varianza	32
4.3	Aplicación de pruebas estadísticas	33
4.3.1	Pruebas de contraste de hipótesis	33
4.3.2	Correlaciones	35
4.3.3	Regresiones	36
5	Representación de los resultados	36
6	Resolución del problema	37

1 Descripción del Dataset

El conjunto que utilizamos es el “Adult dataset” que esta disponible desde Kaggle y del UCI Machine Learning Repository. Consiste de aproximadamente 32000 observaciones, y 15 variables.

El objetivo es ver lo bien que podemos predecir si los ingresos anuales (income) de una persona superior a \$50000 utilizando el conjunto de variables en este conjunto de datos.

Aquí esta la descripción de las variables:

- age – The age of the individual
- workclass – The type of employer the individual has. Whether they are government, military, private, and so on.
- fnlwgt – The # of people the census takers believe that observation represents. We will be ignoring this variable
- education – The highest level of education achieved for that individual
- education.num – Highest level of education in numerical form

- marital.status – Marital status of the individual
- occupation – The occupation of the individual
- relationship – Contains family relationship values like husband, father, and so on, but only contains one per observation.
- race – descriptions of the individuals race. Black, White, etc
- sex – Male or Female
- capital.gain – Capital gains recorded
- capital.loss – Capital Losses recorded
- hours.per.week – Hours worked per week
- native.country – Country of origin for person
- income – Boolean Variable. Whether or not the person makes more than \$50,000 per annum income.

2 Integración y selección de los datos de interés a analizar

2.1 Primer contacto con el juego de datos, visualizamos su estructura.

```
# Cargamos los paquetes R que vamos a usar
library(ggplot2)
library(dplyr)

##
## Attaching package: 'dplyr'

## The following objects are masked from 'package:stats':
##
##   filter, lag

## The following objects are masked from 'package:base':
##
##   intersect, setdiff, setequal, union

library(knitr)
library(nortest)

## Warning: package 'nortest' was built under R version 3.5.2

# Cargamos el juego de datos
datosAdult <- read.csv('adult.csv', stringsAsFactors = TRUE, header = TRUE)

# Nombres de los atributos
#names(datosAdult) <- c("age", "workclass", "fnlwgt", "education", "education-num", "marital-status", "occupa

# Verificamos la estructura del juego de datos
str(datosAdult)

## 'data.frame':   32561 obs. of  15 variables:
## $ age          : int   90 82 66 54 41 34 38 74 68 41 ...
## $ workclass    : Factor w/ 9 levels "?","Federal-gov",...: 1 5 1 5 5 5 8 2 5 ...
## $ fnlwgt       : int  77053 132870 186061 140359 264663 216864 150601 88638 422013 70037 ...
## $ education    : Factor w/ 16 levels "10th","11th",...: 12 12 16 6 16 12 1 11 12 16 ...
## $ education.num: int    9 9 10 4 10 9 6 16 9 10 ...
## $ marital.status: Factor w/ 7 levels "Divorced","Married-AF-spouse",...: 7 7 7 1 6 1 6 5 1 5 ...
## $ occupation   : Factor w/ 15 levels "?","Adm-clerical",...: 1 5 1 8 11 9 2 11 11 4 ...
## $ relationship : Factor w/ 6 levels "Husband","Not-in-family",...: 2 2 5 5 4 5 5 3 2 5 ...
## $ race         : Factor w/ 5 levels "Amer-Indian-Eskimo",...: 5 5 3 5 5 5 5 5 5 5 ...
```

```
## $ sex          : Factor w/ 2 levels "Female","Male": 1 1 1 1 1 1 2 1 1 2 ...
## $ capital.gain : int   0 0 0 0 0 0 0 0 0 0 ...
## $ capital.loss : int  4356 4356 4356 3900 3900 3770 3770 3683 3683 3004 ...
## $ hours.per.week: int   40 18 40 40 40 45 40 20 40 60 ...
## $ native.country: Factor w/ 42 levels "?","Cambodia",...: 40 40 40 40 40 40 40 40 40 1 ...
## $ income        : Factor w/ 2 levels "<=50K", ">50K": 1 1 1 1 1 1 1 2 1 2 ...
```

Tenemos 32561 observaciones en 15 variables

```
kable(head(datosAdult))
```

age	workclass	fnlwgt	education	education.num	marital.status	occupation	relationship	race	sex
90	?	77053	HS-grad	9	Widowed	?	Not-in-family	White	F
82	Private	132870	HS-grad	9	Widowed	Exec-managerial	Not-in-family	White	F
66	?	186061	Some-college	10	Widowed	?	Unmarried	Black	F
54	Private	140359	7th-8th	4	Divorced	Machine-op-inspct	Unmarried	White	F
41	Private	264663	Some-college	10	Separated	Prof-specialty	Own-child	White	F
34	Private	216864	HS-grad	9	Divorced	Other-service	Unmarried	White	F

3 Limpieza de los datos

3.1 Trabajamos en los atributos con valores vacíos

```
# Estadísticas de valores vacíos
```

```
colSums(is.na(datosAdult))
```

```
##          age          workclass          fnlwgt          education          education.num
##           0              0              0              0              0
## marital.status          occupation          relationship          race          sex
##           0              0              0              0              0
## capital.gain          capital.loss          hours.per.week          native.country          income
##           0              0              0              0              0
```

```
colSums(datosAdult=="")
```

```
##          age          workclass          fnlwgt          education          education.num
##           0              0              0              0              0
## marital.status          occupation          relationship          race          sex
##           0              0              0              0              0
## capital.gain          capital.loss          hours.per.week          native.country          income
##           0              0              0              0              0
```

Parece que no existen valores vacíos. Sin embargo, en el fichero adult.names que describe los datos dice:

Conversion of original data as follows:

1. Discretized agrossincome into two ranges with threshold 50,000.
2. Convert U.S. to US to avoid periods.
3. Convert Unknown to “?”
4. Run MLC++ GenCVFiles to generate data,test.

O sea que han cambiado los Unknowns (vacíos) a “?”.

Reimportamos los datos para poner cambiar los “?” a valores vacíos (NA)s.

```
# utilizamos na.strings para definir los caracteres de NA.
datosAdult <- read.csv('adult.csv',stringsAsFactors = TRUE, header = TRUE, na.strings="?")
```

Ahora comprobamos los valores vacios de nuevo.

```
# Estadísticas de valores vacíos
colSums(is.na(datosAdult))
```

```
##          age      workclass      fnlwt      education  education.num
##          0          1836          0          0          0
## marital.status  occupation  relationship      race          sex
##          0          1843          0          0          0
## capital.gain  capital.loss  hours.per.week  native.country      income
##          0          0          0          583          0
```

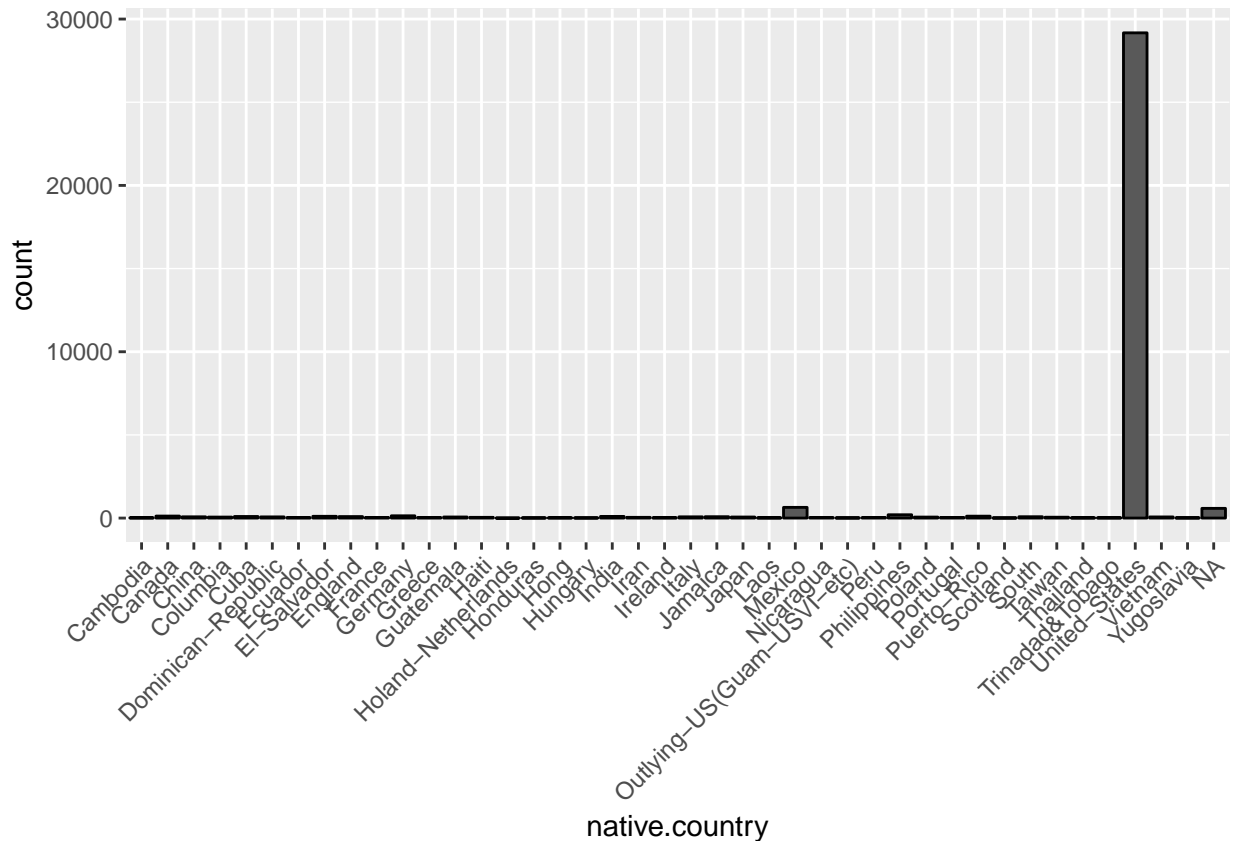
```
colSums(datosAdult=="")
```

```
##          age      workclass      fnlwt      education  education.num
##          0          NA          0          0          0
## marital.status  occupation  relationship      race          sex
##          0          NA          0          0          0
## capital.gain  capital.loss  hours.per.week  native.country      income
##          0          0          0          NA          0
```

Ahora vemos que el atributo workclass tiene 1836 valores vacios, occupation tiene 1843 valores vacios, y native.country tiene 583 valores vacios.

Podemos intentar predecir los valores que son vacios. Primero miramos a **native.country** .

```
# Visualizamos la distribución de la variable "native.country":
ggplot(data=datosAdult,aes(x=native.country))+geom_bar(color='black')+theme(axis.text.x=element_text(ang
```



Podemos asumir que los valores nulos de **native.country** son probablemente de origen EEUU. Ya que la mayoría de los datos son de ahí y normalmente la razón de no especificar el país nativo es que se trata de una persona que ya es un nativo de EEUU.

Podemos borrar los casos que tienen **occupation** de valor vacío - estaría difícil hacer una estimación de los valores correctos.

Podemos borrar los casos que tienen **workclass** de valor vacío - estaría difícil hacer una estimación de los valores correctos.

Además no necesitamos el atributo **fnlwgt** para tratar los datos y se puede eliminarlo.

```
# Aplicamos el valor "United-States" para los valores vacíos de la variable "native.country"
datosAdult$native.country[is.na(datosAdult$native.country)]="United-States"
```

```
#Borramos los casos con valores vacíos de occupation y workclass
#Before the delete we check
summary(datosAdult)
```

```
##      age      workclass      fnlwgt
##  Min.   :17.00   Private      :22696   Min.    : 12285
##  1st Qu.:28.00   Self-emp-not-inc: 2541   1st Qu.: 117827
##  Median :37.00   Local-gov       : 2093   Median : 178356
##  Mean   :38.58   State-gov       : 1298   Mean   : 189778
##  3rd Qu.:48.00   Self-emp-inc    : 1116   3rd Qu.: 237051
##  Max.   :90.00   (Other)         :  981   Max.   :1484705
##                NA's      : 1836
##      education  education.num      marital.status
##  HS-grad      :10501   Min.    : 1.00   Divorced      : 4443
```

```

## Some-college: 7291 1st Qu.: 9.00 Married-AF-spouse : 23
## Bachelors : 5355 Median :10.00 Married-civ-spouse :14976
## Masters : 1723 Mean :10.08 Married-spouse-absent: 418
## Assoc-voc : 1382 3rd Qu.:12.00 Never-married :10683
## 11th : 1175 Max. :16.00 Separated : 1025
## (Other) : 5134 Widowed : 993
## occupation relationship race
## Prof-specialty : 4140 Husband :13193 Amer-Indian-Eskimo: 311
## Craft-repair : 4099 Not-in-family : 8305 Asian-Pac-Islander: 1039
## Exec-managerial: 4066 Other-relative: 981 Black : 3124
## Adm-clerical : 3770 Own-child : 5068 Other : 271
## Sales : 3650 Unmarried : 3446 White :27816
## (Other) :10993 Wife : 1568
## NA's : 1843
## sex capital.gain capital.loss hours.per.week
## Female:10771 Min. : 0 Min. : 0.0 Min. : 1.00
## Male :21790 1st Qu.: 0 1st Qu.: 0.0 1st Qu.:40.00
## Median : 0 Median : 0.0 Median :40.00
## Mean : 1078 Mean : 87.3 Mean :40.44
## 3rd Qu.: 0 3rd Qu.: 0.0 3rd Qu.:45.00
## Max. :99999 Max. :4356.0 Max. :99.00
##
## native.country income
## United-States:29753 <=50K:24720
## Mexico : 643 >50K : 7841
## Philippines : 198
## Germany : 137
## Canada : 121
## Puerto-Rico : 114
## (Other) : 1595

```

#delete the NAs

```
datosAdult <- na.omit(datosAdult)
```

remember to re-factor the effected categories

```

datosAdult$workclass <- factor(datosAdult$workclass)
datosAdult$occupation <- factor(datosAdult$occupation)
datosAdult$native.country <- factor(datosAdult$native.country)

```

#after the delete we check again

```
summary(datosAdult)
```

```

## age workclass fnlwt
## Min. :17.00 Federal-gov : 960 Min. : 13769
## 1st Qu.:28.00 Local-gov : 2093 1st Qu.: 117829
## Median :37.00 Private :22696 Median : 178517
## Mean :38.44 Self-emp-inc : 1116 Mean : 189846
## 3rd Qu.:47.00 Self-emp-not-inc: 2541 3rd Qu.: 237317
## Max. :90.00 State-gov : 1298 Max. :1484705
## Without-pay : 14
## education education.num marital.status
## HS-grad :9968 Min. : 1.00 Divorced : 4258
## Some-college:6775 1st Qu.: 9.00 Married-AF-spouse : 21

```

```

## Bachelors :5182 Median :10.00 Married-civ-spouse :14339
## Masters :1675 Mean :10.13 Married-spouse-absent: 389
## Assoc-voc :1321 3rd Qu.:13.00 Never-married : 9912
## 11th :1056 Max. :16.00 Separated : 959
## (Other) :4741 Widowed : 840
## occupation relationship race
## Prof-specialty :4140 Husband :12704 Amer-Indian-Eskimo: 286
## Craft-repair :4099 Not-in-family : 7865 Asian-Pac-Islander: 974
## Exec-managerial:4066 Other-relative: 918 Black : 2909
## Adm-clerical :3770 Own-child : 4525 Other : 248
## Sales :3650 Unmarried : 3271 White :26301
## Other-service :3295 Wife : 1435
## (Other) :7698
## sex capital.gain capital.loss hours.per.week
## Female: 9930 Min. : 0 Min. : 0.00 Min. : 1.00
## Male :20788 1st Qu.: 0 1st Qu.: 0.00 1st Qu.:40.00
## Median : 0 Median : 0.00 Median :40.00
## Mean : 1106 Mean : 88.91 Mean :40.95
## 3rd Qu.: 0 3rd Qu.: 0.00 3rd Qu.:45.00
## Max. :99999 Max. :4356.00 Max. :99.00
##
## native.country income
## United-States:28060 <=50K:23068
## Mexico : 610 >50K : 7650
## Philippines : 188
## Germany : 128
## Puerto-Rico : 109
## Canada : 107
## (Other) : 1516

```

We now have reduced the observations in the dataset `datosAdult` from 32561 to 30718 records.

Ahora verificamos que no tenemos los valores vacíos.

```
# Estadísticas de valores vacíos
```

```
colSums(is.na(datosAdult))
```

```

## age workclass fnlwgt education education.num
## 0 0 0 0 0
## marital.status occupation relationship race sex
## 0 0 0 0 0
## capital.gain capital.loss hours.per.week native.country income
## 0 0 0 0 0

```

```
colSums(datosAdult=="")
```

```

## age workclass fnlwgt education education.num
## 0 0 0 0 0
## marital.status occupation relationship race sex
## 0 0 0 0 0
## capital.gain capital.loss hours.per.week native.country income
## 0 0 0 0 0

```

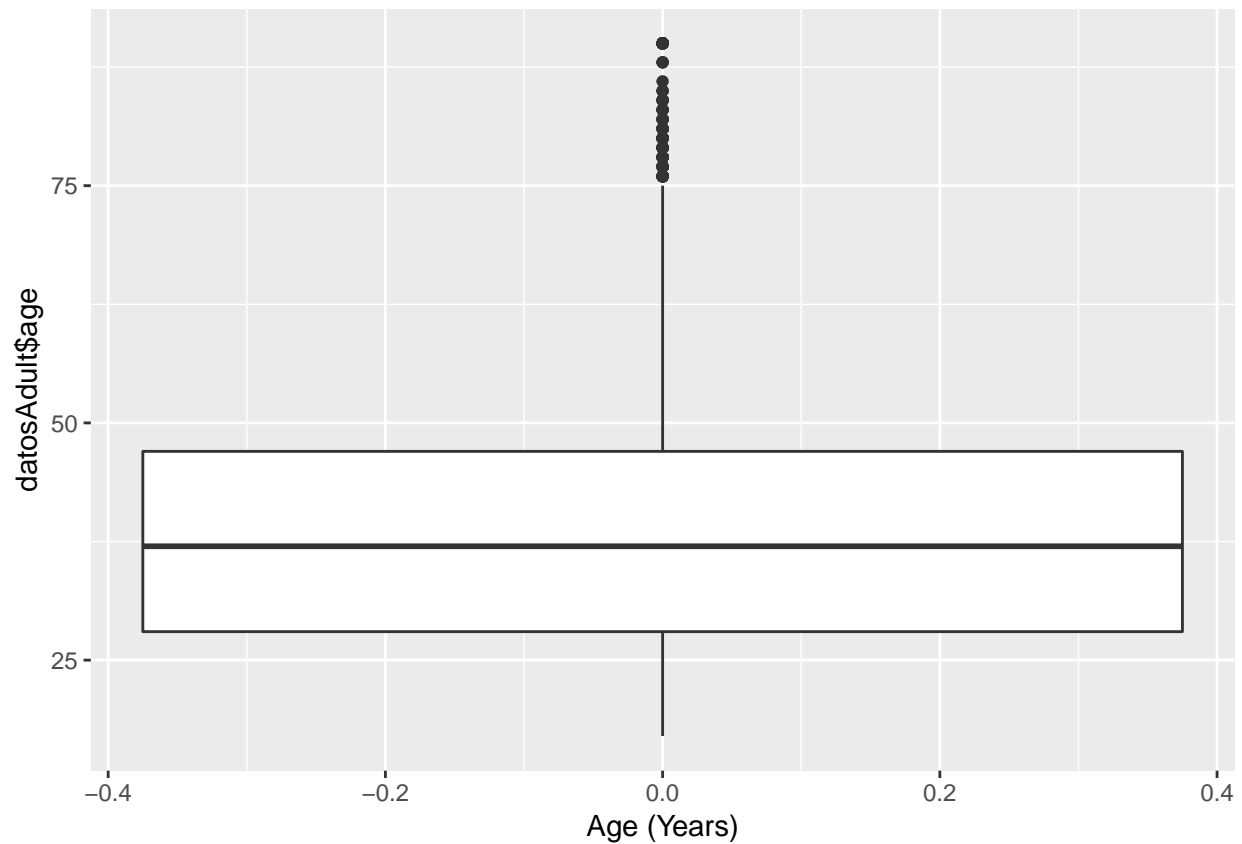
3.2 Identificación y tratamiento de valores extremos

We will check the numeric variables (age, education.num, capital.gain, capital.loss, hours.per.week) for outliers.

3.2.1 Variable age

```
AgeBoxplot<-ggplot(datosAdult,aes(y=datosAdult$age))+geom_boxplot()+labs(x="Age (Years)") + guides(fill=)
```

AgeBoxplot

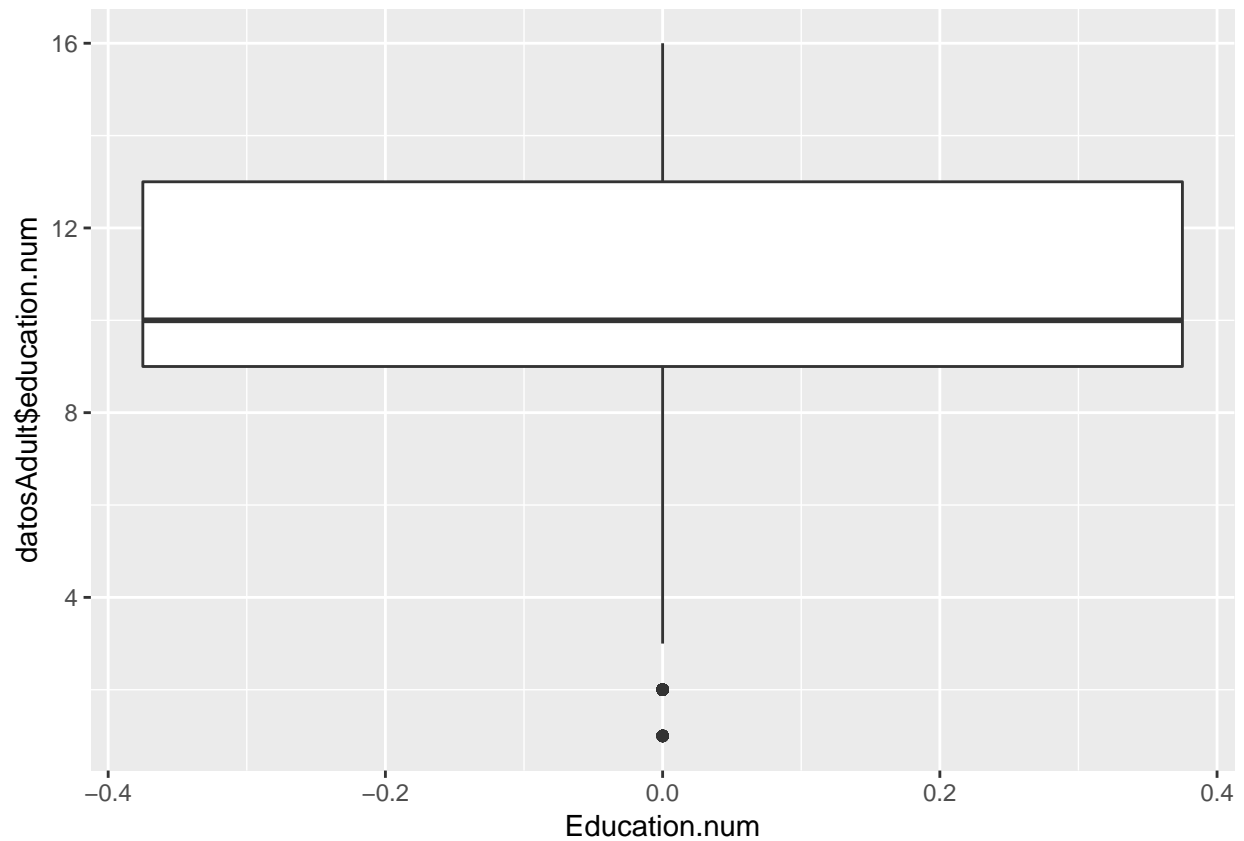


In this case we see that although there are outliers with age above 75, these are not unreasonable data values, so we will keep these values.

3.2.2 Variable Education.num

```
Education.numBoxplot<-ggplot(datosAdult,aes(y=datosAdult$education.num))+geom_boxplot()+labs(x="Educac
```

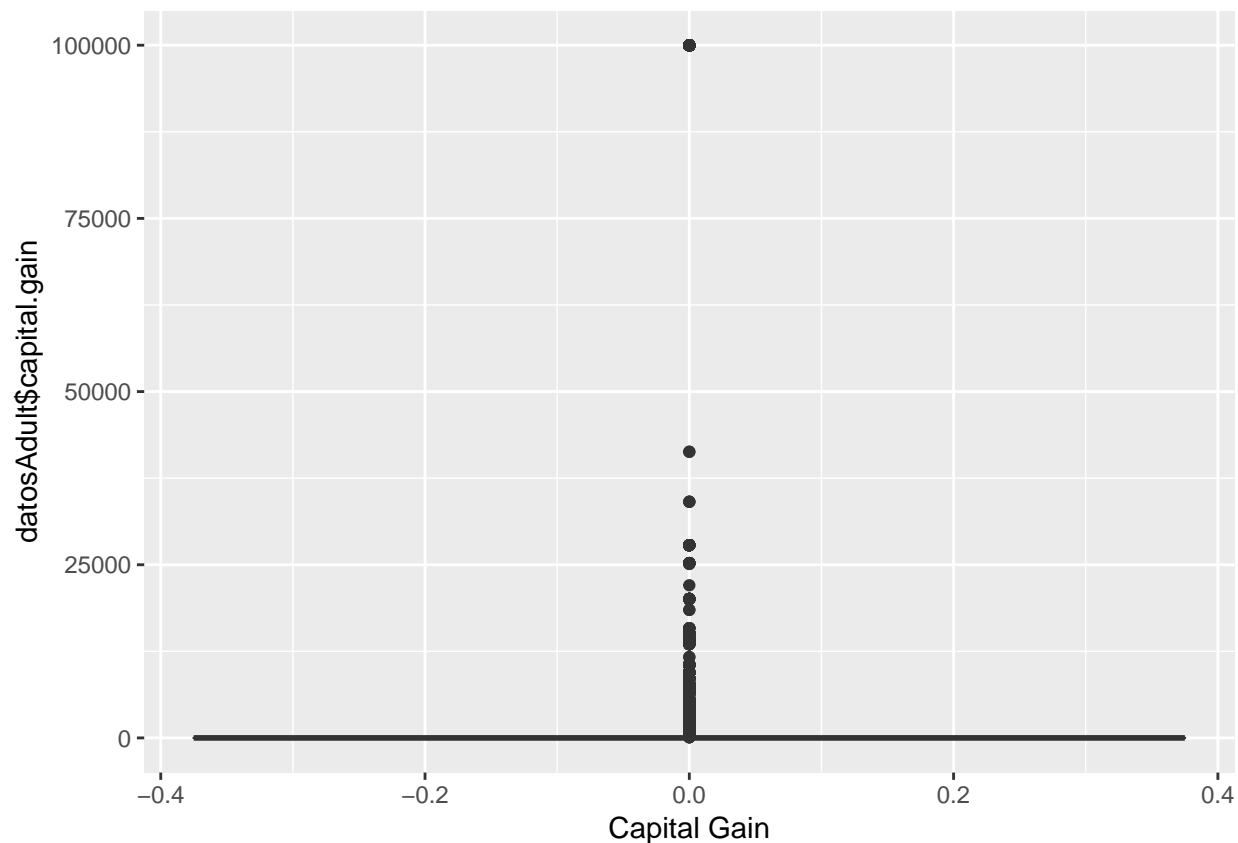
Education.numBoxplot



In this case we see that the outliers with values 1 and 2 are not unreasonable values and correspond to an educational level of the person.

3.2.3 Variable Capital.gain

```
CapGainBoxplot<-ggplot(datosAdult,aes(y=datosAdult$capital.gain))+geom_boxplot()+labs(x="Capital Gain")
CapGainBoxplot
```



Here we see that capital gain values are mostly zeros. The main outlier of concern is the one around 100000. Let's check the variation of capital.gain.

```
summary(datosAdult$capital.gain)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##         0         0         0   1106         0 99999
```

So we have a median value of zero and a mean of 1106. The maximum value of 99999 is an outlier probably caused by data entry field size limitations.

The percentage of zero values is very high for this variable.

```
(nrow(subset(datosAdult, datosAdult$capital.gain == 0))/nrow(datosAdult))*100
```

```
## [1] 91.57172
```

Let's look at the distribution of the non-zero values of **capital.gain**

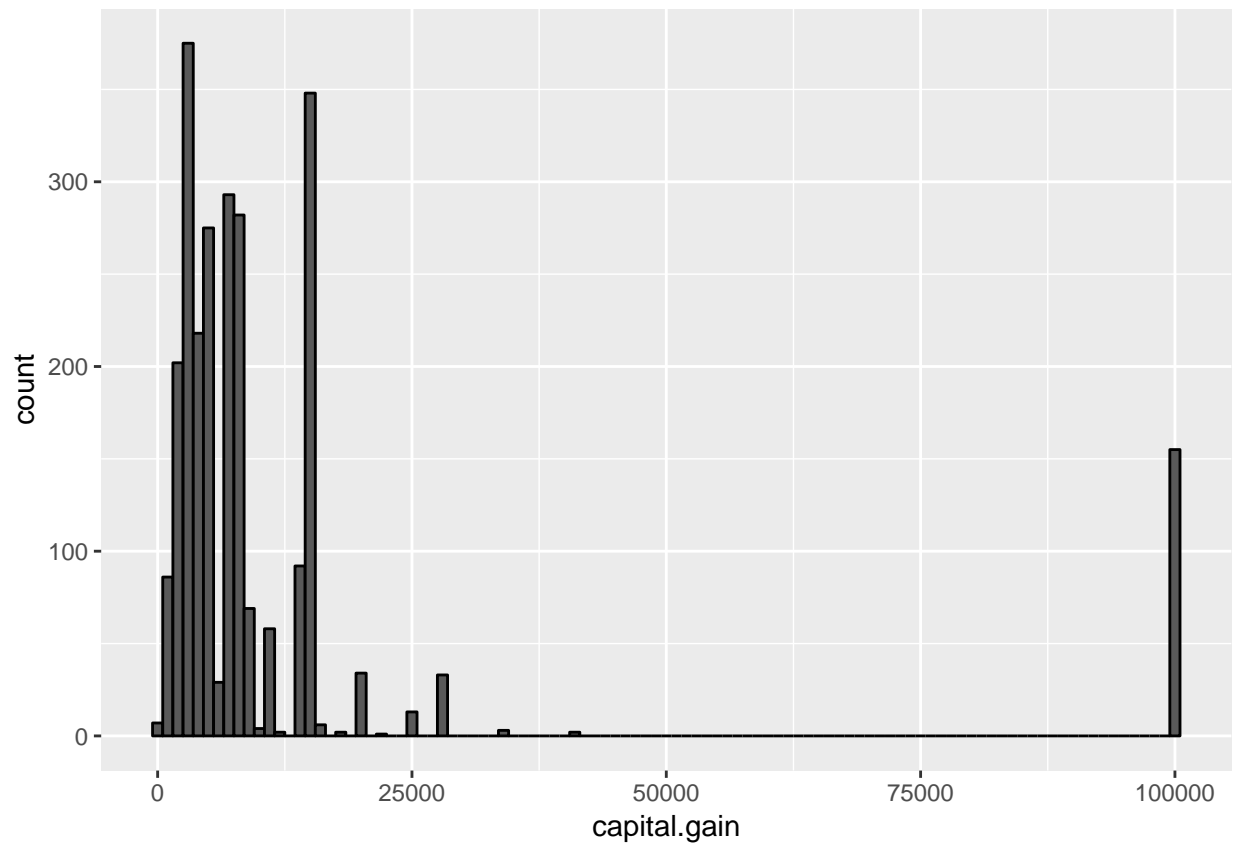
```
summary(datosAdult$capital.gain[datosAdult$capital.gain !=0])
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##     114   3464   7298  13123  14084   99999
```

And let's see a barchart of the non-zero values.

```
# Miramos a capital.gain en bins de tamaño 1000.
```

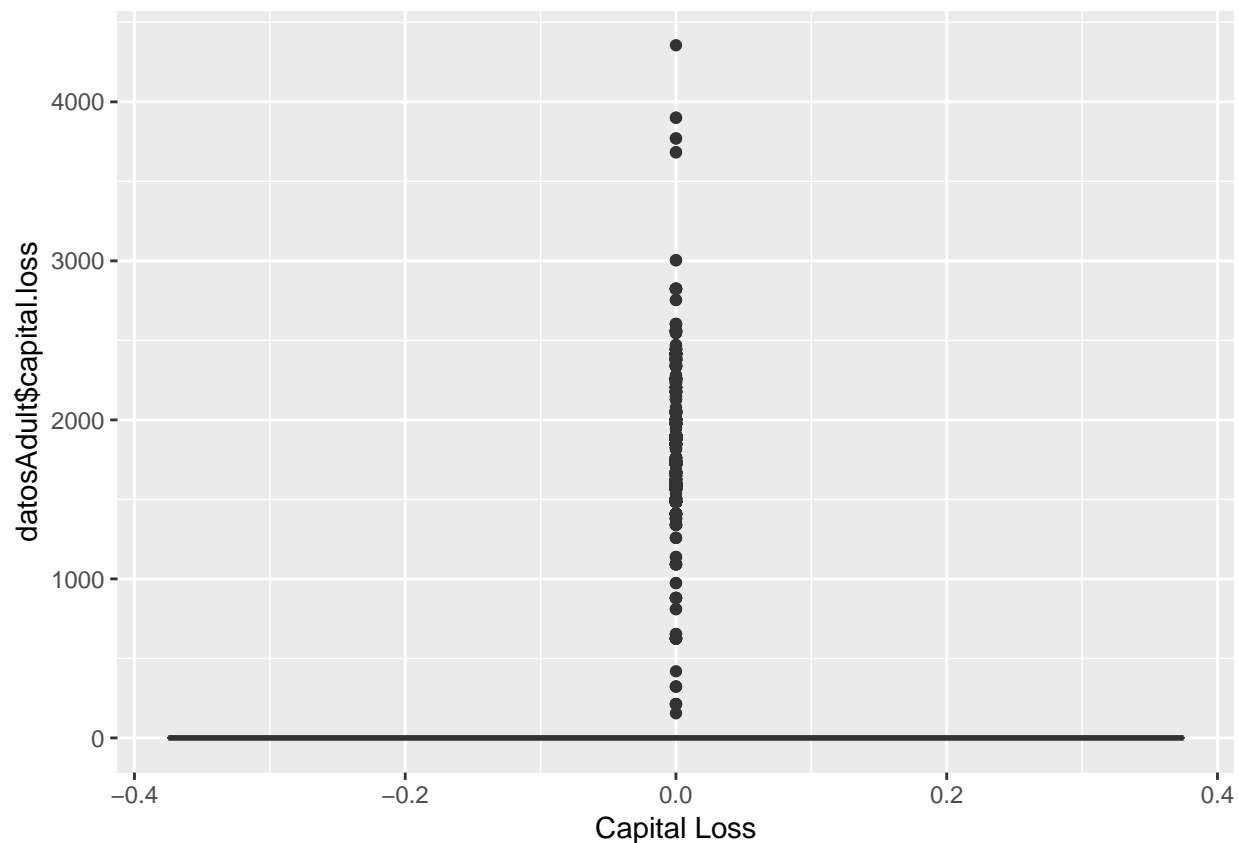
```
ggplot(datosAdult[which(datosAdult$capital.gain !=0),]) + aes(x=capital.gain) +
  geom_histogram(binwidth=1000, color='black')
```



Así que los valores de 99999 representan a gente con capital.gain muy alta y no podemos descartar el valor. Miramos a la otra variable capital.loss

3.2.4 Variable Capital.loss

```
CapLossBoxplot<-ggplot(datosAdult,aes(y=datosAdult$capital.loss))+geom_boxplot()+labs(x="Capital Loss")
CapLossBoxplot
```



Here we see that capital loss values are mostly zeros. Let's check the variation of capital.loss.

```
summary(datosAdult$capital.loss)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      0.00   0.00   0.00   88.91   0.00 4356.00
```

So we have a median value of zero and a mean of 88.91. The maximum value of 4356 is not really an outlier as we have many zero values for capital.loss.

The percentage of zero values is very high for this variable.

```
(nrow(subset(datosAdult, datosAdult$capital.loss == 0))/nrow(datosAdult))*100
```

```
## [1] 95.24383
```

Let's look at the distribution of the non-zero values of **capital.loss**

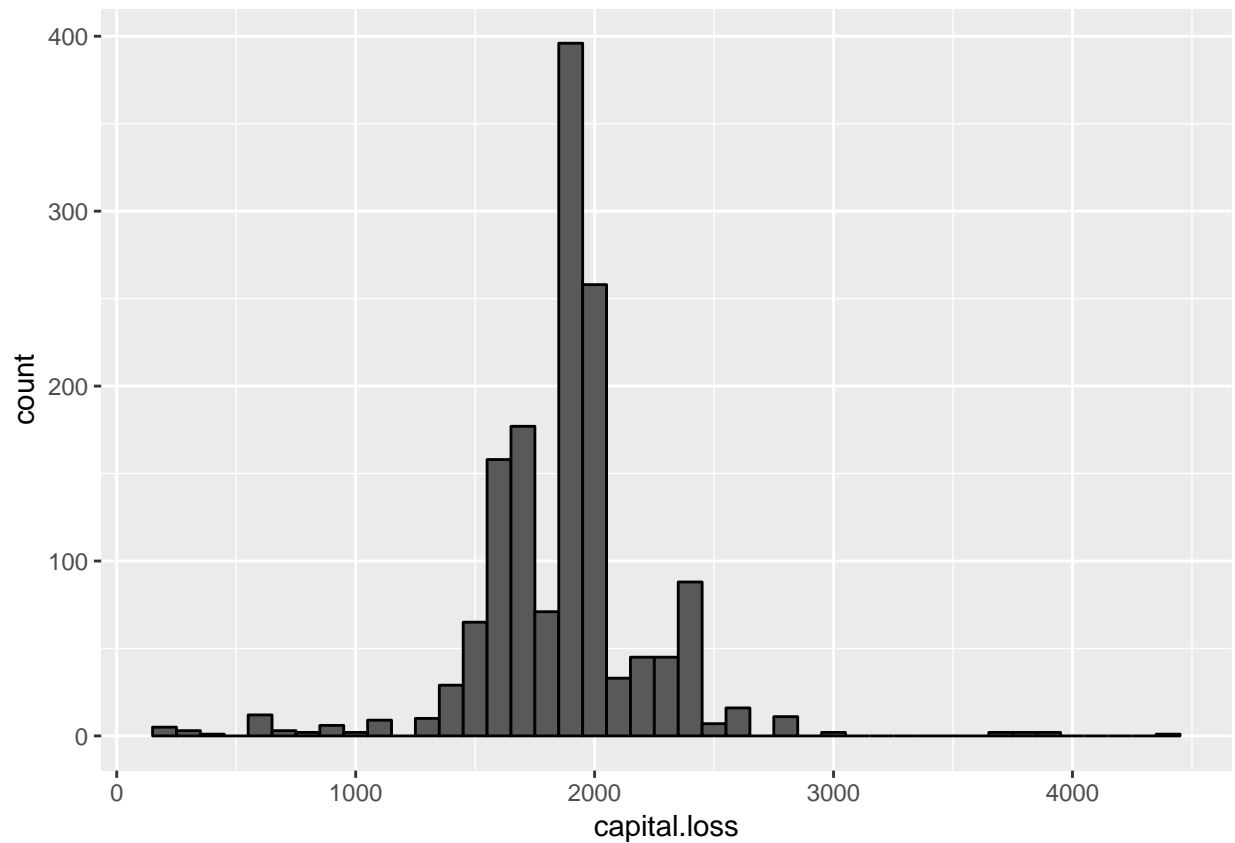
```
summary(datosAdult$capital.loss[datosAdult$capital.loss !=0])
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      155   1672   1887   1869   1977   4356
```

And let's see a barchart of the non-zero values.

```
# Miramos a capital.loss en bins de tamaño 100.
```

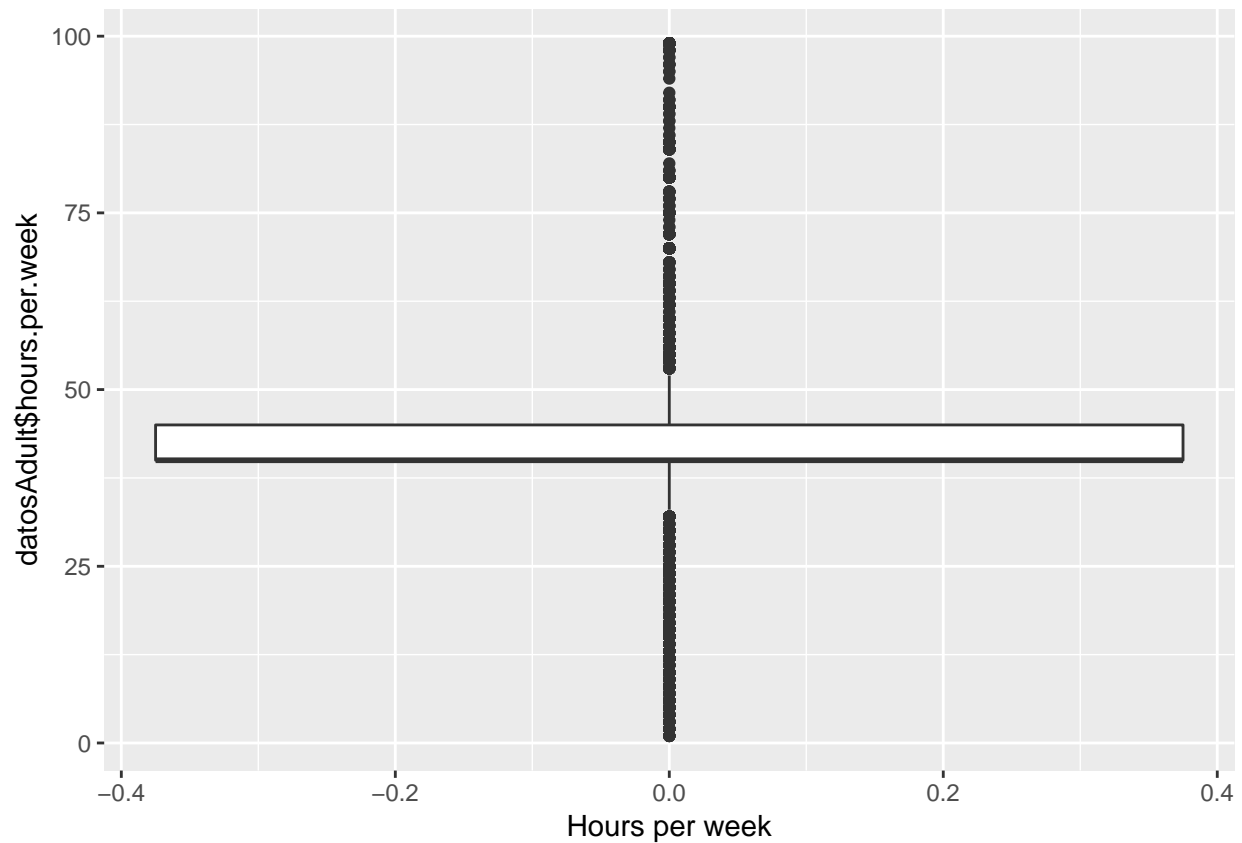
```
ggplot(datosAdult[which(datosAdult$capital.loss !=0),]) + aes(x=capital.loss) +
  geom_histogram(binwidth=100, color='black')
```



Así que los valores de de capital.loss parecen razonables.

3.2.5 Variable hours.per.week

```
HoursBoxplot<-ggplot(datosAdult,aes(y=datosAdult$hours.per.week))+geom_boxplot()+labs(x="Hours per week")
HoursBoxplot
```



Here we see that the boxplot highlights significant numbers of outliers. Let's check the variation of hours.per.week.

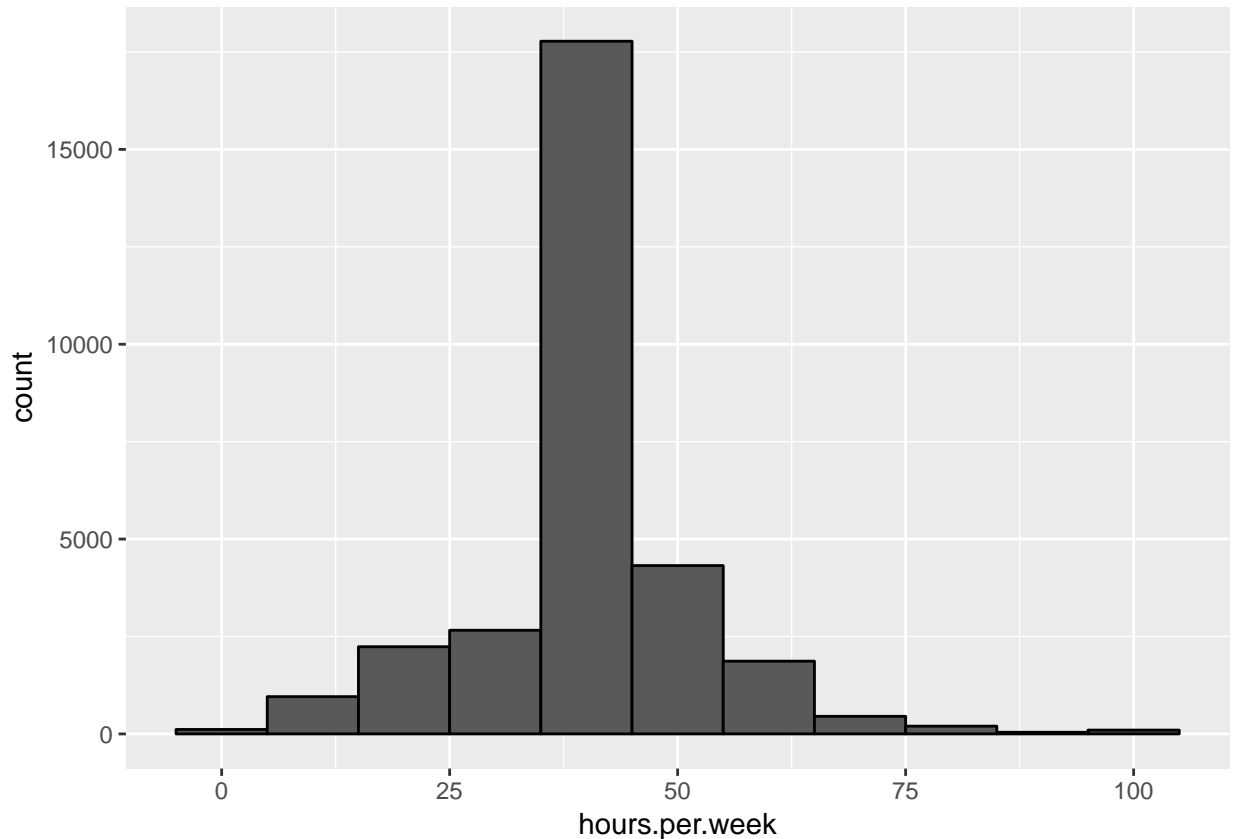
```
summary(datosAdult$hours.per.week)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      1.00  40.00   40.00  40.95  45.00   99.00
```

Let's see a histogram of the distribution of values.

Miramos a hours.per.week en bins de tamaño 10 horas.

```
ggplot(datosAdult) + aes(x=hours.per.week) +
  geom_histogram(binwidth=10, color='black')
```



Aunque hay algunos persona que traban más de 100 horas por semana, la distribución no indica que deberíamos descartar outliers.

4 Análisis de los datos

4.1 Selección de los grupos de datos

We will start by considering which variables may have an important correlation with income bracket (two values <50k and >50k). To begin with, we will remove the variable `fnlwgt` which assigns a weighting related on the population size of the US State in which the person lives.

```
datosAdult$fnlwgt<-NULL
```

Now we will change the `income` factor variable to have the values 0 or 1 to represent <50k and >50k

```
datosAdult$income <- as.numeric(datosAdult$income)-1
```

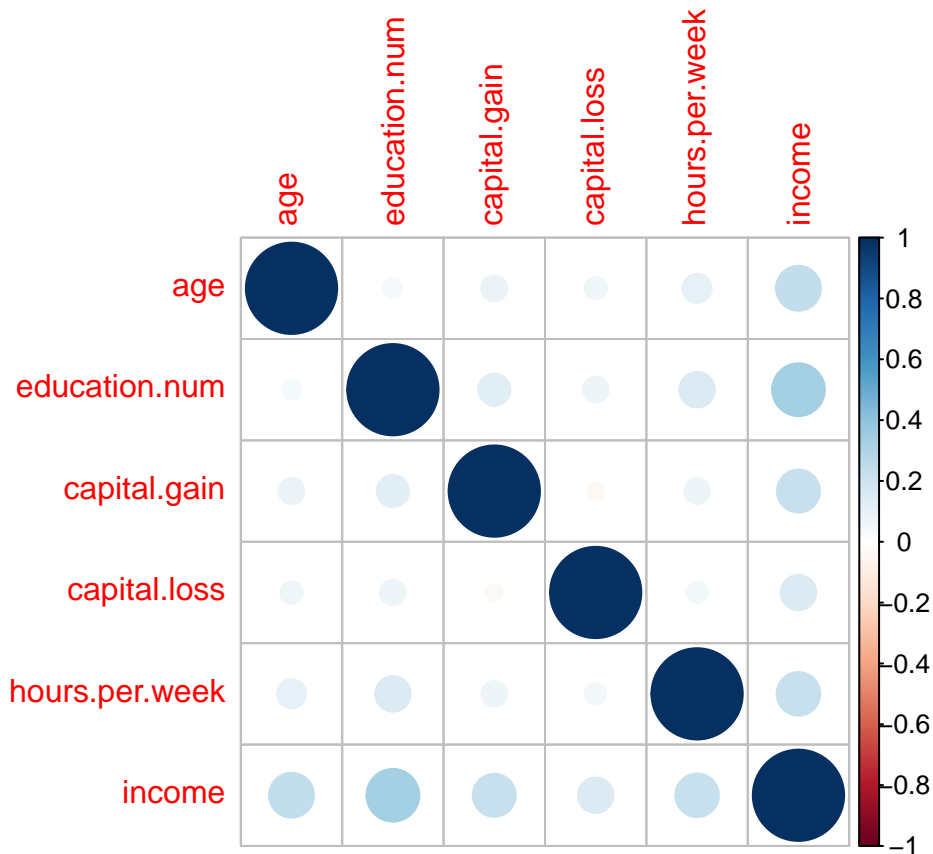
4.1.1 Correlation of numeric variables

Now we will correlate the numeric variables (`age`, `education.num`, `capital.gain`, `capital.loss`, `hours.per.week` and the class `income`) to see what shows up!

```
#Correlation plot
num.var <- c(1,4,10:12, 14)
library("corrplot")
```

```
## corrplot 0.84 loaded
```

```
corrplot(cor(datosAdult[,num.var]))
```



So we see a positive correlation with all numeric variables, but especially with **education.num**, **age** and **hours.per.week**

4.1.2 Category variables

Let's look at the category variables `workclass`, `education`, `marital.status`, `occupation`, `relationship`, `race`, `sex`, `native.country`.

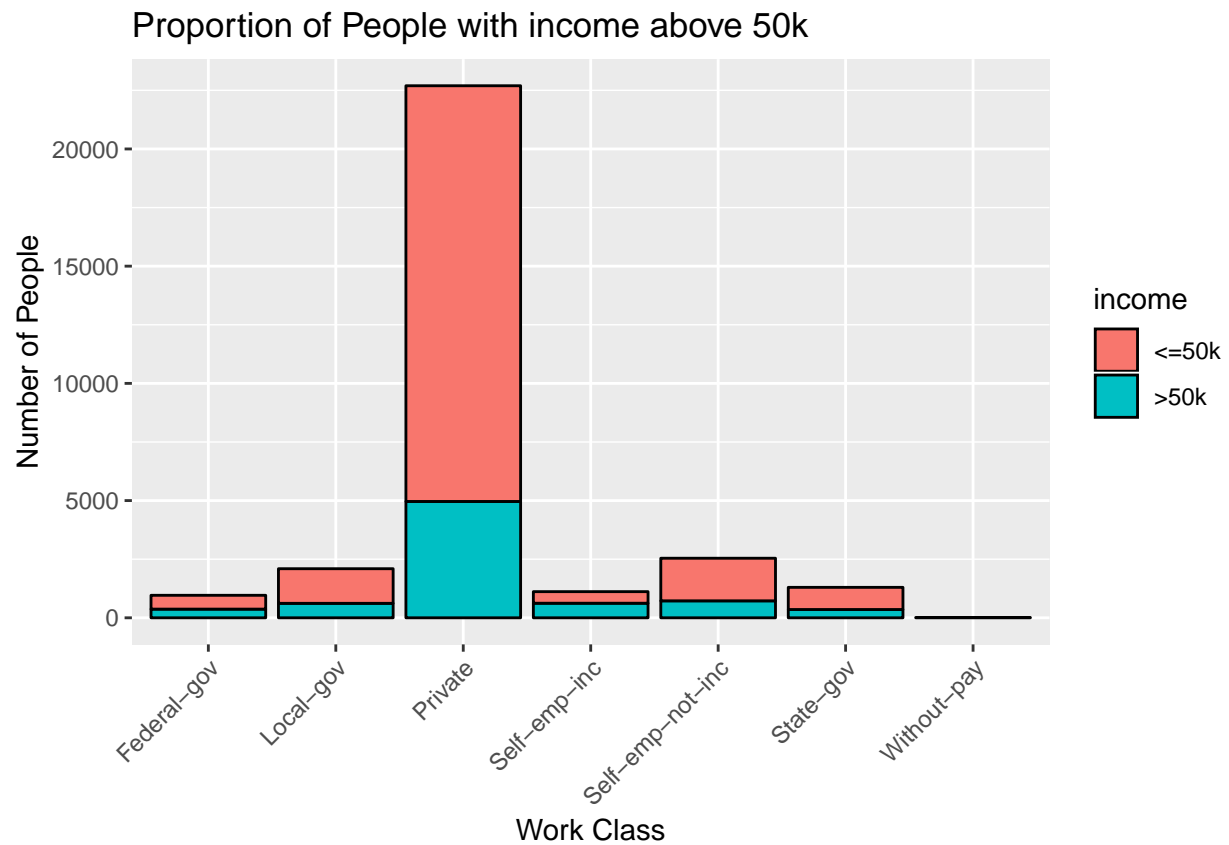
First let's re-factor the income class.

```
datosAdult$income <- factor(datosAdult$income, labels=c("<=50k", ">50k"))
#Checking the levels
levels(datosAdult$income)
```

```
## [1] "<=50k" ">50k"
```

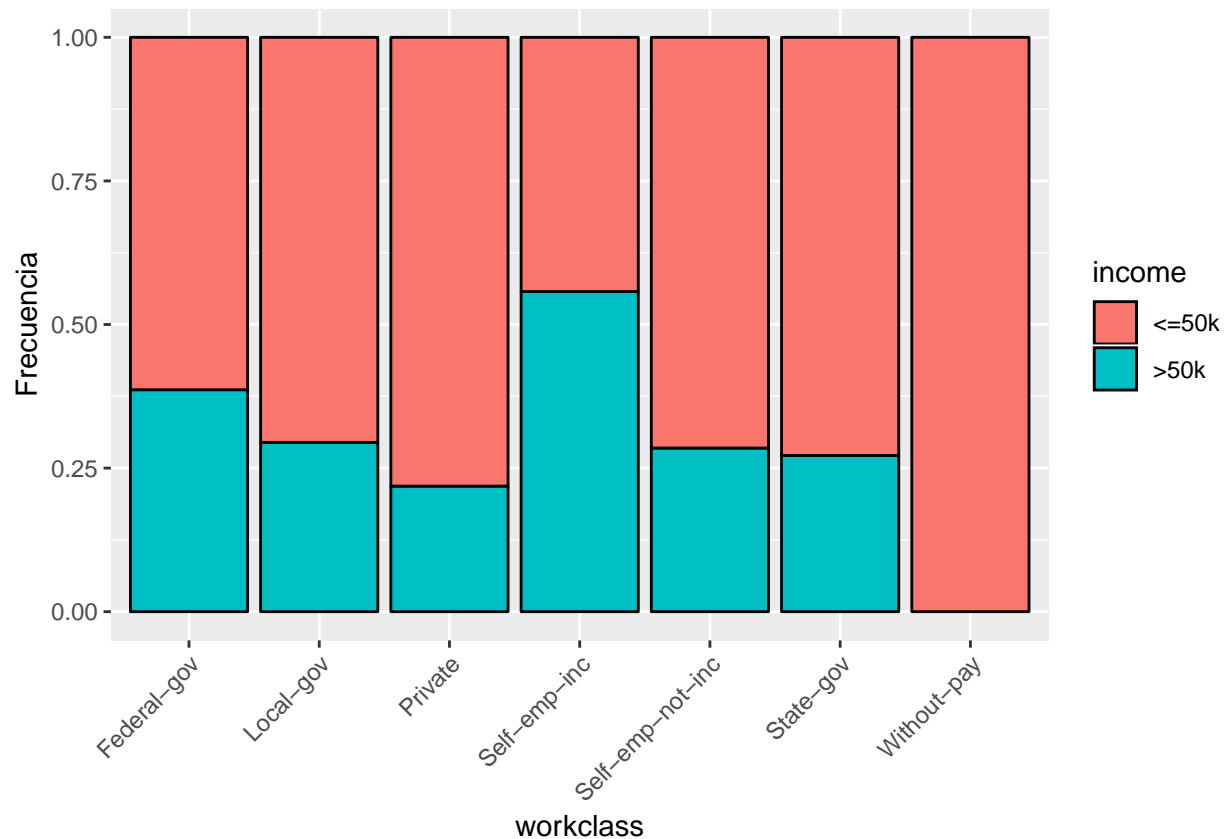
4.1.2.1 workclass

```
ggplot(datosAdult, aes(x=workclass, fill=income)) +
  geom_bar(color='black') +
  theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
  ggtitle('Proportion of People with income above 50k') +
  xlab("Work Class") + ylab("Number of People")
```

Let's display as a frequency plot too.

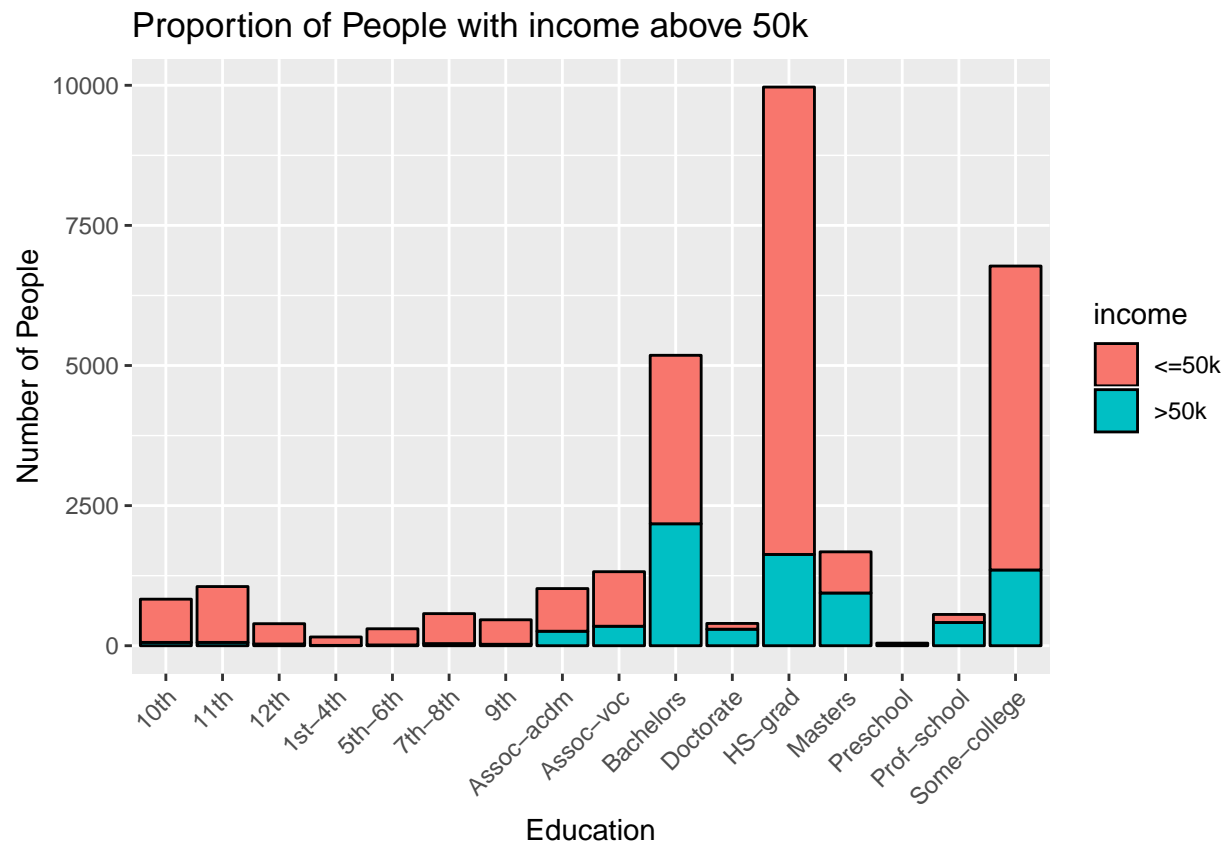
```
ggplot(data = datosAdult, aes(x=workclass, fill=income)) + geom_bar(color='black', position="fill") + theme(ax
```



So the self-employed-inc and federal-gov employees are most likely to have high salaries. Those Without-pay do not have high salaries.

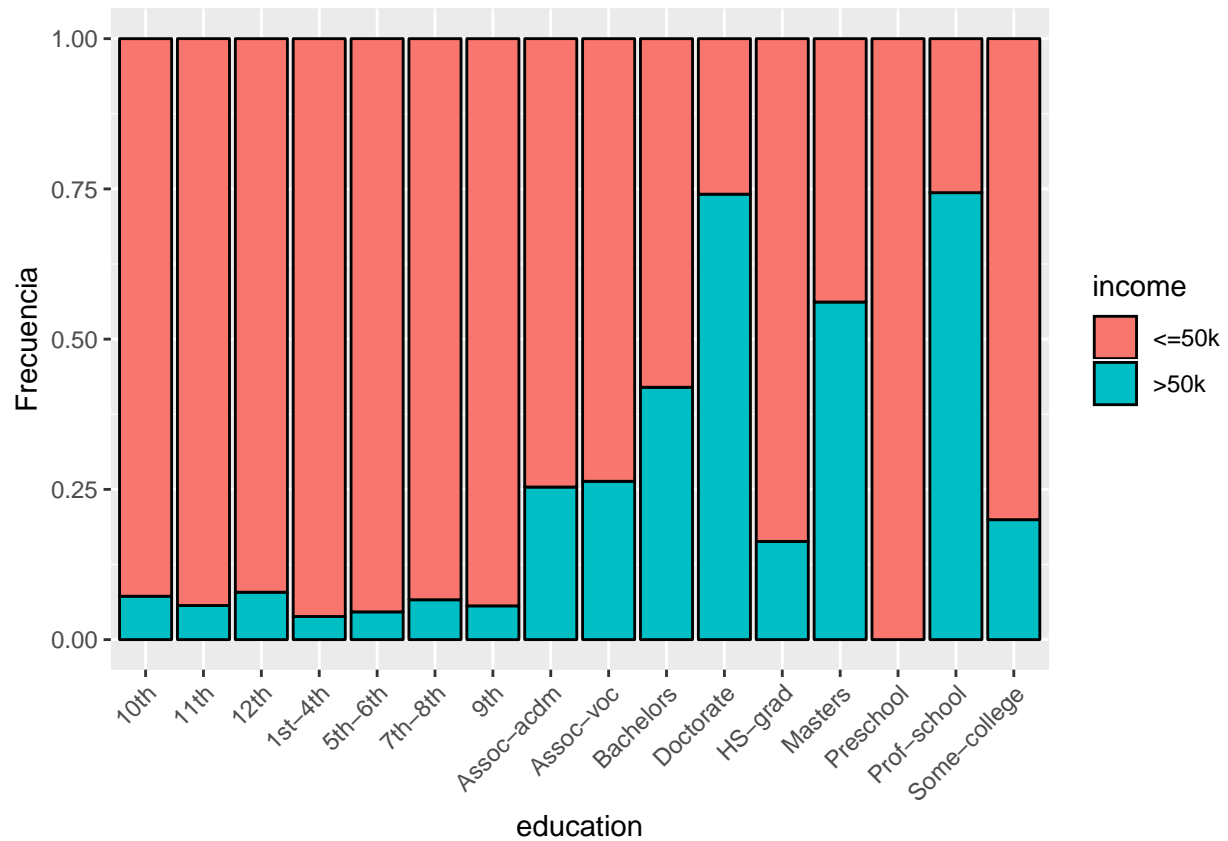
4.1.2.2 education

```
ggplot(datosAdult,aes(x=education,fill=income))+
  geom_bar(color='black')+
  theme(axis.text.x = element_text(angle = 45, hjust = 1))+
  ggtitle('Proportion of People with income above 50k')+
  xlab("Education")+ylab("Number of People")
```



Let's display as a frequency plot too.

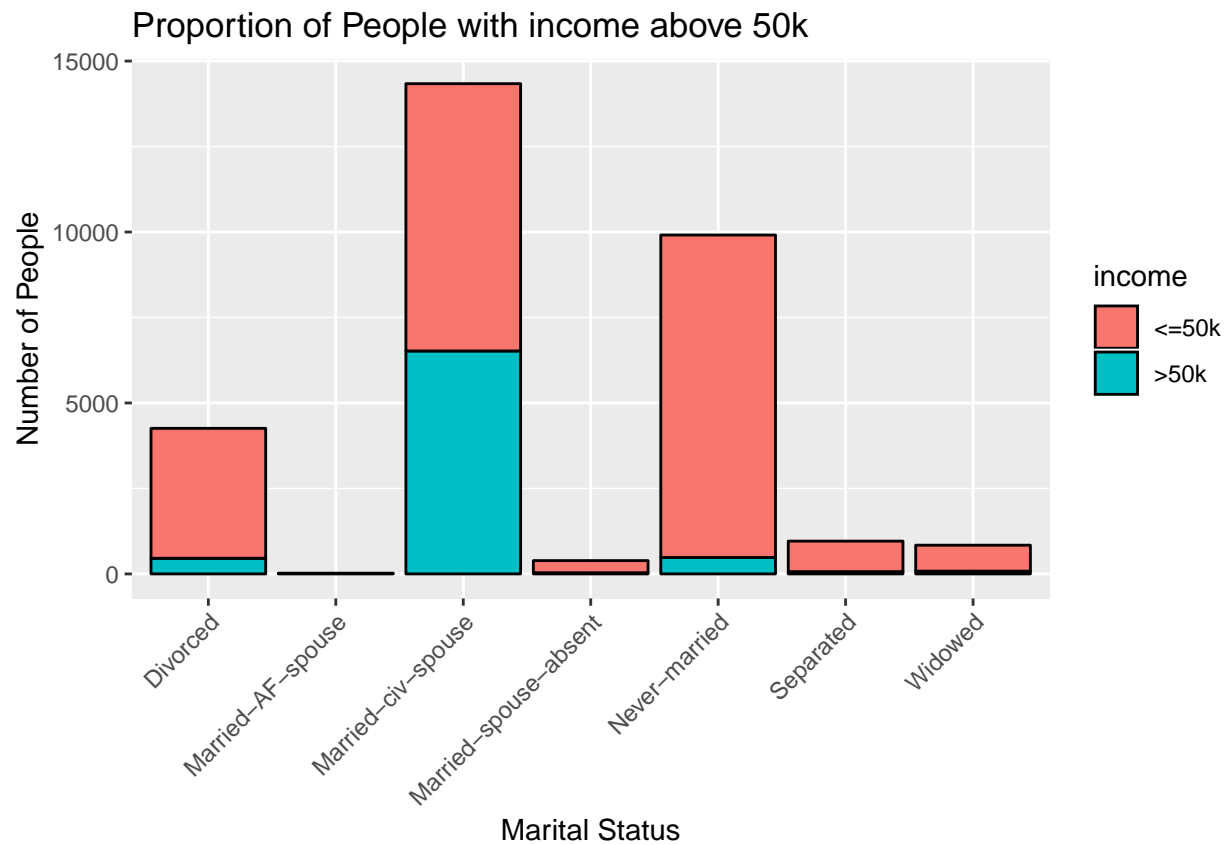
```
ggplot(data = datosAdult, aes(x=education, fill=income)) + geom_bar(color='black', position="fill") + theme(ax
```



So as we might expect the people with degrees and professional schooling are more likely to have high salaries.

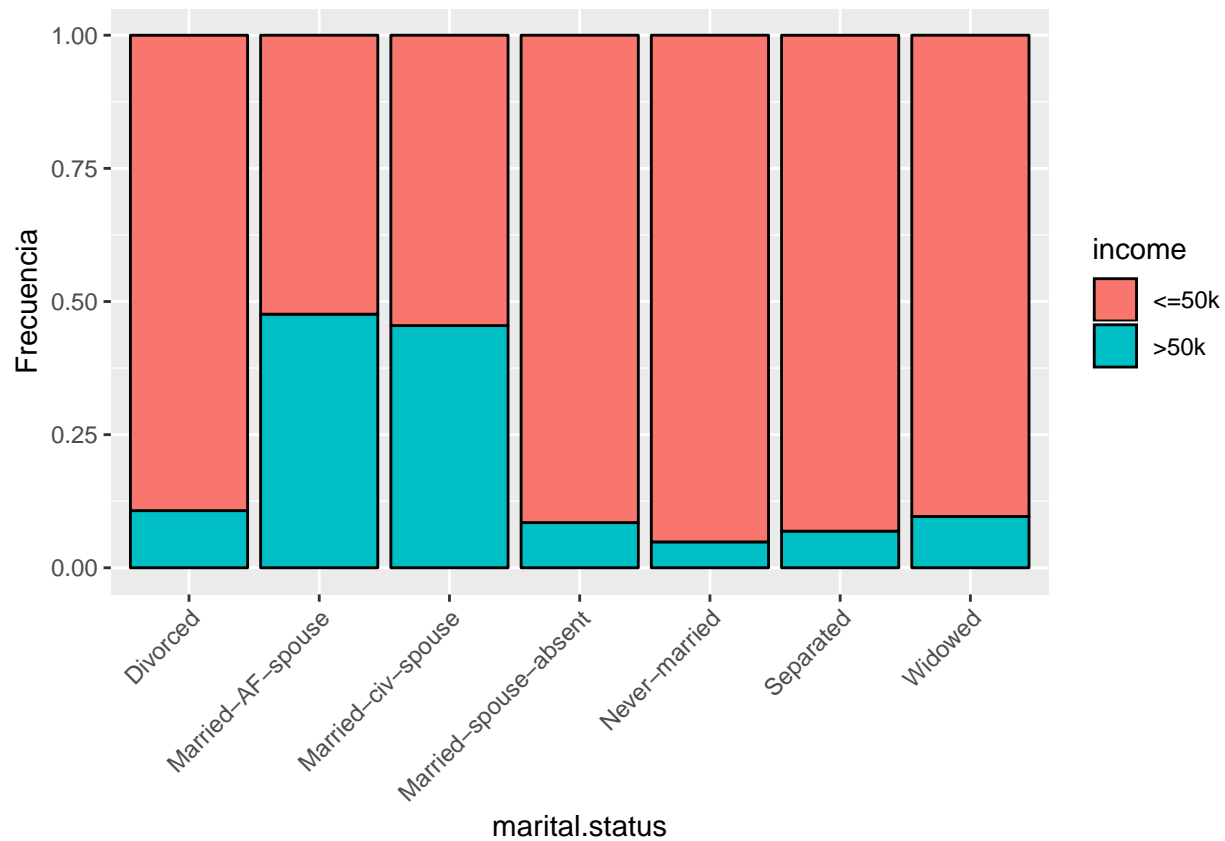
4.1.2.3 marital.status

```
ggplot(datosAdult, aes(x=marital.status, fill=income)) +
  geom_bar(color='black') +
  theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
  ggtitle('Proportion of People with income above 50k') +
  xlab("Marital Status") + ylab("Number of People")
```



Let's display as a frequency plot too.

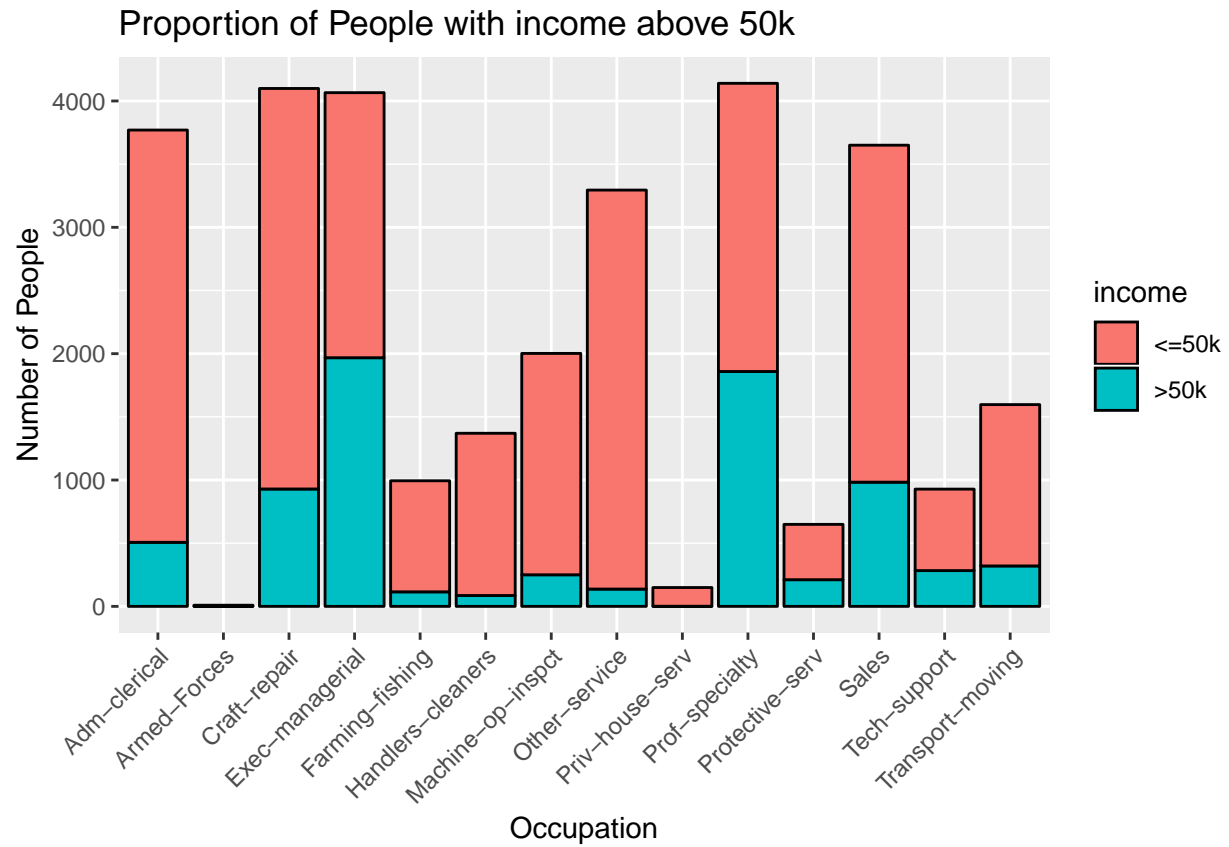
```
ggplot(data = datosAdult, aes(x=marital.status, fill=income)) + geom_bar(color='black', position="fill") + theme_minimal()
```



So we see that people who are married are more likely to have high salaries.

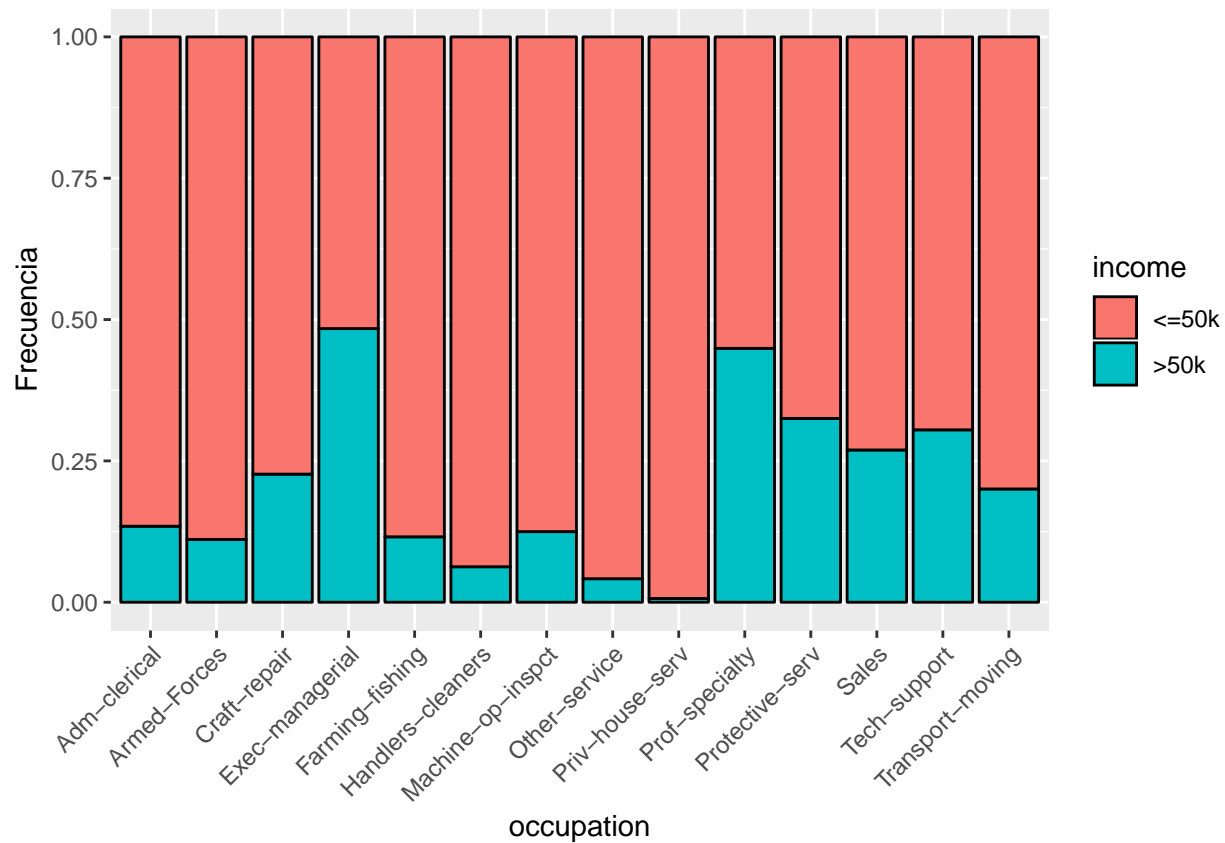
4.1.2.4 occupation

```
ggplot(datosAdult, aes(x=occupation, fill=income)) +
  geom_bar(color='black') +
  theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
  ggtitle('Proportion of People with income above 50k') +
  xlab("Occupation") + ylab("Number of People")
```



Let's display as a frequency plot too.

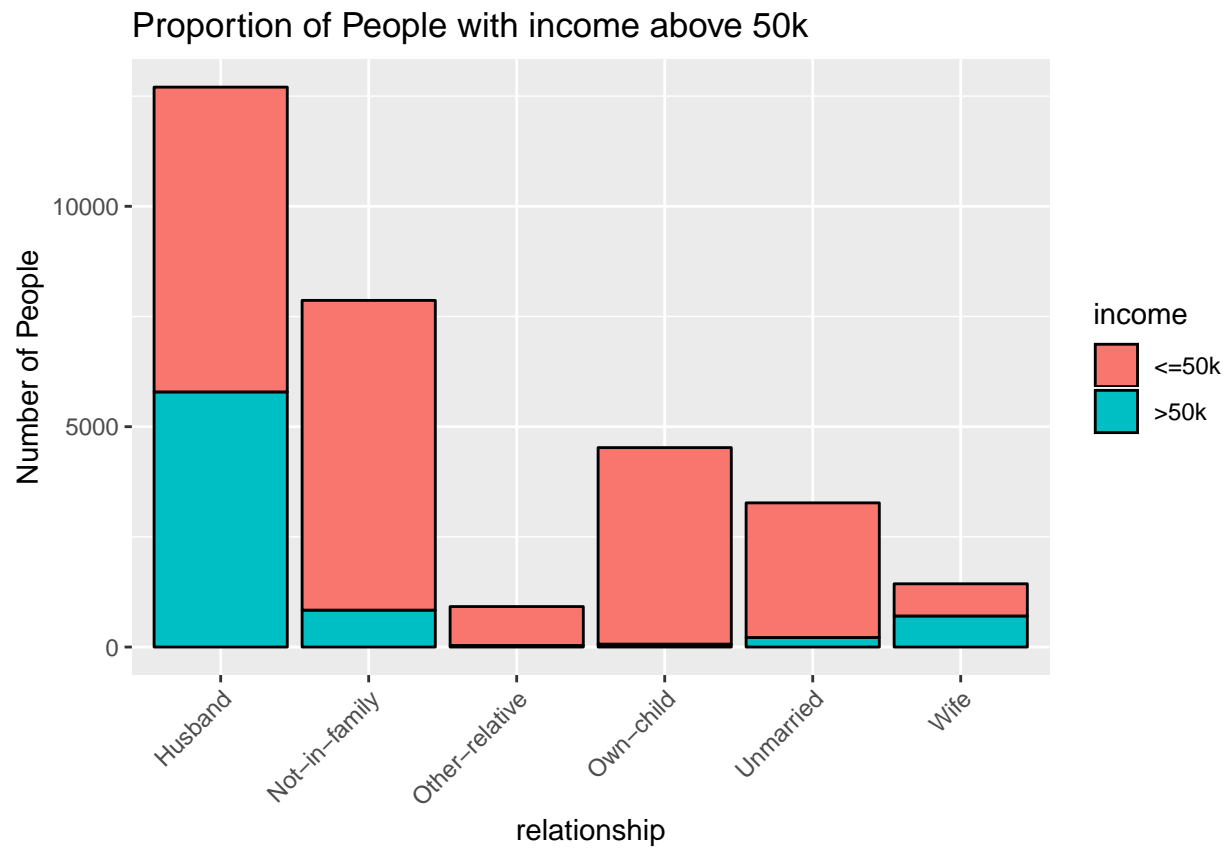
```
ggplot(data = datosAdult, aes(x=occupation, fill=income)) + geom_bar(color='black', position="fill") + theme(a
```



So as we might expect the people who are executive managers or have a professional speciality are more likely to have high salaries.

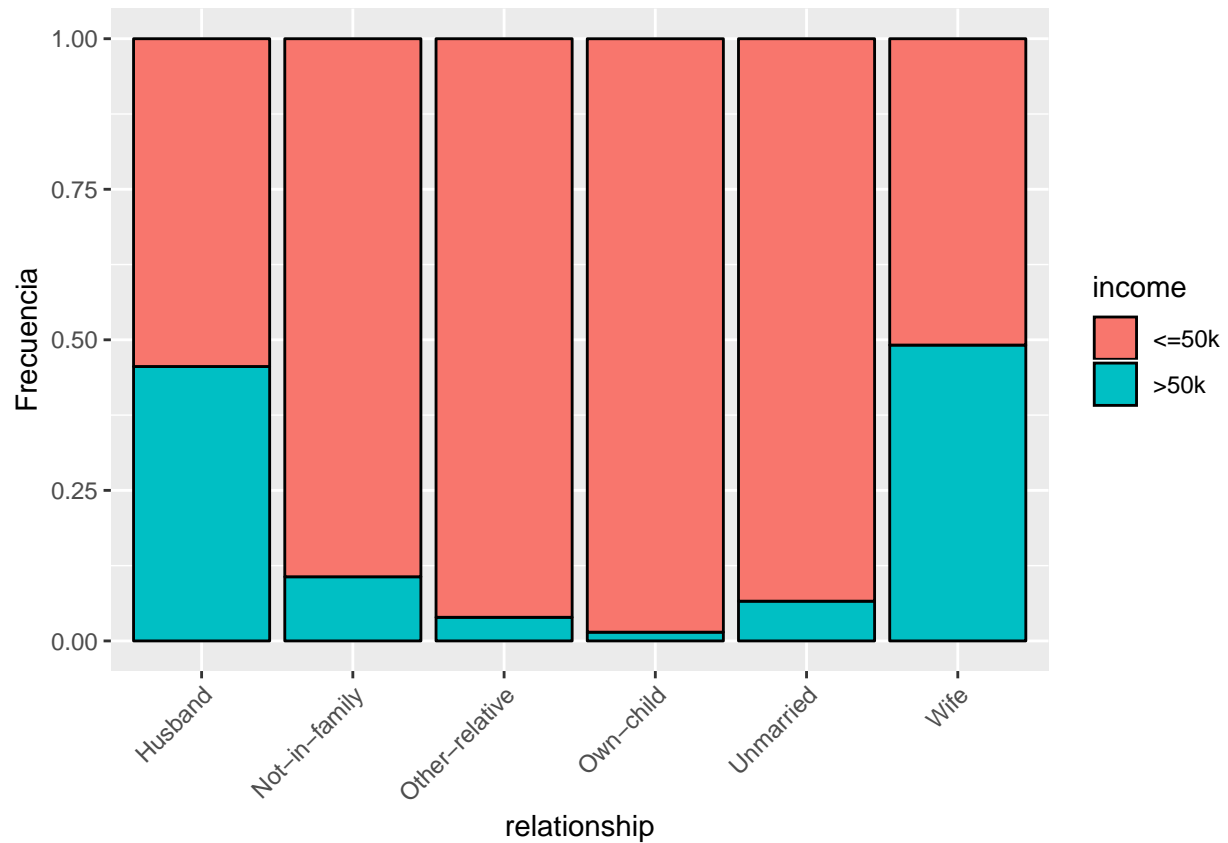
4.1.2.5 relationship

```
ggplot(datosAdult, aes(x=relationship, fill=income)) +
  geom_bar(color='black') +
  theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
  ggtitle('Proportion of People with income above 50k') +
  xlab("relationship") + ylab("Number of People")
```

Let's display as a frequency plot too.

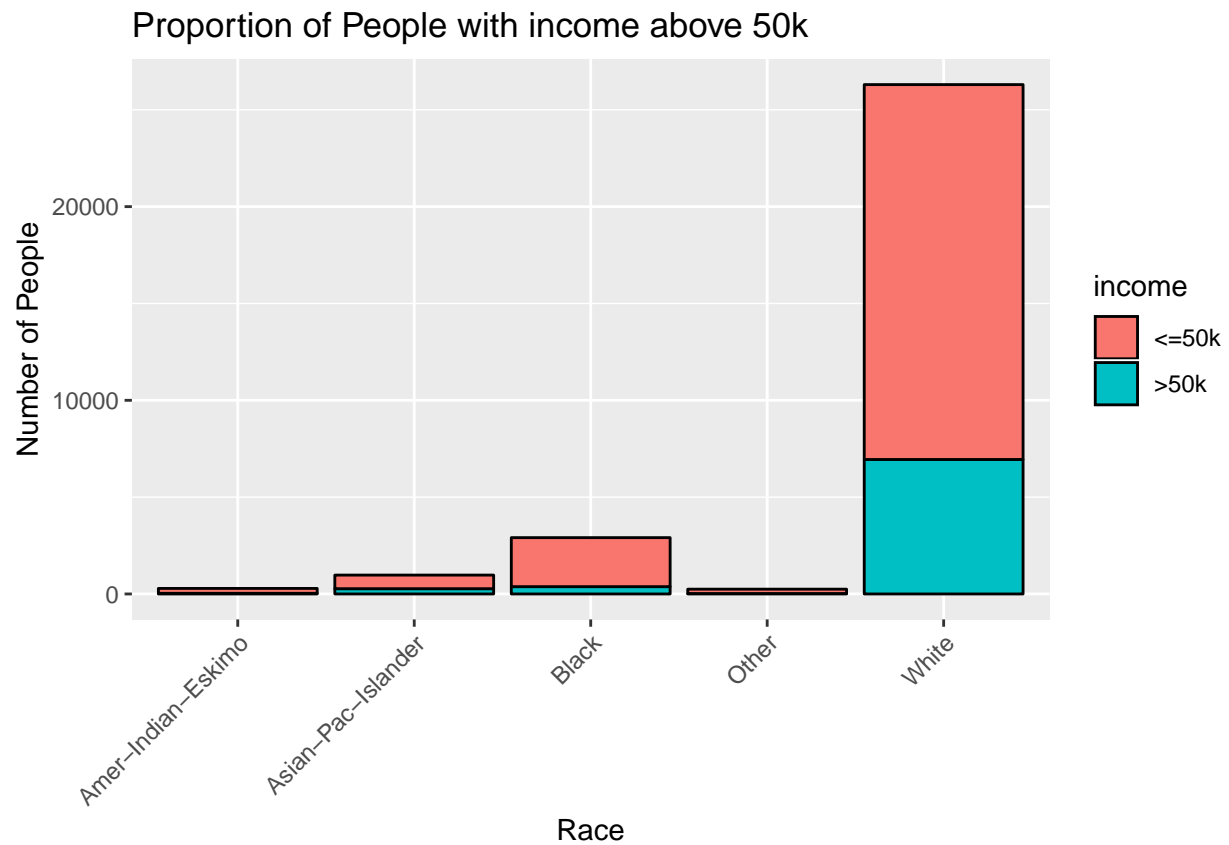
```
ggplot(data = datosAdult, aes(x=relationship, fill=income)) + geom_bar(color='black', position="fill") + theme
```



As with the marital.status variable, people who are married are more likely to have high salaries.

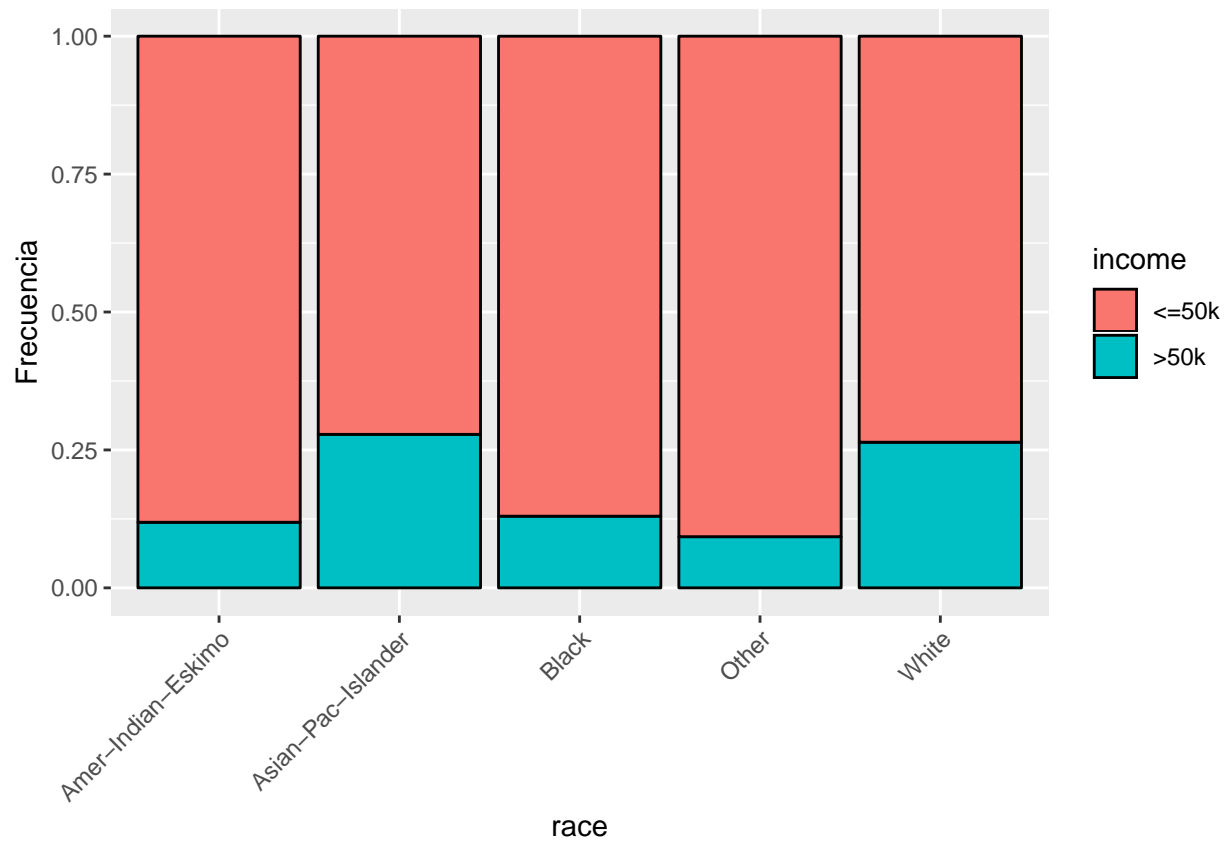
4.1.2.6 race

```
ggplot(datosAdult, aes(x=race, fill=income)) +
  geom_bar(color='black') +
  theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
  ggtitle('Proportion of People with income above 50k') +
  xlab("Race") + ylab("Number of People")
```



Let's display as a frequency plot too.

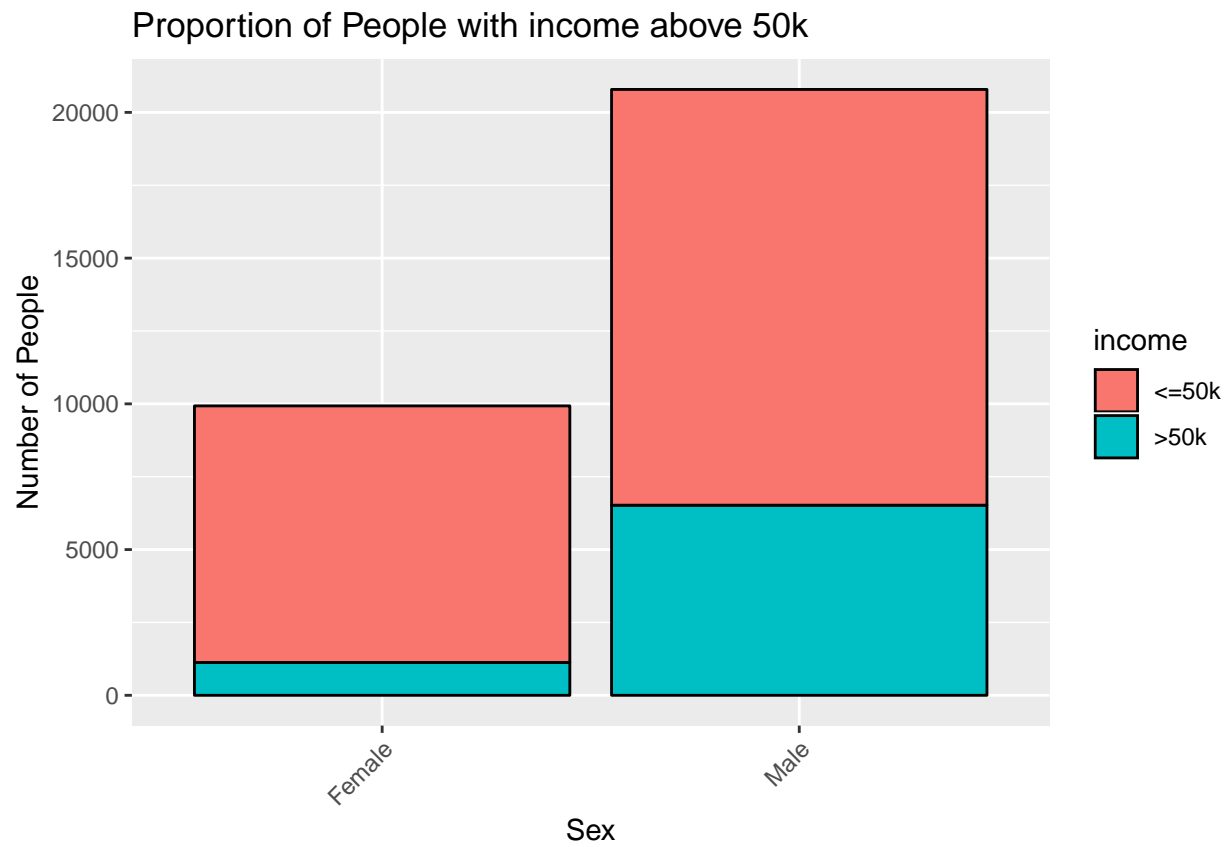
```
ggplot(data = datosAdult, aes(x=race, fill=income)) + geom_bar(color='black', position="fill") + theme(axis.te
```



So we see that White and Asian-Pac-Islander ethnic groups are more likely to have high salaries.

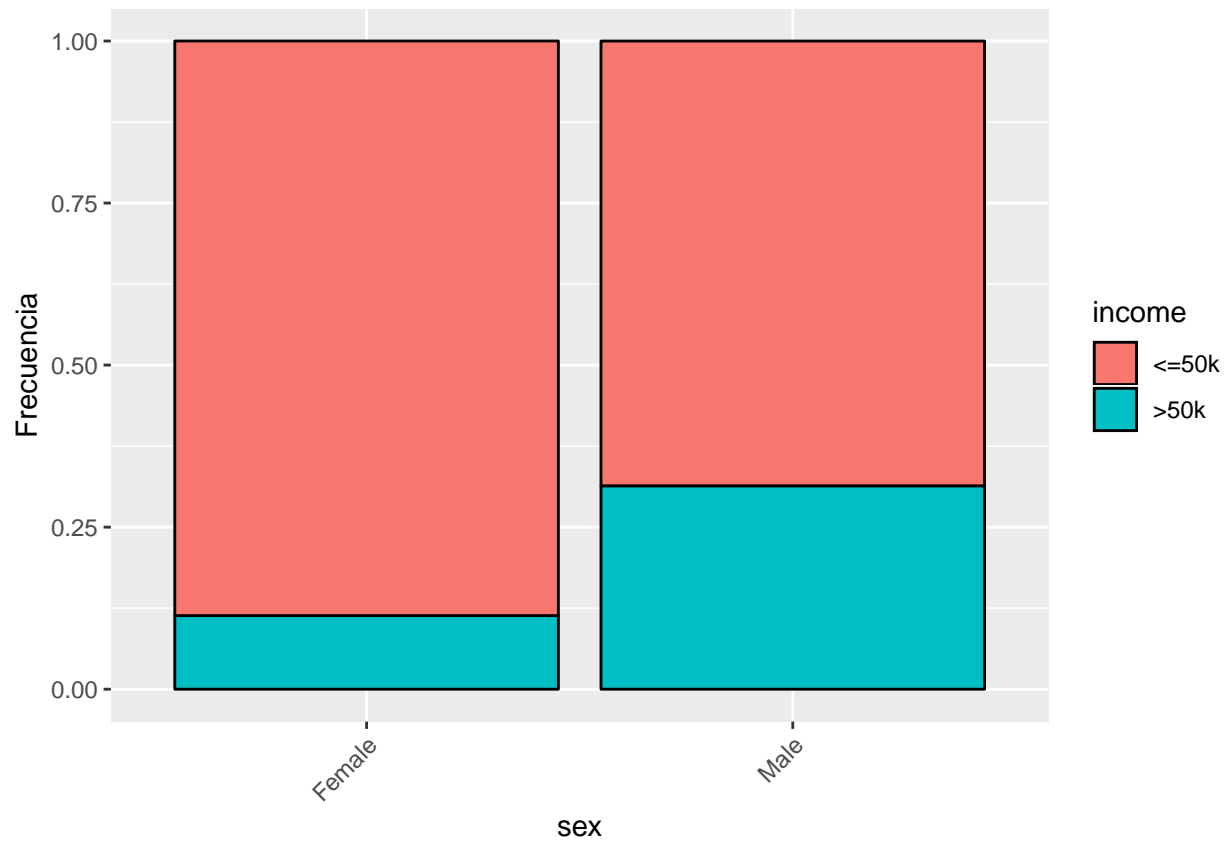
4.1.2.7 sex

```
ggplot(datosAdult, aes(x=sex, fill=income)) +
  geom_bar(color='black') +
  theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
  ggtitle('Proportion of People with income above 50k') +
  xlab("Sex") + ylab("Number of People")
```



Let's display as a frequency plot too.

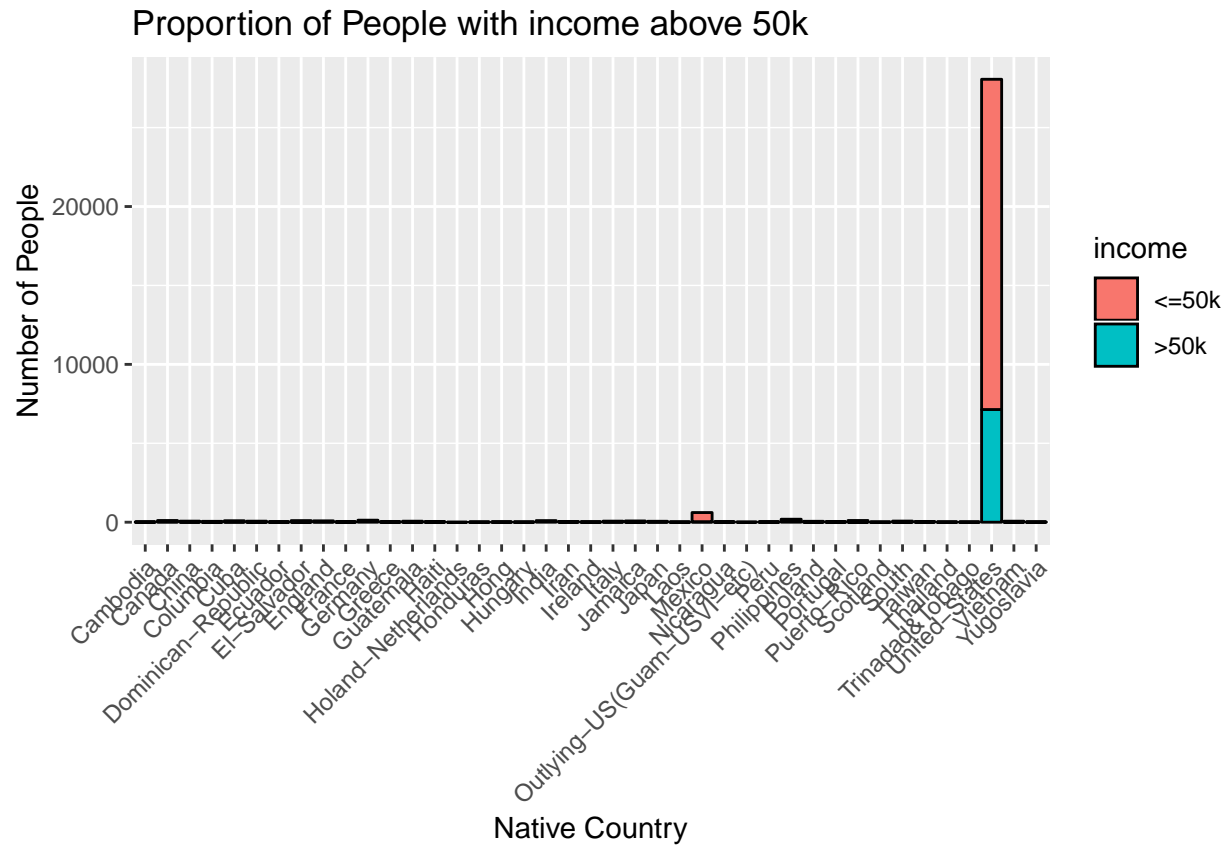
```
ggplot(data = datosAdult, aes(x=sex, fill=income)) + geom_bar(color='black', position="fill") + theme(axis.text.x = angle(45))
```



So we find that Males are more likely to have high salaries than Females.

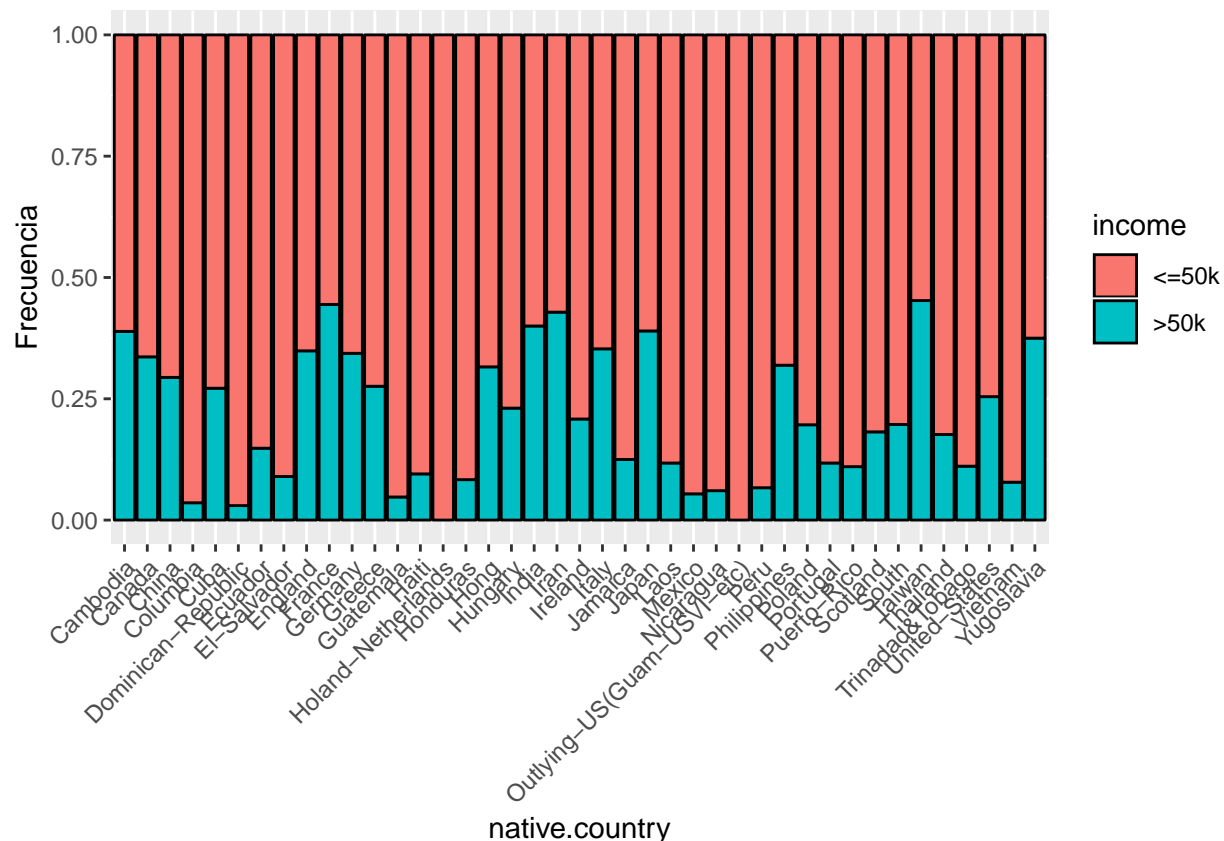
4.1.2.8 native.country

```
ggplot(datosAdult, aes(x=native.country, fill=income)) +
  geom_bar(color='black') +
  theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
  ggtitle('Proportion of People with income above 50k') +
  xlab("Native Country") + ylab("Number of People")
```



Let's display as a frequency plot too.

```
ggplot(data = datosAdult, aes(x=native.country, fill=income)) + geom_bar(color='black', position="fill") + theme_minimal()
```



There are no particularly strong variations for native.country, so it looks like we should remove the variable from the analysis dataset, but we will check with a Chi-squared test for variable dependency first of all.

4.2 Comprobación de la normalidad y homogeneidad de la varianza

Utilizamos la prueba Anderson-Darling normality test for each of the variables age, education.num, capital.gain, capital.loss, hours.per.week.

```
pvalage=ad.test(datosAdult$age)$p.value
pvaledu=ad.test(datosAdult$education.num)$p.value
pvalcapg=ad.test(datosAdult$capital.gain)$p.value
pvalcapl=ad.test(datosAdult$capital.loss)$p.value
pvalhours=ad.test(datosAdult$hours.per.week)$p.value

pvals<-matrix(c(pvalage,pvaledu,pvalcapg,pvalcapl,pvalhours),ncol=1, byrow=TRUE)
colnames(pvals)<-"pvalue"
rownames(pvals)<-c("age","education.num","capital.gain","capital.loss","hours.per.week")

as.table(pvals)
```

```
##           pvalue
## age          3.7e-24
## education.num 3.7e-24
## capital.gain   3.7e-24
## capital.loss   3.7e-24
## hours.per.week 3.7e-24
```


El p.value para todas las variables es menor que 0.05 así que ninguna de las variables tiene una distribución normal.

Utilizamos la prueba Fligner-Killeen para comprobar la homogeneity de las variables.

```
fligner.test(education.num~education, data=datosAdult)
```

```
##  
## Fligner-Killeen test of homogeneity of variances  
##  
## data: education.num by education  
## Fligner-Killeen:med chi-squared = -Inf, df = 15, p-value = 1
```

Así que veremos que education y education.num con un p-value de 1.0 (>0.05) indica que tienen variancias que son homogeneas.

4.3 Aplicación de pruebas estadísticas

4.3.1 Pruebas de contraste de hipótesis

Here we will look at tests for independence of the categorical variables using Pearson's Chi-Squared test. The null hypothesis is: H_0 : *thetwovariablesareindependentinthesample* The alternative hypothesis is: H_A : *thetwovariablesaredependentwithinthesample*

4.3.1.1 Workclass and Income

```
chisq.test(table(datosAdult$workclass, datosAdult$income))
```

```
## Warning in chisq.test(table(datosAdult$workclass, datosAdult$income)): Chi-  
## squared approximation may be incorrect  
  
##  
## Pearson's Chi-squared test  
##  
## data: table(datosAdult$workclass, datosAdult$income)  
## X-squared = 825.27, df = 6, p-value < 2.2e-16
```

The p-value is very small, so we reject the null hypothesis at the 0.05 significance level and we expect that the two variable are dependent.

4.3.1.2 Education and Income

```
chisq.test(table(datosAdult$education, datosAdult$income))
```

```
##  
## Pearson's Chi-squared test  
##  
## data: table(datosAdult$education, datosAdult$income)  
## X-squared = 4133.4, df = 15, p-value < 2.2e-16
```

The p-value is very small, so we reject the null hypothesis at the 0.05 significance level and we expect that the two variable are dependent.

4.3.1.3 Marital.status and Income

```
chisq.test(table(datosAdult$marital.status, datosAdult$income))
```

```
##  
## Pearson's Chi-squared test  
##  
## data: table(datosAdult$marital.status, datosAdult$income)  
## X-squared = 6164.2, df = 6, p-value < 2.2e-16
```

The p-value is very small, so we reject the null hypothesis at the 0.05 significance level and we expect that the two variable are dependent.

4.3.1.4 Occupation and Income

```
chisq.test(table(datosAdult$occupation, datosAdult$income))
```

```
## Warning in chisq.test(table(datosAdult$occupation, datosAdult$income)):  
## Chi-squared approximation may be incorrect  
##  
## Pearson's Chi-squared test  
##  
## data: table(datosAdult$occupation, datosAdult$income)  
## X-squared = 3744.9, df = 13, p-value < 2.2e-16
```

The p-value is very small, so we reject the null hypothesis at the 0.05 significance level and we expect that the two variable are dependent.

4.3.1.5 Relationship and Income

```
chisq.test(table(datosAdult$relationship, datosAdult$income))
```

```
##  
## Pearson's Chi-squared test  
##  
## data: table(datosAdult$relationship, datosAdult$income)  
## X-squared = 6336.7, df = 5, p-value < 2.2e-16
```

The p-value is very small, so we reject the null hypothesis at the 0.05 significance level and we expect that the two variable are dependent.

4.3.1.6 Race and Income

```
chisq.test(table(datosAdult$race, datosAdult$income))
```

```
##  
## Pearson's Chi-squared test  
##  
## data: table(datosAdult$race, datosAdult$income)  
## X-squared = 314.93, df = 4, p-value < 2.2e-16
```

The p-value is very small, so we reject the null hypothesis at the 0.05 significance level and we expect that the two variable are dependent.

4.3.1.7 Sex and Income

```
chisq.test(table(datosAdult$sex, datosAdult$income))
```

```
##  
## Pearson's Chi-squared test with Yates' continuity correction  
##  
## data: table(datosAdult$sex, datosAdult$income)  
## X-squared = 1440.4, df = 1, p-value < 2.2e-16
```

The p-value is very small, so we reject the null hypothesis at the 0.05 significance level and we expect that the two variable are dependent.

4.3.1.8 Native.country and Income

```
chisq.test(table(datosAdult$native.country, datosAdult$income))
```

```
## Warning in chisq.test(table(datosAdult$native.country, datosAdult$income)):  
## Chi-squared approximation may be incorrect  
  
##  
## Pearson's Chi-squared test  
##  
## data: table(datosAdult$native.country, datosAdult$income)  
## X-squared = 317.76, df = 40, p-value < 2.2e-16
```

The p-value is very small, so we reject the null hypothesis at the 0.05 significance level and we expect that the two variable are dependent.

As a consequence, we see that the **income** class is dependent on all the category variables, including **native.country**, so we won't remove this from the result set.

4.3.2 Correlaciones

We will get values for the correlations of the 3 strongest variables that we plotted earlier (i.e. Age, Education.num and Hours.per.week) Now we will change the *income* factor variable to have the values 0 or 1 to represent <50k and >50k

```
datosAdult$income <- as.numeric(datosAdult$income)-1
```

```
corAge=cor(datosAdult$age,datosAdult$income)  
corEducation.num=cor(datosAdult$education.num,datosAdult$income)  
corHours=cor(datosAdult$hours.per.week,datosAdult$income)
```

```
corAge
```

```
## [1] 0.2424308
```

```
corEducation.num
```

```
## [1] 0.3346403
```

```
corHours
```

```
## [1] 0.2285466
```

4.3.3 Regresiones

```
# Regresores cuantitativos con mayor coeficiente
# de correlación con respecto al income

ageV = datosAdult$age
eduV = datosAdult$education.num
hoursV = datosAdult$hours.per.week

# Regresores cualitativos
occupationV = datosAdult$occupation
maritalV = datosAdult$marital.status
nativeV = datosAdult$native.country
sexV = datosAdult$sex

# Variable a predecir
incomeV = datosAdult$income
# Generación de varios modelos
modelo1 <- lm(incomeV ~ ageV + eduV + hoursV + occupationV + maritalV, data = datosAdult)
modelo2 <- lm(incomeV ~ ageV + eduV + hoursV + occupationV + maritalV + nativeV, data = datosAdult)
modelo3 <- lm(incomeV ~ ageV + eduV + hoursV + occupationV + maritalV + nativeV + sexV, data = datosAdult)

tabla.coeficientes <- matrix(c(1, summary(modelo1)$r.squared,
2, summary(modelo2)$r.squared,
3, summary(modelo3)$r.squared),
ncol = 2, byrow = TRUE)

colnames(tabla.coeficientes) <- c("Modelo", "R^2")
tabla.coeficientes

##      Modelo      R^2
## [1,]      1 0.3274863
## [2,]      2 0.3287867
## [3,]      3 0.3305613
```

En este caso el modelo3 es el mejor fit porque tiene un mayor coeficiente de determinación.

Generamos el conjunto de datos para hacer más modelos.

```
write.csv(datosAdult, file = "datosAdult_out.csv", row.names=FALSE)
```

5 Representación de los resultados

As presented graphically and in tables above, we have seen that several variable factors strongly influence the model generation. We have seen the correlations between numerical and categorical variables and the class of income. It seems likely that this dataset can be used to predict income class given the set of variables available.

Although the normality of the variable distributions is proven to be not normal, we can still apply statistical analysis because the sample size is so large (much greater than 30 records).

6 Resolución del problema

We have created a simple regression model that allows for fitting the data and making income predictions for a new set of data. In practice this would be a starting point in order to obtain a much better model using other techniques. In this case, because of the large number of categorical variables as well as numerical variables, the best modelling option may be to use decision trees.